# Base Pricing Analysis and Price Elasticity Estimation

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## 1 Overview

The goal is to conduct a base pricing analysis. We estimate brand-level demand using scanner data, and then we make profitability predictions corresponding to specific base price changes. We estimate log-linear demand models that use (log) prices and promotions as inputs, and predict log quantities, log(1+Q). The models predict the demand for a focal brand, and we control for (log) prices and promotions of three competitors. Obviously, this approach generalizes to an arbitrarily large number of competing products as long as the sample size is large enough.

Our focus is on the two top brands in the liquid laundry detergent category, *Tide* and *Gain*. Both are Procter & Gamble brands. The two closest competitors are  $Arm \ \mathcal{E}\ Hammer$  and Purex.

# 2 Packages

Make sure to install two packages that we have not used before: fixest and knitr.

```
library(bit64)
library(data.table)
library(fixest)
library(knitr)
library(ggplot2)
```

## 3 Data overview

The data are located in this folder:

```
data_folder = "data"
```

The data source is an extract from the Nielsen RMS retail scanner data set. The data set captures weekly price and quantity data for all products (UPC's) sold in the stores of a large number of U.S. retail chains. The Kilts data do not include all retailers (for example, Walmart is not part of the data), and the identity of the retailers is not revealed. However, we know if two stores belong to the same retail chain.

#### 3.1 Brand data

The data.table brands in Brands.RData includes brand information for the top five brands in three categories (product modules):

```
1036 FRUIT JUICE - LEMON/LIME
1040 FRUIT JUICE - ORANGE - OTHER CONTAINER
7012 DETERGENTS - HEAVY DUTY - LIQUID
```

The data include the brand code, brand description, and total revenue calculated across all observations. The top five brands were selected based on total brand revenue.

We will focus on the liquid laundry detergent category with corresponding product\_module\_code 7012.

#### 3.2 Store data

Inspect the table stores in the file Stores.RData. The variable store\_code\_uc identifies each retail stores. For some (but not all) stores we know the corresponding retailer\_code that identifies the chain (banner) that the store belongs to. The data include the Scantrack (SMM) market code and the Scantrack market description. Scantrack markets correspond to large metropolitan market areas such as *Chicago* or *Raleigh-Durham* (see the data manual for a map of the Scantrack markets). The three-digit ZIP code of each store is also included.

#### 3.3 Movement data

The movement data (move) are in files of the form brand\_move\_<module code>.RData. The data are at the brand/store/week level and include prices and quantities (units). The data are aggregates of all UPC's that share the same brand name. Brand prices are measured as the weighted average over all store/week UPC prices in equivalent units, and quantities represent total product volume measured in equivalent units such as ounces. In the liquid laundry detergent category (module 7012), prices represent dollars per ounce and units are total product volume in ounces per store/week. The aggregation weights are based on total store-level UPC revenue across all weeks, and hence the aggregation weights are constant within each store. The movement data also include a promotion indicator (promo\_dummy), a logical TRUE/FALSE variable.

The week\_end variable date is the last day of a Nielsen week, which always starts on a Sunday and ends on a Saturday. Note that prices may change during the period, and hence even the UPC-level price may be an average over more than one posted price. The sample includes data for the 2010-2013 period.

Please consult the official Kilts Center Retail Scanner Dataset Manual for all details.

# 4 Prepare the data for the demand analysis

We first load the brand and store data.

```
load(paste0(data_folder, "/Brands.RData"))
load(paste0(data_folder, "/Stores.RData"))
```

### 4.1 Select the category and brands

\*Choose the laundry detergent category (module) and select the corresponding brand-level meta data from the data table brands. Then sort (order) the brand data corresponding to total brand revenue, and select the **top four brands** (ranked by revenue).

```
selected_module = 7012  # Laundry detergent
laundry = brands[product_module_code == selected_module]
laundry_sorted = laundry[order(-revenue)][1:4]
laundry_sorted
```

```
brand_code_uc
                             brand_descr
                                                      product_module_descr
           <int>
                                  <char>
                          TIDE - H-D LIQ DETERGENTS - HEAVY DUTY - LIQUID
1:
          653791
2:
          557775
                          GAIN - H-D LIQ DETERGENTS - HEAVY DUTY - LIQUID
3:
          507562 ARM & HAMMER - H-D LIQ DETERGENTS - HEAVY DUTY - LIQUID
                         PUREX - H-D LIQ DETERGENTS - HEAVY DUTY - LIQUID
4:
          623280
   product_module_code
                           revenue
                  <int>
                             <niim>
                  7012 3659669291
1:
2:
                  7012 1201306647
                  7012 1010503850
3:
                  7012 495632613
4:
```

Let's assign each brand a new name using a new variable, brand\_name, and give the four brands simple names such as Tide, Gain, ArmHammer, and Purex. These simplified brand names will make our code and the estimation output more readable. More specifically, create a new data containing the four selected brands and add to it the brand\_name variable.

Note that we will add the brand names to the quantity, price, and promotion variables. In R, price\_ArmHammer (as well as price\_Arm\_Hammer) are legal variable names, but price\_Arm&Hammer and price\_Arm & Hammer are not, and hence I do not suggest the brand names Arm&Hammer or Arm & Hammer.

```
selected_brands = data.frame(
  product_id = c(653791, 557775, 507562, 623280),
  brand_name = c('Tide', 'Gain', 'ArmHammer', 'Purex')
)
print(selected_brands)
```

```
product_id brand_name
1 653791 Tide
2 557775 Gain
3 507562 ArmHammer
4 623280 Purex
```

#### 4.2 Prepare the movement data

\*Load the movement data, and—for better readability—change the variable names from units to quantity and from promo\_dummy to promotion (you can use the setnames command for this). Change the data type of the promotion variable from logical to numeric using the as.numeric function. Finally, merge the

new brand\_name variable with the movement table (more precisely, perform an inner join, i.e. retain all observations that are present in both the parent and child data sets).

```
load("data/brand_move_7012.RData")
library(data.table)
setnames(move, old = "promo_dummy", new = "promotion", skip_absent=TRUE)
setnames(move, old = "units", new = "quantity", skip_absent=TRUE)
setnames(move, old = "brand_code_uc", new = "product_id", skip_absent=TRUE)
move$promotion <- as.numeric(move$promotion)</pre>
move_with_brands <- merge(move, selected_brands, by = "product_id", all = FALSE)</pre>
head(move with brands)
Key: cjust_id>
  product_id store_code_uc
                                             price quantity promotion brand_name
                              week_end
                                             <num>
        <int>
                      <int>
                                 <Date>
                                                      <num>
                                                                <num>
                                                                           <char>
                       1123 2010-01-02 0.06528157
       507562
                                                       2000
                                                                    1 ArmHammer
1:
2:
       507562
                       1123 2010-01-09 0.06852484
                                                       3300
                                                                    1 ArmHammer
3:
       507562
                       1123 2010-01-16 0.07700768
                                                       1500
                                                                    0 ArmHammer
4:
       507562
                       1123 2010-01-23 0.07757468
                                                       1275
                                                                    0 ArmHammer
                       1123 2010-01-30 0.06442845
5:
       507562
                                                       4025
                                                                    1 ArmHammer
6:
       507562
                       1123 2010-02-06 0.07757468
                                                       2275
                                                                    0 ArmHammer
final_data = merge(move, selected_brands, by = "product_id", all = FALSE)
print(final data)
Key: cjuid>
         product_id store_code_uc
                                     week_end
                                                   price quantity promotion
              <int>
                            <int>
                                       <Date>
                                                   <num>
                                                            <num>
                                                                      <num>
             507562
                             1123 2010-01-02 0.06528157
                                                           2000.0
                                                                           1
      1:
      2:
             507562
                             1123 2010-01-09 0.06852484
                                                           3300.0
                                                                           1
      3:
             507562
                             1123 2010-01-16 0.07700768
                                                           1500.0
                                                                           0
                                                                           0
      4:
             507562
                             1123 2010-01-23 0.07757468
                                                           1275.0
      5:
             507562
                             1123 2010-01-30 0.06442845
                                                           4025.0
                                                                           1
     ___
                          8386077 2013-11-30 0.17189507
                                                           1000.0
                                                                           0
5256704:
             653791
5256705:
             653791
                          8386077 2013-12-07 0.13699283
                                                           6000.0
                                                                           1
                                                                           0
5256706:
                          8386077 2013-12-14 0.17348442
                                                            650.0
             653791
5256707:
             653791
                          8386077 2013-12-21 0.17500879
                                                            900.0
                                                                           0
5256708:
                          8386077 2013-12-28 0.16948965
                                                           1404.8
                                                                           0
             653791
         brand_name
             <char>
      1: ArmHammer
      2: ArmHammer
      3: ArmHammer
      4: ArmHammer
      5: ArmHammer
5256704:
               Tide
5256705:
               Tide
5256706:
               Tide
5256707:
               Tide
5256708:
               Tide
```

