



Cleaning and Training

Data-driven Photon Particle Identification In the ATLAS Experiment

Benjamin Henckel, Troels C. Petersen



Outline

- **Theory**
- **The ATLAS Experiment**
- **Machine Learning Methods**
- **Datasets**
- **Models**
- **MC Results**
- **Training In Data**
- **Label Confusion**
- **Decorrelation Framework**
- **Data Results**
- **Evaluation on $H \rightarrow \gamma\gamma$**
- **Summary & Outlook**

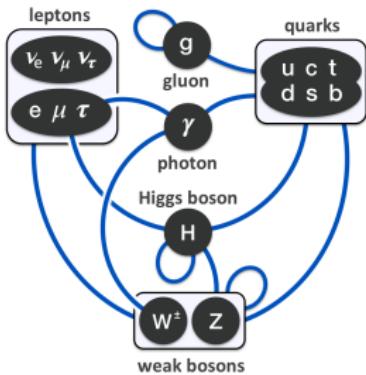
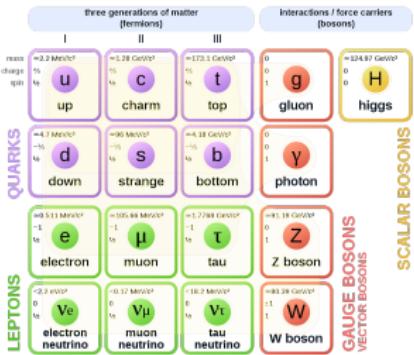
Aim of the thesis

e/γ Particle Identification at the ATLAS Experiment with focus on data-driven methods.



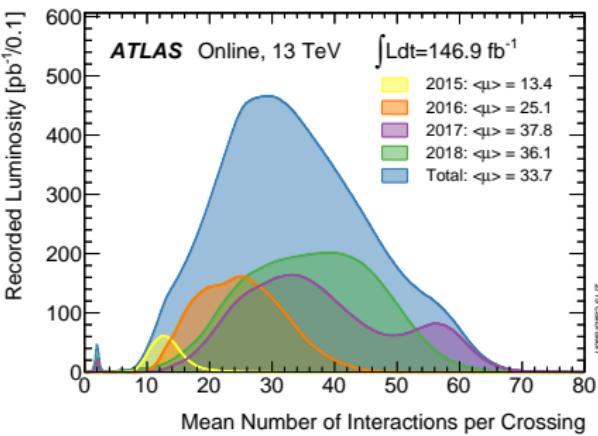
Theory

Standard Model of Elementary Particles



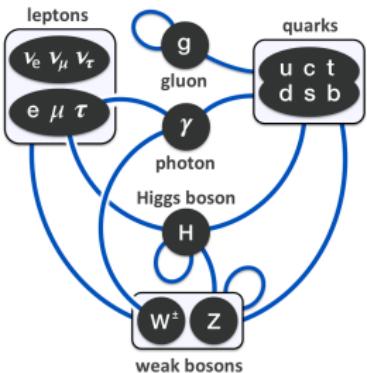
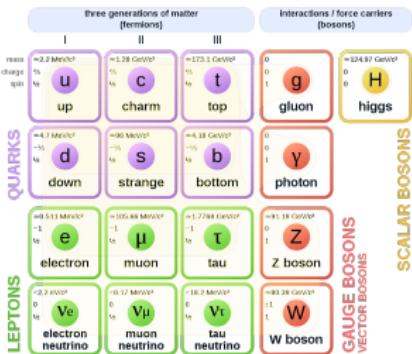
Pileup is a measure of how much is happening in your detector.

Luminosity is a direct measure of your ability to probe interesting physics



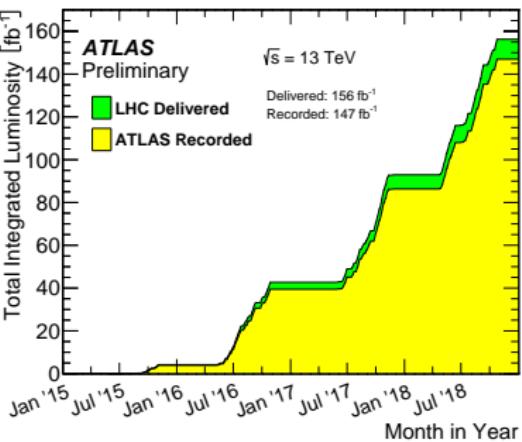
Theory

Standard Model of Elementary Particles



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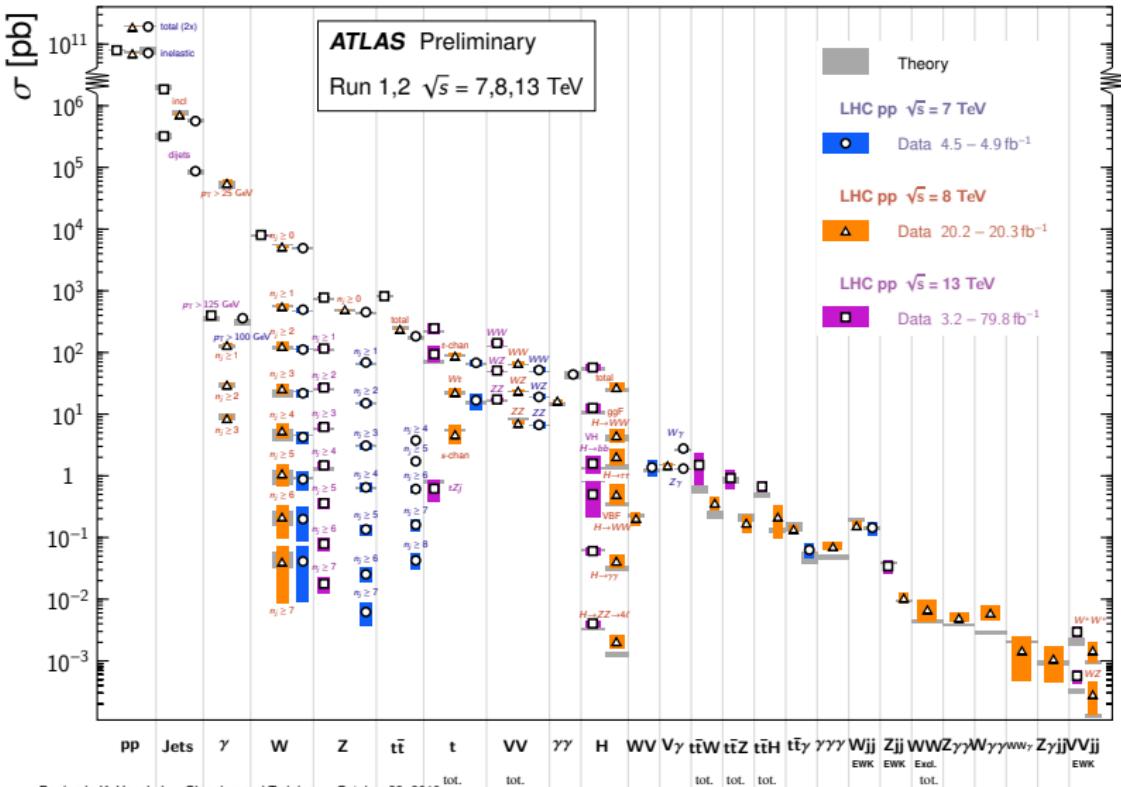
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Theory

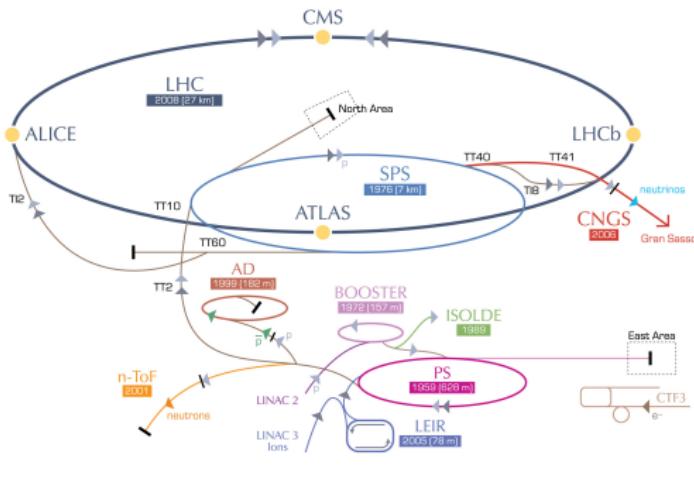
Standard Model Production Cross Section Measurements

Status: July 2018



The ATLAS Experiment

CERN's accelerator complex

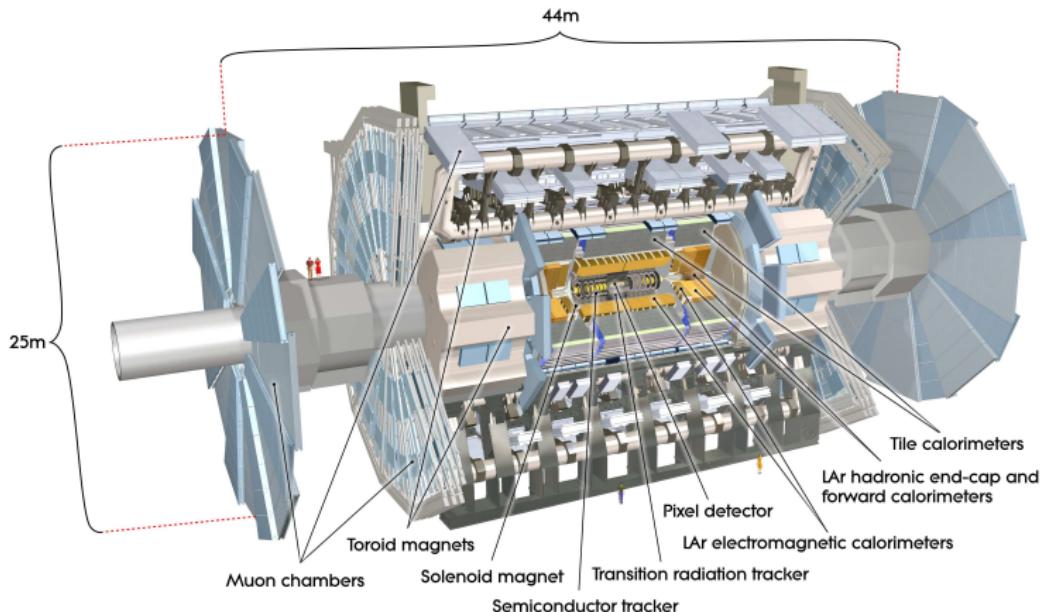


European Organization for Nuclear Research | Organisation européenne pour la recherche nucléaire

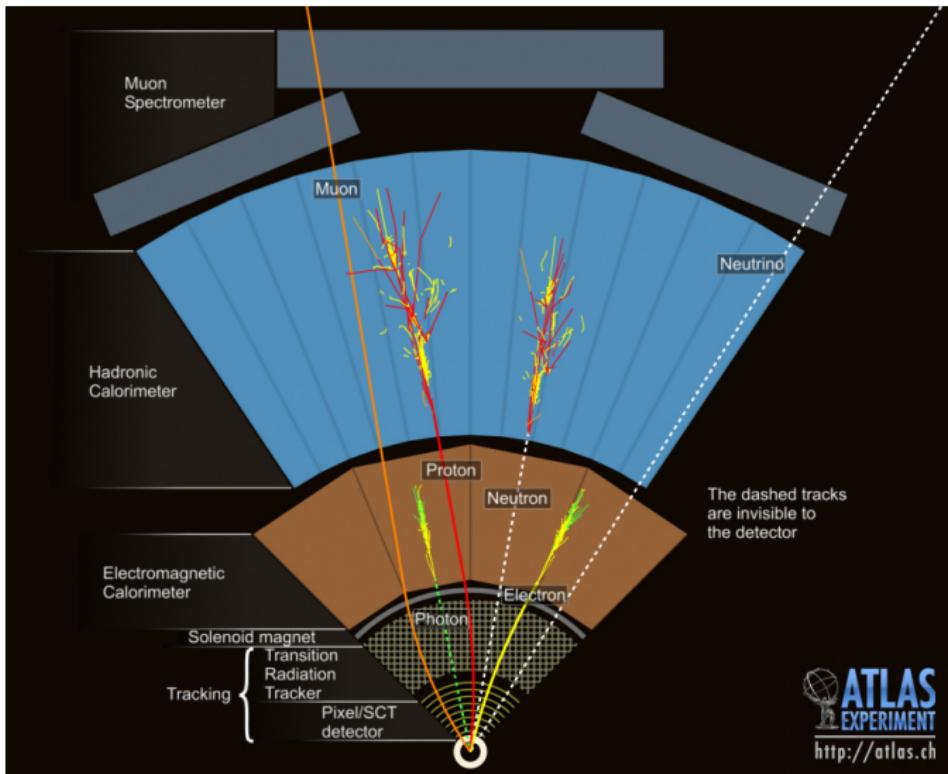
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The ATLAS Experiment



The ATLAS Experiment



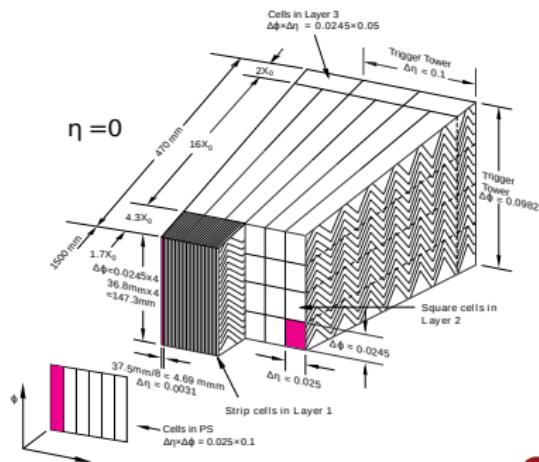
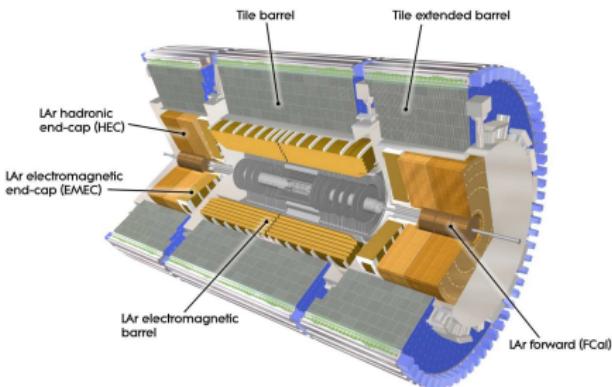
The ATLAS Experiment

The calorimeter measures the energy of the particles by stopping them.

It is separated in electromagnetic (ECAL) and hadronic (HCAL) subdetectors.

The entirety of the ECAL uses a LAr as the active material and have accordion shaped lead absorbers.

The HCAL is a sampling calorimeter. It uses LAr in the end-cap and scintillating material in the rest.



