Lecture 4-1

NumPy

Week 4 Monday

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Based on Python Data Science Handbook by Jake VanderPlas

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This is a convention that everyone follows. If you do not do this, other people will have a hard time reading your code

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In [2]:
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np.__version__
```

Out[2]:
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'1.19.2'
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Out[2]:
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'1.19.2'
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Numpy arrays

- like lists, arrays are mutable
- unlike lists, arrays can only contain data of the same data type

Making Arrays

- direct creation with `np.array()`
- Create a list with square brackets, and put that inside `np.array()`

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np.array( [1,2,3] )
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Out[3]:
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array([1, 2, 3])
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np.array( [1,2,3] )
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Out[3]:
```
array([1, 2, 3])
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In [4]:
```
a = np.array([1, 2, 3])
print(a) # printing an array appears different from the array([]) in ipython
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```
[1 2 3]
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In [5]:
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print([1,2,3]) # a printed list has commas
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A printed array has no commas. A printed list has commas.

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```
[1, 2, 3]
```

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In [6]:
```
type(a)
```

Out[6]:
```
numpy.ndarray
```

Upcasting

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In [7]:

```
b = np.array([1, 2, 3.0, False, True])
print(b) # the 3.0 is a float and will upcast (coerce) other values to floats
```

```
[1. 2. 3. 0. 1.]
```

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print(b) # the 3.0 is a float and will upcast (coerce) other values to floats
```

```
[1. 2. 3. 0. 1.]
```

In [8]:

```
c = np.array([1, 2, "3", True, False]) # upcast (coerced) to strings
print(c)
```

```
['1' '2' '3' 'True' 'False']
```

Arrays in Higher dimensions

If you provide a list of lists, you can create a multi-dimensional array. (Like a matrix)

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In [9]:

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```
[[1 2 3]
 [4 5 6]]
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When you print a multidimensional array, the number of opening square brackets is the number of dimensions. The above array is 2 dimensional.

but if the dimensions don't match, you'll get an array of lists... which is not as useful.

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but if the dimensions don't match, you'll get an array of lists... which is not as useful.

In [10]:

```
e = np.array([ [1,2,3],[4,5] ])
print(e)
```

```
[list([1, 2, 3]) list([4, 5])]
```

```
C:\Users\miles\anaconda3\lib\site-packages\ipykernel_launcher.py:1: VisibleDeprec
ationWarning: Creating an ndarray from ragged nested sequences (which is a list-o
r-tuple of lists-or-tuples-or ndarrays with different lengths or shapes) is depre
cated. If you meant to do this, you must specify 'dtype=object' when creating the
ndarray
  """Entry point for launching an IPython kernel.
```

Other ways to make arrays

Other ways to make arrays

In [11]:

```
np.zeros(5) # makes an array of 0s. similar to rep(0, 5)
```

Out[11]:

```
array([0., 0., 0., 0., 0.])
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In [12]:

```
np.zeros(5, dtype = int)  # default is to make floats, you can specify ints
```

Out[12]:

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```

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array([0, 0, 0, 0, 0])
```

In [13]:
```
np.zeros((2,4))  # give dimensions as a tuple: makes an array 2x4
```

Out[13]:
```
array([[0., 0., 0., 0.],
       [0., 0., 0., 0.]])
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```

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```
array([[0., 0., 0., 0.],
       [0., 0., 0., 0.]])
```

In [14]:

```
np.zeros((2,3,4)) # 3 dimensional array 2 x 3 x 4...
# notice the order of creation: 2 'sheets' of 3 rows by 4 columns
```

Out[14]:

```
array([[[0., 0., 0., 0.],
        [0., 0., 0., 0.],
        [0., 0., 0., 0.]],

       [[0., 0., 0., 0.],
        [0., 0., 0., 0.],
        [0., 0., 0., 0.]]])
```

In [15]:

```python
np.zeros((2,3,4,5))
# make 2 'blocks', each with 3 'sheets', of 4 rows, and 5 columns
```

Out[15]:

```
array([[[[0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.]],

        [[0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.]],

        [[0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.]]],


       [[[0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.]],

        [[0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.]],

        [[0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.],
         [0., 0., 0., 0., 0.]]]])
```

In addition to `np.zeros` there is `np.ones` and `np.full` which can create new arrays.

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np.ones(5)  # similar, but inserts ones
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Out[16]:
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array([1., 1., 1., 1., 1.])
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Out[16]:
```
array([1., 1., 1., 1., 1.])
```

In [17]:
```
np.full((2,3), 1.2)  # similar, but you specify one value that gets repeated
```

Out[17]:
```
array([[1.2, 1.2, 1.2],
       [1.2, 1.2, 1.2]])
```

Making arrays of random numbers

numpy uses the Mersenne Twister

- All random generator functions begin with `np.random.`

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In [19]:
```
np.random.random(5)  # random.random for random values on the interval [0,1)
```

Out[19]:
```
array([4.17022005e-01, 7.20324493e-01, 1.14374817e-04, 3.02332573e-01,
       1.46755891e-01])
```

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       1.46755891e-01])
```

In [20]:
```
np.random.randn(5)
# random.randn for random normal from standard normal
# this command will produce 5 values
```

Out[20]:
```
array([-1.10593508, -1.65451545, -2.3634686 ,  1.13534535, -1.01701414])
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```

In [21]:
```
np.random.normal(10, 3, (2, 4))
# random.randn for random normal from normal with mean 10 and sd 3
# arranged in a 2 x 4 matrix
```

Out[21]:
```
array([[11.91208544,  7.42028018, 15.31782289,  6.66891084],
       [10.5436428 , 11.6930346 ,  8.30046931, 12.18992679]])
```

In [22]:

```
np.random.randint(0, 10, 20)
# select random integers from 0 inclusive to 10 exclusive
# and return 20 values
```

Out[22]:

```
array([1, 8, 8, 3, 9, 8, 7, 3, 6, 5, 1, 9, 3, 4, 8, 1, 4, 0, 3, 9])
```

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Out[22]:
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```

In [23]:
```
# simulate dice rolls
np.random.randint(1,7, 50)
```

Out[23]:
```
array([3, 1, 5, 2, 3, 3, 2, 1, 2, 4, 6, 5, 4, 6, 2, 4, 1, 1, 3, 3, 2, 4,
       5, 3, 1, 1, 2, 2, 6, 4, 1, 1, 6, 6, 5, 6, 3, 5, 4, 6, 4, 6, 1, 4,
       5, 4, 5, 5, 6, 5])
```

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# select random integers from 0 inclusive to 10 exclusive
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Out[22]:

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array([1, 8, 8, 3, 9, 8, 7, 3, 6, 5, 1, 9, 3, 4, 8, 1, 4, 0, 3, 9])
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Out[23]:

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array([3, 1, 5, 2, 3, 3, 2, 1, 2, 4, 6, 5, 4, 6, 2, 4, 1, 1, 3, 3, 2, 4,
       5, 3, 1, 1, 2, 2, 6, 4, 1, 1, 6, 6, 5, 6, 3, 5, 4, 6, 4, 6, 1, 4,
       5, 4, 5, 5, 6, 5])
```

More random generation at: https://docs.scipy.org/doc/numpy-1.15.1/reference/routines.random.html

Array sequences

make sequences with

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- makes an **a**rray **range** from start (inclusive) to stop (exclusive), by step

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range(0, 10, 2) # range object in regular python
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range(0, 10, 2) # range object in regular python
```

Out[24]:
```
range(0, 10, 2)
```

In [25]:
```
list(range(0, 10, 2))
```

Out[25]:
```
[0, 2, 4, 6, 8]
```

In [26]:
```
np.arange(0, 10, 2)  # numpy's arange function
```

Out[26]:
```
array([0, 2, 4, 6, 8])
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In [27]:

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np.array(range(0,10,2)) # equivalent 'manual' creation
```

Out[27]:

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array([0, 2, 4, 6, 8])
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Out[27]:
```
array([0, 2, 4, 6, 8])
```

In [28]:
```python
np.arange(0, 100, 5)
```

Out[28]:
```
array([ 0,  5, 10, 15, 20, 25, 30, 35, 40, 45, 50, 55, 60, 65, 70, 75, 80,
       85, 90, 95])
```

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array([0, 2, 4, 6, 8])
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       85, 90, 95])
```

In [29]:
```python
np.arange(20) # quickest
```

Out[29]:
```
array([ 0,  1,  2,  3,  4,  5,  6,  7,  8,  9, 10, 11, 12, 13, 14, 15, 16,
       17, 18, 19])
```

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- makes an array of **lin**ear **space**d values beginning with start, ending with stop (inclusive), with a length of num

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In [30]:
```
np.linspace(0, 100, 11)
```

Out[30]:
```
array([  0.,  10.,  20.,  30.,  40.,  50.,  60.,  70.,  80.,  90., 100.])
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Out[30]:
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```

In [31]:
```
np.linspace(0, 100, 10)
```

Out[31]:
```
array([  0.        ,  11.11111111,  22.22222222,  33.33333333,
        44.44444444,  55.55555556,  66.66666667,  77.77777778,
        88.88888889, 100.        ])
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        88.88888889, 100.        ])
```

In [32]:
```
np.linspace(0, 100, 10, endpoint = False)  # optional parameter endpoint to exclude the stop value
```

Out[32]:
```
array([ 0., 10., 20., 30., 40., 50., 60., 70., 80., 90.])
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```
In [32]:
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```
Out[32]:
```
array([ 0., 10., 20., 30., 40., 50., 60., 70., 80., 90.])
```
In [33]:
```
np.linspace(0, 100, 9, endpoint = False)
# if you use the endpoint argument, the last number in the array will depend on the output length
```
Out[33]:
```
array([ 0.        , 11.11111111, 22.22222222, 33.33333333, 44.44444444,
       55.55555556, 66.66666667, 77.77777778, 88.88888889])
```

Array Attributes

- `array.ndim` for number of dimensions
- `array.shape` for the size of each dimension
- `array.dtype` for the data type

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In [34]:

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x = np.ones((3,4))
print(x)
```

```
[[1. 1. 1. 1.]
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In [35]:
```
x.ndim
```

Out[35]:
```
2
```

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```

In [35]:
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x.ndim
```

Out[35]:
```
2
```

In [36]:
```
x.shape
```

Out[36]:
```
(3, 4)
```

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[[1. 1. 1. 1.]
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In [35]:
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x.ndim
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Out[35]:
```
2
```

In [36]:
```
x.shape
```

Out[36]:
```
(3, 4)
```

In [37]:
```
x.dtype
```

Out[37]:
```
dtype('float64')
```

In [38]:

```python
y = np.arange(0, 12, 1)
print(y)
```

```
[ 0  1  2  3  4  5  6  7  8  9 10 11]
```

In [38]:
```
y = np.arange(0, 12, 1)
print(y)
```

```
[ 0  1  2  3  4  5  6  7  8  9 10 11]
```

In [39]:
```
y.ndim
```

Out[39]:
```
1
```

In [38]:
```
y = np.arange(0, 12, 1)
print(y)
```

```
[ 0  1  2  3  4  5  6  7  8  9 10 11]
```

In [39]:
```
y.ndim
```

Out[39]:
```
1
```

In [40]:
```
y.shape # a one dimensional array. Note that there's no second dimension.
```

Out[40]:
```
(12,)
```

Reshaping Arrays

- `np.reshape(array, [new shape])` returns a new array that is reshaped
    - you can also use the method `array.reshape(shape)`
- `array.T` is the transpose method, but leaves the original array unaffected

Reshaping Arrays

- `np.reshape(array, [new shape])` returns a new array that is reshaped
    - you can also use the method `array.reshape(shape)`
- `array.T` is the transpose method, but leaves the original array unaffected

In [41]:

```
j = np.arange(0,12,1)
print(j) # j is one dimensional
```

```
[ 0  1  2  3  4  5  6  7  8  9 10 11]
```

Reshaping Arrays

- `np.reshape(array, [new shape])` returns a new array that is reshaped
    - you can also use the method `array.reshape(shape)`
- `array.T` is the transpose method, but leaves the original array unaffected

In [41]:

```
j = np.arange(0,12,1)
print(j) # j is one dimensional
```

```
[ 0  1  2  3  4  5  6  7  8  9 10 11]
```

In [42]:

```
k = np.reshape(j, (3,4))  # note that it fills row-wise unlike R
print(k)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

Reshaping Arrays

- `np.reshape(array, [new shape])` returns a new array that is reshaped
    - you can also use the method `array.reshape(shape)`
- `array.T` is the transpose method, but leaves the original array unaffected

In [41]:
```
j = np.arange(0,12,1)
print(j) # j is one dimensional
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```
[ 0  1  2  3  4  5  6  7  8  9 10 11]
```

In [42]:
```
k = np.reshape(j, (3,4))  # note that it fills row-wise unlike R
print(k)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [43]:
```
j # j is left unchanged
```

Out[43]:
```
array([ 0,  1,  2,  3,  4,  5,  6,  7,  8,  9, 10, 11])
```

In [44]:
```python
j.reshape(4,3)  # you can also call the method reshape() on the array j
```

Out[44]:
```
array([[ 0,  1,  2],
       [ 3,  4,  5],
       [ 6,  7,  8],
       [ 9, 10, 11]])
```

In [44]:

```
j.reshape(4,3)  # you can also call the method reshape() on the array j
```

Out[44]:

```
array([[ 0,  1,  2],
       [ 3,  4,  5],
       [ 6,  7,  8],
       [ 9, 10, 11]])
```

In [45]:

```
j # j is left unchanged here as well
```

Out[45]:

```
array([ 0,  1,  2,  3,  4,  5,  6,  7,  8,  9, 10, 11])
```

In [46]:

```
print(k)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [46]:

```
print(k)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [47]:

```
print(k.T)  # the transpose of k
```

```
[[ 0  4  8]
 [ 1  5  9]
 [ 2  6 10]
 [ 3  7 11]]
```

In [46]:

```python
print(k)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [47]:

```python
print(k.T)  # the transpose of k
```

```
[[ 0  4  8]
 [ 1  5  9]
 [ 2  6 10]
 [ 3  7 11]]
```

In [48]:

```python
print(k) # calling k.T does not modify the original k array
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [49]:

```
# can combine the above methods and steps into one:
l = np.arange(0,12,1).reshape((3,4)).T
# create a-range >> reshape >> transpose
print(l)
```

```
[[ 0  4  8]
 [ 1  5  9]
 [ 2  6 10]
 [ 3  7 11]]
```

In [50]:

```
y = np.arange(0,12, 1)
print(y)
```

```
[ 0  1  2  3  4  5  6  7  8  9 10 11]
```

In [50]:

```
y = np.arange(0,12, 1)
print(y)
```

```
[ 0  1  2  3  4  5  6  7  8  9 10 11]
```

In [51]:

```
y.shape
```

Out[51]:

```
(12,)
```

In [50]:
```
y = np.arange(0,12, 1)
print(y)
```

```
[ 0  1  2  3  4  5  6  7  8  9 10 11]
```

In [51]:
```
y.shape
```

Out[51]:
```
(12,)
```

In [52]:
```
print(y.T) # the transpose of a one dimensional array doesn't suddenly give it a second dimension
```

```
[ 0  1  2  3  4  5  6  7  8  9 10 11]
```

In [50]:
```python
y = np.arange(0,12, 1)
print(y)
```

```
[ 0  1  2  3  4  5  6  7  8  9 10 11]
```

In [51]:
```python
y.shape
```

Out[51]:
```
(12,)
```

In [52]:
```python
print(y.T) # the transpose of a one dimensional array doesn't suddenly give it a second dimension
```

```
[ 0  1  2  3  4  5  6  7  8  9 10 11]
```

In [53]:
```python
y.T.shape
```

Out[53]:
```
(12,)
```

In [54]:

```
z = np.reshape(y, (1,12)) # the array now has two dimensions
print(z)
```

```
[[ 0  1  2  3  4  5  6  7  8  9 10 11]]
```

In [54]:
```
z = np.reshape(y, (1,12)) # the array now has two dimensions
print(z)
```

```
[[ 0  1  2  3  4  5  6  7  8  9 10 11]]
```

In [55]:
```
z.shape
```

Out[55]:
```
(1, 12)
```

In [54]:
```python
z = np.reshape(y, (1,12)) # the array now has two dimensions
print(z)
```

```
[[ 0  1  2  3  4  5  6  7  8  9 10 11]]
```

In [55]:
```python
z.shape
```

Out[55]:
```
(1, 12)
```

In [56]:
```python
print(z.T)  # with two dimensions, the transpose become a column
```

```
[[ 0]
 [ 1]
 [ 2]
 [ 3]
 [ 4]
 [ 5]
 [ 6]
 [ 7]
 [ 8]
 [ 9]
 [10]
 [11]]
```

In [54]:
```
z = np.reshape(y, (1,12)) # the array now has two dimensions
print(z)
```

```
[[ 0  1  2  3  4  5  6  7  8  9 10 11]]
```

In [55]:
```
z.shape
```

Out[55]:
```
(1, 12)
```

In [56]:
```
print(z.T)  # with two dimensions, the transpose become a column
```

```
[[ 0]
 [ 1]
 [ 2]
 [ 3]
 [ 4]
 [ 5]
 [ 6]
 [ 7]
 [ 8]
 [ 9]
 [10]
 [11]]
```

In [57]:
```
z.T.shape
```

Out[57]:
```
(12, 1)
```

Subsetting and Slicing Arrays

- very similar to subsetting and slicing lists

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- very similar to subsetting and slicing lists

In [59]:
```
y[4]
```

Out[59]:
```
4
```

Subsetting and Slicing Arrays

- very similar to subsetting and slicing lists

In [59]:
```
y[4]
```
Out[59]:
```
4
```
In [60]:
```
y.shape
```
Out[60]:
```
(12,)
```

Subsetting and Slicing Arrays

- very similar to subsetting and slicing lists

In [59]:
```
y[4]
```
Out[59]:
```
4
```
In [60]:
```
y.shape
```
Out[60]:
```
(12,)
```
In [61]:
```
y[4:6]
```
Out[61]:
```
array([4, 5])
```

you can slice with a second colon. The array gets subset with `array[start:stop:step]`

you can slice with a second colon. The array gets subset with `array[start:stop:step]`

In [62]:
```
y[1:8:3]
```

Out[62]:
```
array([1, 4, 7])
```

you can slice with a second colon. The array gets subset with `array[start:stop:step]`

In [62]:
```
y[1:8:3]
```

Out[62]:
```
array([1, 4, 7])
```

In [63]:
```
np.arange(100)[:100:2] # to get even values
```

Out[63]:
```
array([ 0,  2,  4,  6,  8, 10, 12, 14, 16, 18, 20, 22, 24, 26, 28, 30, 32,
       34, 36, 38, 40, 42, 44, 46, 48, 50, 52, 54, 56, 58, 60, 62, 64, 66,
       68, 70, 72, 74, 76, 78, 80, 82, 84, 86, 88, 90, 92, 94, 96, 98])
```

you can slice with a second colon. The array gets subset with `array[start:stop:step]`

In [62]:
```
y[1:8:3]
```
Out[62]:
```
array([1, 4, 7])
```
In [63]:
```
np.arange(100)[:100:2] # to get even values
```
Out[63]:
```
array([ 0,  2,  4,  6,  8, 10, 12, 14, 16, 18, 20, 22, 24, 26, 28, 30, 32,
       34, 36, 38, 40, 42, 44, 46, 48, 50, 52, 54, 56, 58, 60, 62, 64, 66,
       68, 70, 72, 74, 76, 78, 80, 82, 84, 86, 88, 90, 92, 94, 96, 98])
```
In [64]:
```
np.arange(0,100,2)
```
Out[64]:
```
array([ 0,  2,  4,  6,  8, 10, 12, 14, 16, 18, 20, 22, 24, 26, 28, 30, 32,
       34, 36, 38, 40, 42, 44, 46, 48, 50, 52, 54, 56, 58, 60, 62, 64, 66,
       68, 70, 72, 74, 76, 78, 80, 82, 84, 86, 88, 90, 92, 94, 96, 98])
```

Subsetting and slicing higher dimensional arrays is similar, and uses a comma to separate subsetting instructions for each dimension.

Subsetting and slicing higher dimensional arrays is similar, and uses a comma to separate subsetting instructions for each dimension.

In [65]:

```
z = np.reshape(y, [3,4])
print(z)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

Subsetting and slicing higher dimensional arrays is similar, and uses a comma to separate subsetting instructions for each dimension.

In [65]:
```
z = np.reshape(y, [3,4])
print(z)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [66]:
```
print(z[1,2]) # returns what is at row index 1, col index 2
```

```
6
```

Subsetting and slicing higher dimensional arrays is similar, and uses a comma to separate subsetting instructions for each dimension.

In [65]:

```
z = np.reshape(y, [3,4])
print(z)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [66]:

```
print(z[1,2]) # returns what is at row index 1, col index 2
```

```
6
```

In [67]:

```
type(z[1,2]) # with only one value, the type is the integer. It is no longer an array.
```

Out[67]:

```
numpy.int32
```

In [68]:

```
print(z)
z[0:2, 0:2] # note the type remains a numpy array
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

Out[68]:

```
array([[0, 1],
       [4, 5]])
```

In [68]:

```python
print(z)
z[0:2, 0:2] # note the type remains a numpy array
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

Out[68]:

```
array([[0, 1],
       [4, 5]])
```

In [69]:

```python
print(z[2, :]) # returns row at index 2
```

```
[ 8  9 10 11]
```

In [68]:
```
print(z)
z[0:2, 0:2] # note the type remains a numpy array
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

Out[68]:
```
array([[0, 1],
       [4, 5]])
```

In [69]:
```
print(z[2, :]) # returns row at index 2
```

```
[ 8  9 10 11]
```

In [70]:
```
z[2, :].shape  # the shape is one dimensional
```

Out[70]:
```
(4,)
```

In [68]:
```
print(z)
z[0:2, 0:2] # note the type remains a numpy array
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

Out[68]:
```
array([[0, 1],
       [4, 5]])
```

In [69]:
```
print(z[2, :]) # returns row at index 2
```

```
[ 8  9 10 11]
```

In [70]:
```
z[2, :].shape  # the shape is one dimensional
```

Out[70]:
```
(4,)
```

In [71]:
```
print(z[:,2]) # returns column at index 2
```

```
[ 2  6 10]
```

In [68]:
```
print(z)
z[0:2, 0:2] # note the type remains a numpy array
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

Out[68]:
```
array([[0, 1],
       [4, 5]])
```

In [69]:
```
print(z[2, :]) # returns row at index 2
```

```
[ 8  9 10 11]
```

In [70]:
```
z[2, :].shape  # the shape is one dimensional
```

Out[70]:
```
(4,)
```

In [71]:
```
print(z[:,2]) # returns column at index 2
```

```
[ 2  6 10]
```

In [72]:
```
z[:,2].shape # shape is one dimensional
```

Out[72]:
```
(3,)
```

Slices of numpy arrays are view objects, and automatically update if the original array is updated.

Slices of numpy arrays are view objects, and automatically update if the original array is updated.

In [73]:
```
z = np.arange(12).reshape([3,4])
print(z)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

Slices of numpy arrays are view objects, and automatically update if the original array is updated.

