

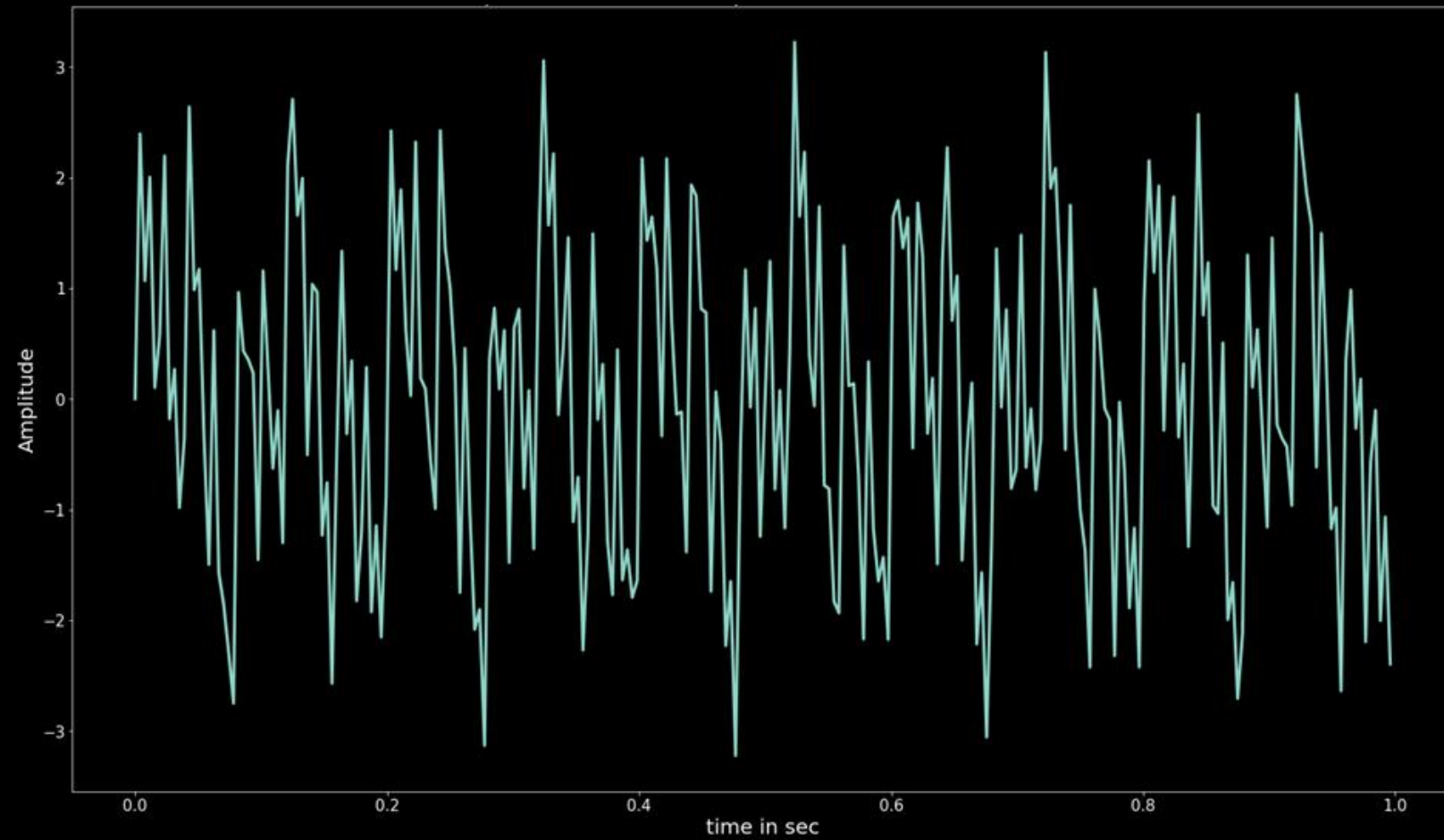
Frequency Domain Filtering

Topics to be covered

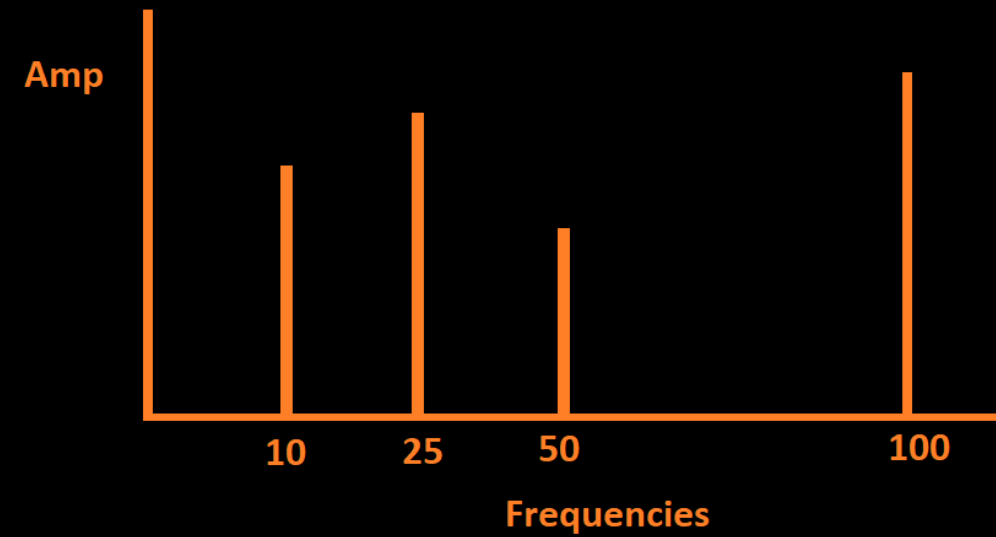