#### 4.3 Remove outliers

Most data contain some "flaws" or outliers. Here is an easy way of removing such outliers:

First, we create a function that flags all observations in a vector  $\mathbf{x}$ , for example a price series, as outliers if the ratio between a value and the median value among all  $\mathbf{x}$  observations is below or above a threshold.

```
isOutlier <- function(x, threshold_bottom, threshold_top) {
  is_outlier = rep(FALSE, times = length(x))
  median_x = median(x, na.rm = TRUE)
  is_outlier[x/median_x < threshold_bottom | x/median_x > threshold_top] = TRUE
  return(is_outlier)
}
```

Now run this function on the price data, separately for each brand and store. Then tabulate the number of outliers, and remove the corresponding observations from the data set. I recommend to use a lower threshold (threshold\_bottom) value of 0.35 and an upper threshold (threshold\_top) of 2.5.

```
[1] 17268
final_data = final_data[outlier_flag == FALSE]

# removing flag
final_data[, outlier_flag := NULL]

final_data
```

```
Key: cjust_id>
         product_id store_code_uc
                                     week_end
                                                   price quantity promotion
                                                             <num>
                                                                       <num>
              <int>
                             <int>
                                       <Date>
                                                   <num>
             507562
                             1123 2010-01-02 0.06528157
                                                            2000.0
                                                                           1
      1:
      2:
             507562
                             1123 2010-01-09 0.06852484
                                                            3300.0
                                                                           1
                             1123 2010-01-16 0.07700768
                                                                           0
      3:
             507562
                                                            1500.0
      4:
             507562
                             1123 2010-01-23 0.07757468
                                                            1275.0
                                                                           0
      5:
             507562
                             1123 2010-01-30 0.06442845
                                                            4025.0
                                                                           1
5239436:
                          8386077 2013-11-30 0.17189507
                                                            1000.0
                                                                           0
             653791
5239437:
             653791
                           8386077 2013-12-07 0.13699283
                                                            6000.0
                                                                           1
5239438:
             653791
                          8386077 2013-12-14 0.17348442
                                                             650.0
                                                                           0
5239439:
             653791
                          8386077 2013-12-21 0.17500879
                                                             900.0
                                                                           0
                          8386077 2013-12-28 0.16948965
                                                                           0
5239440:
             653791
                                                            1404.8
```

brand\_name <char>

- 1: ArmHammer
- 2: ArmHammer
- 3: ArmHammer
- 4: ArmHammer
- 5: ArmHammer

---

```
5239436: Tide
5239437: Tide
5239438: Tide
5239439: Tide
5239440: Tide
```

17065:

8387558

## 4.4 Reshape the movement data from long to wide format

To prepare the data for the regression analysis, we need to **reshape the data from long to wide format** using dcast.

All the details on casting and the reverse operation (melting from wide to long format using melt) are explained in the data.table html vignettes:

https://rdatatable.gitlab.io/data.table/articles/datatable-reshape.html

Let's be specific about the structure of the data that we need to use to estimate a demand model. We would like to obtain a table with observations, characterized by a combination of store id (store\_code\_uc) and week (week\_end) in rows, and information on quantities, prices, and promotions in columns. Quantities, prices, and promotions are brand-specific.

```
final_data = final_data[, .(store_code_uc, week_end, brand_name, quantity, price, promotion)]
final_data <- dcast(
    final_data,
    store_code_uc + week_end ~ brand_name,
    value.var = c("quantity", "price", "promotion")
)</pre>
```

## 4.5 Merge store information with the movement data

Now merge the movement data with the store meta data, in particular with the retailer code, the Scantrack (SMM) market code, and the Scantrack market description. But only with the store meta data where we have a valid retailer code. Hence, we need to remove store data if the retailer code is missing (NA). Use the is.na function to check if retailer\_code is NA or not.

```
load("data/Stores.RData")
ls()
 [1] "brands"
                          "data_folder"
                                               "final_data"
                                                                   "isOutlier"
 [5] "laundry"
                          "laundry_sorted"
                                               "move"
                                                                   "move_with_brands"
 [9] "selected_brands"
                          "selected_module"
                                               "stores"
                                                                   "threshold_bottom"
[13] "threshold_top"
print(stores)
Key: <store_code_uc>
       store_code_uc retailer_code store_zip3 SMM_code
                                                             SMM description
                <int>
                               <int>
                                           <int>
                                                     <int>
                                                                       <char>
                                                                   Cleveland
    1:
                 1123
                                  89
                                              441
                                                        16
    2:
                 1852
                                  89
                                              165
                                                        16
                                                                   Cleveland
    3:
                 2324
                                  NA
                                              606
                                                         2
                                                                     Chicago
                                                                    Urban NY
    4:
                 4809
                                  98
                                              100
                                                         9
                                                                    Urban NY
    5:
                 4954
                                  NA
                                              100
                                                         9
   ---
                                                                     Chicago
17063:
              8385693
                                             606
                                                         2
                                  NΑ
17064:
              8386077
                                4904
                                              113
                                                         9
                                                                    Urban NY
```

38

Phoenix

851

128

```
17066:
              8388006
                                  NA
                                              279
                                                        49
                                                                    Richmond
17067:
              8388364
                                  NΑ
                                              274
                                                        39 Raleigh - Durham
valid_store_meta <- stores[!is.na(stores$retailer_code)]</pre>
final_data_with_store <- merge(final_data, valid_store_meta, by = "store_code_uc", all = FALSE)
head(final_data_with_store)
Key: <store_code_uc>
                    week_end quantity_ArmHammer quantity_Gain quantity_Purex
   store_code_uc
            <int>
                       <Date>
                                            <num>
                                                            <num>
                                                                            <num>
             1123 2010-01-02
                                              2000
                                                              400
                                                                             1060
1:
             1123 2010-01-09
                                                              700
2:
                                              3300
                                                                             1582
3:
             1123 2010-01-16
                                             1500
                                                              600
                                                                             4988
4:
             1123 2010-01-23
                                             1275
                                                             1300
                                                                              832
             1123 2010-01-30
5:
                                             4025
                                                              300
                                                                             1142
             1123 2010-02-06
                                             2275
                                                              300
                                                                             1786
6:
   quantity Tide price ArmHammer price Gain price Purex price Tide
            <num>
                             <num>
                                         <num>
                                                      <num>
                                                                  <num>
1:
             3000
                        0.06528157
                                    0.1209109
                                                0.08248828
                                                                    NaN
             9600
                                    0.1209109
2:
                        0.06852484
                                                0.08248828
                                                              0.1299496
3:
             3450
                        0.07700768
                                    0.1209109
                                                0.06126852
4:
             2700
                        0.07757468
                                    0.1015777
                                                 0.08214914
                                                              0.1524072
5:
             2100
                        0.06442845
                                    0.1209109
                                                0.08214914
                                                              0.1524981
6:
             3300
                        0.07757468 0.1209109
                                                0.08214914
                                                              0.1519637
   promotion_ArmHammer promotion_Gain promotion_Purex promotion_Tide
                  <num>
                                   <num>
                                                    <num>
                                                                     <num>
1:
                       1
                                       0
                                                        0
                                                                        NA
                                       0
                                                        0
2:
                       1
                                                                         1
3:
                       0
                                       0
                                                        1
                                                                         0
4:
                       0
                                       1
                                                        0
                                                                         0
                                       0
5:
                       1
                                                        0
                                                                         0
                                       0
                                                                         0
6:
                       0
                                                        0
   retailer_code store_zip3 SMM_code SMM_description
            <int>
                        <int>
                                  <int>
                                                  <char>
                                              Cleveland
1:
               89
                          441
                                     16
2:
               89
                          441
                                     16
                                               Cleveland
3:
               89
                          441
                                               Cleveland
                                     16
4:
               89
                          441
                                     16
                                               Cleveland
5:
               89
                                               Cleveland
                          441
                                     16
6:
               89
                          441
                                     16
                                               Cleveland
```

#### 4.6 Create time variables or trends

A time trend records the progress of time. For example, a time trend at the week-level may equal 1 in the first week in the data, 2 in the second week, etc., whereas a trend at the month-level may equal 1 in the first month, 2 in the second month, etc.

