Chapter 8 Lists for Multi-dimensional Data



Motivations

Distance Table (in miles)

	Chicago	Boston	New York	Atlanta	Miami	Dallas	Houston
Chicago	0	983	787	714	1375	967	1087
Boston	983	0	214	1102	1763	1723	1842
New York	787	214	0	888	1549	1548	1627
Atlanta	714	1102	888	0	661	781	810
Miami	1375	1763	1549	661	0	1426	1187
Dallas	967	1723	1548	781	1426	0	239
Houston	1087	1842	1627	810	1187	239	0

distances = [
[0, 983, 787, 714, 1375, 967, 1087],
[983, 0, 214, 1102, 1763, 1723, 1842],
[787, 214, 0, 888, 1549, 1548, 1627],
[714, 1102, 888, 0, 661, 781, 810],
[1375, 1763, 1549, 661, 0, 1426, 1187],
[967, 1723, 1548, 781, 1426, 0, 239],
[1087, 1842, 1627, 810, 1187, 239, 0]

Objectives

- To give examples of representing data using two-dimensional lists (§8.1).
- To access elements in a two-dimensional list using row and column indexes (§8.2).
- To program common operations for two-dimensional lists (displaying lists, summing all elements, finding min and max elements, and random shuffling) (§8.2).
- To pass two-dimensional lists to functions (§8.3).
- To write a program for grading multiple-choice questions using two-dimensional lists (§8.4).
- To solve the closest-pair problem using two-dimensional lists (§§8.5-8.6).
- To check a Sudoku solution using two-dimensional lists (§§8.7-8.8).
- To use multidimensional lists (§8.9).

Processing Two-Dimensional lists

You can view a two-dimensional list as a list that consists of rows. Each row is a list that contains the values. The rows can be accessed using the index, conveniently called a *row index*. The values in each row can be accessed through another index, conveniently called a *column index*.

matr	ix =	= [
	[1,	2,	3,	4,	5],
	[6,	7,	Ο,	Ο,	0],
	[0,	1,	Ο,	Ο,	0],
	[1,	Ο,	Ο,	Ο,	8],
	[0,	Ο,	9,	Ο,	3],
]					

	[0]	[1]	[2]	[3]	[4]
[0]	1	2	3	4	5
[1]	6	7	0	0	0
[2]	0	1	0	0	0
[3]	1	0	0	0	8
[4]	0	0	9	0	3

```
matrix[0] is [1, 2, 3, 4, 5]
matrix[1] is [6, 7, 0, 0, 0]
matrix[2] is [0, 1, 0, 0, 0]
matrix[3] is [1, 0, 0, 0, 8]
matrix[4] is [0, 0, 9, 0, 3]

matrix[0][0] is 1
matrix[4][4] is 3
```

Processing Two-Dimensional lists

See the examples in the text.

- 1. (Initializing lists with input values)
- 2. (Initializing lists with random values)
- 3. (Printing lists)
- 4. (Summing all elements)
- 5. (Summing all elements by column)
- 6. (Which row has the largest sum)
- 7. (Random shuffling)



Initializing lists with input values

```
matrix = [] # Create an empty list
numberOfRows = eval(input("Enter the number of rows: "))
numberOfColumns = eval(input("Enter the number of columns: "))
for row in range(0, numberOfRows):
  matrix.append([]) # Add an empty new row
  for column in range(0, numberOfColumns):
    value = eval(input("Enter an element and press Enter: "))
    matrix[row].append(value)
print(matrix)
```



Initializing lists with random values

```
import random
matrix = [] # Create an empty list
numberOfRows = eval(input("Enter the number of rows: "))
numberOfColumns = eval(input("Enter the number of columns: "))
for row in range(0, numberOfRows):
  matrix.append([]) # Add an empty new row
  for column in range(0, numberOfColumns):
    matrix[row].append(random.randrange(0, 100))
print(matrix)
```



Printing lists

```
matrix = [[1, 2, 3], [4, 5, 6], [7, 8, 9]] # Assume a list is given
for row in range(0, len(matrix)):
    for column in range(0, len(matrix[row])):
        print(matrix[row][column], end = " ")
        print() # Print a newline
```



Summing all elements

```
matrix = [[1, 2, 3], [4, 5, 6], [7, 8, 9]] # Assume a list is given total = 0
```

```
for row in range(0, len(matrix)):
for column in range(0, len(matrix[row])):
total += matrix[row][column]
```

print("Total is " + str(total)) # Print the total



Summing elements by column

```
matrix = [[1, 2, 3], [4, 5, 6], [7, 8, 9]] # Assume a list is given
total = 0

for column in range(0, len(matrix[0])):
   for row in range(0, len(matrix)):
     total += matrix[row][column]
   print("Sum for column " + str(column) + " is " + str(total))
```