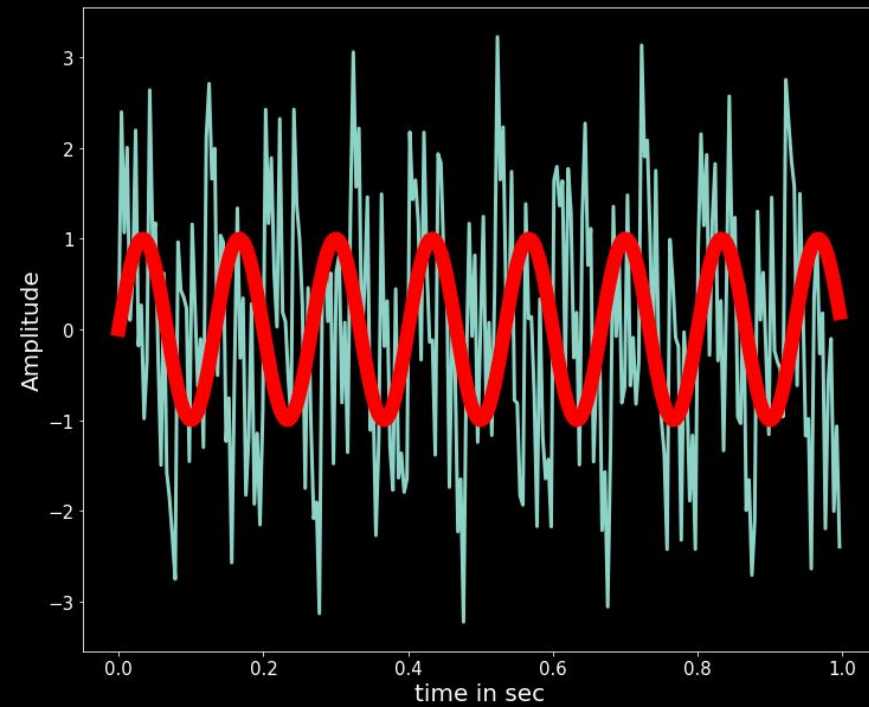
- 2D Fourier Transform
- Frequency Domain Filtering
- Low Pass Filter
- High Pass Filter
- High Boost and Other Filters