I suggest you create a monthly time trend. Use the functions year and month to extract the year and month components of the week (week\_end) variable in the movement data (alternatively, you could use the week function if you wanted to create a time trend at the week-level). Then, use the following code to create the monthly trend:

```
library(lubridate)
final_data_with_store$week_end <- as.Date(final_data_with_store$week_end)
final_data_with_store[, year := year(week_end)]
final_data_with_store[, month := month(week_end)]</pre>
```

```
final_data_with_store[, month_trend := 12*(year - min(year)) + month]
head(final_data_with_store[, .(week_end, year, month, month_trend)])
```

```
week_end year month month_trend
       <Date> <num> <num>
                                 <niim>
1: 2010-01-02
               2010
                         1
                                     1
2: 2010-01-09
               2010
                                     1
                        1
3: 2010-01-16 2010
                         1
                                     1
4: 2010-01-23 2010
                                     1
                        1
5: 2010-01-30
               2010
                         1
                                     1
6: 2010-02-06 2010
                         2
                                     2
```

## 4.7 Remove missing values

Finally, retain only complete cases, i.e. rows without missing values:

```
final_data_with_store = final_data_with_store[complete.cases(final_data_with_store)]
print(final_data_with_store)
```

```
Key: <store_code_uc>
         store code uc
                          week_end quantity_ArmHammer quantity_Gain
                 <int>
                            <Date>
                                                 <num>
                                                               <num>
                  1123 2010-01-09
                                                  3300
                                                                 700
      1:
      2:
                  1123 2010-01-16
                                                  1500
                                                                 600
                  1123 2010-01-23
                                                                1300
      3:
                                                  1275
      4:
                  1123 2010-01-30
                                                  4025
                                                                 300
                                                                 300
      5:
                  1123 2010-02-06
                                                  2275
               8386077 2013-11-30
                                                                 450
1259348:
                                                   730
               8386077 2013-12-07
                                                   245
                                                                 200
1259349:
1259350:
               8386077 2013-12-14
                                                   100
                                                                 750
1259351:
               8386077 2013-12-21
                                                  2535
                                                                 100
1259352:
               8386077 2013-12-28
                                                   240
                                                                    0
         quantity_Purex quantity_Tide price_ArmHammer price_Gain price_Purex
                                 <num>
                  <num>
                                                  <num>
                                                             <num>
                 1582.0
                                9600.0
                                                         0.1209109 0.08248828
      1:
                                            0.06852484
      2:
                 4988.0
                                3450.0
                                            0.07700768
                                                         0.1209109
                                                                    0.06126852
      3:
                                2700.0
                                            0.07757468 0.1015777
                                                                    0.08214914
                  832.0
      4:
                 1142.0
                                2100.0
                                            0.06442845
                                                         0.1209109
                                                                    0.08214914
                 1786.0
                                3300.0
                                            0.07757468 0.1209109 0.08214914
      5:
1259348:
                    0.0
                                1000.0
                                            0.05608577
                                                         0.1154987
                                                                    0.17257275
1259349:
                  100.0
                                6000.0
                                            0.14538576
                                                         0.1424117
                                                                    0.15909961
1259350:
                 1200.0
                                 650.0
                                            0.14538576
                                                         0.1128853
                                                                    0.13586151
1259351:
                  550.0
                                 900.0
                                            0.07233923
                                                        0.1508381
                                                                    0.13191491
1259352:
                  559.9
                                1404.8
                                            0.13363888 0.1508381
                                                                    0.09229263
         price_Tide promotion_ArmHammer promotion_Gain promotion_Purex
              <num>
                                   <num>
                                                   <num>
                                                                    <num>
                                                       0
      1: 0.1299496
                                                                        0
                                       1
      2: 0.1519637
                                       0
                                                       0
                                                                        1
      3: 0.1524072
                                       0
                                                       1
                                                                        0
      4: 0.1524981
                                                       0
                                                                        0
                                       1
      5:
         0.1519637
                                       0
                                                       0
                                                                        0
                                                                        0
1259348: 0.1718951
                                       1
                                                       1
```

1259349:	0.1369	928		0	1	1	
1259350:	0.1734	844		0	1	1	
1259351:	0.1750	088		1	0	1	
1259352:	0.1694	897		1	0	1	
	promoti	on_Tide ret	ailer_code	store_zip3	SMM_code	SMM_description	year
	-	<num></num>	<int></int>	<int></int>	<int></int>	<char></char>	<num></num>
1:		1	89	441	16	Cleveland	2010
2:		0	89	441	16	Cleveland	2010
3:		0	89	441	16	Cleveland	2010
4:		0	89	441	16	Cleveland	2010
5:		0	89	441	16	Cleveland	2010
1259348:		0	4904	113	9	Urban NY	2013
1259349:		1	4904	113	9	Urban NY	2013
1259350:		0	4904	113	9	Urban NY	2013
1259351:		0	4904	113	9	Urban NY	2013
1259352:		0	4904	113	9	Urban NY	2013
	month month_trend						
	<num></num>	<num></num>					
1:	1	1					
2:	1	1					
3:	1	1					
4:	1	1					
5:	2	2					
1259348:	11	47					
1259349:	12	48					
1259350:	12	48					
1259351:	12	48					
1259352:	12	48					

# 5 Data inspection

## 5.1 Observations and geographic coverage

First, document the number of observations and the number of unique stores in the data.

Second, we assess if the included stores have broad geographic coverage. We hence create a summary table that records the number of observations for each separate Scantrack market:

```
market_coverage = final_data_with_store[, .(n_obs = .N), by = SMM_description]
```

Note the use of the data.table internal .N: .N is the number of observations, either in the whole data table, or—as in this case—the number of observations within each group defined by the by = statement.

A convenient way to print a table is provided by the **kable** function that is included in the **knitr** package. Please consult the documentation for **kable** to see all options. Particularly useful are the options **col.names**, which is used below, and **digits**, which allows you to set the number of digits to the right of the decimal point.

Now use kable to document the number of observations within each Scantrack market.

kable(market\_coverage, col.names = c("Scantrack market", "No. obs."))

Scantrack market	No. obs.
Cleveland	24891
Chicago	88257
Boston	42219
New Orleans - Mobile	27704
Urban NY	23363
Suburban NY	39284
Albany	8918
San Francisco	40263
Rem Omaha	6672
Nashville	5880
Rem Los Angeles - Collar	19850
Exurban NY	12285
Salt Lake City	23812
Atlanta	10049
Miami	56504
Jacksonville	16962
Oklahoma City - Tulsa	6654
Sacramento	14089
Rem Jacksonville	14786
Kansas City	7979
Memphis	5388
Richmond	8701
Phoenix	29709
Los Angeles	127244
Rem Atlanta	9014
Rem Richmond - Norfolk	2061
Washington DC	8636
Rem Seattle - Portland	9465
West Texas	8798
Las Vegas	19845
San Antonio	16650
Minneapolis	18830

Scantrack market	No. obs.
Detroit	13109
Rem Boston	24688
Louisville	7487
St. Louis	17079
Rem Milwaukee	11217
Omaha	6903
Milwaukee	15987
Tampa	41020
Rem St. Louis	7633
Raleigh - Durham	7478
Charlotte	4166
Seattle	25835
Rem Indianapolis	5664
Pittsburgh	20966
Rem Charlotte	6884
San Diego	22955
Birmingham	11440
Orlando	29707
Portland OR	17985
Dallas	21053
Rem Denver	13596
Philadelphia	14982
Houston	22434
Baltimore	6533
Cincinnati	7528
Des Moines	5260
Rem Philadelphia	1235
Buffalo - Rochester	4172
Denver	15460
Rem New Orleans - Mobile	7358
Rem West Texas	18370
Grand Rapids	5605
Hartford - New Haven	11056
Columbus	6064
Rem Pittsburgh	2151
Indianapolis	6331
Rem North California	13171
Rem Kansas City	8380
Rem Minneapolis	3995
Rem Detroit	1771
Rem Greenville	2274
Little Rock	2838
Rem Memphis - Little Rock	2487
Syracuse	2283

## 5.2 Price variation

Before estimating the demand models we would like to understand the degree of price variation in the data. Comment on why this is important for a regression analysis such as demand estimation!