The ATLAS Experiment

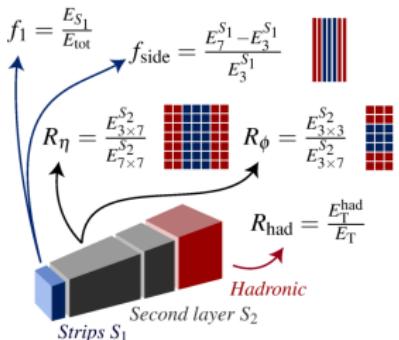
Photon Identification

Loose

1 dimensional cuts on 4 variables

Optimized in bins of $|\eta|$

Designed to select all signal ($\approx 99\%$),
while reducing background by a factor
1000

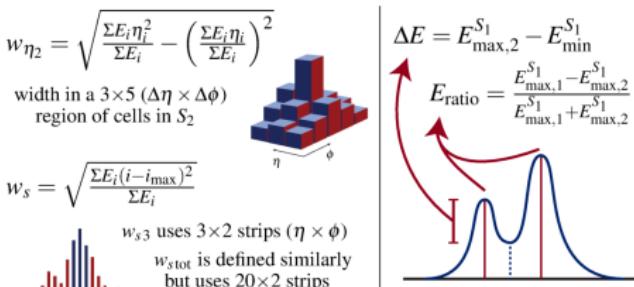


Tight

1 dimensional cuts on 10 variables

Optimized in bins of $|\eta|$ and E_T

Designed for analyses.



Machine Learning Methods

Different types of Machine Learning models have been trained. Tree based models: **Random Forest** (RF) and **Boosted Decision Trees** (BDTs) and feed-forward **Neural Networks** (NN).

The trees based models are implemented using the LightGBM framework provided by Microsoft.

The Neural Networks are implemented using Keras with TensorFlow backend.

Many other frameworks have been used for crucial parts in the model development.

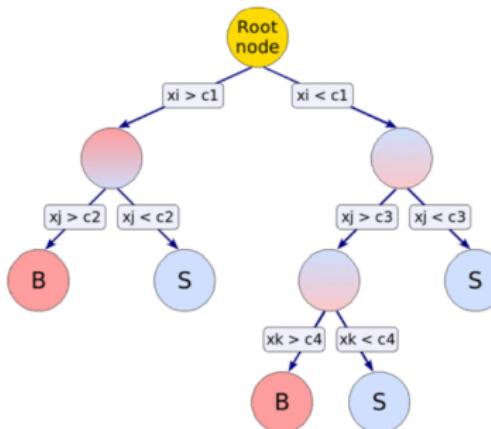
Optimization is done using the *gp_minimize* and *rf_minimize* packages from Sci-kit Optimize.

Feature importance has been estimated using SHapely Additive exPlanations (SHAP).

Reweighting has been done using the GBReweighter package from *hep_ml*.



Machine Learning Methods



Random Forest

Creates independent decision trees

Using **bagging** and **subsampling**

Majority vote makes a strong classifier

Boosted Decision Trees

Creates dependent decision trees

Using **Boosting** and **gradient descent**

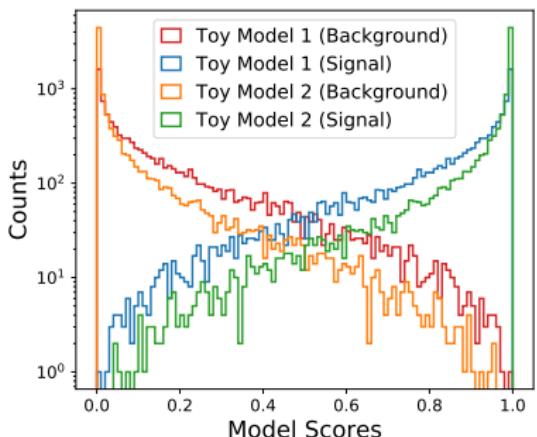
Continued training will lead to over training!



Machine Learning Methods: Evaluation

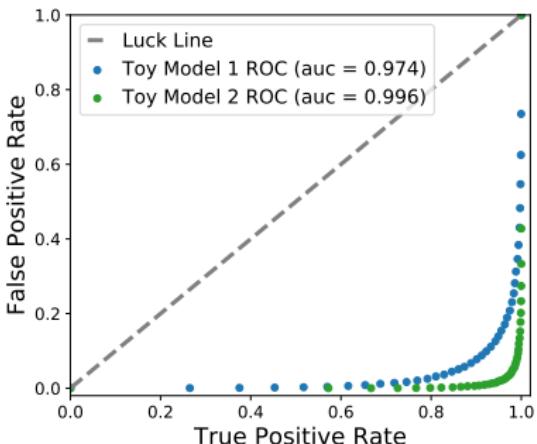
Four possible outcomes: True Positive (TP), True Negative (TN), False Positive (FP), and False Negative (FN).

$$TPR = \frac{TP}{TP + FN} \quad \text{and} \quad FPR = \frac{FP}{FP + TN}$$

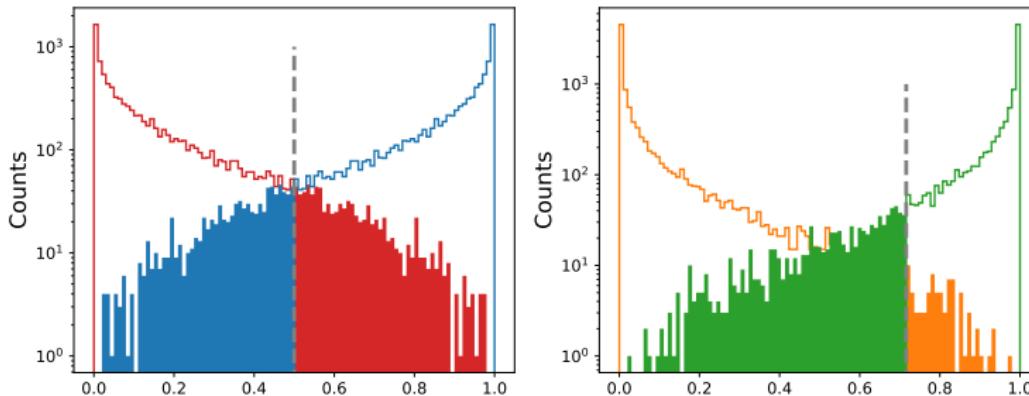


The **ROC** curve is a visualization of TPR and FPR.

AUC reduces the ROC curve to one number.



ML Methods



Improvement factors are defined:

$$Imp_{FPR} = \frac{FPR_{m1}}{FPR_{m2}} - 1 = \frac{FP_{m1}}{FP_{m2}} - 1 \quad \text{and} \quad Imp_{TPR} = \frac{TPR_{m1}}{TPR_{m2}} - 1 = \frac{TP_{m1}}{TP_{m2}} - 1$$



Datasets

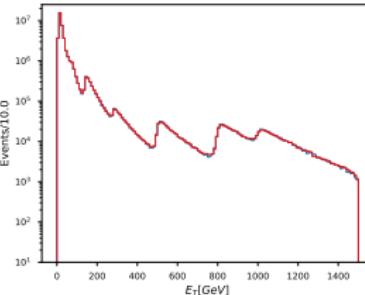
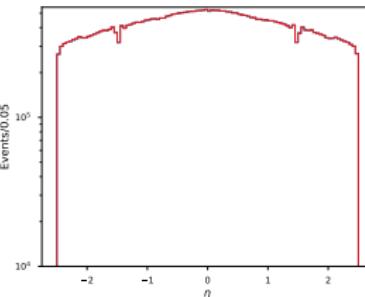
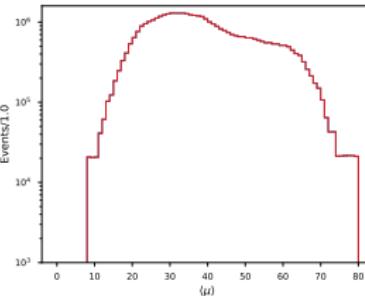
MC Photon Dataset

High statistics (104,976,458 datapoints)
 dataset taking advantage of the truth matching
 available in MC.

The only selection applied $p_T < 4.5\text{ GeV}$

Covers a massive energy range, but has many potential flaws.

Label	Total [%]	Composition [%] and Description	
Signal	7.91	100.0	Isolated Photons
Background	92.09	70.31	Background Photons
		19.30	Non truthmatched Objects
		8.23	Hadrons
		1.36	Electrons
		0.73	Non Isolated Photons



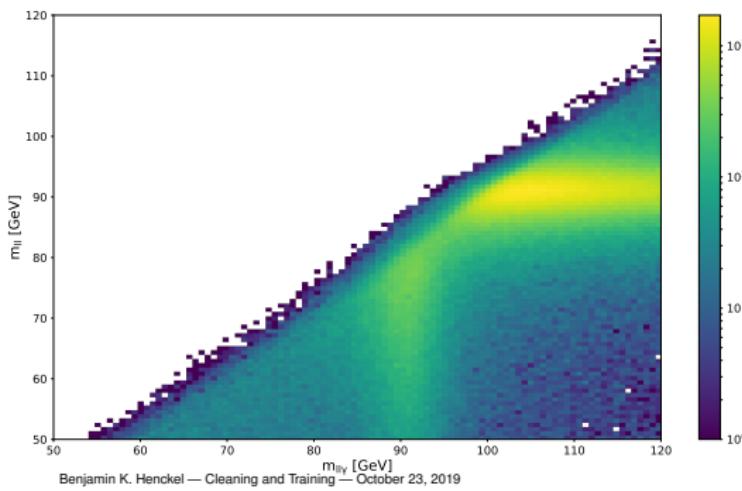
Datasets

DATA Photon Dataset

A Tag, Tag, and Probe (TPP) framework intended to select $Z \rightarrow l l/\gamma$ in DATA.

Uses all of data17 (9,576,799 probes selected)

The 2D histogram of the invariant mass of the tag pair and of the tag pair plus the probe reveals significant background in output.



TagElectronPairs

- ✓ Both have $pT > 26$ GeV
- ✓ Both have track
- ✓ Both from first primary vertex
- ✓ Both pass Medium ID
- ✓ Both pass Loose Isolation
- ✓ Triggers

TagMuonPairs

- ✓ Both have $pT > 26$ GeV
- ✓ Both have track in ID
- ✓ Both from first primary vertex
- ✓ Both pass medium quality
- ✓ Both pass Loose isolation
- ✓ Triggers

probePhotons

- ✓ Has $pT > 9.5$ GeV
- ✓ Pass Object Quality (cluster)

llGamma Candidates

- ✓ $\Delta R(\text{Tag}, \text{Probe}) > 0.4$ (0.2) for electron (muon) tags

$N(\text{Candidate}) = 1$

Selected Events

Models

Models will be trained on an **increasing** number of variables.

The variables are based on the ones directly and indirectly used by the current methods.

A few **new**, carefully chosen, variables have been added in the **extra** variable set.

Name	Nvars	Vars
Showershape (pdf)	11	Rhad1 Rhad Reta weta1 weta2 Rphi Reta fracs1 DeltaE Eratio f1
Conversion (conv)	15	ConversionType ConversionRadius VertexConvEtOverPt VertexConvPtRatio
Binning (bin)	18	η E_T $\langle \mu \rangle$
Extra (ext)	22	maxEcell_time maxEcell_energy core57cellsEnergyCorrection r33over37allcalo

The namingscheme of the models follow this outline:

Modelname : " MODELTYPE" (" DATATYPE" , " varlist")



Models

The isolation models are trained on the following 9 variables:

topoetcone20, topoetcone30, topoetcone40,

ptvarcone20, ptvarcone30, ptvarcone40,

E_T, NvtxReco, averageInteractionsPerCrossing

For training and evaluation of all models the datasets have been split into training, validation and evaluation sets

Training set is shown to the models during training

Validation set is used for early stopping

Evaluation set is only used for making final plots

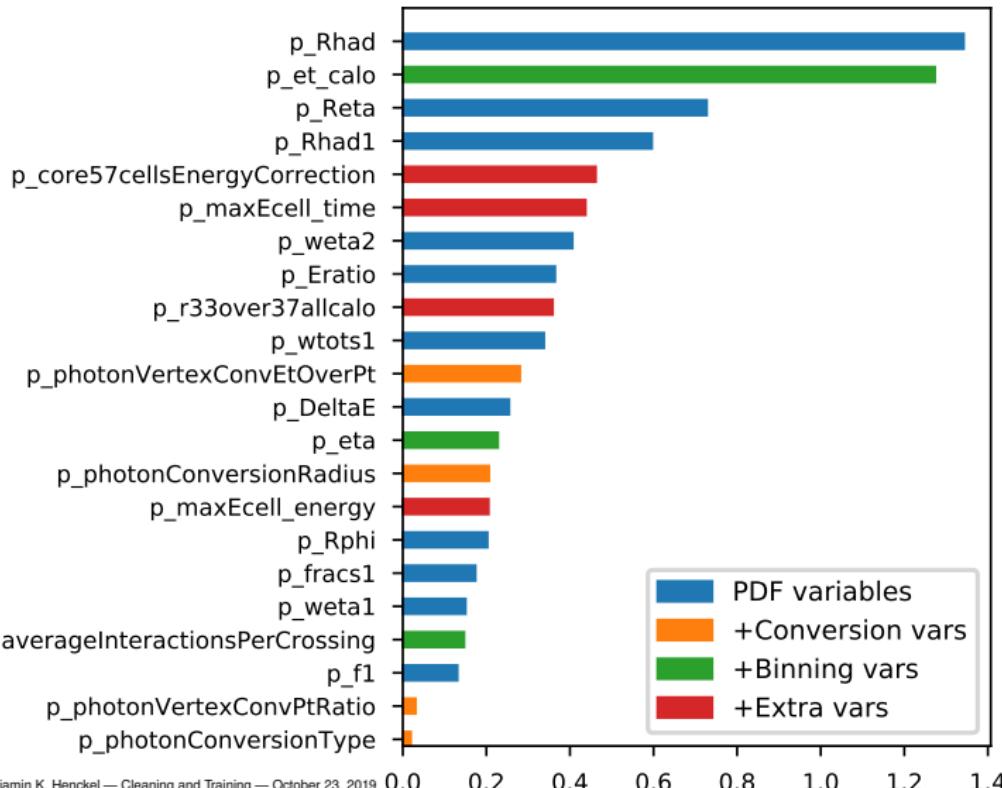
The training is done **inclusively** in E_T , η and conversions