2D Fourier Transform

Signal with Frequencies 10, 25, 50 and 100 Hz

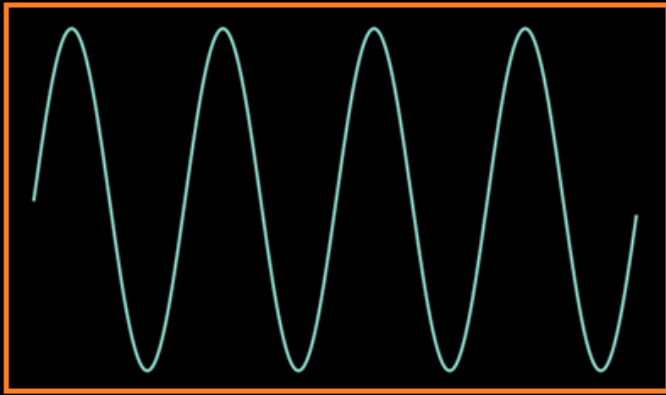


Signal with frequencies 10, 25, 50 and 100 Hz

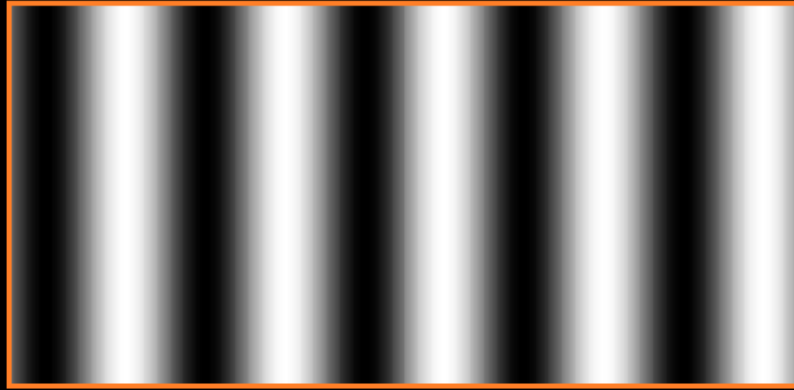


Sinusoidal gratings

A sinusoidal grating is a two-dimensional representation in which the amplitude varies sinusoidally along a certain direction.