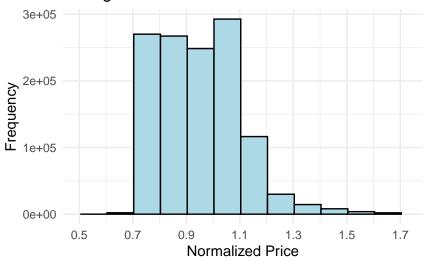
We will predict demand for Tide and Gain. For each of these two brands separately, we would like to visualize the overall degree of price variation across observations, and also the variation in relative prices with respect to the competing brands.

• To visualize the (own) price variation, normalize the prices of Tide and Gain by dividing by the average of these prices, and show the histogram of normalized prices.

Warning: Removed 3779 rows containing non-finite outside the scale range (`stat\_bin()`).

Warning: Removed 2 rows containing missing values or values outside the scale range (`geom\_bar()`).

# Histogram of Normalized Prices of Tide

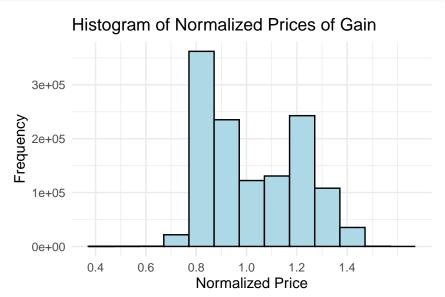


```
gain_average = final_data_with_store[, mean(price_Gain, na.rm = TRUE)]
norm_gain = final_data_with_store[, price_Gain / gain_average]

df_gain = data.frame(norm_gain)

ggplot(df_gain, aes(x = norm_gain)) +
    geom_histogram(binwidth = 0.1, fill = "lightblue", color = "black") +
    scale_x_continuous(breaks = seq(min(df_gain$norm_gain, na.rm = TRUE), max(df_gain$norm_gain, na.rm = TRUE)
    labels = scales::number_format(accuracy = 0.1)) +
```

```
labs(title = "Histogram of Normalized Prices of Gain",
    x = "Normalized Price",
    y = "Frequency") +
theme_minimal()
```

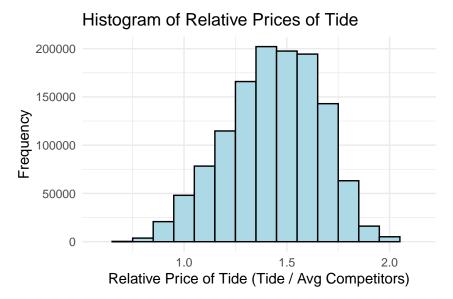


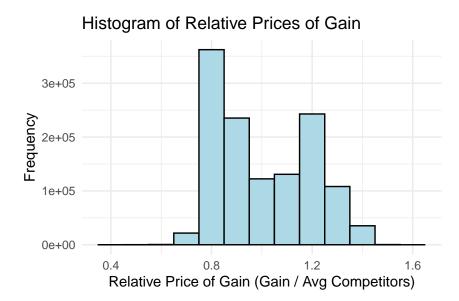
• To visualize relative prices, calculate the ratio of Tide and Gain prices with respect to the three competing brands, and show the histogram of relative prices.

Note: To avoid that the scale of a graph is distorted by a few outliers, use the limits option in scale\_x\_continuous (see the ggplot2 introduction). This also helps to make the graphs comparable with each other.

Warning: Removed 3779 rows containing non-finite outside the scale range (`stat bin()`).

Warning: Removed 2 rows containing missing values or values outside the scale range (`geom\_bar()`).





## 5.3 Summary of data inspection

Discuss the data description, including sample size, geographic coverage, and the results on own and relative price variation.

From having visualized the provided data, we are able to determine that the largest single market in terms

of number of observations, is Los Angeles, with 127 244 unique instances. This is followed by Chicago and Miami, with 88 257 and 56 504 observations respectively.

In terms of own price variation over time, we can see two very different graphs for Tide and Gain products. The graph of the normalized price variation of Tide tells us that for the majority of the time, the price of the product is (mostly) evenly distributed between 70% and 110% of the average price, with most instances of the product being priced between 100-110% of the average price. This stands in contrast to Gain products, who display a bimodal distribution, with the majority of prices being between 75%-95%, and 115%-125% of the average price. The most common price was around 80% of the average price.

Controlling for the prices of three competitors, Tide product prices were close to normally distributed around 135-140% of their competitors' prices. In contrast, Gain displayed a bimodal distribution with peaks centered at the 80% and 120% of competitors' prices.

## 6 Estimation

Now we are ready to estimate demand models for Tide and Gain.

We want to estimate a sequence of models with an increasing number of controls and compare the stability of the key results across these models. In all models the output is log(1+quantity\_<br/>brand name>).

To keep things simple, we will initially estimate demand for Tide only.

Let's start with the following models:

- 1. log of own price as only input
- 2. Add store fixed effects
- 3. Add a time trend—maybe linear, or a polynomial with higher-order terms
- 4. Instead of a time trend add fixed effects for each month (more precisely: for each year/month combination)

Estimate the models using the feols function from the fixest package (consult the corresponding fixest guide included among the R learning resources on Canvas). Store the regression outputs in some appropriately named variables (objects).

head(final\_data\_with\_store)

<pre>Key: <store_code_uc></store_code_uc></pre>									
	store_code_uc	week_end o	quantity_A	rmHammer	quanti	ty_Gai	n quar	ntity_F	urex
	<int></int>	<date></date>		<num></num>		<num< td=""><td>&gt;</td><td>&lt;</td><td><num></num></td></num<>	>	<	<num></num>
1:	1123	2010-01-09		3300		70	0		1582
2:	1123	2010-01-16		1500		60	0		4988
3:	1123	2010-01-23		1275		130	0		832
4:	1123	2010-01-30		4025		30	0		1142
5:	1123	2010-02-06		2275		30	0		1786
6:	1123	2010-02-13		1600			0		1288
	quantity_Tide	price_ArmHar	nmer price	_Gain pri	ce_Pur	ex pri	ce_Tic	le	
	<num></num>	<1	num> ·	<num></num>	<nu< td=""><td>m&gt;</td><td><nun< td=""><td>1&gt;</td><td></td></nun<></td></nu<>	m>	<nun< td=""><td>1&gt;</td><td></td></nun<>	1>	
1:	9600	0.0685	2484 0.120	09109 0.	082488	28 0.	129949	96	
2:	3450	0.07700	0768 0.120	09109 0.	061268	52 0.	151963	37	
3:	2700	0.0775	7468 0.10	15777 0.	082149	14 0.	152407	72	
4:	2100	0.06442	2845 0.120	09109 0.	082149	14 0.	152498	31	
5:	3300	0.0775	7468 0.120	09109 0.	082149	14 0.	151963	37	
6:	6100	0.0775	7468 0.120	09109 0.	082149	14 0.	130330	9	
	promotion_ArmI	Hammer promot	tion_Gain ]	promotion	_Purex	promo	tion_7	Tide	
		<num></num>	<num></num>		<num></num>		<r< td=""><td>num&gt;</td><td></td></r<>	num>	
1:		1	0		0			1	
2:		0	0		1			0	
3:		0	1		0			0	
4:		1	0		0			0	
5:		0	0		0			0	
6:		0	0		0			1	
	retailer_code	store_zip3 \$	SMM_code SI	MM_descri	ption	year	month	month_	trend
	<int></int>	<int></int>	<int></int>	<	char>	<num></num>	<num></num>		<num $>$
1:	89	441	16	Clev	reland	2010	1		1
2:	89	441	16	Clev	reland	2010	1		1
3:	89	441	16	Clev	reland	2010	1		1
4:	89	441	16	Clev	eland	2010	1		1
5:	89	441	16	Clev	eland	2010	2		2
6:	89	441	16	Clev	reland	2010	2		2

```
fit_base <- feols(</pre>
 log(1 + quantity_Tide) ~ log(price_Tide),
 data = final_data_with_store
fit_store_FE <- feols(</pre>
 log(1 + quantity_Tide) ~ log(price_Tide) | store_code_uc,
 data = final_data_with_store
)
fit_trend <- feols(</pre>
 log(1 + quantity_Tide) ~ log(price_Tide) + month | store_code_uc,
 data = final data with store
fit_month_FE <- feols(</pre>
 log(1 + quantity_Tide) ~ log(price_Tide) | store_code_uc + year + month,
 data = final_data_with_store
)
fit_promo_Tide <- feols(</pre>
 log(1 + quantity_Tide) ~ log(price_Tide) +
   promotion_Tide | store_code_uc + year + month,
 data = final_data_with_store
etable(fit_base, fit_store_FE, fit_trend, fit_month_FE, fit_promo_Tide)
                         fit base
                                  fit store FE
                                                               fit trend
Dependent Var.: log(1+quantity_Tide) log(1+quantity_Tide) log(1+quantity_Tide)
Constant
               -6.374*** (0.0127)
log(price_Tide) -7.465*** (0.0067) -5.612*** (0.0440) -5.607*** (0.0440)
                                                      -0.0101*** (0.0002)
month
promotion_Tide
Fixed-Effects: -----
store_code_uc
                              No
                                                Yes
                                                                     Yes
                              No
                                                 No
year
                                                                     No
month
                              No
                                                 No
                          IID by: store_code_uc by: store_code_uc
S.E. type
Observations
                       1,259,352 1,259,352 1,259,352
R2
                         0.49632
                                            0.84607
                                                               0.84652
                                             0.29829
                                                               0.30034
Within R2
                     fit_month_FE fit_promo_Tide
Dependent Var.: log(1+quantity_Tide) log(1+quantity_Tide)
Constant
log(price_Tide) -5.647*** (0.0440) -4.076*** (0.0541)
month
                              0.3665*** (0.0078)
promotion_Tide
Fixed-Effects: -----
store_code_uc
                              Yes
                                                 Yes
```

```
year
                                 Yes
                                                      Yes
                                 Yes
                                                      Yes
month
S.E. type
                 by: store_code_uc by: store_code_uc
Observations
                           1,259,352
                                                1,259,352
                                                  0.85703
                             0.85144
Within R2
                             0.30448
                                                  0.33064
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Hint: Recall that it is perfectly legitimate in R to write model formulas such as