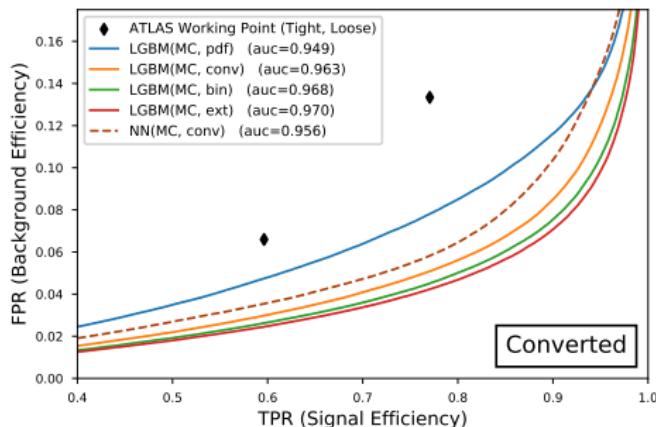
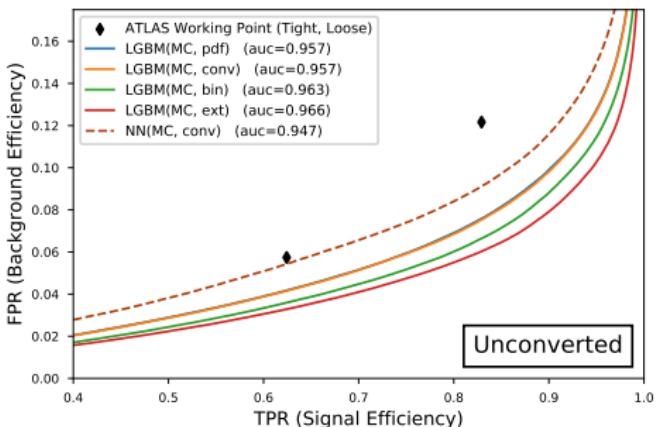
MC Trained Model Evaluation



MC Results



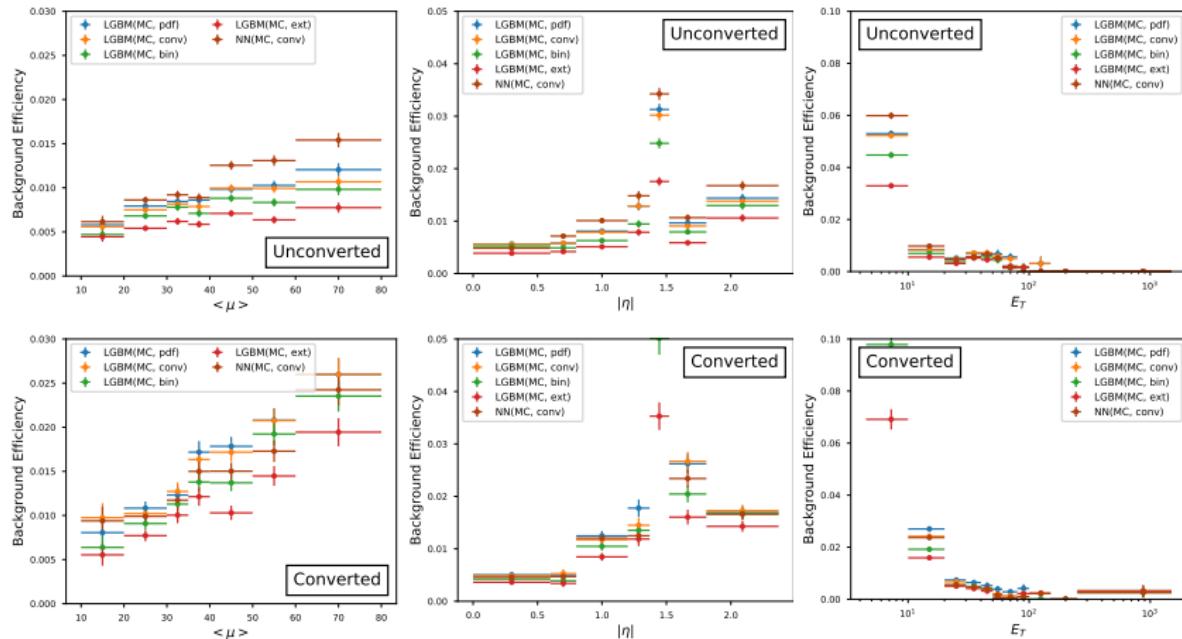
MC Results



The results in MC will be evaluated separately for the Unconverted and Converted channels. The ROC curves reveal a good overall performance across all models, in both channels.



MC Results



The background efficiency as a function of $\langle \mu \rangle$, $|\eta|$, and E_T , at a fixed signal efficiency of 90% against hadronic background.



Training in DATA

Bigest advantage is training directly on real variable distributions

Bigest disadvantage is lack of true labels

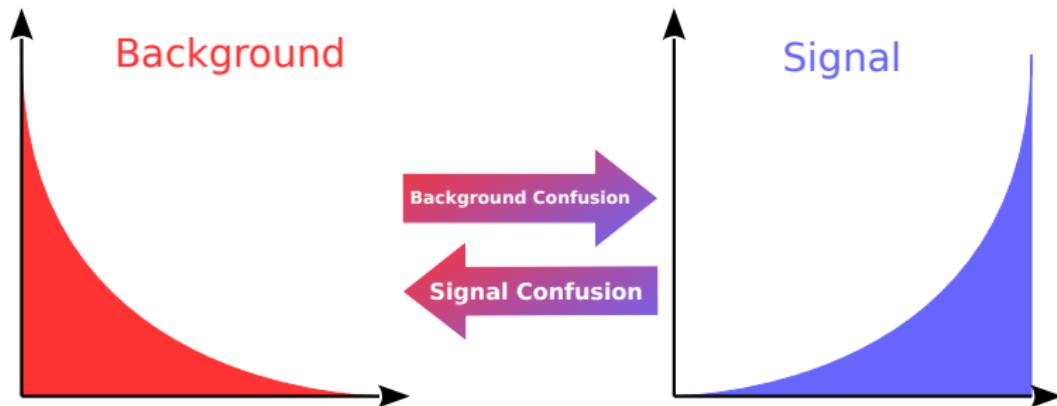
This leaves two major questions to be answered:

How does our models behave when given imperfect labels?

How do we aquire labels in DATA?



Label Confusion

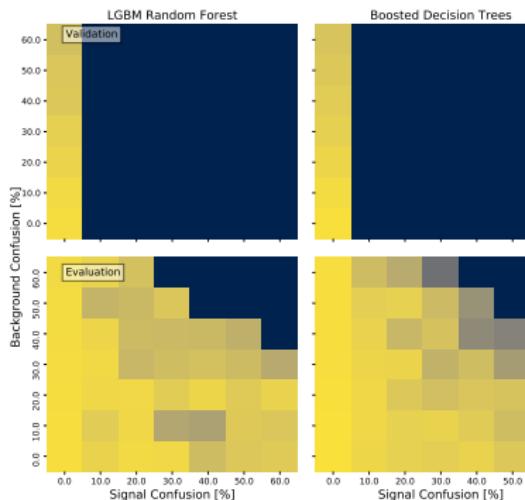


Label Confusion describes the presence of wrongly assigned signal and background labels in the dataset. This is inescapable in DATA.

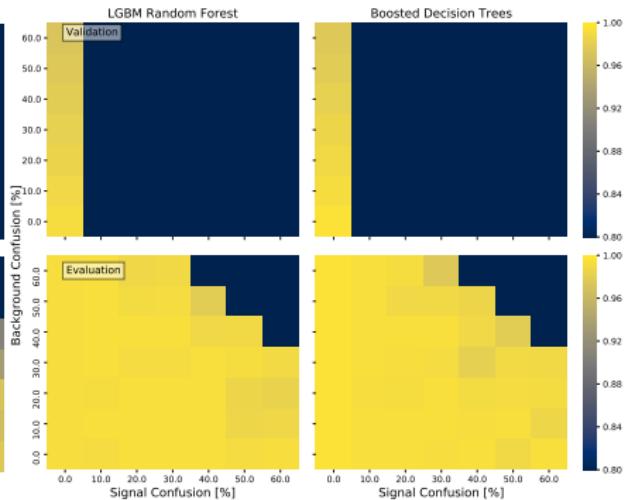


Label Confusion

(a) Low Statistics Training



(b) High Statistics Training



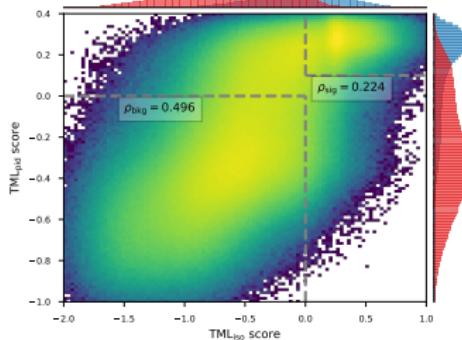
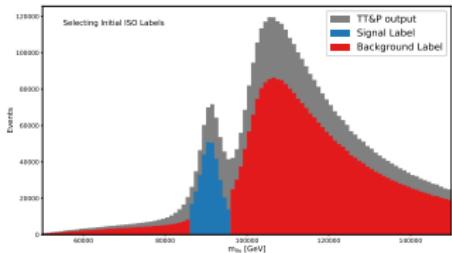
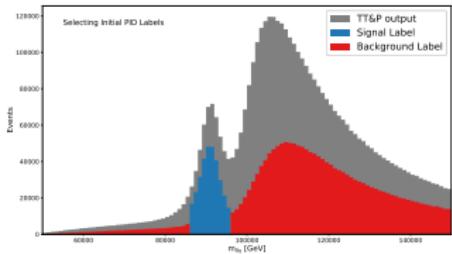
Evolution of **AUC** as a function of increasing confusion, for validation (top) and evaluation (bottom) sets.



Decorrelation Framework

Initial labels are chosen using the following cuts:

Task	Signal Selection	Background Selection
Identification	$ m_{\ell\ell} - m_Z < 10\text{GeV}$, $\frac{etcone40}{ET} < 0.06$	$ m_{\ell\ell} - m_Z > 10\text{GeV}$, $\frac{etcone40}{ET} > 0.15$
Isolation	$ m_{\ell\ell} - m_Z < 10\text{GeV}$, Loose	$ m_{\ell\ell} - m_Z > 10\text{GeV}$, !Loose



The logit transformation is the following:

$$TML = -\log(1/ML - 1)/k$$



Decorrelation Framework

A linear decorrelation usually applies a rotation, which in turn changes both values. The intend is to only change the isolation variable. This is achieved by defining the following variables:

$$x = \frac{pid}{\sigma_{pid}} \quad \text{and} \quad y = \frac{iso}{\sigma_{iso}}$$

Then the following is true:

$$\sigma^2(x) = \sigma^2(y) \quad \text{and} \quad \text{Cov}(x, y) = \rho_{xy}$$

We can then define a new y variable that is linearly uncorrelated from x :

$$y' = y - \rho \times x$$

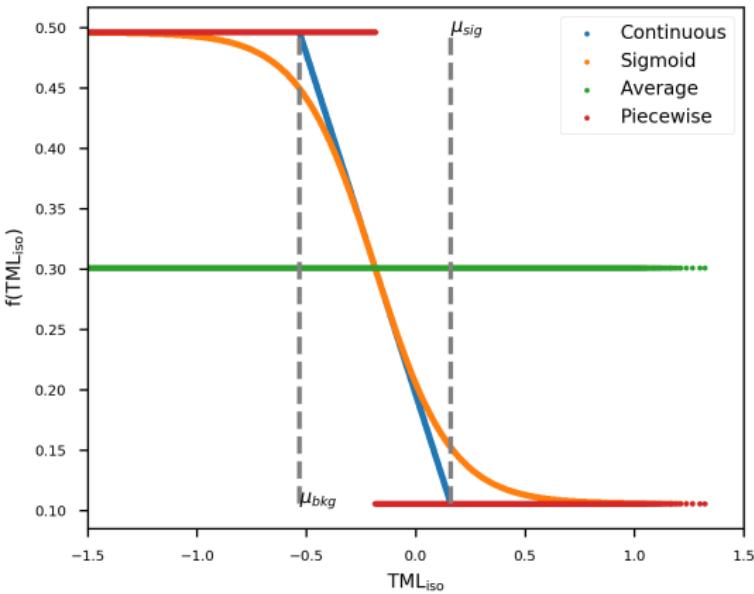
Inserting x and y , we find the following recipe for an isolation variable that is linearly uncorrelated from particle identification:

$$iso' = iso - \rho_{iso,pid} \times \frac{\sigma_{iso}}{\sigma_{pid}} \times pid^{-1}$$

¹ Mistakenly used variance in thesis



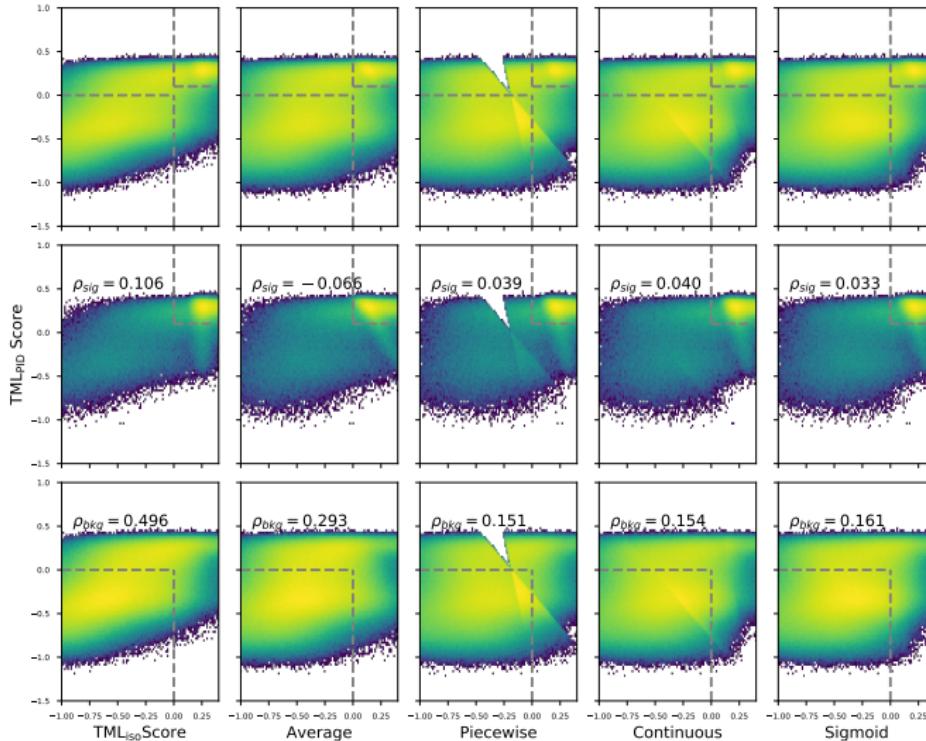
Decorrelation Framework



A visualization of the decorrelation methods. $\rho_{sig,bkg}$, σ_{iso} and σ_{pid} are calculated following these recipes.