In [73]:
```
z = np.arange(12).reshape([3,4])
print(z)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [74]:
```
# we use numpy array slicing to create z_sub, the top left corner of z
z_sub = z[:2, :2]
print(z_sub)
```

```
[[0 1]
 [4 5]]
```

Slices of numpy arrays are view objects, and automatically update if the original array is updated.

In [73]:

```
z = np.arange(12).reshape([3,4])
print(z)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [74]:

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# we use numpy array slicing to create z_sub, the top left corner of z
z_sub = z[:2, :2]
print(z_sub)
```

```
[[0 1]
 [4 5]]
```

In [75]:

```
# I modify the first element of z to be 99.
z[0,0] = 99
```

Slices of numpy arrays are view objects, and automatically update if the original array is updated.

In [73]:

```
z = np.arange(12).reshape([3,4])
print(z)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [74]:

```
# we use numpy array slicing to create z_sub, the top left corner of z
z_sub = z[:2, :2]
print(z_sub)
```

```
[[0 1]
 [4 5]]
```

In [75]:

```
# I modify the first element of z to be 99.
z[0,0] = 99
```

In [76]:

```
print(z_sub)  # z_sub is updated, even though we never redefined it
```

```
[[99  1]
 [ 4  5]]
```

Slices of numpy arrays are view objects, and automatically update if the original array is updated.

In [73]:
```
z = np.arange(12).reshape([3,4])
print(z)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [74]:
```
# we use numpy array slicing to create z_sub, the top left corner of z
z_sub = z[:2, :2]
print(z_sub)
```

```
[[0 1]
 [4 5]]
```

In [75]:
```
# I modify the first element of z to be 99.
z[0,0] = 99
```

In [76]:
```
print(z_sub)  # z_sub is updated, even though we never redefined it
```

```
[[99  1]
 [ 4  5]]
```

In [77]:
```
z
```

Out[77]:
```
array([[99,  1,  2,  3],
       [ 4,  5,  6,  7],
```

```
       [ 8,  9, 10, 11]])
```

In [78]:

```python
z = np.arange(15).reshape([3,5]) # here z gets redefined to an entirely new object
# we are not modifying the object that used to be called z
# we created a new object, and the name z now points to the new object
```

In [78]:

```
z = np.arange(15).reshape([3,5]) # here z gets redefined to an entirely new object
# we are not modifying the object that used to be called z
# we created a new object, and the name z now points to the new object
```

In [79]:

```
z
```

Out[79]:

```
array([[ 0,  1,  2,  3,  4],
       [ 5,  6,  7,  8,  9],
       [10, 11, 12, 13, 14]])
```

In [78]:
```
z = np.arange(15).reshape([3,5]) # here z gets redefined to an entirely new object
# we are not modifying the object that used to be called z
# we created a new object, and the name z now points to the new object
```

In [79]:
```
z
```

Out[79]:
```
array([[ 0,  1,  2,  3,  4],
       [ 5,  6,  7,  8,  9],
       [10, 11, 12, 13, 14]])
```

In [80]:
```
print(z_sub)  # the view z_sub still points to the object formerly known as z, which was not modifie
```

```
[[99  1]
 [ 4  5]]
```

If you want a copy that will not update if the original is updated, use `array.copy()`

If you want a copy that will not update if the original is updated, use `array.copy()`

In [81]:

```
print(z)
```

```
[[ 0  1  2  3  4]
 [ 5  6  7  8  9]
 [10 11 12 13 14]]
```

If you want a copy that will not update if the original is updated, use `array.copy()`

In [81]:
```
print(z)
```

```
[[ 0  1  2  3  4]
 [ 5  6  7  8  9]
 [10 11 12 13 14]]
```

In [82]:
```
z_sub_copy = z[:2, :2].copy()
print(z_sub_copy)
```

```
[[0 1]
 [5 6]]
```

If you want a copy that will not update if the original is updated, use `array.copy()`

In [81]:

```
print(z)
```

```
[[ 0  1  2  3  4]
 [ 5  6  7  8  9]
 [10 11 12 13 14]]
```

In [82]:

```
z_sub_copy = z[:2, :2].copy()
print(z_sub_copy)
```

```
[[0 1]
 [5 6]]
```

In [83]:

```
z[0,0] = 55 # modify the first element of z
```

If you want a copy that will not update if the original is updated, use `array.copy()`