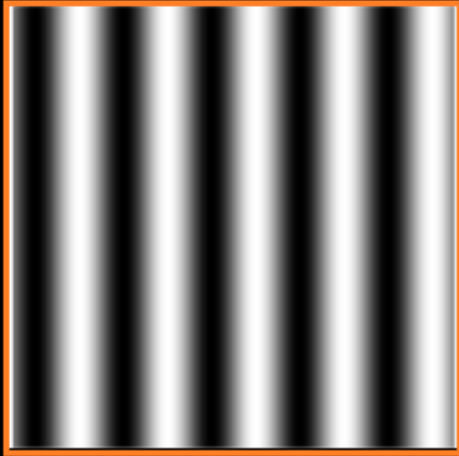


Sine Wave

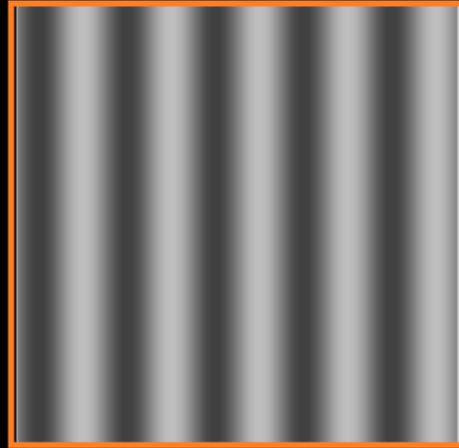


Grating of Sine Wave

Sinusoidal gratings



Large Amplitude

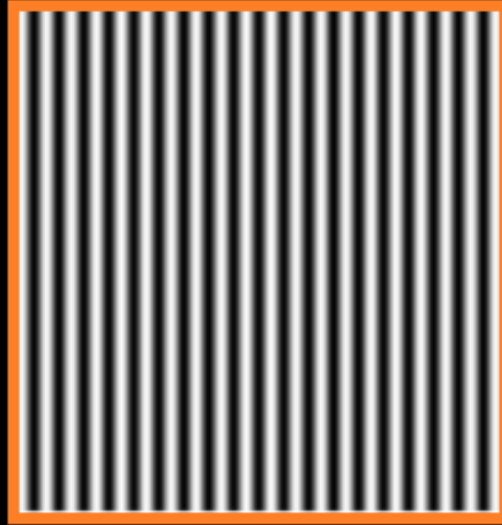


Small Amplitude

Sinusoidal gratings

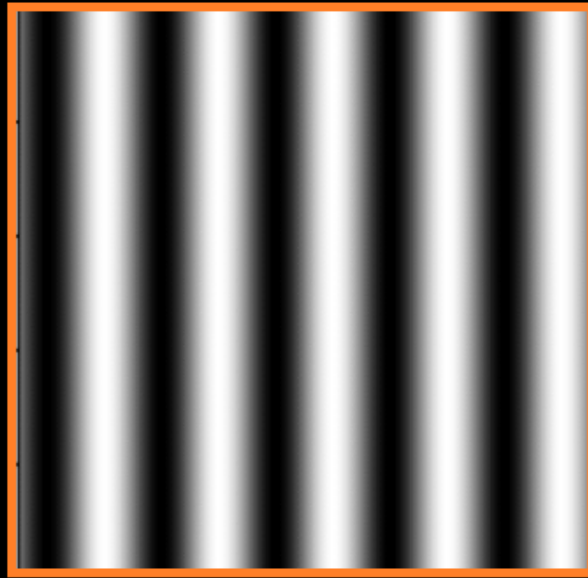


Low Frequency

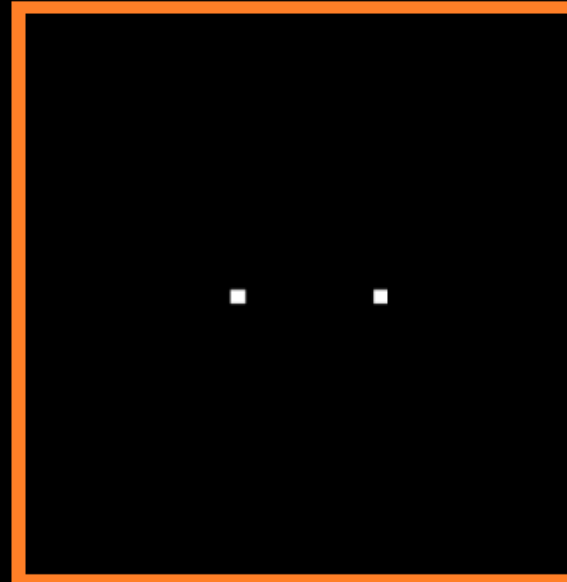


High Frequency

Fourier Transform of Grating

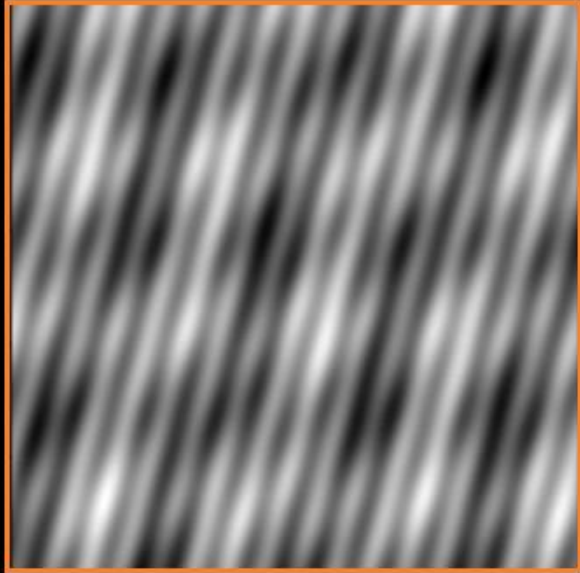


Grating

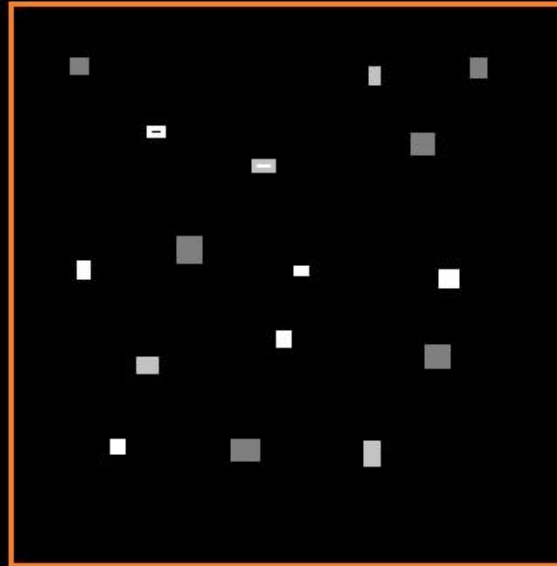