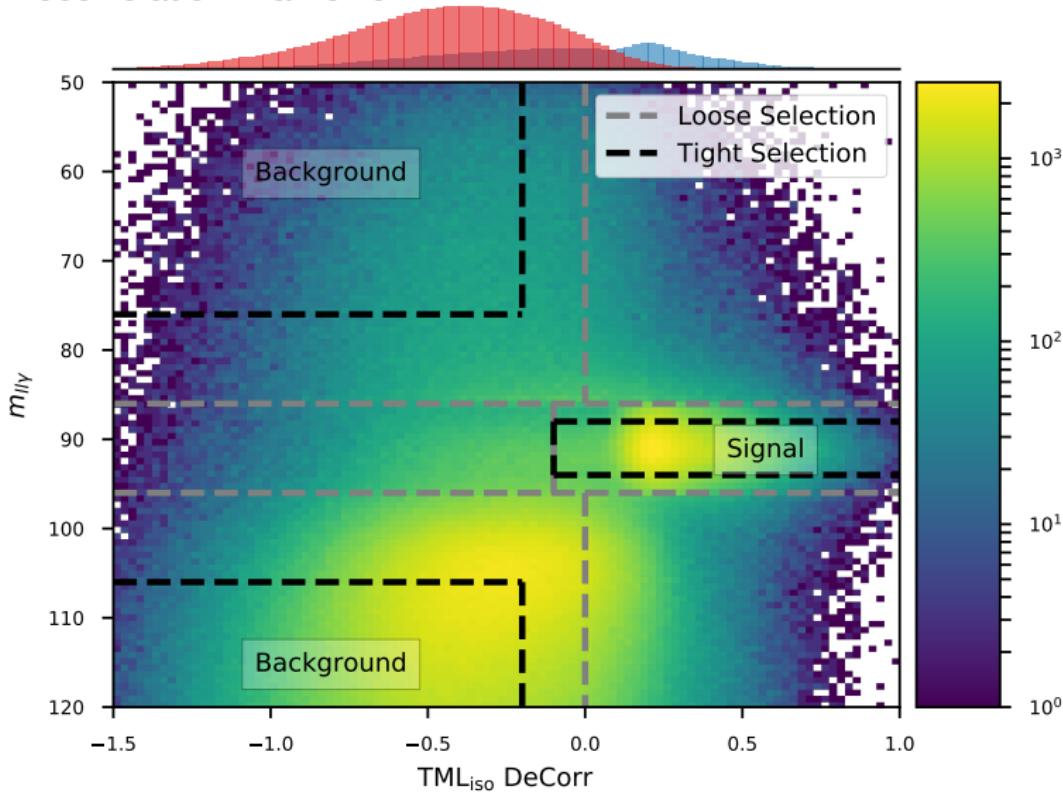
Decorrelation Framework



The resulting decorrelation, when applying the different methods.



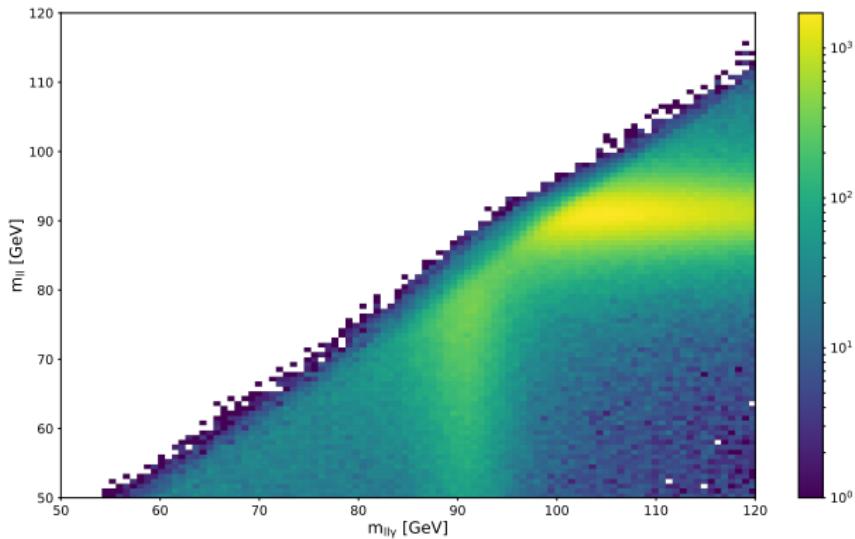
Decorrelation Framework



Results in DATA

The background efficiency was matched in a background region
 $(m_{\ell\ell\gamma} > 110\text{GeV})$

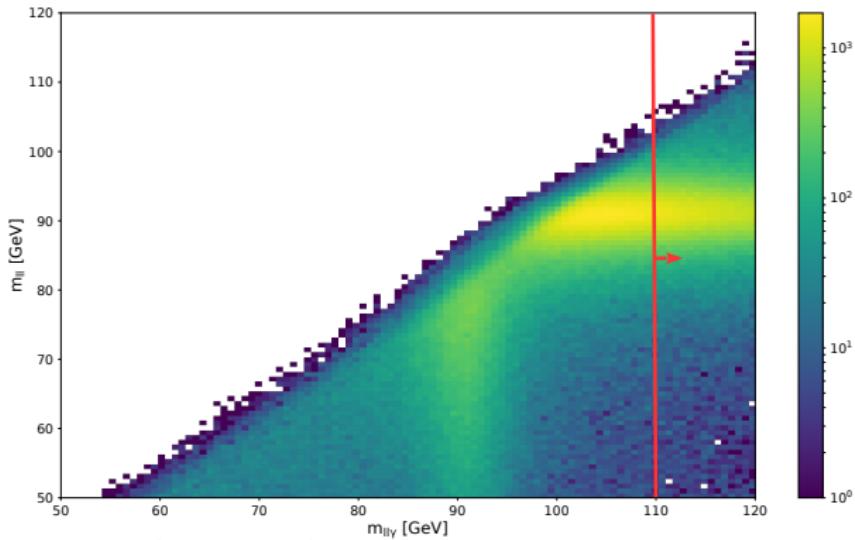
For evaluation $m_{\ell\ell} < 82\text{GeV}$ cut was applied. Improvement calculated from all events left after cut.



Results in DATA

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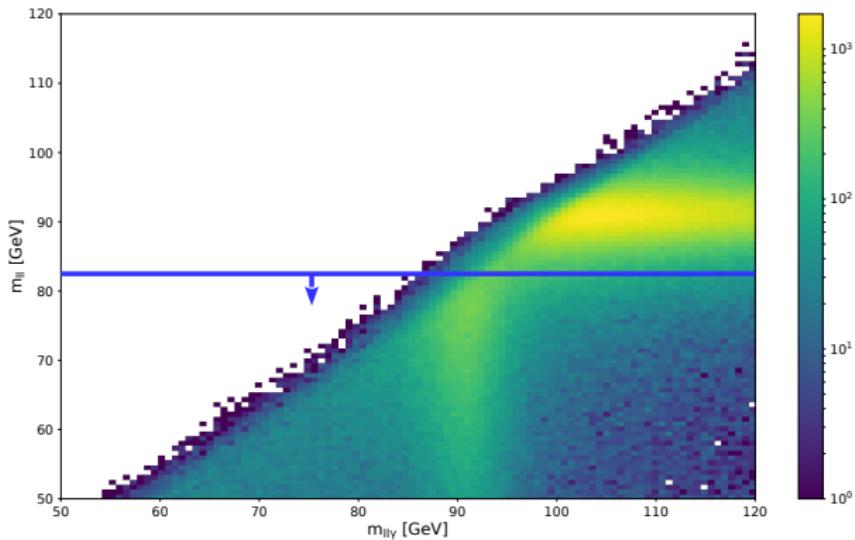
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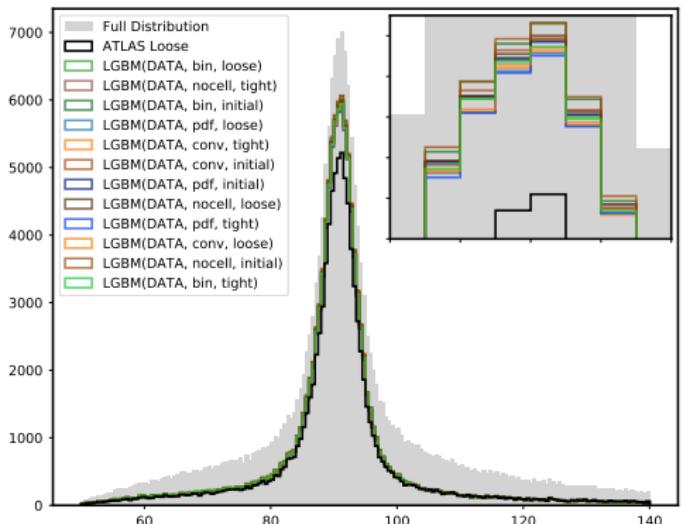
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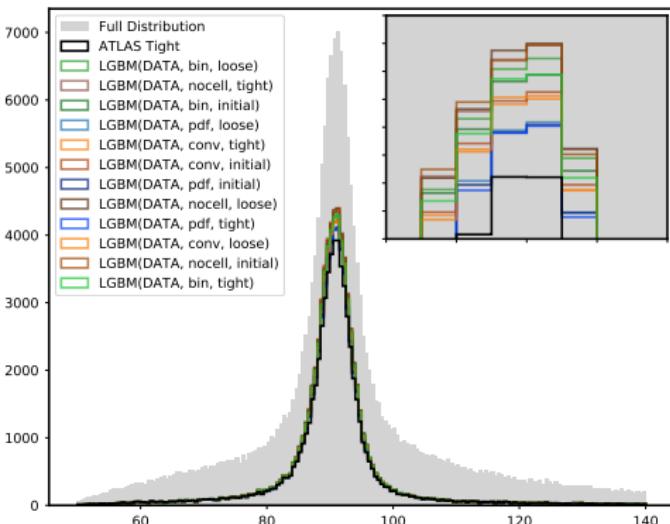


Results in DATA

Loose



Tight



The **DATA** trained models evaluated on the $Z \rightarrow ll\gamma$ peak, with background efficiency matched to the Loose (left) and Tight (right) working points.



Results in DATA

		Improvement [%] (ATLAS Loose)			
DATA Models		pdf	conv	bin	nocell
initial		12.10 ± 0.05	12.60 ± 0.05	13.94 ± 0.06	14.33 ± 0.06
loose		11.40 ± 0.05	11.89 ± 0.05	13.12 ± 0.06	13.39 ± 0.06
tight		11.12 ± 0.05	11.60 ± 0.05	12.72 ± 0.05	12.94 ± 0.06
MC Models					
Truth		12.59 ± 0.05	12.92 ± 0.06	13.78 ± 0.06	14.08 ± 0.06

Improvement factor of all models evaluated on the $Z \rightarrow \ell\ell\gamma$ peak, with background efficiency matched to the Loose (top) and Tight (bottom) working points. The first column indicate the label selection the model was trained on.



Results in DATA

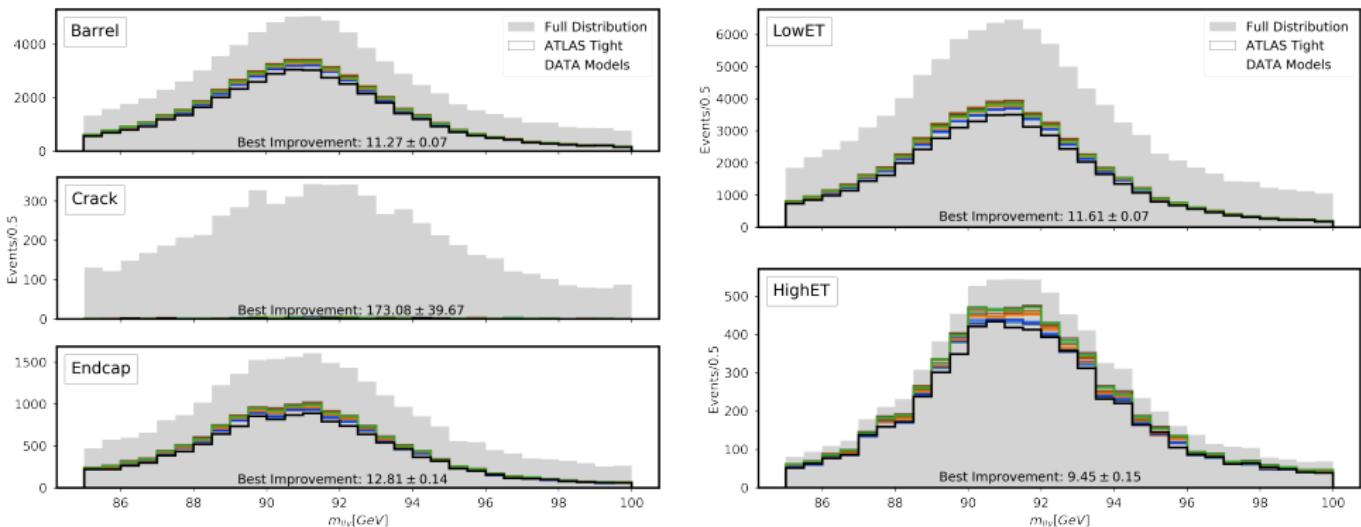
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tight	11.12 ± 0.05	11.60 ± 0.05	12.72 ± 0.05	12.94 ± 0.06
MC Models				
Truth	12.59 ± 0.05	12.92 ± 0.06	13.78 ± 0.06	14.08 ± 0.06

Improvement [%] (ATLAS Tight)				
DATA Models	pdf	conv	bin	nocell
initial	4.61 ± 0.03	7.45 ± 0.04	9.06 ± 0.05	10.87 ± 0.06
loose	4.77 ± 0.03	7.17 ± 0.04	9.92 ± 0.05	11.11 ± 0.06
tight	4.19 ± 0.02	6.97 ± 0.04	9.05 ± 0.05	10.78 ± 0.06
MC Models				
Truth	1.42 ± 0.01	5.74 ± 0.03	6.47 ± 0.04	7.96 ± 0.04

Improvement factor of all models evaluated on the $Z \rightarrow \ell\ell\gamma$ peak, with background efficiency matched to the Loose (top) and Tight (bottom) working points. The first column indicate the label selection the model was trained on.



Results in DATA



Split DATA $Z \rightarrow \ell\ell\gamma$ evaluation of DATA models in the barrel ($|\eta| < 1.37$), crack ($1.37 < |\eta| < 1.52$), and end-cap ($1.52 < |\eta| < 2.37$), and at low and high E_T . Compared to the Tight (right) working point.



Evaluation on $H \rightarrow \gamma\gamma$

The $H \rightarrow \gamma\gamma$ MC dataset is selected by a simple selection, that does not include background.

The background efficiencies of the models are matched to the **Tight** working point in the MC photon dataset in the energy range $50\text{GeV} < E_T < 80\text{GeV}$.

This is a favourable comparison for the models, but the best one available.