Summing elements by column

matrix = [[1, 2, 3], [4, 5, 6], [7, 8, 9]] # Assume a list is given maxRow = sum(matrix[0]) # Get sum of the first row in maxRow

```
indexOfMaxRow = 0
for row in range(1, len(matrix)):
  if sum(matrix[row]) > maxRow:
    maxRow = sum(matrix[row])
  indexOfMaxRow = row
```

print("Row " + str(indexOfMaxRow)



Random shuffling

```
import random
matrix = [[1, 2, 3], [4, 5, 6], [7, 8, 9]] # Assume a list is given
for row in range(0, len(matrix)):
     for column in range(0, len(matrix[row])):
     i = random.randrange(0, len(matrix))
     j = random.randrange(0, len(matrix[row]))
     # Swap matrix[row][column] with matrix[i][j]
     matrix[row][column], matrix[i][j] = \
        matrix[i][j], matrix[row][column]
```

print(matrix)

Passing Tow-Dimensional Lists to Functions

PassTwoDimensionalList



Problem: Grading Multiple-Choice Test

Students' Answers to the Questions:

0 1 2 3 4 5 6 7 8 9

Student	0
Student	1
Student	2
Student	3
Student	4
Student	5
Student	6
Student	7

Α	В	А	С	С	D	Ε	Ε	A A A	D	
D	В	Α	В	С	Α	E	Ε	Α	D	
Ε	D	D	Α	С	В	E	Ε	Α	D	
С	В	A	E	D	С	E	Ε	A A	D	
Α	В	D	С	С	D	E	Ε	Α	D	
В	В	E	С	С	D	E	Ε	A A	D	
В	В	A	С	С	D	E	Ε	Α	D	
Ε	В	E	С	С	D	E	Ε	А	D	

→ Objective: write a program that grades multiple-choice test.

Key to the Questions:

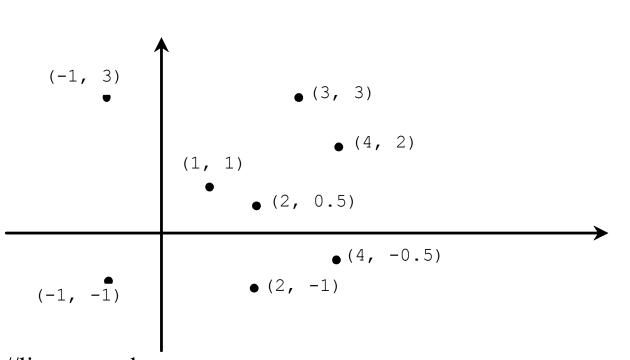
0 1 2 3 4 5 6 7 8 9

DBDCCDAEAD

Key

GradeExam

Problem: Finding Two Points Nearest to Each Other



X

У

https://liveexample.pearsoncmg.com/dsanimation/ClosestPaireBook.html

FindNearestPoints

What is Sudoku?

5	3			7			
6			1	9	5		
	9	8				6	
8				6			3
4			8		3		1
7				2			6
	6						
			4	1	9		5
				8		7	9

https://liveexample.pearsoncmg.com/dsanimation/Sudoku.html





Every row contains the numbers 1 to 9

5	3			7			
6			1	9	5		
	9	8				6	
8				6			3
4			8		3		1
7				2			6
	6						
			4	1	9		5
				8		7	9

	_	2	1	_	7	O	0	1	<u> </u>	I
	5	3	4	6	7	ŏ	9	1	<u> </u>	
	6	7	2	1	9	5	2	1	Q	
	0	/	<u> </u>	1	9	5	<mark>3</mark>	4	O	
	1	9	8	3	<mark>-4</mark>	2	<u>5</u>	6	7	
	1			_					Ĺ	
	8	<u>5</u>	9	7	6	1	4	2	3	
		_				_				
	4	2	6	8	- <mark>5</mark>	3	7	9	1	
	_		_		_			_		
	7	<u> </u>	<u>3</u>	9	2	4	8	<u> </u>	6	
	9	6	7		3	7		Q	1	
	9	O	<u> </u>	<mark>.</mark>	<u> </u>	/	<u> </u>	Ŏ	4	
	2	8	7	4	1	9	6	3	5	
-	4	<u> </u>	/		1		<u> </u>	<u> </u>	<i>J</i>	
	3	4	5	2	8	6	1	7	9	
)	,	<u> </u>	_	U	<u> </u>	1	,		

Every column contains the numbers 1 to 9

5	3			7			
6			1	9	5		
	9	8				6	
8				6			3
4			8		3		1
7				2			6
	6						
			4	1	9		5
				8		7	9

