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Candy Distribution 3

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Combinatorics Math Medium Edit

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```

1. /*
2. ID: ashish1610
3. PROG:
4. LANG: C++
5. */
6. #include<bits/stdc++.h>
7. using namespace std;
8. #define ll long long int
9. #define vi vector<int>
10. #define vl vector<ll>
11. #define pii pair<int,int>
12. #define pil pair<int, ll>
13. #define pll pair<ll, ll>
14. #define pli pair<ll, int>
15. #define pb(v, a) v.push_back(a)
16. #define mp(a, b) make_pair(a, b)
17. #define MOD 1000000007
18. #define rep(i, a, b) for(i=a; i<=b; ++i)
19. #define rrep(i, a, b) for(i=a; i>=b; --i)
20. #define si(a) scanf("%d", &a)
21. #define sl(a) scanf("%lld", &a)
22. #define pi(a) printf("%d", a)
23. #define pl(a) printf("%lld", a)
24. #define pn printf("\n")
25. ll pow_mod(ll a, ll b)
26. {
27.     ll res = 1;
28.     while(b)
29.     {
30.         if(b & 1)
31.             res = (res * a) % MOD;

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32.         a = (a * a) % MOD;
33.         b >= 1;
34.     }
35.     return res;
36. }
37. ll pow2[1000005], pow3[1000005];
38. void pre_compute()
39. {
40.     int i;
41.     pow2[0] = 1;
42.     pow3[0] = 1;
43.     rep(i, 1, 1000000)
44.     {
45.         pow2[i] = (2 * pow2[i - 1]) % MOD;
46.         pow3[i] = (3 * pow3[i - 1]) % MOD;
47.     }
48. }
49. int main()
50. {
51.     pre_compute();
52.     int t, i, n;
53.     si(t);
54.     ll ans;
55.     rep(i, 1, t)
56.     {
57.         si(n);
58.         ans = (pow2[n] * pow2[n]) % MOD;
59.         ans -= 2 * pow3[n];
60.         while(ans < 0)
61.             ans += MOD;
62.         if(ans >= MOD)
63.             ans = ans % MOD;
64.         ans += pow2[n];
65.         if(ans >= MOD)
66.             ans = ans % MOD;
67.         pl(ans);
68.         pn;
69.     }
70.     return 0;
71. }

```

Tester Solution by Akash Agrawal

```

1.  /*****
2.      Akash Agrawal
3.      IIIT HYDERABAD
4.      *****/
5.
6.
7.  #include<cstdio>
8.  #include<iostream>
9.  #include<stdlib>
10. #include<cmath>

```