Candidate Selection

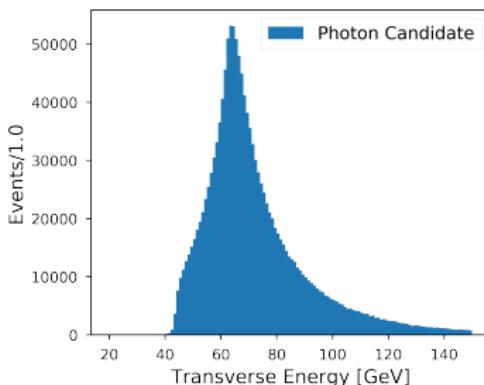
Overlap Removal

$$E_T > 25\text{GeV}$$

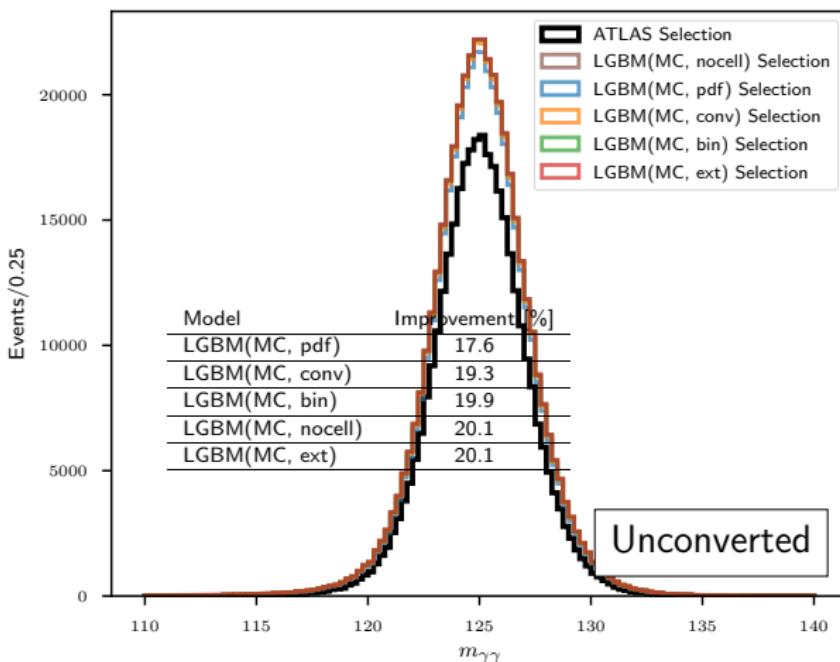
$$E_T/m_{\gamma\gamma} > 0.35(0.25)$$

Veto Crack

Loose Isolation



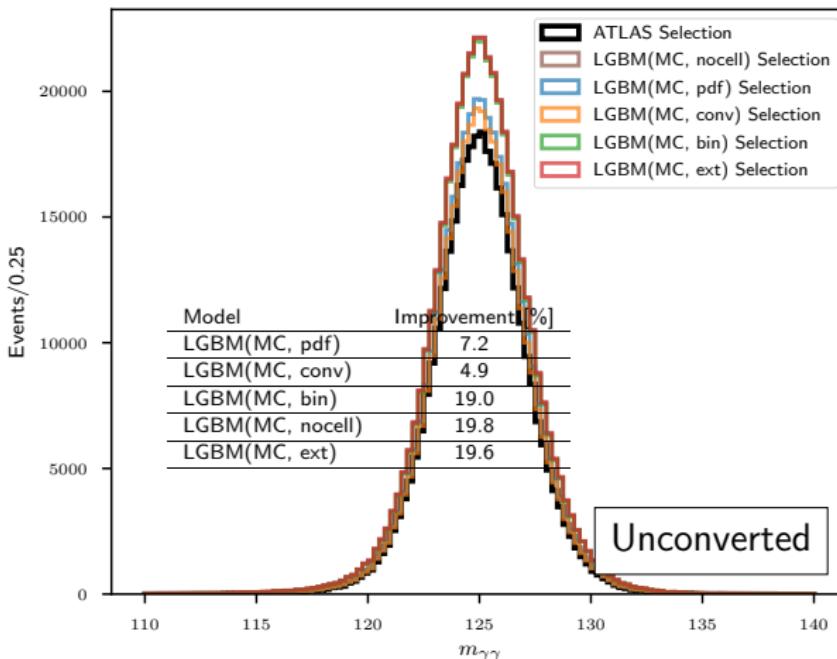
Evaluation on $H \rightarrow \gamma\gamma$



The unconverted channel shows incredibly promising improvements.



Evaluation on $H \rightarrow \gamma\gamma$



To increase confidence in the improvements, the background efficiency has been matched to the Tight working point against **hadronic** background only.

Summary & Outlook

Several MC- and DATA-driven models have been trained and evaluated

A method for selecting high purity samples in DATA has been developed, using an ML isolation model

Evaluation in DATA $Z \rightarrow \ell\ell\gamma$, MC $H \rightarrow \gamma\gamma$ shows promising improvements.



Summary & Outlook

Several MC- and DATA-driven models have been trained and evaluated

A method for selecting high purity samples in DATA has been developed, using an ML isolation model

Evaluation in DATA $Z \rightarrow \ell\ell\gamma$, MC $H \rightarrow \gamma\gamma$ shows promising improvements.

Implement models in Athena → Test them through proper channels

Use data from whole of Run2 for training of DATA models.

Test on full $H \rightarrow \gamma\gamma$ analysis or similar high profile channel (Most importantly, with background).

Expand onto more complex models.



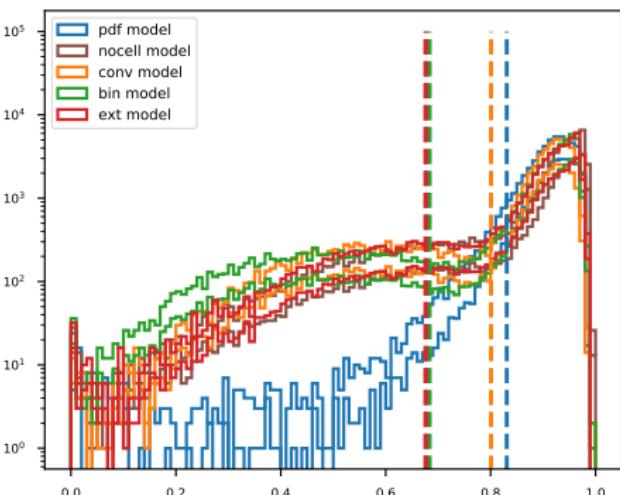
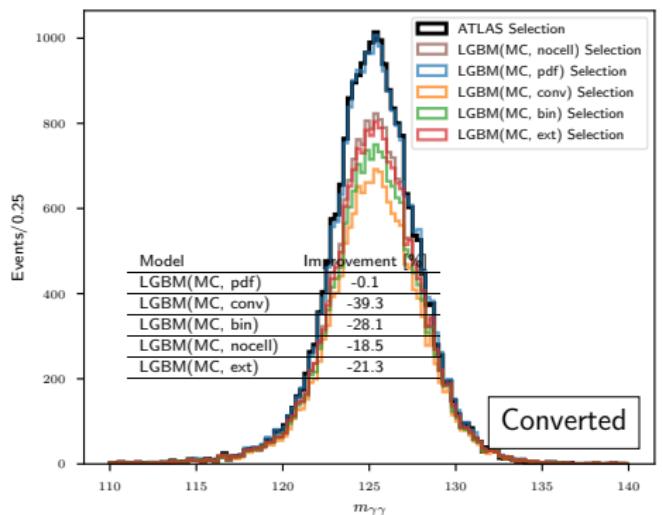
Appendix



$H \rightarrow \gamma\gamma$ Bug in Converted Channel



Evaluation on $H \rightarrow \gamma\gamma$



Unfortunately a bug caused the calculation of the conversion variables to fail.
 This causes all the models that include these variables to collapse. It is hard to conclude anything from the converted channel



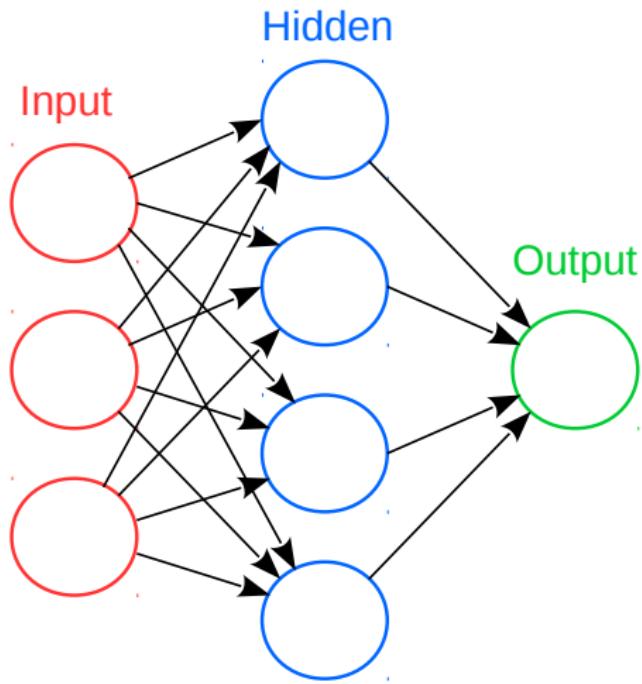
Neural Networks



Machine Learning Methods

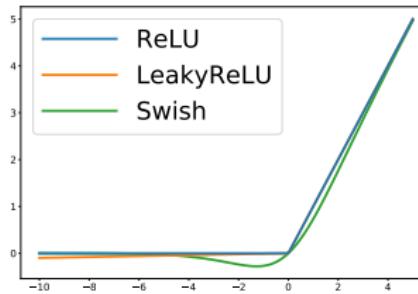
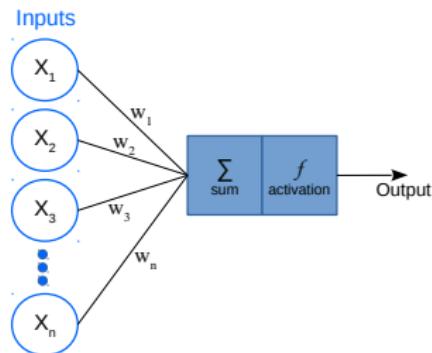
Neural Network

Universal Function Approximators.



Benjamin K. Henckel — Cleaning and Training — October 23, 2019

Slide 5/43



Electron PID Results

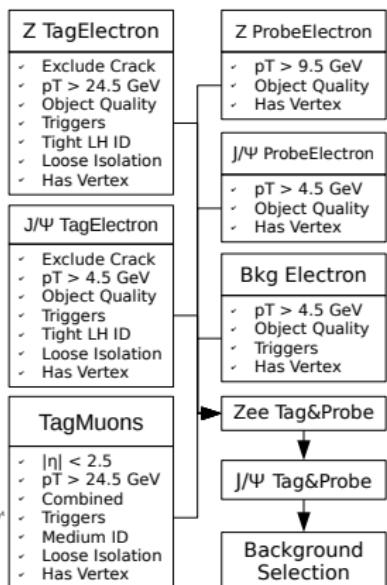
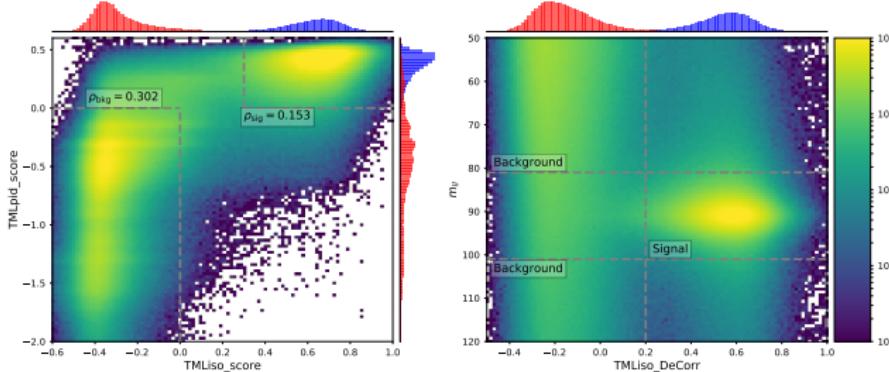


Electron PID results

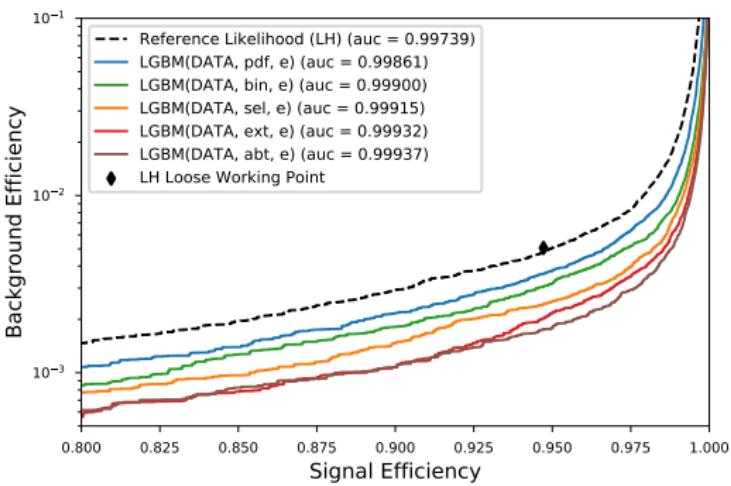
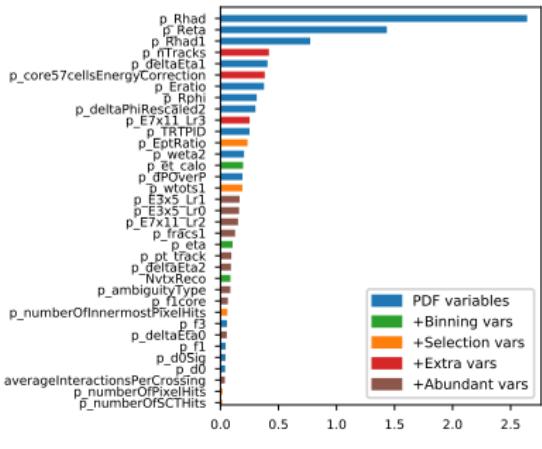
The Electron dataset is a signal $Z \rightarrow ee$ and accompanying background selection run on a large subset of data from 2017.

It was used as a test for the decorrelation framework, however, models trained perform well.

Training in DATA yielded 3 new variables, which did not perform well on MC.



