

Properties

IS Rule (Applied in diff. field, including NLP)

your own Naïve Bayes Tweet Classifier

Corpus of Tweets

A hand-drawn diagram consisting of a grid of colored squares. The top row is orange, and the bottom row is blue. The left column contains the word "Positive" written vertically, and the right column contains the word "Negative" written vertically. The grid is divided into four quadrants by black lines. The top-left quadrant (orange) has a red arrow pointing from the center to the top-left corner. The top-right quadrant (orange) has a red arrow pointing from the center to the top-right corner. The bottom-left quadrant (blue) has a blue arrow pointing from the center to the bottom-left corner. The bottom-right quadrant (blue) has a blue arrow pointing from the center to the bottom-right corner.

Tweets containing the word "happy".

A child's drawing of a window frame made of black lines. The window is divided into six panes. The top-left pane is filled with orange washes. The other five panes are filled with blue washes. In the bottom-left pane, the word "happy" is written in black, outlined letters.

→ Positive Tweet

B → tweet containing "happy"

$$A) = N_{\text{pos}} / N \rightarrow 13/20$$

$$P(B) = P(\text{happy}) = N_{\text{happy}} / N$$

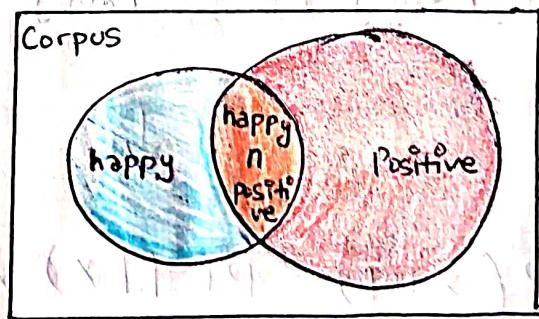
$$\rightarrow 0.65 \quad P(B) = 4/20 \rightarrow 0.2$$

$$\text{negative}) = 1 - P(\text{positive})$$

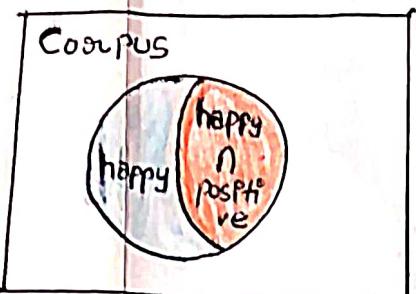
$$\rightarrow 1 - 0.65 \rightarrow 0.35$$

Probability of the intersection

A 4x4 grid of colored squares. The colors are as follows: Row 1: Brown, Tan, Red, Tan. Row 2: Tan, Pink, Tan, Tan. Row 3: Tan, Tan, Tan, Tan. Row 4: Tan, Tan, Tan, Tan. The bottom-left square (row 4, column 1) contains the word "happy" in black, handwritten-style font.



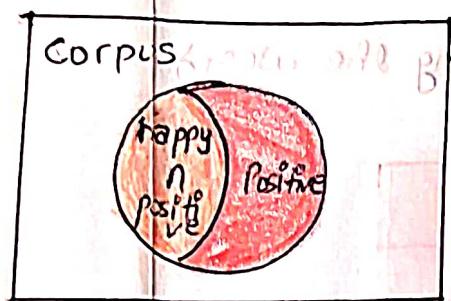
$$A \cap B) = P(A, B) = \frac{3}{20} = 0.15$$



$$P(A|B) = P(\text{"positive"} | \text{"happy"})$$

$$= \frac{3}{4} \Rightarrow 0.75$$

prob. of tweet is Positive given that it contains word happy ~~is~~



$$P(B|A) = P(\text{"happy"} | \text{"positive"})$$

$$= \frac{3}{13} \Rightarrow 0.231$$

Baye's Rule →

$$P(\text{"Positive"} | \text{"happy"}) = \frac{P(\text{"Positive"} \cap \text{"happy"})}{P(\text{"happy"})}$$

$$P(\text{"happy"} | \text{"Positive"}) = \frac{P(\text{"happy"} \cap \text{"Positive"})}{P(\text{"Positive"})}$$



$$P(\text{"Positive"} | \text{"happy"}) = P(\text{"happy"} | \text{"Positive"}) \times \frac{P(\text{"Positive"})}{P(\text{"happy"})}$$

$$P(x|\varphi) = P(\varphi|x) \times \frac{P(x)}{P(\varphi)}$$

Bayes for Sentiment Analysis

five tweets

am happy Because I am learning NLP.
am happy, not sad.

