

ASSIGNMENT- 02

Advanced Data Structures and Algorithms

1. INSERT

```
1. insert(value)
2.     rbtree.insert(value)
```

1.1. Average Time Complexity

RBTree insert has $O(\log n)$ average time complexity.

1.2. Worst Case Time Complexity

As RBTree's are balanced, worst case time complexity for insert is also $O(\log n)$.

2. DELETE

```
1. delete(value)
2.     rbtree.deleteByValue(value)
```

2.1. Average Time Complexity

RBTree delete has $O(\log n)$ average time complexity.

2.2. Worst Case Time Complexity

As RBTree's are balanced, worst case time complexity for delete is also $O(\log n)$.

3. QUERY

```
1. RBtree::inorderList(node, array, index)
2.     if(node == null)
3.         return index
4.     index = inorderList(node->left, array, index)
5.     array[index++] = node
6.     index = inorderList(node->right, array, index)
7.     return index
8.
9. RBtree::getSortedList()
10.    array = new array[tree.count]
11.    index = 0
12.    inorderList(tree.root, array, index)
13.    return array
14.
15. query(a, b)
16.    targets = new(rbtree)
17.    sortedList = rbtree.getSortedList()
18.    count = rbtree.count()
19.    if(abs(b-a)<count)
20.        for(i = a to b)
21.            xIndex = 0, yIndex = count-1
22.            while(xIndex < yIndex)
23.                sum = sortedList[xIndex] + sortedList[yIndex]
24.                if(sum == i)
25.                    targets.insertUnique(i)
26.                    break;
```

```

27.         else if(sum < i)
28.             xIndex++
29.         else
30.             yIndex--
31.     else
32.         for(xIndex = 0 to count-1)
33.             for(yIndex = 0 to count-1)
34.                 sum = sortedList[xIndex] + sortedList[yIndex]
35.                 if(sum>=a and sum<=b)
36.                     targets.insertUnique(i)
37.     return targets.count()

```

3.1. Time Complexity for different functions

Function	Average Time Complexity	Worst Time Complexity
getSortedList	$O(n)$	$O(n)$
insertUnique	$O(\log n)$	$O(\log n)$
count	$O(1)$	$O(1)$

$T(\text{getSortedList}) = T(\text{inorderTraversal}) = O(n)$

3.2. Average Time Complexity

Condition : $b-a < n$

$$\begin{aligned}
 T(\text{query}) &= T(\text{getSortedList}) + T(\text{count}) + (b-a) * n * T(\text{insertUnique}) + T(\text{count}) \\
 &= O(n) + O(1) + (b-a)*n*O(\log(b-a)) + O(1) \\
 &= O(n) + (b-a)*n*\log(b-a) \\
 &= O((b-a)*n*(\log(b-a)))
 \end{aligned}$$

3.3. Worst Case Time Complexity

Condition : $b-a > n$

$$\begin{aligned}
 T(\text{query}) &= T(\text{getSortedList}) + T(\text{count}) + n * n + T(\text{count}) \\
 &= O(n) + O(1) + O(n * n) + O(1) \\
 &= O(n^2)
 \end{aligned}$$

PLAGIARISM STATEMENT

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