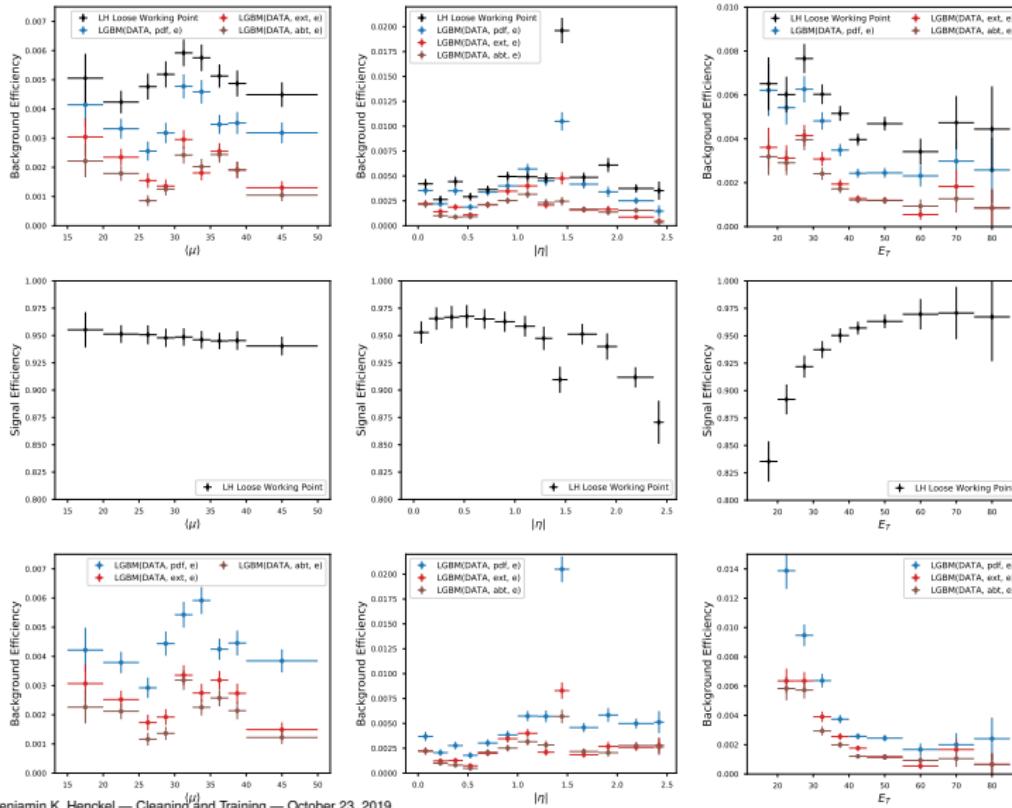
Electron PID results



The great performance of the 3 variables in the extra variable set is unique to training in DATA. All models show promising overall performance.



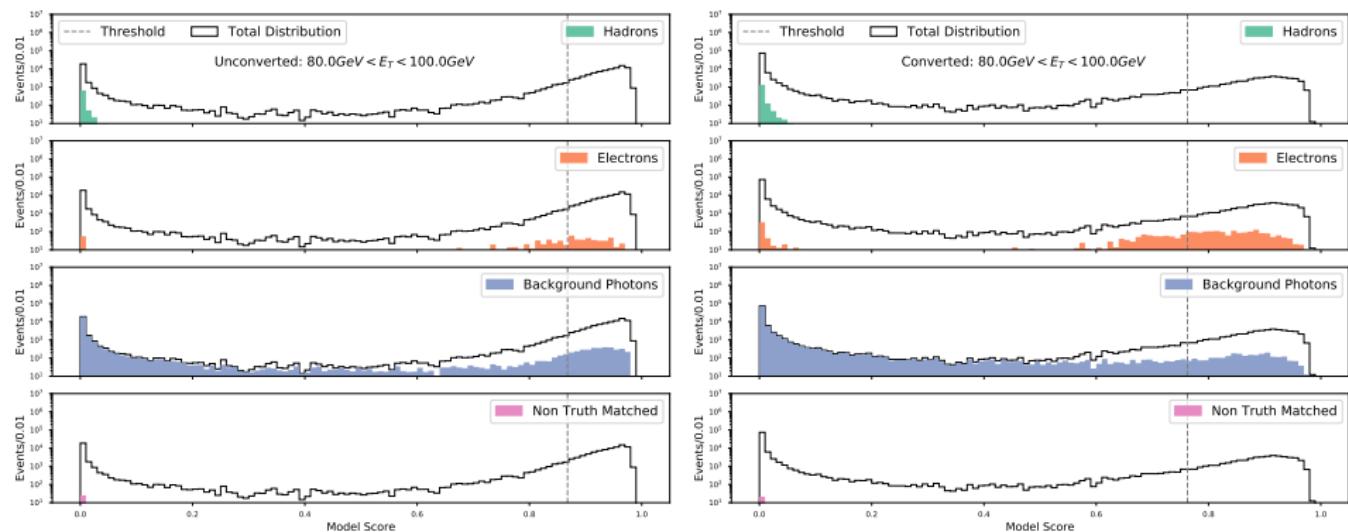
Electron PID results



Background Composition in MC Photon Dataset



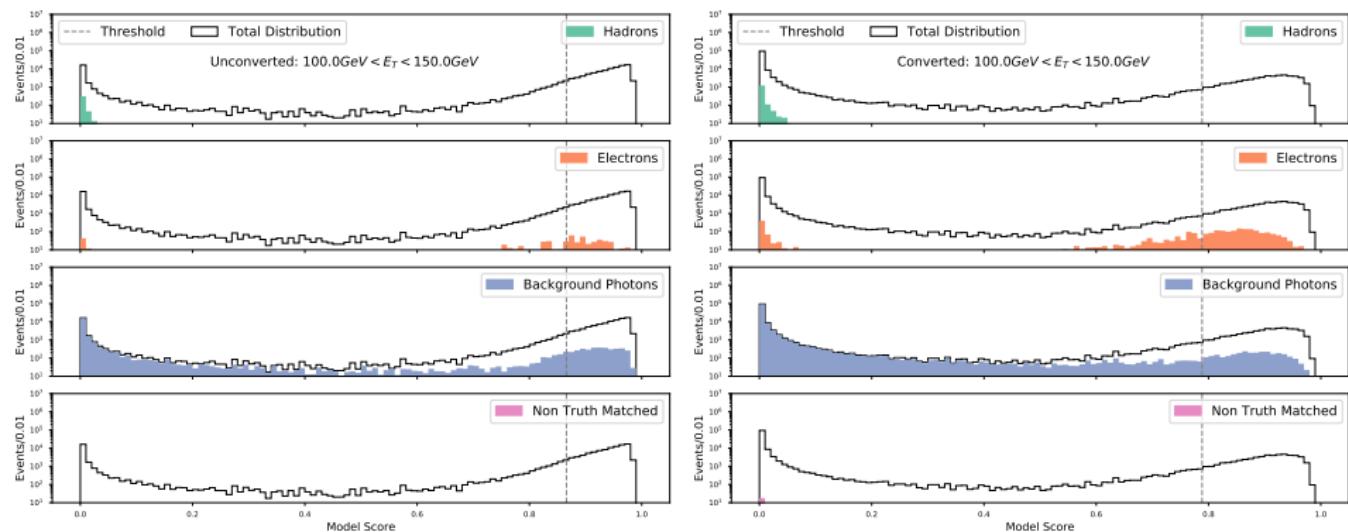
Background Composition In MC Photon Dataset



The problematic behaviour in the unconverted channel is caused by background photons, with increasing energy, they become increasingly signal-like. This effect is barely present in the converted channel.



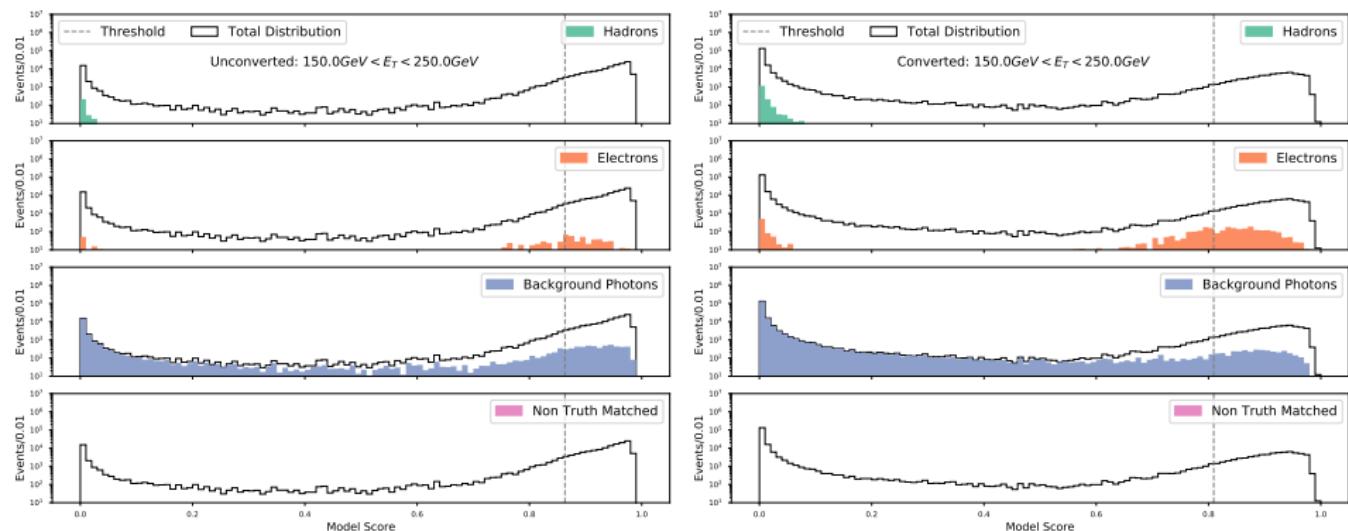
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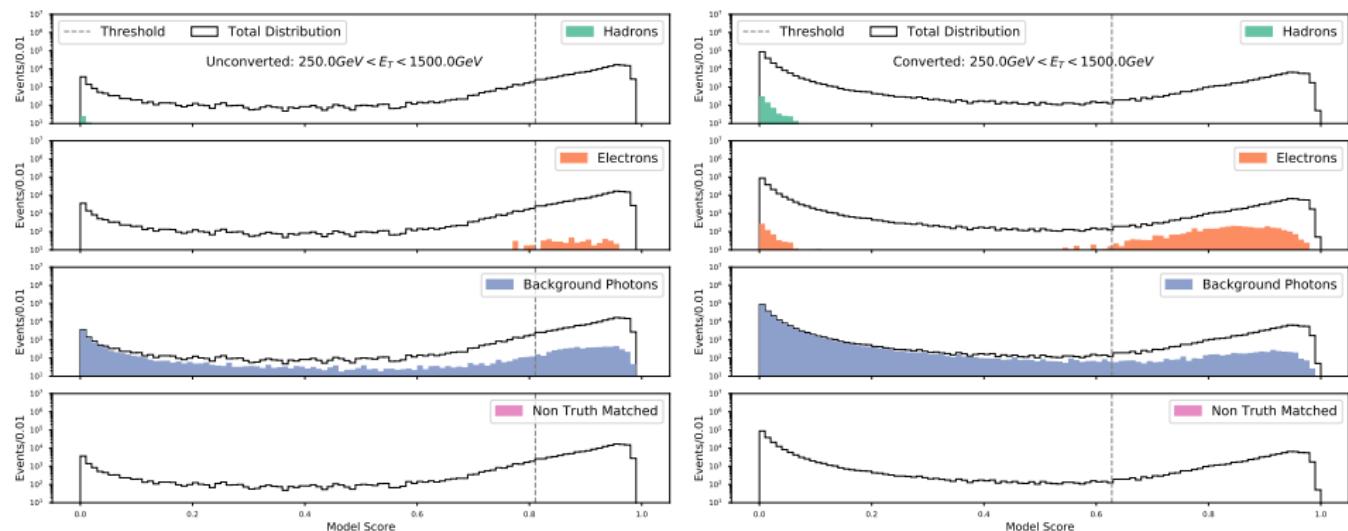
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Background Composition In MC Photon Dataset



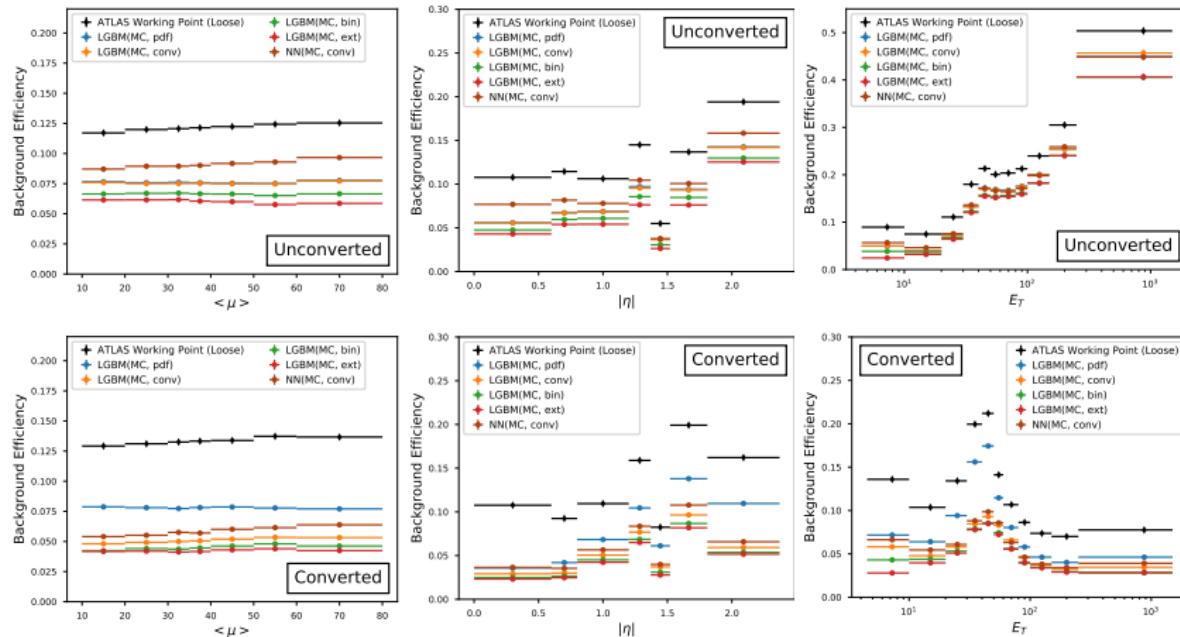
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MC Photon Results



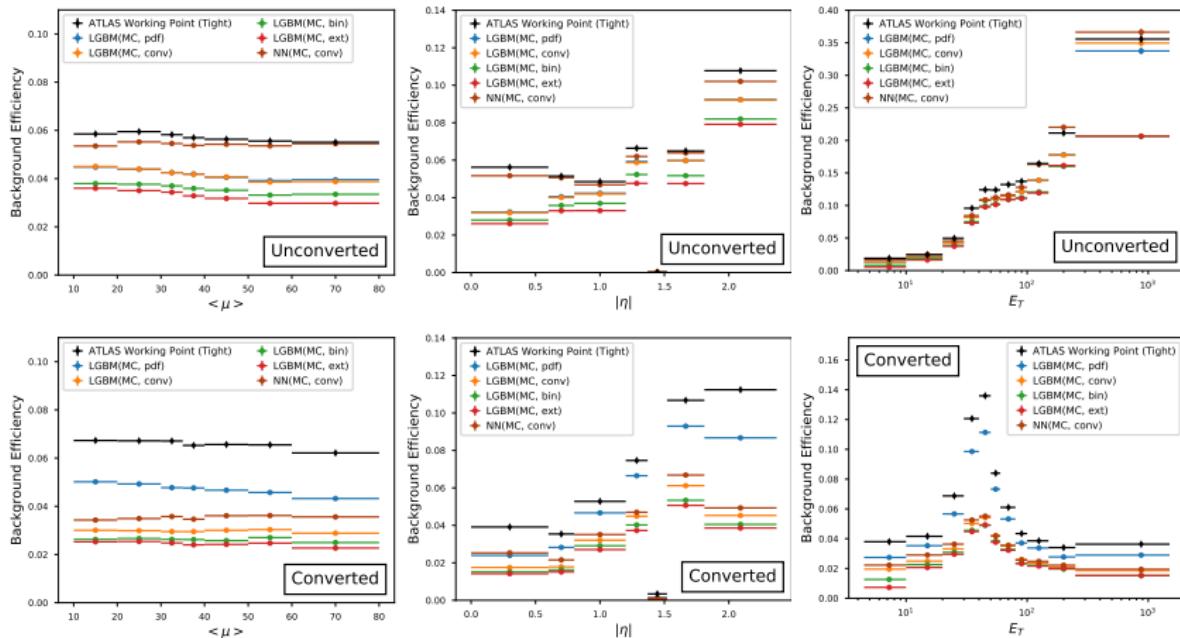
MC Results



The background efficiency as a function of $\langle \mu \rangle$, $|\eta|$, and E_T , at the same signal efficiency as the **Loose** working point.