```

11. #include<stdio.h>
12. #include<string.h>
13. #include<cassert>
14. using namespace std;
15. #define FOR(i,a,b) for(i= a ; i < b ; ++i)
16. #define rep(i,n) FOR(i,0,n)
17. #define pln(n) printf("%lld\n",n)
18. #define sl(n) scanf("%lld",&n)
19. #define mod (int)(1e9 + 7)
20. #define ll long long int
21. ll modpow(ll a,ll n,ll temp){ll res=1,y=a;while(n>0){if(n&1)res=(res*y)%mod;if(n>>1)y=y*y%mod;n>>1;}return res;}
22. inline ll checkit(ll n)
23. {
24.     while(n<0)
25.         n+=mod;
26.     if(n>=mod)
27.         n%=mod;
28.     return n;
29. }
30. ll mod2[1000006],mod3[1000006];
31. //The final formula after solving the combinatorics is (2^n-1)(2^n-1)/2
32. int main()
33. {
34.     ll c1,c2,t,n,i;
35.     mod2[0]=1;
36.     mod3[0]=1;
37.     FOR(i,1,1000004)
38.     {
39.         mod2[i]=2*mod2[i-1];
40.         mod3[i]=3*mod3[i-1];
41.         mod2[i]=checkit(mod2[i]);
42.         mod3[i]=checkit(mod3[i]);
43.     }
44.     sl(t);
45.     while(t-->0)
46.     {
47.         sl(n);
48.         c1=mod2[n]-2;
49.         c1=checkit(c1);
50.         c2=mod2[n]+1;
51.         c2=checkit(c2);
52.         c1=c1*c2;
53.         c1=checkit(c1);
54.
55.         c2=mod3[n]-mod2[n]-1;
56.         c2=checkit(c2);
57.         c2*=2;
58.         c2=checkit(c2);
59.
60.         c1-=c2;
61.         c1=checkit(c1);
62.         pln(c1);
63.     }
64.     return 0;

```

65. }

COMMENTS (4)

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**Tarun Dutt** 9 months ago

Can you please explain how the formula was obtained?

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**ankur malik** 8 months ago

yes.. Please someone add some link or something, where this thing is explained

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**artisticoder** 2 months ago

A possible answer can be:

A and B cannot contain neither 0 nor n elements (otherwise conditions does not hold). If A contains k elements, then B can be any subset of n elements apart the subset with n and 0 elements, i.e. $2^n - 2$, minus the subsets of A apart the empty set, i.e. $2^k - 1$, minus all subsets containing the k elements, that is all subsets with n-k elements, apart from subsets with n-k and 0 elements, i.e. $2^{(n-k)} - 2$. So with A having k elements, the total ways to have A and B are $C(n, k) * (2^n - 2 - (2^k - 1) - (2^{(n-k)} - 2)) = C(n, k) * (2^n - 2^k - 2^{(n-k)} + 1)$. If the range of k is $1 \leq k \leq n-1$ then we have to sum the above formula over this range. Let's break the formula into three parts. First is $\text{Sum}(C(n, k) * (2^n + 1)) = (2^n + 1) * (2^n - 2)$. ($\text{Sum}(C(n, k)) = 2^n$ by definition, the minus 2 is because the range of k does not include n and 0, for which C is 1 for each one). The second part is $\text{Sum}(C(n, k) * 2^k)$ which by definition of the binomial coefficient is $(1 + 2)^n - 1 - 2^n$. The minus is again for excluding 0 and n from k. The third part $\text{Sum}(C(n, k) * 2^{(n-k)})$ is equal to the second one because $C(n, k) = C(n, n-k)$. Thus, the final formula is:

$(2^n + 1) * (2^n - 2) - 2 * (3^n - 2^n - 1)$. In the comments of the 2nd solution the formula has a small error, but the code computes the result correctly.

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**himanshu pal** 2 months ago

Let A be a set containing k elements (k is non zero quantity and cannot be equal to n as per the condition given in question)

Now nCk is the number of ways of choosing this set A. Now number of ways of choosing $B = T - b \subseteq a - a \subseteq b$ where

T(Total number of sets ignoring null and complete set ie $2^n - 2$)

$b \subseteq a$ (case when B is a subset of A ie $2^k - 1$ ignoring null set "note: we are not ignoring complete set of k element because b can have all elements of k")

$a \subseteq b$ (case when A is a subset of B ie all k elements already present so $2^{(n-k)} - 1$ (because if B does not contain any extra element other than k elements that ie $B=A$ we have considered that case in 2nd part $b \subseteq a$) - 1(because if B contains all elements of $n=k+n-k$ than B becomes complete set which we have to ignore))

So the complete formula of B becomes $(2^n - 2 - (2^k - 1) - (2^{(n-k)} - 2))$. Now $1 \leq k \leq n-1$ we have to sum the series $nCk * (2^n - 2 - (2^k - 1) - (2^{(n-k)} - 2))$. Now by using binomial series $\text{Sum}(nCk) = 2^n - 2$, $\text{Sum}(nCk * (2^k)) = 3^n - 1 - 2^n = \text{Sum}(nCk * (2^{(n-k)}))$

because $C(n, k) = C(n, n-k)$ so the whole formula reduces to $(2^{n-2})(2^{n+1}) - (2^*(3^n - 1 - 2^n))$ which is simplified further to $2^{2n} + 2^n - 2*(3^n)$

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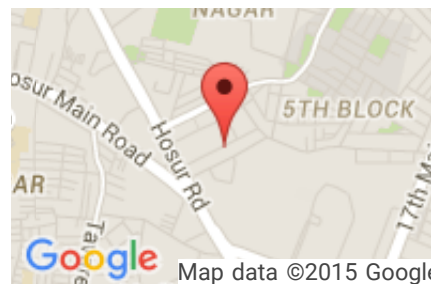
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