5	3	4	<u>6</u>	7	8	9	1	2
6	7	2	1	9	5	3	<mark>4</mark> !	8
1	9	8	<mark>3</mark>	4	<u>2</u>	<mark>.5</mark>	6	7
8	5	9	7	6	1	4	2	3
4	2	<u>6</u>	8	5	3	7	9	1
7	1	3	9	2	<mark>4</mark>	8	5	6
9	6	1	<mark>.5</mark>	3	7	2	8	4
2	8	7	4	1	9	6	3	5
3	4	<u>5</u>	<mark>.2</mark>	8	<u>6</u>	1	7	9

Every 3×3 box contains the numbers 1 to 9

5	3			7			
6			1	9	5		
	9	8				6	
8				6			3
4			8		3		1
7				2			6
	6						
			4	1	9		5
				8		7	9

5	3	4	<u>6</u>	7	8	9	1	2
6	7	2	1	9	5	<u>3</u>	4	8
1	9	8	<u>3</u>	<u>4</u>	2	<u>5</u>	6	7
8	<u>5</u>	9	7	6	1	4	2	3
4	2	<u>6</u>	8	<u>5</u>	3	7	<mark>9</mark>	1
7	1	3	9	2	4	8	<u>5</u>	6
9	6	1	<u>5</u>	3	7	2	8	4
2	8	7	4	1	9	<u>6</u>	3	5
3	4	5	2	8	<u>6</u>	1	7	9

Checking Whether a Solution Is Correct

5	3			7			
6			1	9	5		
	9	8				6	
8				6			3
4			8		3		1
7				2			6
	6						
			4	1	9		5
				8		7	9

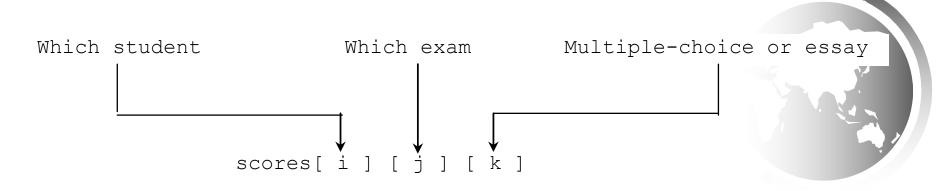
5	3	<mark>4</mark>	<u>6</u>	7	8	<mark>9</mark>	1	<u>2</u>
6	7	2	1	9	5	<u>3</u>	4	8
1	9	8	<mark>3</mark>	4	<mark>2</mark>	<u>5</u>	6	7
8	<u>5</u>	9	7	6	1	<u>4</u>	<u>2</u>	3
4	2	<u>6</u>	8	<u>5</u>	3	7	9	1
7	1	<u>3</u>	9	2	4	8	<u>5</u>	6
9	6	1	<u>5</u>	<u>3</u>	7	<u>2</u>	8	4
2	8	7	4	1	9	<u>6</u>	3	5
3	4	<u>5</u>	2	8	<u>6</u>	1	7	9

CheckSudokuSolution

TestCheckSudokuSolution

Multidimensional lists

```
scores = [
[[9.5, 20.5], [9.0, 22.5], [15, 33.5], [13, 21.5], [15, 2.5]],
[[4.5, 21.5], [9.0, 22.5], [15, 34.5], [12, 20.5], [14, 9.5]],
[[6.5, 30.5], [9.4, 10.5], [11, 33.5], [11, 23.5], [10, 2.5]],
[[6.5, 23.5], [9.4, 32.5], [13, 34.5], [11, 20.5], [16, 9.5]],
[[8.5, 26.5], [9.4, 52.5], [13, 36.5], [13, 24.5], [16, 2.5]],
[[9.5, 20.5], [9.4, 42.5], [13, 31.5], [12, 20.5], [16, 6.5]]]
```



Problem: Weather Information

Suppose a meteorology station records the temperature and humidity at each hour of every day and stores the data for the past ten days in a text file named weather.txt. Each line of the file consists of four numbers that indicate the day, hour, temperature, and humidity. Your task is to write a program that calculates the average daily temperature and humidity for the 10 days.

```
1 1 76.4 0.92
1 2 77.7 0.93
...
10 23 97.7 0.71
10 24 98.7 0.74
```

```
10 24 98.7 0.74
1 2 77.7 0.93
...
10 23 97.7 0.71
1 1 76.4 0.92
```





Problem: Guessing Birthday

Listing 3.8, GuessBirthday.java, gives a program that guesses a birthday. The program can be simplified by storing the numbers in five sets in a three-dimensional list, and it prompts the user for the answers using a loop, as shown in Listing 8.6.

GuessBirthdayUsingList