MC Results



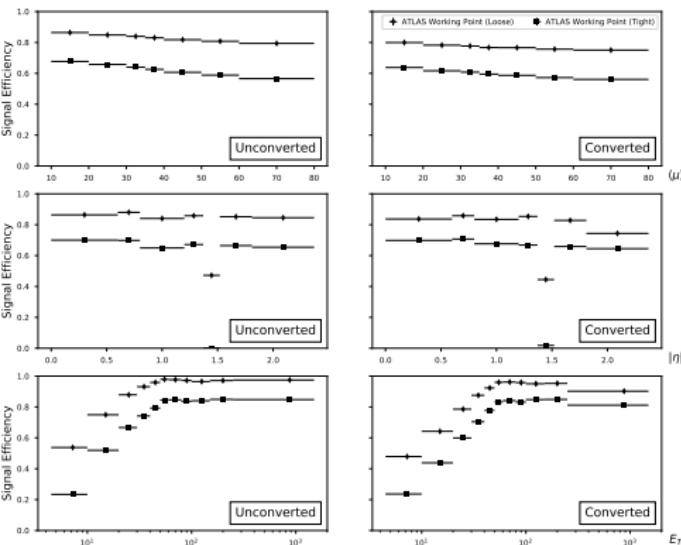
The background efficiency as a function of $\langle \mu \rangle$, $|\eta|$, and E_T , at the same signal efficiency as the **Tight** working point.



MC Results

The odd behaviour of the working points (mimiced by the models) seem to be due to background composition.

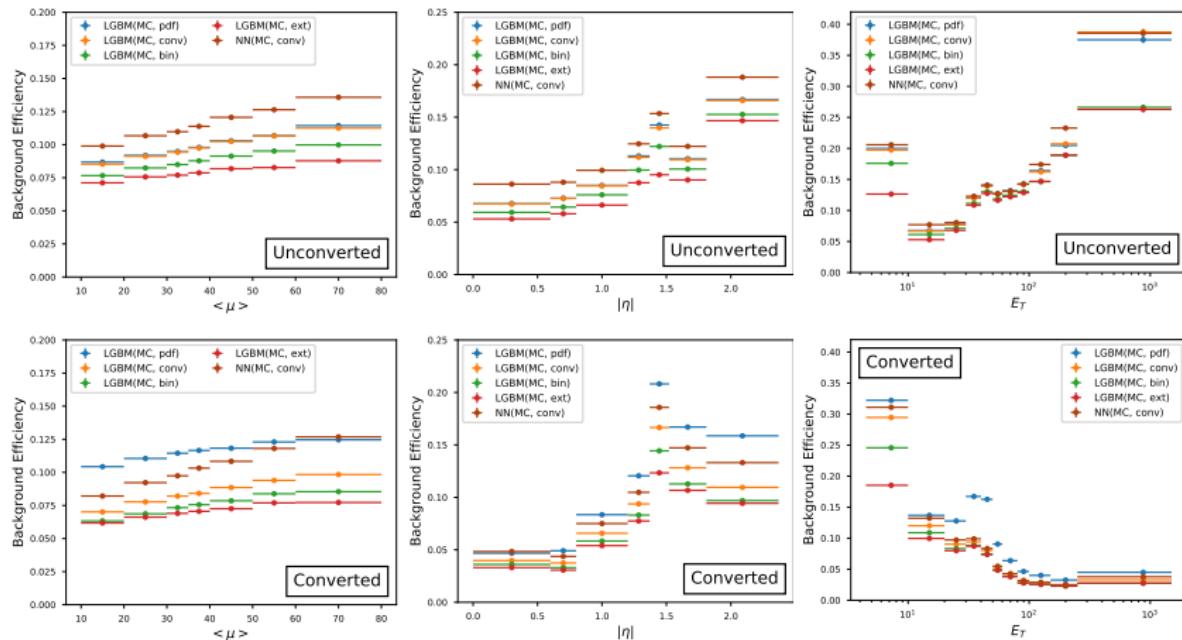
Supported by the signal efficiency of the working points.



The models should be more robust to this, as they are optimized against this problematic background composition. To gauge this the signal efficiency of the models are fixed at 90%.



MC Results



The background efficiency as a function of $\langle \mu \rangle$, $|\eta|$, and E_T , at a fixed signal efficiency of 90%.



Label Confusion



Label Confusion

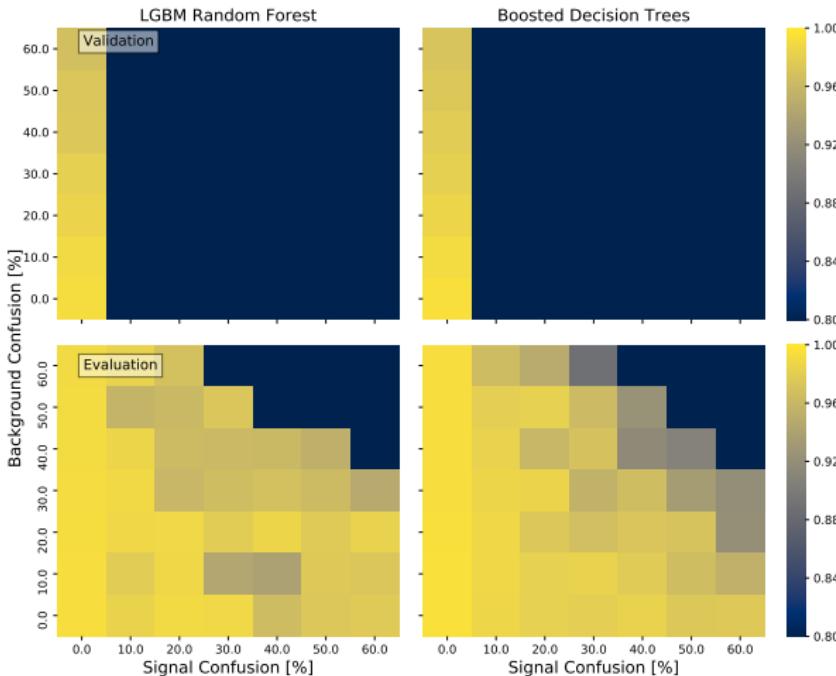
This concept was tested by simulating label confusion on a subset of the truthmatched MC photon dataset. The background was chosen to be hadrons, in order to best simulate the background found in data.

The training and validation sets were designed as equal amount of signal and background and exposed to increasing levels of random signal and background confusion (0, 10, 20, 30, 40, 50, 60%), while the evaluation set remained truth labeled.

Set	Run 1	Run 2	Run 3
Train	20000	500000	2000000
Validation	10000	50000	100000
Evaluation	157797	1647348	1647348



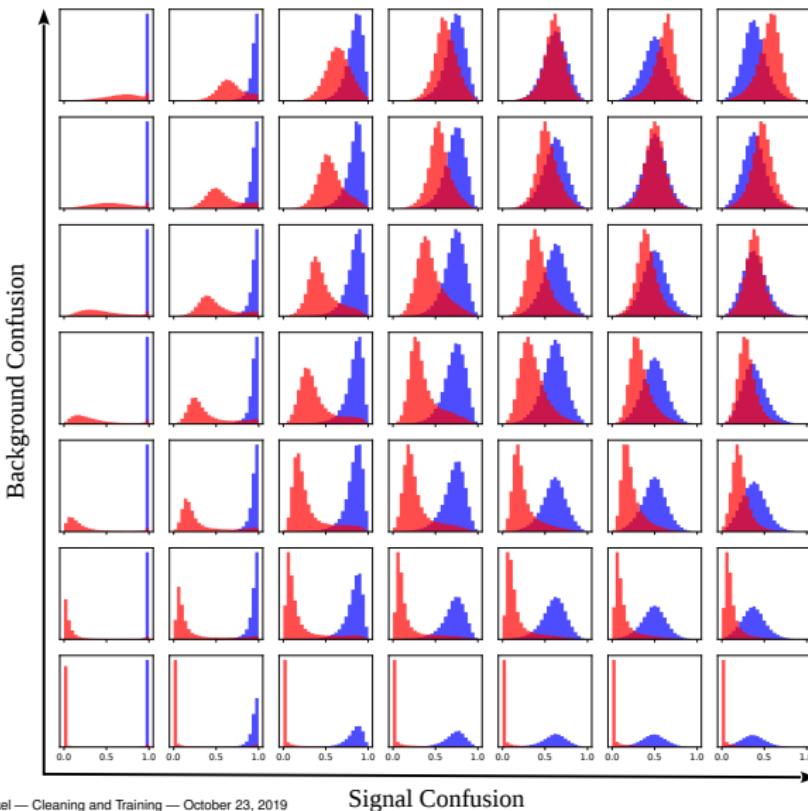
Run 1 Evaluation



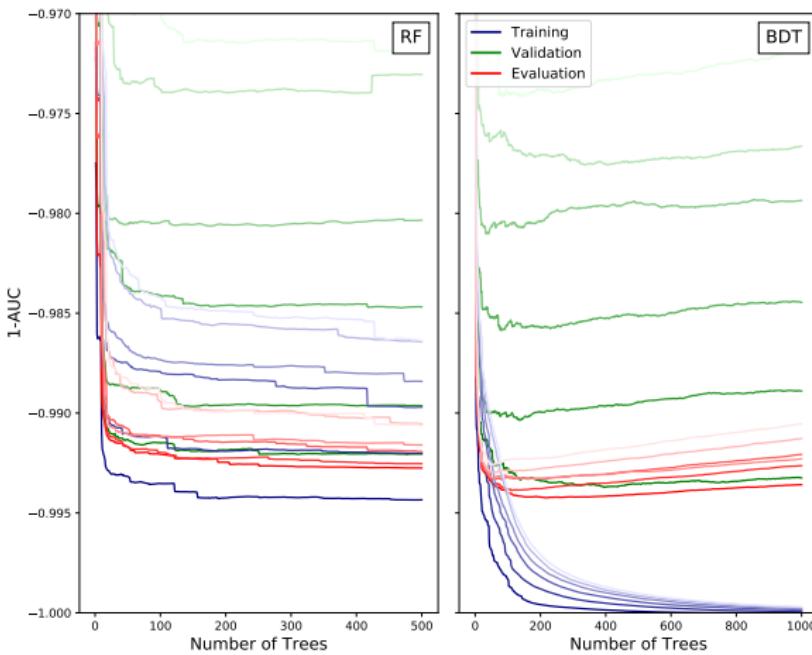
Evolution of metric as a function of increasing confusion, for validation and evaluation sets.



Run 1 Evaluation



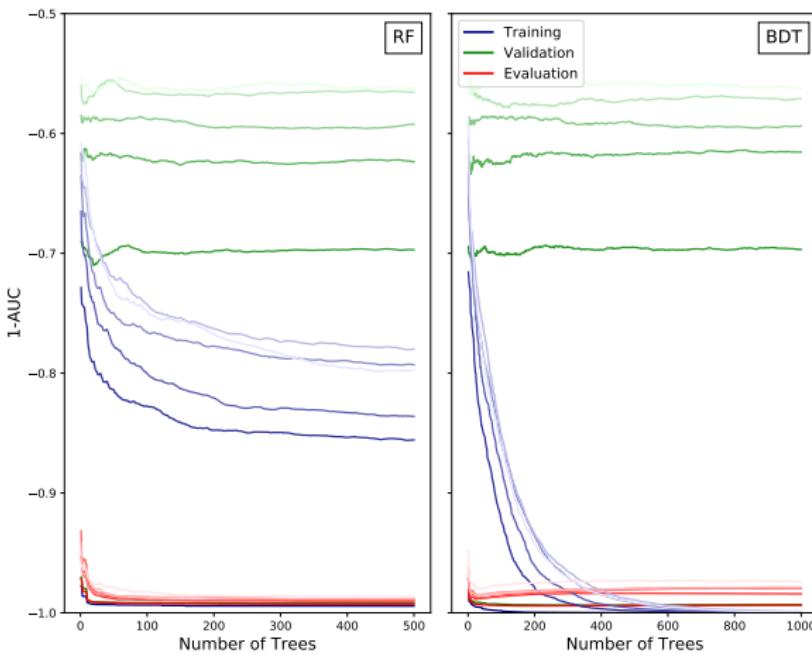
Run 1 Evaluation



Evolution of metric as a function of building trees with increasing **background** confusion, for the training, validation and evaluation sets.



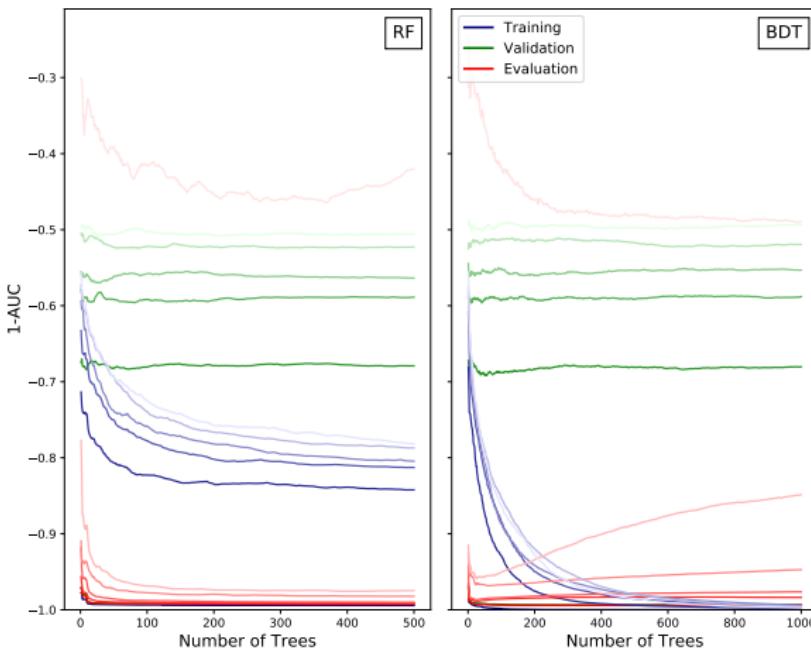
Run 1 Evaluation



Evolution of metric as a function of building trees with increasing **signal** confusion, for the training, validation and evaluation sets.