```
log(1+quantity_<brand name>) ~ log(price_<brand name>)
```

Hence, there is no need to create new variables such as the logarithm of own price, etc., before estimating a demand model.

You can display the regression coefficients using the summary function. As a much more elegant solution, however, I recommend using the etable function in the fixest package, which produces nicely formatted output.

Please consult the fixest guide on how to use etable, and go through the *Checklist for creating* LaTeX tables using etable!

Here is an example (note that the fit objects are the regression outputs—adjust the names if necessary):

Note the option cluster = c("store\_code\_uc", "month\_trend"), which tells etable to show standard errors that are clustered at the store and month level. These clustered standard errors will be larger and more accurate than regular standard errors because they reflect that the error terms in the regression are likely correlated at the store and month level.

Before moving on, you may want to remove the regression output objects that are no longer used, because they take up much space in memory:

```
rm(fit_base, fit_store_FE, fit_trend)
```

#### 6.1 Controlling for competitor prices

Now add the competitor prices to the demand model.

```
library(fixest)

fit_base_competitor <- feols(
   log(1 + quantity_Tide) ~ log(price_Tide) + log(price_Gain),
   data = final_data_with_store
)

fit_store_FE_competitor <- feols(
   log(1 + quantity_Tide) ~ log(price_Tide) + log(price_Gain) +
        log(price_ArmHammer) + log(price_Purex) | store_code_uc,
   data = final_data_with_store</pre>
```

```
fit_trend_competitor <- feols(</pre>
 log(1 + quantity_Tide) ~ log(price_Tide) + log(price_Gain) +
   log(price_ArmHammer) + log(price_Purex) + month | store_code_uc,
  data = final_data_with_store
fit_month_FE_competitor <- feols(</pre>
  log(1 + quantity_Tide) ~ log(price_Tide) + log(price_Gain) +
   log(price_ArmHammer) + log(price_Purex) | store_code_uc + year + month,
  data = final_data_with_store)
etable(fit_base_competitor, fit_store_FE_competitor, fit_trend_competitor,
      fit_month_FE_competitor)
                     fit_base_competitor fit_store_FE_compe..
                    log(1+quantity_Tide) log(1+quantity_Tide)
Dependent Var.:
                     -7.559*** (0.0128)
Constant
log(price_Tide) -5.792*** (0.0084) -5.639*** (0.0436)
log(price_Gain)
                     -2.126*** (0.0068) 0.7171*** (0.0180)
log(price_ArmHammer)
                                         0.1360*** (0.0052)
log(price_Purex)
                                         -0.0544*** (0.0054)
month
Fixed-Effects:
store code uc
year
                                     Nο
                                                         No
month
                                  IID by: store_code_uc
S.E. type
                                           1,259,352
Observations
                              1,259,352
                                0.53281
                                                    0.84867
Within R2
                                                     0.31013
                    fit_trend_competitor fit_month_FE_compe..
                    log(1+quantity_Tide) log(1+quantity_Tide)
Dependent Var.:
Constant
log(price_Tide)
                    -5.636*** (0.0435) -5.643*** (0.0430)
log(price_Gain) 0.7075*** (0.0181) 0.6279*** (0.0188)
log(price_ArmHammer) 0.1229*** (0.0051) 0.1048*** (0.0050)
log(price_Purex) -0.0495*** (0.0054) 0.1565*** (0.0075)
month
                    -0.0083*** (0.0002)
Fixed-Effects:
store_code_uc
                                    Yes
                                     No
                                                        Yes
year
month
                                     No
S.E. type
                      by: store_code_uc    by: store_code_uc
                              1,259,352
Observations
                                          1,259,352
                                0.84896
                                                    0.85368
Within R2
                                0.31148
                                                    0.31498
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

### 6.2 Controlling for promotions

Now add the promotions dummies, first just for Tide, then for all brands. Compare the results. Did controlling for promotions change the own price elasticity estimate in an expected manner?

```
#Tide
fit_base_competitor_promo <- feols(</pre>
  log(1 + quantity_Tide) ~ log(price_Tide) + log(price_Gain) +
    log(price_ArmHammer) + log(price_Purex) + promotion_Tide,
  data = final_data_with_store
fit_store_FE_competitor_promo <- feols(</pre>
 log(1 + quantity_Tide) ~ log(price_Tide) + log(price_Gain) +
    log(price_ArmHammer) + log(price_Purex) + promotion_Tide | store_code_uc,
  data = final_data_with_store
)
fit_trend_competitor_promo <- feols(</pre>
  log(1 + quantity_Tide) ~ log(price_Tide) + log(price_Gain) +
    log(price_ArmHammer) + log(price_Purex) + month +
    promotion_Tide | store_code_uc,
 data = final_data_with_store
fit_month_FE_competitor_promo <- feols(</pre>
  log(1 + quantity_Tide) ~ log(price_Tide) + log(price_Gain) +
    log(price_ArmHammer) + log(price_Purex) +
    promotion_Tide | store_code_uc + year + month,
  data = final_data_with_store
etable(fit_base_competitor_promo, fit_store_FE_competitor_promo,
       fit_trend_competitor_promo, fit_month_FE_competitor_promo)
```

```
fit_base_competito.. fit_store_FE_compe..
Dependent Var.:
                     log(1+quantity_Tide) log(1+quantity_Tide)
Constant
                       -7.072*** (0.0129)
log(price_Tide)
                       -4.127*** (0.0096)
                                            -3.971*** (0.0527)
log(price_Gain)
                       -1.770*** (0.0075)
                                          0.5498*** (0.0177)
                                          0.0931*** (0.0051)
log(price_ArmHammer)
                     -1.111*** (0.0039)
                      -0.2270*** (0.0029) -0.0422*** (0.0048)
log(price_Purex)
promotion_Tide
                       0.4755*** (0.0023)
                                           0.3907*** (0.0080)
month
Fixed-Effects:
store_code_uc
                                       No
                                                           Yes
                                       No
year
                                                            No
month
                                       No
S.E. type
                                      IID
                                             by: store_code_uc
                                                    1,259,352
Observations
                               1,259,352
```

```
R2
                                0.56996
                                                     0.85513
Within R2
                                                     0.33962
                    fit_trend_competit.. fit_month_FE_compe..
Dependent Var.:
                    log(1+quantity_Tide) log(1+quantity_Tide)
Constant
log(price Tide)
                     -3.985*** (0.0528)
                                         -4.180*** (0.0548)
log(price_Gain)
                      0.5448*** (0.0178)
                                          0.4990*** (0.0185)
log(price_ArmHammer) 0.0843*** (0.0051)
                                        0.0753*** (0.0049)
log(price_Purex)
                    -0.0389*** (0.0048)
                                        0.1315*** (0.0071)
                     0.3869*** (0.0080)
                                          0.3416*** (0.0077)
promotion_Tide
month
                     -0.0058*** (0.0002)
                    _____
Fixed-Effects:
store_code_uc
                                    Yes
                                                        Yes
                                     No
                                                        Yes
year
                                     Nο
                                                        Yes
month
S.E. type
                      by: store_code_uc by: store_code_uc
Observations
                              1,259,352
                                                 1,259,352
R2
                                0.85528
                                                    0.85844
Within R2
                                0.34028
                                                     0.33727
___
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

When comparing the models without promotions against the ones with promotions, the latter has less own price elasticity: 3.961 (promotions) vs 5.659 (no promotions). Without controlling for promotions, their effect is mistakenly attributed to price, which inflates the price elasticity. When promotions are included, the model correctly attributes the demand increase to them, resulting in a more accurate, lower price elasticity. This reflects the fact that consumers are less sensitive to price changes alone than the model without promotions suggested, as promotions are often more effective at boosting demand than small price reductions.

