

## CSE340: Theory of Computation (Quiz 1)

13th August, 2019

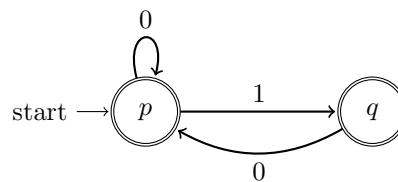
Total Number of Pages: 2

Total Points 30

**Instructions**

1. Cheating or resorting to unfair means will be severely penalized.
2. Using pens (blue/black ink) and not pencils. Do not use red pens for answering.

**Question 1.** (5 points) Describe the language accepted by the following finite automata in the simplest possible form.



$\{w \in 0, 1^* | w \text{ does not contain } \underline{\hspace{1cm}} \text{ as a substring}\}$

**Solution:**

$\{w \in \{0, 1\}^* \mid w \text{ does not contain } 11 \text{ as a substring}\}$

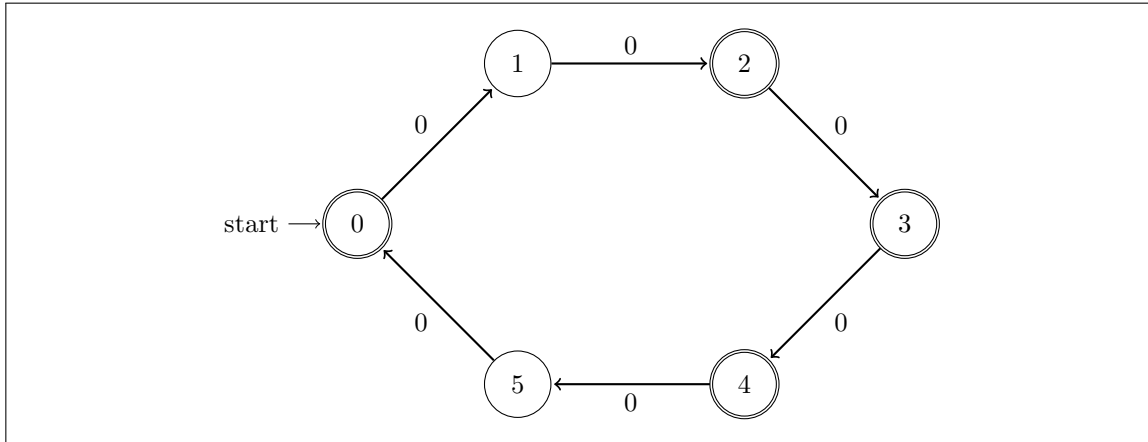
**Question 2.** Design a DFAs that accepts the following languages

- (a) (5 points)  $L_1 = \{w \in 0^* \mid |w| \text{ is divisible by 2 or 3}\}$

**Solution:**

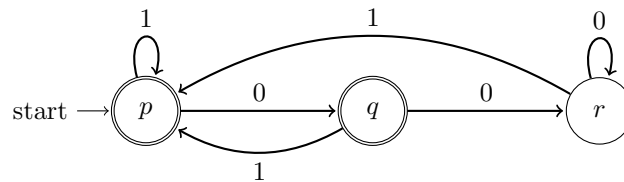
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(b) (5 points)  $L_2 = \{w \in \{0,1\}^* \mid w \text{ does not end with } 00\}$

**Solution:**



**Question 3.** (10 points) State whether the following statements are true or false (T/F).

- (a) **T** Every regular language has an NFA with a single accept state.
- (b) **F** The minimum number of state in a DFA corresponding to an NFA with  $n$  states is  $2^n$ .
- (c) **F** Every language has at least one DFA accepting it.
- (d) **T** An NFA accepts its input if all computation paths end at an accept state.
- (e) **T** Complement of a regular language is regular.

**Question 4.** (5 points) Let  $N = (Q, \Sigma, \delta, q_0, F)$  be an NFA with no  $\epsilon$ -transitions and  $w = a_1 \dots a_n$  be a string of length  $n$  over  $\Sigma$ . Then the number of computation paths of  $N$  on  $w$  is at most \_\_\_\_\_.

**Solution:**  $|Q|^n$