

Totally fair — these terms sound abstract until you see **what they're actually measuring**. Let's ground this in your exact code and think like a machine, not a textbook.

1 What Time Complexity really means

Time complexity = how many steps the code runs as input grows

Not actual seconds. Just **how work increases**.

Your code

```
for (int i = 1; i < nums.length; i++) {  
    sum = sum + nums[i];  
    nums[i] = sum;  
}
```

If array size = n

- Loop runs **once per element**
- For n elements \rightarrow about n operations

So we say:

💖 **Time Complexity = $O(n)$**

Real meaning:

- If array size doubles \rightarrow work doubles
- If array size = 1,000 \rightarrow ~1,000 steps
- If array size = 1,000,000 \rightarrow ~1,000,000 steps

That's it. No magic.

2 What Space Complexity really means

Space complexity = extra memory used by your algorithm

⚠ Important: We **do NOT count the input array** because it's already given.

What extra memory do you use?

```
int sum = nums[0];
```

That's it.

- `sum` → one integer
- `i` → loop variable

These do **not grow** with input size.

Whether array has:

- 5 elements
- 5 million elements

You still use:

- 1 `int`
- 1 loop variable

So we say:

OK Space Complexity = $O(1)$ (constant space)

Real meaning:

- Extra memory stays **constant**
- Does not depend on `n`

3 Why we say “ $O(1)$ extra space”

Because:

- We reused the input array (`nums`)
- We did NOT create a new array like:

```
int[] result = new int[n]; // ❌ extra space  $O(n)$ 
```

If you had done that, space would be **$O(n)$** .

4 Tiny comparison (this will click 🎯)

❌ Extra space $O(n)$

```
int[] result = new int[n];
```

Memory grows with input → $O(n)$

✓ Extra space $O(1)$

```
int sum = 0;
```

Memory stays same $\rightarrow O(1)$

One-line intuition (remember this forever)

- **$O(n)$ time** \rightarrow loop depends on input size
 - **$O(1)$ space** \rightarrow only fixed number of variables
-

Space complexity is about growth, not absolute memory. A small fixed variable counts as **$O(1)$ constant space** even though it technically uses memory.

So we consider space complexity constant even if we take extra variable or array **till it's not growing with input**.

- **Extra variable(s)** (like `sum`, `i`, `temp`) $\rightarrow O(1)$ because they exist only once, no matter how big the input is.
- **Extra array / collection** whose size depends on input `n` $\rightarrow O(n)$ because memory grows with input.

So the rule is:

Space complexity = how memory usage grows with input size. If it doesn't grow, it's constant $\rightarrow O(1)$.

Even if you declare 2-3 extra variables, it's still $O(1)$ — only **memory proportional to `n` or more** counts as $O(n)$, $O(n^2)$, etc.

You got it perfectly.