Fourier Transform

Fourier Transform of Grating



Grating

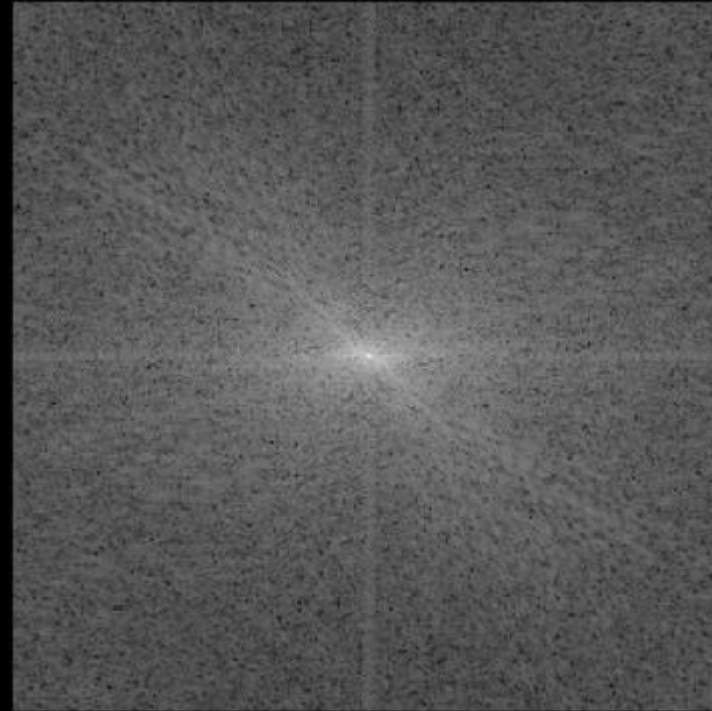


Fourier Transform

Fourier Transform of Image



Image

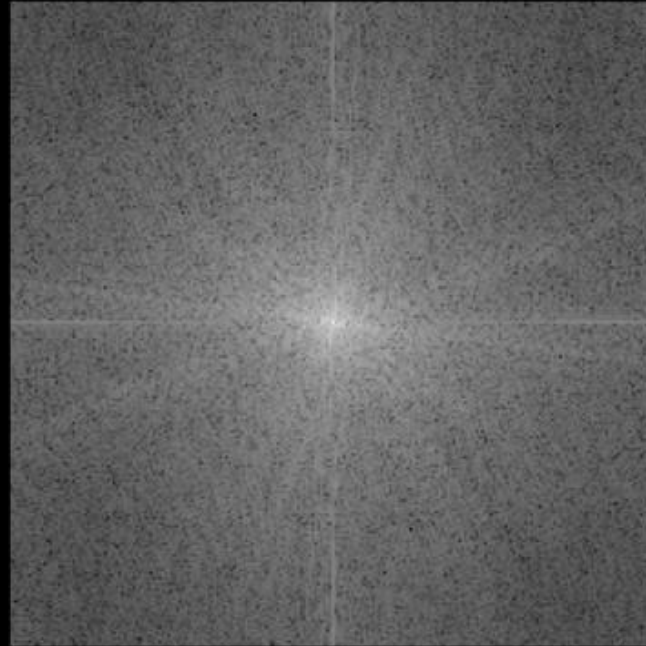


Fourier Transform

Fourier Transform of Image



Image



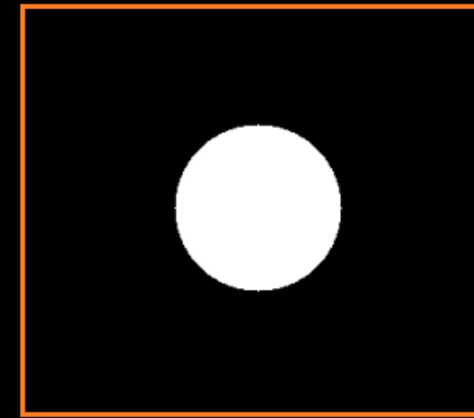
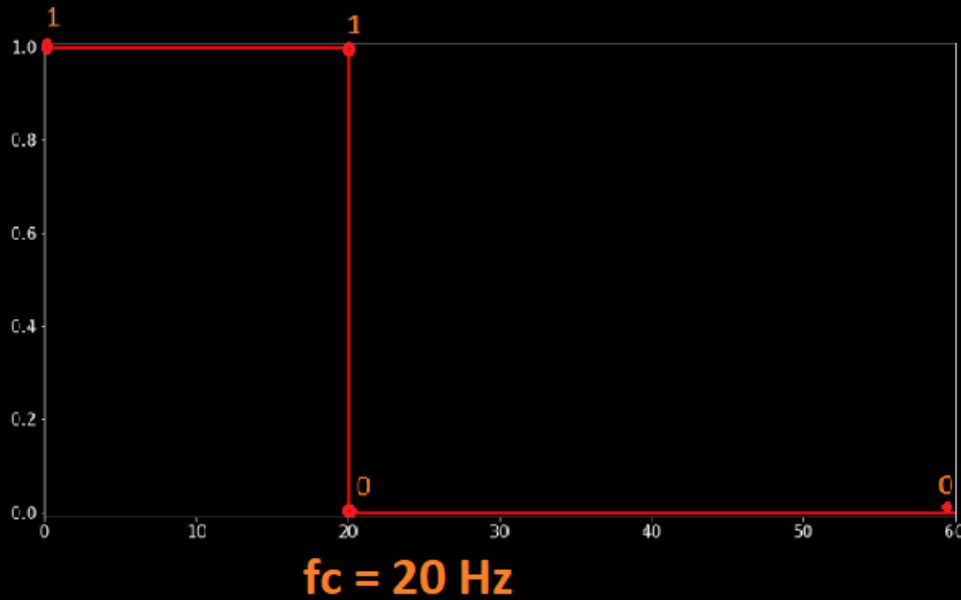
Fourier Transform

Frequency Domain Filtering

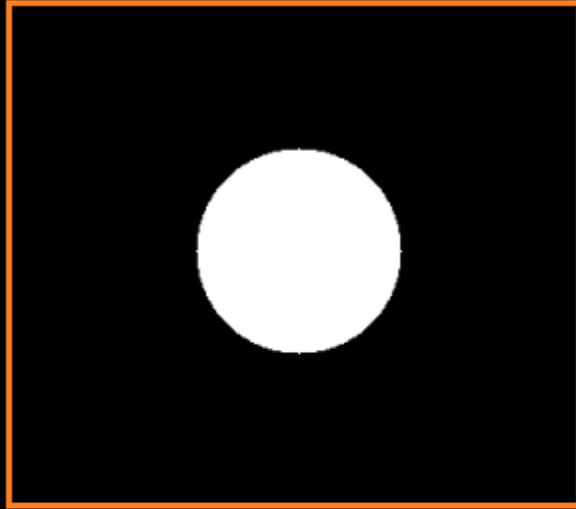
- Compute Fourier Transform of the image.
- Design a filter in frequency domain and define the cut-off frequency.
- Multiply the results of Fourier Transform of the image with the filter.
- Compute inverse Fourier Transform to get the filtered image.

Low Pass Filter

Low pass filter enhances all frequency components within a specified radius while attenuating all other frequencies.



2D Low Pass Filter



2D Low Pass Filter

$$H(u, v) = \begin{cases} 1, & \text{if } D(u, v) < D_0. \\ 0, & \text{if } D(u, v) > D_0. \end{cases}$$

