

Problem Solving Applied: Freezing Temperature of Seawater:

Basics: The **salinity** of seawater is a measure of the amount of dissolved material in the seawater. **Seawater** is primarily water with about 3.5% dissolved materials (salts, metals, and gases). **Note:** The higher the salinity, the lower the temperature at which the seawater freezes.

The following table contains a set of salinity measurements and corresponding freezing temperatures:

Salinity (ppt)	Freezing Temperature (°F)
0 (fresh water)	32
10	31.1
20	30.1
24.7	29.6
30	29.1
35	28.6

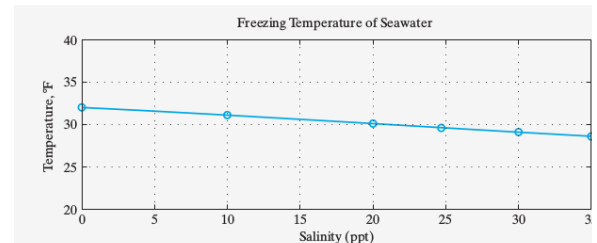


Figure 2.6 Freezing temperature of seawater.

1. PROBLEM STATEMENT

Use linear interpolation to compute a new freezing temperature for water with a specified salinity

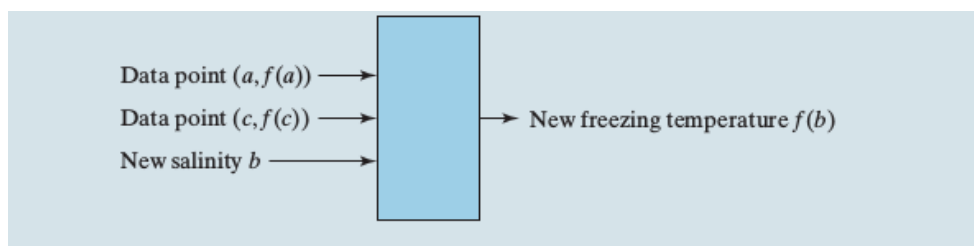
2. INPUT/OUTPUT DESCRIPTION

The following diagram shows that the input to the program includes two consecutive points $(a, f(a))$ and $(c, f(c))$ and the new salinity measurement b , while the output is the new freezing temperature:

Example : If a is salinity and then $F(a)$ is Freezing temperature (From the **graph**)

New freezing temperature $(f(b))$ for New salinity measurement b is given by :

$$f(b) = f(a) + (b - a)/(c - a) * (f(c) - f(a))$$

**3. HAND EXAMPLE**

Suppose that we want to determine the freezing temperature for water with a salinity measurement of 33 ppt. From the data, we see that this point falls between 30 and 35 ppt:

a	30	29.1	$f(a)$
b	33	?	$f(b)$
c	35	28.6	$f(c)$

Using the linear equation formula, we can compute $f(b)$:

$$\begin{aligned}
 f(b) &= f(a) + (b - a)/(c - a) * (f(c) - f(a)) \\
 &= 29.1 + 3/5 * (28.6 - 29.1) \\
 &= 28.8.
 \end{aligned}$$

4. ALGORITHM DEVELOPMENT

1. Read the coordinates of the adjacent points and the new salinity value.
2. Compute the new freezing temperature.
3. Print the new freezing temperature.

```
#include <stdio.h>
#include <math.h>
int main(void)
{
    double a, f_a, b, f_b, c, f_c;
    printf ("Use ppt for salinity values. \n");
    printf ("Use degrees F for temperatures. \n");
    printf ("Enter first salinity and freezing temperature: \n");
    scanf ("%lf %lf",&a,&f_a);
    printf ("Enter second salinity and freezing temperature: \n");
    scanf ("%lf %lf",&c,&f_c);
    printf ("Enter new salinity: \n");
    scanf ("%lf",&b);
    f_b = f_a + (b-a)/(c-a)*(f_c - f_a);
    /* Print new freezing temperature. */
    printf("New freezing temperature in degrees F: %4.1f \n",f_b);
    /* Exit program.
    return 0;
*/
}
```

5. TESTING

We first test the program using the data from the hand example.

```
Enter first salinity and freezing temperature:
30 29.1
Enter second salinity and freezing temperature:
35 28.6
Enter new salinity:
33
```

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New freezing temperature in degrees F: 28.8

The value computed matches the hand example.