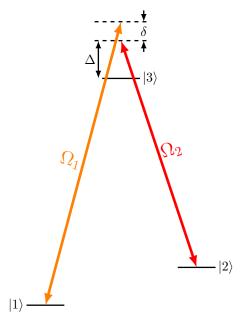
Electromagnetically Induced Transparency (EIT)

November 17, 2023



With Ω_2 coupling $|2\rangle$ and $|3\rangle$ together, the energies of the coupled states are (relative to the original energy of $|3\rangle$)

$$E_{\pm} = \frac{\Delta \pm \sqrt{\Delta^2 + \Omega_2^2}}{2}$$

The eigenstates are

$$|\pm\rangle = \frac{\sqrt{\sqrt{\Delta^2 + \Omega_2^2} \pm \Delta}}{\sqrt{2}\sqrt[4]{\Delta^2 + \Omega_2^2}}|2\rangle + \frac{\Omega_2}{\sqrt{2}\sqrt[4]{\Delta^2 + \Omega_2^2}\sqrt{\sqrt{\Delta^2 + \Omega_2^2} \pm \Delta}}|3\rangle$$

The Rabi frequencies from the $|1\rangle$ state to the $|\pm\rangle$ states are

$$\Omega_{\pm} = \frac{\Omega_{1}\Omega_{2}}{\sqrt{2}\sqrt[4]{\Delta^{2} + \Omega_{2}^{2}}\sqrt{\sqrt{\Delta^{2} + \Omega_{2}^{2}} \pm \Delta}}$$

and the detunings,

$$\begin{split} \delta_{\pm} = & \delta - E_{\pm} \\ = & \delta - \frac{\Delta \pm \sqrt{\Delta^2 + \Omega_2^2}}{2} \end{split}$$

Lifetime of the $|\pm\rangle$ states

$$\Gamma_{\pm} = \frac{\Gamma\Omega_{2}^{2}}{2\sqrt{\Delta^{2} + \Omega_{2}^{2}} \left(\sqrt{\Delta^{2} + \Omega_{2}^{2}} \pm \Delta\right)}$$

Scattering rate

$$\gamma = \left(\frac{\sqrt{\Gamma_{+}}\Omega_{+}}{\sqrt{\Gamma_{+}^{2} + 4\delta_{+}^{2} + 2\Omega_{+}^{2}}} + \frac{\sqrt{\Gamma_{-}}\Omega_{-}}{\sqrt{\Gamma_{-}^{2} - 4\delta_{-}^{2} - 2\Omega_{-}^{2}}} \right)^{2}$$

$$= \Gamma\Omega_{1}^{2}\Omega_{2}^{4} \left(\frac{1}{2\sqrt{\Delta^{2} + \Omega_{2}^{2}} \left(\sqrt{\Delta^{2} + \Omega_{2}^{2} \pm \Delta}\right)} \frac{1}{\sqrt{\Gamma_{+}^{2} + 4\delta_{+}^{2} + 2\Omega_{+}^{2}}} + \frac{1}{2\sqrt{\Delta^{2} + \Omega_{2}^{2}} \left(\sqrt{\Delta^{2} + \Omega_{2}^{2} \pm \Delta}\right)} \frac{1}{\sqrt{\Gamma_{-}^{2} - 4\delta_{-}^{2} - 2\Omega_{-}^{2}}} \right)^{2}$$