where,

$D(u, v)$ is the distance between point (u, v)
and the origin of $2D$ frequency

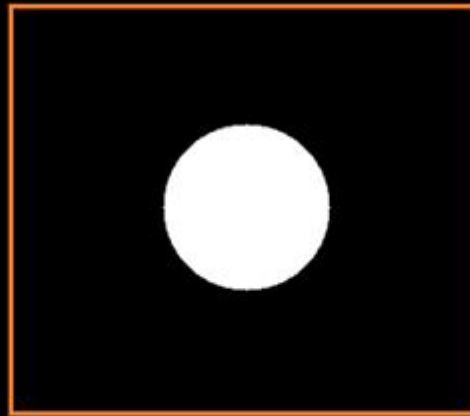
D_0 = Cut-off frequency

Frequency Domain Low Pass Filtering



Image

*



2D Low Pass Filter

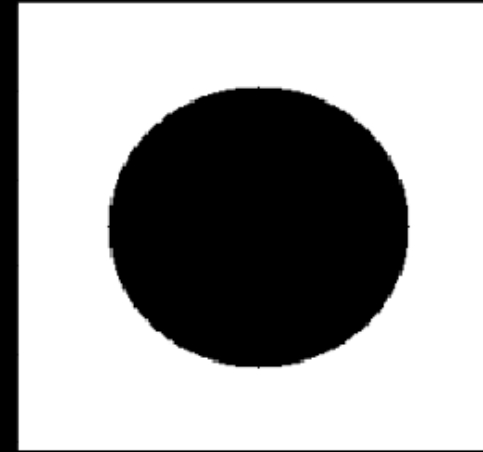
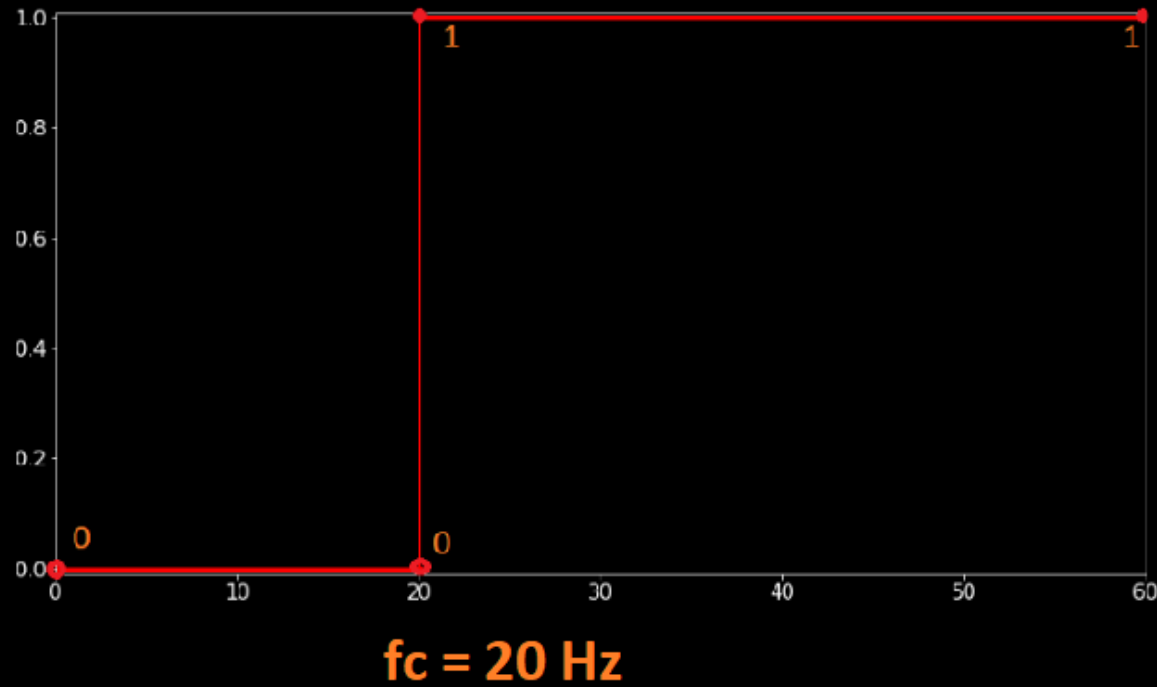
=



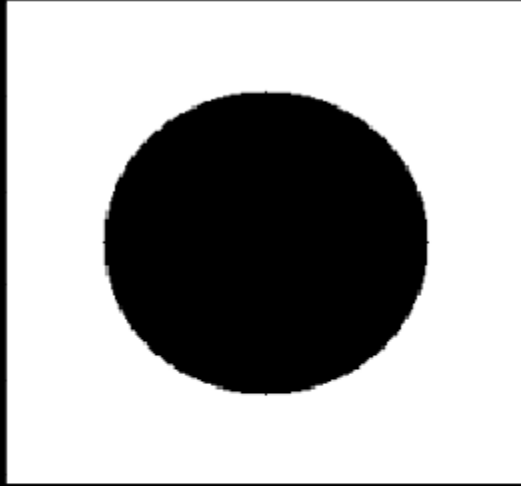
Low Pass Filtered

High Pass Filter

High pass filter enhances high frequency components while attenuating low frequencies. High pass filter controls the sharpening of the image.