```
In [81]: print(z)
```

```
[[ 0  1  2  3  4]
 [ 5  6  7  8  9]
 [10 11 12 13 14]]
```

```
In [82]: z_sub_copy = z[:2, :2].copy()
         print(z_sub_copy)
```

```
[[0 1]
 [5 6]]
```

```
In [83]: z[0,0] = 55 # modify the first element of z
```

```
In [84]: print(z_sub_copy) # the copy remains unaffected by the change
```

```
[[0 1]
 [5 6]]
```

If you want a copy that will not update if the original is updated, use `array.copy()`

In [81]:
```
print(z)
```

```
[[ 0  1  2  3  4]
 [ 5  6  7  8  9]
 [10 11 12 13 14]]
```

In [82]:
```
z_sub_copy = z[:2, :2].copy()
print(z_sub_copy)
```

```
[[0 1]
 [5 6]]
```

In [83]:
```
z[0,0] = 55 # modify the first element of z
```

In [84]:
```
print(z_sub_copy) # the copy remains unaffected by the change
```

```
[[0 1]
 [5 6]]
```

In [85]:
```
print(z)
```

```
[[55  1  2  3  4]
 [ 5  6  7  8  9]
 [10 11 12 13 14]]
```

Modifying the view object modifies the underlying array

Modifying the view object modifies the underlying array

In [86]:
```
z = np.arange(12).reshape((3,4))
print(z)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

Modifying the view object modifies the underlying array

In [86]:
```
z = np.arange(12).reshape((3,4))
print(z)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [87]:
```
view = z[:2,:2]
```

Modifying the view object modifies the underlying array

In [86]:

```
z = np.arange(12).reshape((3,4))
print(z)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [87]:

```
view = z[:2,:2]
```

In [88]:

```
view[0,0] = 99
```

Modifying the view object modifies the underlying array

In [86]:
```
z = np.arange(12).reshape((3,4))
print(z)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [87]:
```
view = z[:2,:2]
```

In [88]:
```
view[0,0] = 99
```

In [89]:
```
view
```

Out[89]:
```
array([[99,  1],
       [ 4,  5]])
```

Modifying the view object modifies the underlying array

In [86]:
```
z = np.arange(12).reshape((3,4))
print(z)
```

```
[[ 0  1  2  3]
 [ 4  5  6  7]
 [ 8  9 10 11]]
```

In [87]:
```
view = z[:2,:2]
```

In [88]:
```
view[0,0] = 99
```

In [89]:
```
view
```

Out[89]:
```
array([[99,  1],
       [ 4,  5]])
```

In [90]:
```
z
```

Out[90]:
```
array([[99,  1,  2,  3],
       [ 4,  5,  6,  7],
       [ 8,  9, 10, 11]])
```

In [91]:

```
type(view) # view objects themselves are arrays and have all the same methods and attributes
```

Out[91]:

```
numpy.ndarray
```

In [91]:

```python
type(view) # view objects themselves are arrays and have all the same methods and attributes
```

Out[91]:

```
numpy.ndarray
```

In [92]:

```python
view.T
```

Out[92]:

```
array([[99,  4],
       [ 1,  5]])
```

In [91]:
```
type(view) # view objects themselves are arrays and have all the same methods and attributes
```

Out[91]:
```
numpy.ndarray
```

In [92]:
```
view.T
```

Out[92]:
```
array([[99,  4],
       [ 1,  5]])
```

In [93]:
```
view.T.reshape((4,))
```

Out[93]:
```
array([99,  4,  1,  5])
```

In [91]:
```
type(view) # view objects themselves are arrays and have all the same methods and attributes
```
Out[91]:
```
numpy.ndarray
```
In [92]:
```
view.T
```
Out[92]:
```
array([[99,  4],
       [ 1,  5]])
```
In [93]:
```
view.T.reshape((4,))
```
Out[93]:
```
array([99,  4,  1,  5])
```
In [94]:
```
view # attributes like .T do not affect the orignal array
```
Out[94]:
```
array([[99,  1],
       [ 4,  5]])
```