word

I
am

happy

because

learning

NLP

sad

not

negative tweets.

am sad, I am not learning NLP.
am sad, not happy

freq

word	Pos	neg	word	pos	neg
I	3	3	I	$P(I pos) = \frac{3}{13}$ = 0.24	$P(I neg) = \frac{3}{12}$ = 0.25
am	3	3	am	$P(am pos) = \frac{3}{13}$ = 0.24	$P(am neg) = \frac{3}{12}$ = 0.25
happy	2	1	happy	0.15	0.08
because	1	0	because	0.08	0.01
learning	1	1	learning	0.08	0.08
NLP	1	1	NLP	0.08	0.08
sad	1	2	sad	0.08	0.17
not	1	2	not	0.08	0.17
class	13	12			

ps in computing the
conditional probabilities
word in the class

$$P(W_i | \text{class})$$

(4) predict sentiment of whole tweet
eg, predict sentiment of whole tweet

Tweet: I am happy today ; I am Learning

$$\prod_{i=1}^m \frac{P(w_i | \text{pos})}{P(w_i | \text{neg})}$$

$\frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.14}{0.10} * \frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.10}{0.10}$

$$\equiv \frac{0.14}{0.10} \Rightarrow 1.4 > 1$$

(positive sentiment)

a nearly identical conditional probability, words the equally probable & don't add anything to the sent

These are your power words, These carry a lot of weights in determining in your tweet sentiments

conditional probability for the negative class is when this happens no way of comparing b/w positive tweets & negative tweets corpora.

which will become a problem for your calculations

$$\prod_{i=1}^m \frac{P(w_i | \text{Pos})}{P(w_i | \text{Neg})}$$

Naïve Baye's inference conditional probabilities for binary classification

This expression says you are going to take the product of all of the words in your tweets of the probability for words in Positive class divide it by the prob. in neg. class

Bayes Classifier is a supervised learning algorithm based on Baye's theorem.

probabilistic classifier, which means it predicts on the probability of an object.

Theorem \rightarrow

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

$$P(B|A) = \frac{P(A \cap B)}{P(A)}$$

$$P(A|B) * P(B) = P(B|A) * P(A)$$

$$P(A \cap B) = \frac{P(B|A) * P(A)}{P(B)}$$

or

\Rightarrow Bayes Theorem

$$P(Y|X) = \frac{P(X|Y) * P(Y)}{P(X)}$$

where Y is class variable and X is dependent feature vector

$$\hookrightarrow (x_1, x_2, x_3, \dots, x_n)$$

$$P(Y|x_1, x_2, \dots, x_n) = \frac{P(Y) * P(x_1, x_2, x_3, \dots, x_n | Y)}{P(x_1, x_2, x_3, \dots, x_n)}$$

$$\rightarrow \frac{P(Y) * P(x_1|y_1) * P(x_2|y_2) * \dots * P(x_n|y_n)}{(P(x_1) * P(x_2) * P(x_3) * \dots * P(x_n))}$$

"yes or no / 0 or 1 / T or F."

	Outlook	Temp	Humidity	Wind	Play
1	Sunny	Hot	High	Weak	No
2	Sunny	Hot	High	Strong	No
3	Overcast	Hot	High	Weak	Yes
4	Rain	Mild	High	Weak	Yes
5	Rain	Cool	Normal	Weak	Yes
6	Rain	Cool	Normal	Strong	No
7	Overcast	Cool	Normal	Strong	Yes
8	Sunny	Mild	High	Weak	No
9	Sunny	Cool	Normal	Weak	Yes
10	Rain	Mild	Normal	Strong	Yes
11	Sunny	Mild	Normal	Strong	Yes
12	Overcast	Mild	High	Strong	Yes
13	Overcast	Hot	Normal	Weak	Yes
14	Rain	Mild	High	Strong	No
15	Sunny	Cool	High	Strong	?