```
# All Brands
fit_base_competitor_promo2 <- feols(</pre>
  log(1 + quantity_Tide) ~ log(price_Tide) + log(price_Gain) +
    log(price_ArmHammer) + log(price_Purex) + promotion_Tide +
    promotion_Gain + promotion_ArmHammer + promotion_Purex,
  data = final_data_with_store
)
fit_store_FE_competitor_promo2 <- feols(</pre>
  log(1 + quantity_Tide) ~ log(price_Tide) + log(price_Gain) +
    log(price_ArmHammer) + log(price_Purex) + promotion_Tide +
    promotion_Gain + promotion_ArmHammer + promotion_Purex | store_code_uc,
  data = final_data_with_store
)
fit_trend_competitor_promo2 <- feols(</pre>
  log(1 + quantity_Tide) ~ log(price_Tide) + log(price_Gain) +
    log(price_ArmHammer) + log(price_Purex) + month +
    promotion_Tide + promotion_Gain + promotion_ArmHammer + promotion_Purex
    store_code_uc, data = final_data_with_store
)
```

```
fit_month_FE_competitor_promo2 <- feols(</pre>
 log(1 + quantity_Tide) ~ log(price_Tide) + log(price_Gain) +
   log(price_ArmHammer) + log(price_Purex) + promotion_Tide +
   promotion_Gain + promotion_ArmHammer + promotion_Purex | store_code_uc +
   year + month, data = final_data_with_store
)
etable(fit base competitor promo2, fit store FE competitor promo2,
      fit_trend_competitor_promo2, fit_month_FE_competitor_promo2)
                  fit_base_competit..2 fit_store_FE_comp..2
Dependent Var.:
                  log(1+quantity_Tide) log(1+quantity_Tide)
Constant
                    -6.583*** (0.0131)
log(price_Tide)
                  -3.307*** (0.0100) -4.003*** (0.0531)
log(price_Gain)
                   -2.273*** (0.0090) 0.6922*** (0.0238)
log(price_ArmHammer) -1.210*** (0.0049) 0.1437*** (0.0092)
log(price_Purex) -0.2223*** (0.0031) -0.0661*** (0.0060)
                  0.5647*** (0.0023) 0.3832*** (0.0082)
promotion_Tide
promotion_ArmHammer -0.2909*** (0.0024) 0.0331*** (0.0062)
promotion Purex -0.0807*** (0.0021) -0.0404*** (0.0050)
month
Fixed-Effects:
store_code_uc
                                  No
                                  No
year
                                                    Nο
month
                               IID
S.E. type
                                       by: store_code_uc
Observations
                           1,259,352 1,259,352
R2
                             0.58840
                                               0.85540
Within R2
                                                0.34084
                  fit_trend_competi..2 fit_month_FE_comp..2
Dependent Var.:
                  log(1+quantity_Tide) log(1+quantity_Tide)
Constant
                  -4.015*** (0.0532) -4.196*** (0.0549)
log(price_Tide)
                  0.6830*** (0.0238) 0.5748*** (0.0242)
log(price_Gain)
log(price_ArmHammer) 0.1325*** (0.0092) 0.1223*** (0.0087)
log(price_Purex) -0.0624*** (0.0060) 0.1515*** (0.0129)
promotion_ArmHammer 0.0311*** (0.0062) 0.0346*** (0.0059)
promotion_Purex -0.0394*** (0.0050) 0.0222** (0.0072)
                  -0.0054*** (0.0002)
month
Fixed-Effects:
store_code_uc
                                 Yes
                                                    Yes
                                  No
                                                    Yes
year
month
S.E. type
                     by: store_code_uc by: store_code_uc
Observations
                        1,259,352 1,259,352
R2
                             0.85553
                                               0.85856
```

```
Within R2 0.34142 0.33782 ---
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

With the exception of the fit\_base model, all other models are generally the same compared to the models with the single promotion.

Summarize and comment on the estimation results. Was it necessary to control for store fixed effects, time trends/fixed effects, as well as competitor prices and promotions? What do we learn from the magnitudes of the own and cross-price elasticities?

In the base model, Tide's own-price elasticity is quite large, with a coefficient of -7.47, indicating that a 1% increase in Tide's price would result in a 7.47% decrease in demand. However, after including store fixed effects, the magnitude of this elasticity decreases to -5.61, suggesting that the initial model without controls overestimated Tide's price sensitivity by failing to account for unobserved differences across stores. The R-squared value also jumps from 0.496 in the base model to 0.846, which demonstrates the significant improvement in model fit when store-specific factors are considered.

Time trends and month fixed effects did not have much of an impact on the overall results. After introducing a month trend, the price elasticity remains at -5.61, and the inclusion of fixed effects for each year and month leads to a slight decrease in price elasticity to -5.65. The R-squared improves marginally to 0.851, indicating that time trends capture some of the seasonality in Tide's demand, but store fixed effects remain the most important control.

Lastly, the introduction of Tide's promotional activities further improves the model's explanatory power, with the R-squared rising to 0.857. The own-price elasticity decreases further to -4.08, indicating that promotions significantly mitigate the negative impact of price increases. Promotions for Tide have a strong and positive effect on sales, increasing demand by approximately 36.65%. This confirms that promotions are a major driver of Tide's demand and should be accounted for when estimating price sensitivity.

We will use the final model including all variables (I called it fit\_promo\_comp) as our preferred model. To make this final model distinguishable from the regression output for Gain we rename it:

```
fit_promo_comp <- feols(
   log(1 + quantity_Tide) ~ log(price_Tide) + log(price_Gain) + log(price_Purex)
   + log(price_ArmHammer) + promotion_Tide + promotion_Gain + promotion_ArmHammer
   + promotion_Purex | store_code_uc + year + month, data = final_data_with_store
)

fit_Tide = fit_promo_comp</pre>
```