2D High Pass Filter



2D High Pass Filter

$$H(u, v) = \begin{cases} 1, & \text{if } D(u, v) > D_0. \\ 0, & \text{if } D(u, v) < D_0. \end{cases}$$

where,

$D(u, v)$ is the distance between point (u, v)
and the origin of $2D$ frequency

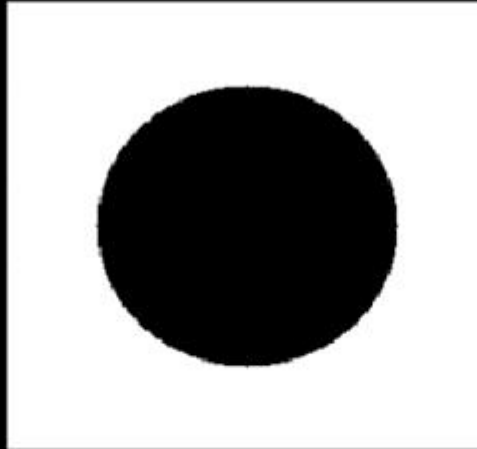
$D_0 = \text{Cut-off frequency}$

Frequency Domain High Pass Filtering



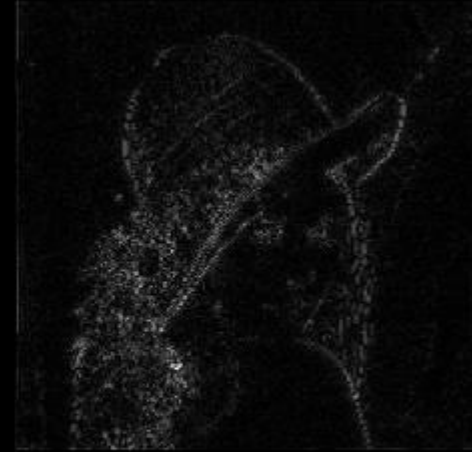
Image

*



2D High Pass Filter

=

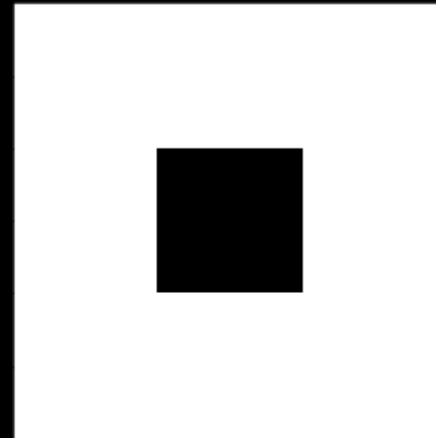


High Pass Filtered

High Boost Filter is High Pass Filter

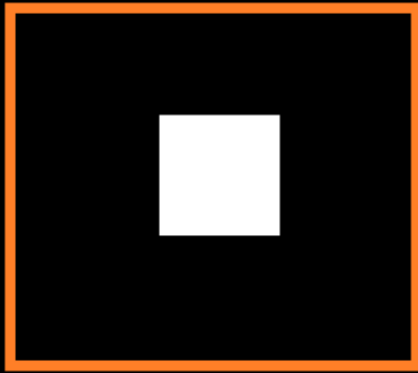
$$\begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$

High Boost Filter

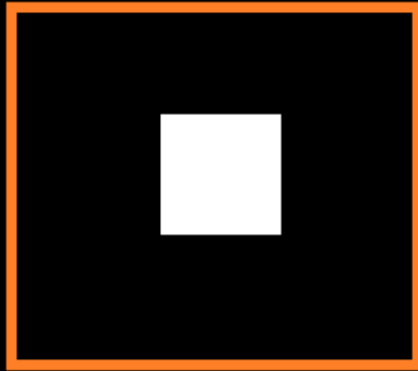


**High Boost Filter
in frequency domain**

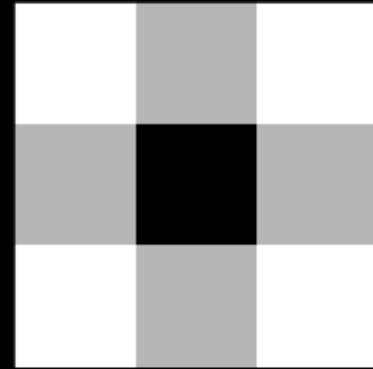
Other Filters



Mean Filter



Gaussian Filter



The Laplacian