Day 15

$$P(\text{Yes} | \text{sunny}, \text{cool}, \text{high}, \text{strong})$$

↑
class
variable

↓
dependent feature vector

$$\Rightarrow P(\text{Yes}) * P(\text{sunny}, \text{cool}, \text{high}, \text{strong} | \text{Yes})$$

$$P(\text{sunny}, \text{cool}, \text{high}, \text{strong})$$

$$\Rightarrow P(\text{Yes}) * P(\text{sunny} | \text{Yes}) * P(\text{cool} | \text{Yes, sunny}) * P(\text{high}$$

$$\text{Yes, sunny, cool}) * P(\text{strong} | \text{Yes, sunny, cool})$$

$$P(\text{sunny}, \text{cool}, \text{high}, \text{strong})$$

$$\rightarrow \frac{9}{14} * \frac{2/14}{9/14} * \frac{3}{9} * \frac{3}{9} * \frac{4}{9} \Rightarrow \frac{g \rightarrow 2 \times 3 \times 1}{14 \times 9 \times 9 \times 9}$$

↑ $P(\text{high} | \text{Yes})$ $\rightarrow P(\text{strong} | \text{Yes})$

$$\frac{P(\text{cool} \cap \text{Yes} \cap \text{sunny})}{P(\text{Yes})} \rightarrow P(\text{cool} | \text{Yes})$$

$$\rightarrow 0.007$$

Sunny, cool, high, strong
 ↓
 dependent feature vector

$$P(\text{No}) * P(\text{sunny} | \text{No}) * P(\text{cool} | \text{No}, \text{sunny}) * P(\text{high} | \text{No}, \text{sunny}, \text{cool}) * P(\text{strong} | \text{No}, \text{sunny}, \text{cool}, \text{high})$$

$$P(\text{No}) * P(\text{sunny} | \text{No}) * P(\text{cool} | \text{No}) * P(\text{high} | \text{No}) * P(\text{strong} | \text{No})$$

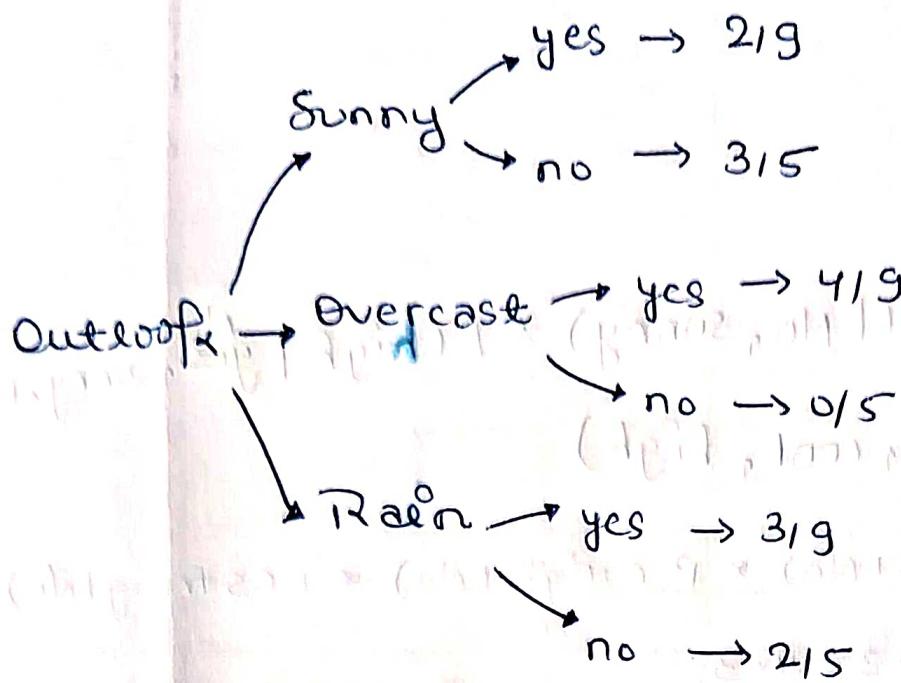
$$* \frac{3}{5} * \frac{1}{5} * \frac{4}{5} * \frac{3}{5} \rightarrow \frac{5 \times 3 \times 14 \times 3}{14 \times 5 \times 5 \times 5} \rightarrow 0.0206$$