#### 6.3 Demand model for Gain

Now repeat the steps to estimate demand for Gain.

```
fit_base <- feols(
  log(1 + quantity_Gain) ~ log(price_Gain),
  data = final_data_with_store
)

fit_store_FE <- feols(
  log(1 + quantity_Gain) ~ log(price_Gain) | store_code_uc,
  data = final_data_with_store
)

fit_trend <- feols(</pre>
```

```
log(1 + quantity_Gain) ~ log(price_Gain) + month | store_code_uc,
 data = final_data_with_store
)
fit_month_FE <- feols(</pre>
 log(1 + quantity_Gain) ~ log(price_Gain) | store_code_uc + year + month,
 data = final_data_with_store
fit_promo_Gain <- feols(</pre>
 log(1 + quantity_Gain) ~ log(price_Gain) + promotion_Gain | store_code_uc +
   year + month,
 data = final_data_with_store
etable(fit_base, fit_store_FE, fit_trend, fit_month_FE, fit_promo_Gain)
                        fit_base fit_store_FE
                                                          fit_trend
Dependent Var.: log(1+quantity_Gain) log(1+quantity_Gain) log(1+quantity_Gain)
Constant -14.55**** (0.0160)
log(price_Gain) -9.967*** (0.0078) -6.709*** (0.0326) -6.690*** (0.0326)
month
                                                   0.0157*** (0.0005)
promotion_Gain
Fixed-Effects: -----
                                             Yes
store_code_uc
                            No
                                                                Yes
year
                            No
                                              No
month
                            No
                                              No
__________
                      IID by: store_code_uc by: store_code_uc
S.E. type
                                  1,259,352
                                                    1,259,352
                     1,259,352
Observations
R2
                       0.56615
                                          0.74513
                                                            0.74559
Within R2
                                           0.23514
                                                             0.23651
                    fit_month_FE fit_promo_Gain
Dependent Var.: log(1+quantity_Gain) log(1+quantity_Gain)
Constant
log(price_Gain) -6.626*** (0.0328) -4.779*** (0.0417)
month
promotion_Gain
                                 0.7303*** (0.0121)
Fixed-Effects: -----
store_code_uc
                            Yes
                                              Yes
year
                            Yes
                                              Yes
month
                            Yes
S.E. type by: store_code_uc by: store_code_uc Observations 1,259,352 1,259,352
                                          0.75396
R2
                        0.74747
Within R2
                        0.22771
                                           0.24756
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
library(fixest)
fit_base_competitor <- feols(</pre>
  log(1 + quantity_Gain) ~ log(price_Tide) + log(price_Gain),
  data = final_data_with_store
fit store FE competitor <- feols(</pre>
  log(1 + quantity_Gain) ~ log(price_Gain) + log(price_Tide) + log(price_Purex)
  + log(price_ArmHammer) | store_code_uc,
  data = final_data_with_store
)
fit_trend_competitor <- feols(</pre>
  log(1 + quantity_Gain) ~ log(price_Gain) + log(price_Tide) + log(price_Purex)
  + log(price_ArmHammer) + month | store_code_uc,
  data = final_data_with_store
fit_month_FE_competitor <- feols(</pre>
  log(1 + quantity_Gain) ~ log(price_Gain) + log(price_Tide) + log(price_Purex)
  + log(price_ArmHammer) + log(price_Purex) +
    log(price_ArmHammer) | store_code_uc + year + month,
  data = final_data_with_store
)
etable(fit_base_competitor, fit_store_FE_competitor, fit_trend_competitor,
       fit_month_FE_competitor)
                      fit_base_competitor fit_store_FE_compe..
Dependent Var.:
                     log(1+quantity_Gain) log(1+quantity_Gain)
Constant
                       -15.33*** (0.0190)
log(price_Tide)
                     -0.9372*** (0.0124) 1.585*** (0.0299)
log(price_Gain)
                       -9.483*** (0.0101) -6.745*** (0.0324)
                                            0.1075*** (0.0070)
log(price_Purex)
                                             -0.0193* (0.0080)
log(price_ArmHammer)
month
Fixed-Effects:
store_code_uc
                                       No
                                                           Yes
                                       No
                                                            No
year
month
S.E. type
                                      IID
                                             by: store code uc
                                1,259,352
Observations
                                                   1,259,352
R2
                                 0.56810
                                                      0.74748
Within R2
                                                       0.24219
                     fit_trend_competitor fit_month_FE_compe..
Dependent Var.:
                    log(1+quantity_Gain) log(1+quantity_Gain)
Constant
                      1.580*** (0.0300)
log(price_Tide)
                                           1.569*** (0.0293)
log(price_Gain)
                     -6.728*** (0.0324) -6.659*** (0.0324)
```

```
log(price_Purex) 0.0987*** (0.0069) 0.0898*** (0.0089)
log(price_ArmHammer)
                       0.0041 (0.0079) 0.0394*** (0.0080)
month
                    0.0148*** (0.0005)
                    _____
Fixed-Effects:
store_code_uc
                                    Yes
                                                        Yes
                                     No
                                                        Yes
year
month
                                                        Yes
S.E. type by: store_code_uc by: store_code_uc
Observations
                        1,259,352 1,259,352
                                0.74788
                                                    0.74962
Within R2
                                0.24339
                                                    0.23428
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
#Gain
fit_base_competitor_promo <- feols(</pre>
 log(1 + quantity_Gain) ~ log(price_Gain) + log(price_Tide) + log(price_Purex)
 + log(price_ArmHammer) + promotion_Gain,
 data = final_data_with_store
)
fit_store_FE_competitor_promo <- feols(</pre>
 log(1 + quantity_Gain) ~ log(price_Gain) + log(price_Tide) + log(price_Purex)
 + log(price_ArmHammer) + promotion_Gain | store_code_uc,
 data = final data with store
)
fit_trend_competitor_promo <- feols(</pre>
 log(1 + quantity_Gain) ~ log(price_Gain) + log(price_Tide) + log(price_Purex)
  + log(price_ArmHammer) + month + promotion_Gain | store_code_uc,
 data = final_data_with_store
)
fit month FE competitor promo <- feols(</pre>
  log(1 + quantity_Gain) ~ log(price_Gain) + log(price_Tide) + log(price_Purex)
 + log(price_ArmHammer) + promotion_Gain | store_code_uc + year + month,
 data = final_data_with_store
)
etable(fit_base_competitor_promo, fit_store_FE_competitor_promo,
      fit_trend_competitor_promo, fit_month_FE_competitor_promo)
                    fit_base_competito.. fit_store_FE_compe..
Dependent Var.:
                    log(1+quantity_Gain) log(1+quantity_Gain)
Constant
                     -14.80*** (0.0197)
log(price_Gain)
                    -8.576*** (0.0127) -5.020*** (0.0382)
                    -0.4411*** (0.0137) 1.457*** (0.0303)
log(price_Tide)
log(price_Purex) -0.0312*** (0.0045) 0.1401*** (0.0067)
log(price_ArmHammer) -0.8967*** (0.0060) -0.0337*** (0.0077)
```

promotion\_Gain 0.1573\*\*\* (0.0043) 0.6878\*\*\* (0.0121)