$$\begin{array}{ll} \xrightarrow{\text{yes}} & P(\text{strong} | \text{yes}) = 4/9 \quad \frac{P(\text{strong} \cap \text{yes})}{P(\text{yes})} \\ \xrightarrow{\text{strong}} & \xrightarrow{\text{no}} P(\text{strong} | \text{no}) = 3/5 \quad \frac{P(\text{strong} \cap \text{no})}{P(\text{no})} \\ \xrightarrow{\text{weak}} & \xrightarrow{\text{yes}} P(\text{weak} | \text{yes}) = 5/9 \\ & \xrightarrow{\text{no}} P(\text{weak} | \text{no}) = 2/5 \end{array}$$

$$\begin{array}{ll} \xrightarrow{\text{yes}} & P(\text{High} | \text{yes}) = \frac{P(\text{High} \cap \text{yes})}{P(\text{yes})} \rightarrow 3/9 \\ \xrightarrow{\text{High}} & \xrightarrow{\text{No}} P(\text{High} | \text{No}) = \frac{P(\text{High} \cap \text{No})}{P(\text{No})} \rightarrow 4/5 \\ \xrightarrow{\text{Normal}} & \xrightarrow{\text{yes}} P(\text{Normal} | \text{yes}) = \frac{P(\text{Normal} \cap \text{yes})}{P(\text{yes})} \rightarrow 6/9 \\ & \xrightarrow{\text{No}} P(\text{Normal} | \text{No}) = \frac{P(\text{Normal} \cap \text{No})}{P(\text{No})} \rightarrow 1/5 \end{array}$$

$$\begin{array}{ll} \xrightarrow{\text{Hot}} & \xrightarrow{\text{yes}} 2/9 \\ & \xrightarrow{\text{no}} 2/5 \\ \xrightarrow{\text{Mid}} & \xrightarrow{\text{yes}} 4/9 \\ & \xrightarrow{\text{no}} 2/5 \\ \xrightarrow{\text{Cold}} & \xrightarrow{\text{yes}} 3/9 \\ & \xrightarrow{\text{no}} 1/5 \end{array}$$

⑨



Laplacian Smoothing :

(ii)

Sometimes you try to calculate the probability of a word happening after a word. To do that you might want to count the nos of times those two words showed up. One after another, divided by the number of times the first word appears. Now what if the two words never showed up next to each other in the training corpus. You get a probability of zero, and the probability of an entire sequence might go to zero.

Now, how can we fix this?

$$\text{previously, } P(w_i | \text{class}) = \frac{\text{freq}(w_i; \text{class})}{N_{\text{class}}}$$

Class $\in \{\text{positive, negative}\}$

N_{class} = frequency of all words in class

V_{class} = nos of unique words in class

$$P(w_i | \text{class}) = \frac{\text{freq}(w_i | \text{class}) + 1}{N_{\text{class}} + V_{\text{class}}} \quad \begin{matrix} \rightarrow \\ \text{avoids the prob.} \\ \text{being zero.} \end{matrix}$$

[Laplacian Smoothing].

word	pos	neg	word	pos	neg
I	3	3		$P(I pos)$	
am	3	3		$\Rightarrow \frac{3+1}{13+8}$	
happy	2	1	I		
Because	1	0	$\Rightarrow [0, 19]$		
Learning	1	1		0.19	
NLP	1	1			
sad	1	2	happy	0.14	0.1
not	1	2	Because	0.10	0.09

Nclass $\downarrow V=8$ (Review Report)

$\sum_{i=1}^m P(w_i|pos) = 1.12$

[Laplacian Smoothing]

• Laplacian smoothing to avoid $\prod_{i=1}^m \frac{P(w_i|pos)}{P(w_i|neg)}$

$P(w_i|class)$

$$\frac{\sum_{i=1}^m (P(w_i|pos) + 1)}{m} = \frac{0.19 + 0.19}{2} = 0.19$$

$$\Rightarrow \frac{0.000005054}{0.0000045} \Rightarrow 1.12 > 1$$