month

Fixed-Effects:

```
No
                                                         Yes
store_code_uc
                                      Nο
                                                          No
year
month
                                      No
S.E. type
                                     IID by: store_code_uc
Observations
                              1,259,352
                                             1,259,352
                                 0.57562
                                                     0.75332
                                                     0.25970
Within R2
                    fit_trend_competit.. fit_month_FE_compe..
Dependent Var.:
                    log(1+quantity_Gain) log(1+quantity_Gain)
Constant
log(price_Gain)
                     -4.985*** (0.0384) -4.857*** (0.0404)
log(price_Tide)
                      1.451*** (0.0303) 1.439*** (0.0297)
                      0.1304*** (0.0066) 0.0859*** (0.0085)
log(price_Purex)
                      -0.0076 (0.0077) 0.0327*** (0.0077)
log(price_ArmHammer)
                   0.6943*** (0.0121) 0.7117*** (0.0123)
promotion_Gain
                     0.0167*** (0.0005)
month
Fixed-Effects:
                    -----
store_code_uc
                                                         Yes
                                     Yes
                                     No
year
                                                         Yes
                                     No
month
                                                         Yes
S.E. type
                       by: store_code_uc by: store_code_uc
Observations
                              1,259,352
                                            1,259,352
                                 0.75382
                                                    0.75577
                                 0.26121
Within R2
                                                     0.25308
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
fit_base_competitor_promo2 <- feols(</pre>
 log(1 + quantity_Gain) ~ log(price_Gain) + log(price_Tide) + log(price_Purex)
  + log(price_ArmHammer) + promotion_Gain + promotion_Tide + promotion_ArmHammer
  + promotion_Purex, data = final_data_with_store
)
fit_store_FE_competitor_promo2 <- feols(</pre>
 log(1 + quantity_Gain) ~ log(price_Gain) + log(price_Tide) + log(price_Purex)
  + log(price_ArmHammer) + promotion_Gain + promotion_Tide + promotion_ArmHammer
  + promotion_Purex | store_code_uc, data = final_data_with_store
)
fit_trend_competitor_promo2 <- feols(</pre>
 log(1 + quantity_Gain) ~ log(price_Gain) + log(price_Tide) + log(price_Purex)
  + log(price_ArmHammer) + month + promotion_Gain + promotion_Tide +
   promotion_ArmHammer + promotion_Purex | store_code_uc,
  data = final_data_with_store
fit_month_FE_competitor_promo2 <- feols(</pre>
  log(1 + quantity_Gain) ~ log(price_Gain) + log(price_Tide) + log(price_Purex)
  + log(price_ArmHammer)+ promotion_Gain + promotion_Tide + promotion_ArmHammer
  + promotion_Purex | store_code_uc + year + month,
```

```
data = final_data_with_store
)
fit_Gain = fit_month_FE_competitor_promo2
etable(fit_base_competitor_promo, fit_store_FE_competitor_promo,
       fit_trend_competitor_promo, fit_month_FE_competitor_promo2)
                    fit_base_competito.. fit_store_FE_compe..
                    log(1+quantity_Gain) log(1+quantity_Gain)
Dependent Var.:
                      -14.80*** (0.0197)
Constant
log(price_Gain)
                      -8.576*** (0.0127)
                                         -5.020*** (0.0382)
log(price_Tide)
                     -0.4411*** (0.0137) 1.457*** (0.0303)
log(price_Purex)
                     -0.0312*** (0.0045)
                                          0.1401*** (0.0067)
log(price_ArmHammer) -0.8967*** (0.0060) -0.0337*** (0.0077)
                     0.1573*** (0.0043) 0.6878*** (0.0121)
promotion_Gain
month
promotion_Tide
promotion_ArmHammer
promotion_Purex
Fixed-Effects:
store_code_uc
                                      No
                                                         Yes
                                      No
year
month
                                                          No
                                      Nο
                                 IID by: store_code_uc
S.E. type
                                               1,259,352
Observations
                               1,259,352
R2
                                 0.57562
                                                     0.75332
Within R2
                                                     0.25970
                    fit_trend_competit.. fit_month_FE_comp..2
Dependent Var.:
                    log(1+quantity_Gain) log(1+quantity_Gain)
Constant
log(price_Gain)
                      -4.985*** (0.0384) -4.901*** (0.0403)
log(price_Tide)
                      1.451*** (0.0303) 1.712*** (0.0369)
log(price_Purex)
                      0.1304*** (0.0066)
                                          0.1281*** (0.0133)
log(price ArmHammer)
                      -0.0076 (0.0077) 0.1401*** (0.0115)
                      0.6943*** (0.0121)
                                          0.7079*** (0.0123)
promotion_Gain
month
                      0.0167*** (0.0005)
                                           0.0681*** (0.0055)
promotion_Tide
promotion_ArmHammer
                                           0.0827*** (0.0061)
                                           0.0521*** (0.0071)
promotion_Purex
Fixed-Effects:
store_code_uc
                                     Yes
                                                         Yes
year
                                      No
                                                         Yes
month
                                      No
                                                         Yes
S.E. type
                       by: store_code_uc by: store_code_uc
Observations
                               1,259,352
                                            1,259,352
R2
                                 0.75382
                                                     0.75605
Within R2
                                 0.26121
                                                     0.25396
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Briefly comment on the estimates, as you did before with Tide.

The above analysis reveals a lot of the information about demand dynamics for Gain, especially the effects of its own price, competitor prices, and promotional activities. Initially, the base model suggests that Gain exhibits a strong own-price elasticity, with a 1% increase in price leading to a 9.54% decrease in demand. However, this sensitivity is notably reduced once store fixed effects are introduced, where the elasticity drops to -5.06%. This reduction indicates that the initial model overestimated price sensitivity by not accounting for the difference between stores. Additionally, the introduction of store fixed effects reveals a positive cross-price elasticity with Tide, suggesting that the two brands behave as substitutes after accounting for differences across stores.

Promotional activities were also shown to play a substantial role in influencing demand. Interestingly, the base model showed a negative coefficient for promotion\_Gain, which implied that promotions were ineffective or potentially cannibalizing future sales. However, once store-specific effects were controlled for, the promotion effect turned strongly positive, with Gain's promotion coefficient being 0.697 – linked to an increase in sales. This shift emphasizes the importance of accounting for local market conditions when analyzing promotional effectiveness. Promotions by competing brands, such as Tide and ArmHammer, were found to have positive spillover effects on Gain's demand, indicating that competitive promotions may enhance overall consumer awareness and drive sales across brands.

Finally, the inclusion of time trends and fixed effects for months and years provided further refinement of the model, but the core findings remained consistent. Gain's own-price elasticity remained high, though slightly reduced, and the positive cross-price elasticity with Tide continued, which confirmed the substitutability of these two brands. The strong and consistent impact of promotional activities was further reinforced, with promotions for Gain, as well as its competitors, significantly boosting demand.

. . .

# 7 Profitability analysis

The goal is to fine-tune prices jointly for Tide and Gain. We hence use the estimates of the preferred demand models and evaluate the product-line profits when we change the prices of the two brands.

To predict profits, let's only retain data for one year, 2013:

```
final_data_with_store = final_data_with_store[year == 2013]
```

Although we have excellent demand data, we do not know the production costs of the brands (this is confidential information). We can infer the cost making an informed assumption on retail margins and the gross margin of the brand.

```
gross_margin = 0.35
retail_margin = 0.18

price_Tide = mean(final_data_with_store$price_Tide)
price_Gain = mean(final_data_with_store$price_Gain)

cost_Tide = (1-gross_margin)*(1-retail_margin)*mean(price_Tide, na.rm = TRUE)
cost_Gain = (1-gross_margin)*(1-retail_margin)*mean(price_Gain, na.rm = TRUE)
```

As prices are measured in dollars per ounce, these marginal costs are also per ounce.

Now create a vector indicating the percentage price changes that we consider within an acceptable range, up to +/-5%.

```
percentage_delta = seq(-0.05, 0.05, 0.025) # Identical to = c(-0.5, -0.025, 0.0, 0.025, 0.05)
```

We will consider all possible combinations of price changes for Tide and Gain. This can be easily achieved by creating a data table with the possible combinations in rows (please look at the documentation for the rep function):

Inspect the resulting table. The profit column will allow us to store the predicted profits.

Now we are ready to iterate over each row in profit\_DT and evaluate the total product-line profits of Tide and Gain for the corresponding percentage price changes. You can perform this iteration with a simple for-loop:

```
original_Prices <- final_data_with_store[, c("price_Tide", "price_Gain")]

for (i in 1:nrow(profit_DT)) {
    # Perform profit calculations for the price changes indicated in row i of the profit_DT table
    final_data_with_store$price_Tide = original_Prices$price_Tide * (1 + profit_DT$delta_Tide[i])
    final_data_with_store$price_Gain = original_Prices$price_Gain * (1 + profit_DT$delta_Gain[i])

    final_data_with_store$quantity_Tide = exp(predict(fit_Tide, newdata = final_data_with_store)) - 1
    final_data_with_store$quantity_Gain = exp(predict(fit_Gain, newdata = final_data_with_store)) - 1

    total_profit_Tide = sum(final_data_with_store$price_Tide * final_data_with_store$quantity_Tide)</pre>
```

```
total_profit_Gain = sum(final_data_with_store$price_Gain * final_data_with_store$quantity_Gain)
profit_DT$profit[i] = total_profit_Tide + total_profit_Gain
}
print(profit_DT)
```

```
delta_Tide delta_Gain
                               profit
         <num>
                     <num>
                                <num>
 1:
        -0.050
                    -0.050 328460762
 2:
        -0.050
                    -0.025 325033992
 3:
        -0.050
                     0.000 322421020
 4:
        -0.050
                     0.025 320504552
 5:
        -0.050
                     0.050 319186049
 6:
        -0.025
                    -0.050 311683186
 7:
        -0.025
                    -0.025 307623430
 8:
        -0.025
                     0.000 304419662
9:
        -0.025
                     0.025 301949067
                     0.050 300108452
10:
        -0.025
         0.000
                    -0.050 297029150
11:
12:
         0.000
                    -0.025 292361338
13:
         0.000
                     0.000 288592082
14:
         0.000
                     0.025 285592962
                     0.050 283256060
15:
         0.000
16:
         0.025
                    -0.050 284244024
                    -0.025 278989304
17:
         0.025
18:
         0.025
                     0.000 274676127
19:
         0.025
                     0.025 271170379
20:
         0.025
                     0.050 268359339
21:
         0.050
                    -0.050 273109708
22:
         0.050
                    -0.025 267285998
23:
         0.050
                     0.000 262447265
24:
         0.050
                     0.025 258453612
25:
         0.050
                     0.050 255187443
    delta_Tide delta_Gain
                               profit
```

#### Some hints:

- Before you start the loop, store the original price levels of Tide and Gain.
- Update the price columns in move\_predict and then predict demand.
- Calculate total profits at the new price levels for both brands and then store the total profit from Tide and Gain in profit\_DT.

Show a table of profits in levels and in ratios relative to the baseline profit at current price levels, in order to assess the percent profit differences resulting from the contemplated price changes.

Discuss the profitability predictions and how prices should be changed, if at all. How do you reconcile the recommended price changes with the own-price elasticity estimates?

The profitability predictions seen in the table above show that the greatest profits occur when both Tide and Gain are discounted by 5%, with overall projected profits decreasing as prices rise. Purely off of this data, Proctor&Gamble should consider lowering the prices of their products to maximize profits. However, previous analysis showed that customer demand is not overly reactive to permanent price changes, but are much more elastic to promotions. These two seemingly contradictory points could potentially be reconciled by Proctor&Gamble by increasing the frequency of promotions, but decreasing the amount by which products are discounted, as the demand-boosting affects of running a "promotion" could still be present.