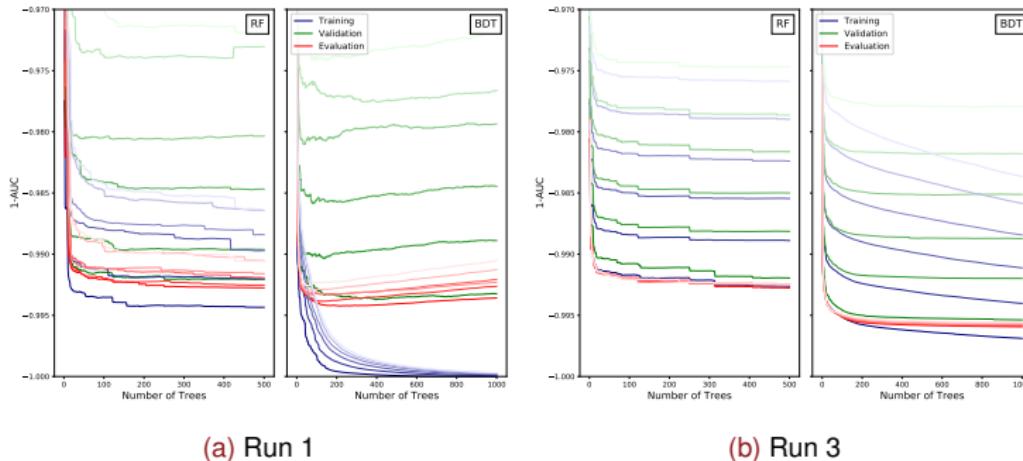
Run 1 Evaluation



Evolution of metric as a function of building trees with increasing **symmetric** confusion, for the training, validation and evaluation sets.



Label Confusion



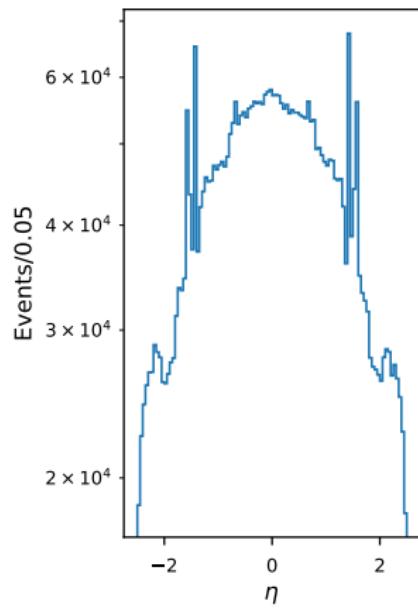
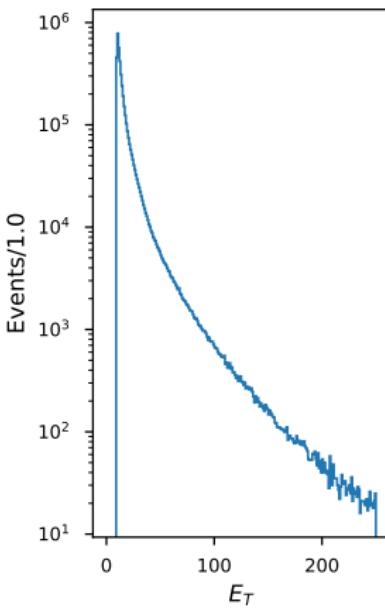
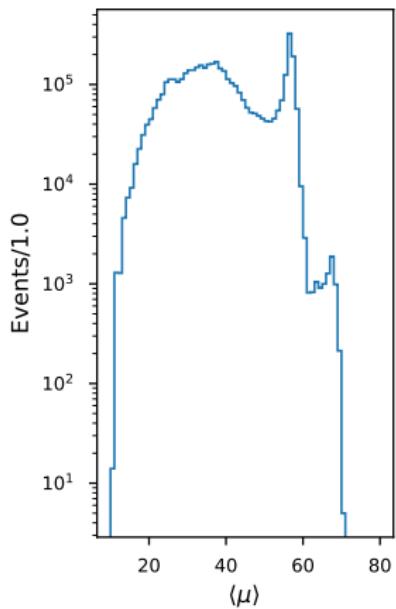
Evolution of metric as a function of building trees with increasing **background** confusion, for the training, validation and evaluation sets.



DATA Photon dataset Distributions



DATA Photon Dataset



Decorrelation Framework

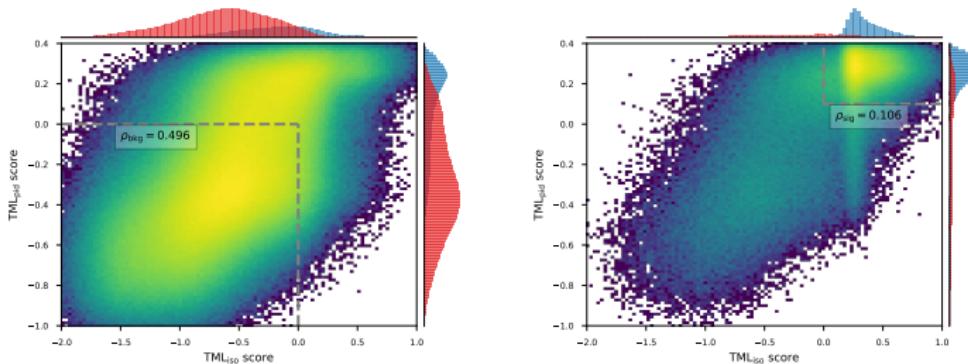


Decorrelation Framework

The correlations ρ and standard deviations σ is different from the signal and background distributions. This means one has to measure ρ_{bkg} , σ_{bkg} and ρ_{sig} , σ_{sig} on their respective distributions with as little contamination from the other as possible. Signal and background distributions are isolated using the following cuts:

Signal : $m_{\ell\ell} < 83\text{GeV}$ and $86\text{GeV} < m_{\ell\ell\gamma} < 96\text{GeV}$

Background : $m_{\ell\ell} > 83\text{GeV}$ and $m_{\ell\ell\gamma} > 101\text{GeV}$ ²



²Wrongly quoted in thesis



Decorrelation Framework

The background and signal correlations and standard deviations can be combined in many ways and the following ways have been attempted:

- **Average:**

$$\rho_{pid,iso} = \frac{1}{2}(\rho_{bkg} + \rho_{sig}) \quad \sigma_{pid} = \frac{1}{2}(\sigma_{pid,bkg} + \sigma_{pid,sig}) \quad \sigma_{iso} = \frac{1}{2}(\sigma_{iso,bkg} + \sigma_{iso,sig})$$

- **Piecewise:** Decorrelate using ρ_{sig} and σ_{sig} above and ρ_{bkg} and σ_{bkg} below a threshold in isolation.
- **Continuous:**

$$f(iso) = \alpha iso + \beta \quad \alpha = \frac{x_{sig} - x_{bkg}}{\mu_{sig} - \mu_{bkg}} \quad \beta = x_{sig} - \mu_{sig} \times \alpha$$

- **Sigmoid:**

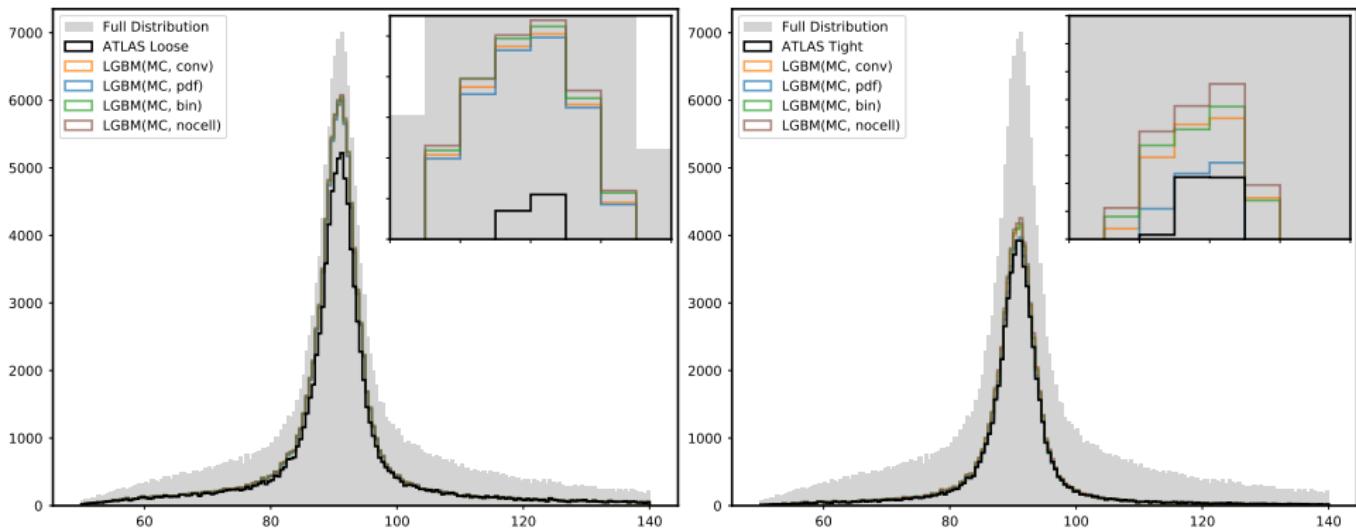
$$f(iso) = x_{sig} + \frac{x_{bkg} + x_{sig}}{1 + e^{(iso+\mu)/\sigma}} \quad \mu = \frac{1}{2}(\mu_{sig} - \mu_{bkg}) \quad \sigma = \frac{1}{2}(\mu_{sig} - \mu)$$



Results in DATA



Results in DATA



The **MC** trained models evaluated on the $Z \rightarrow ll\gamma$ peak, with background efficiency matched to the Loose (left) and Tight (right) working points.



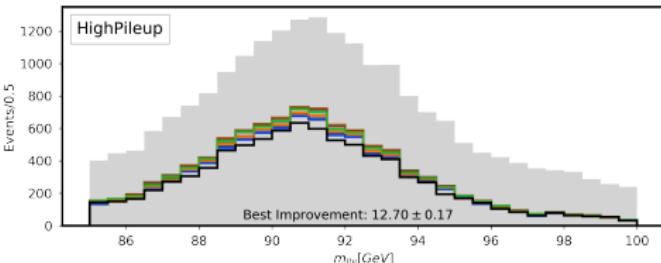
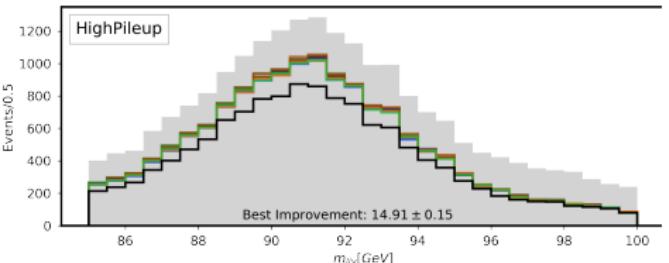
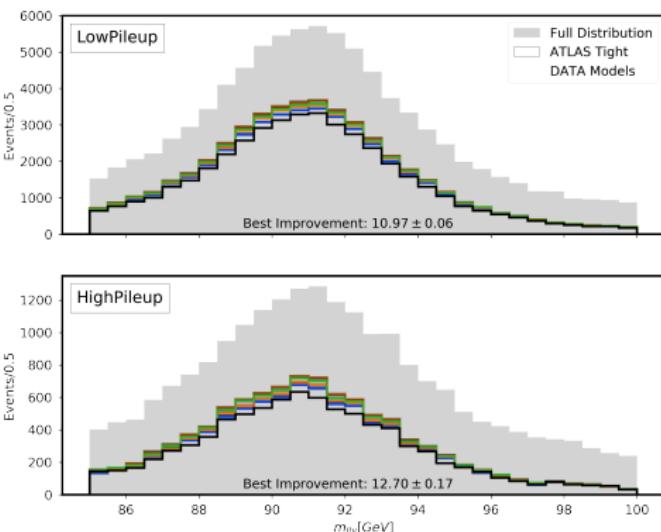
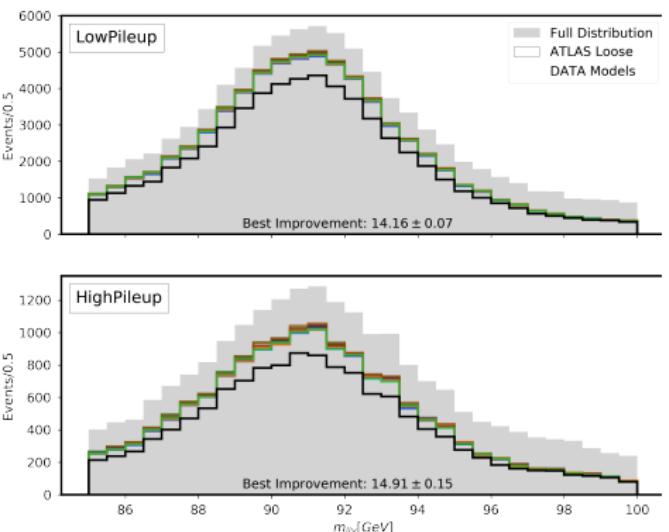
Results in DATA

Improvement [%] (ATLAS Loose)				
DATA Models	pdf	conv	bin	nocell
initial	12.10 ± 0.05	12.60 ± 0.05	13.94 ± 0.06	14.33 ± 0.06
loose	11.30 ± 0.05	11.82 ± 0.05	12.91 ± 0.06	13.24 ± 0.06
tight	11.23 ± 0.05	11.62 ± 0.05	12.70 ± 0.05	13.14 ± 0.06
MC Models				
Truth	12.59 ± 0.05	12.92 ± 0.06	13.78 ± 0.06	14.08 ± 0.06
Improvement [%] (ATLAS Tight)				
DATA Models	pdf	conv	bin	nocell
initial	4.61 ± 0.03	7.45 ± 0.04	9.06 ± 0.05	10.87 ± 0.06
loose	4.92 ± 0.03	7.13 ± 0.04	10.00 ± 0.05	11.17 ± 0.06
tight	4.31 ± 0.02	6.66 ± 0.04	9.25 ± 0.05	10.97 ± 0.06
MC Models				
Truth	1.42 ± 0.01	5.74 ± 0.03	6.47 ± 0.04	7.96 ± 0.04

Improvement factor of all models evaluated on the $Z \rightarrow \ell\ell\gamma$ peak, with background efficiency matched to the Loose (top) and



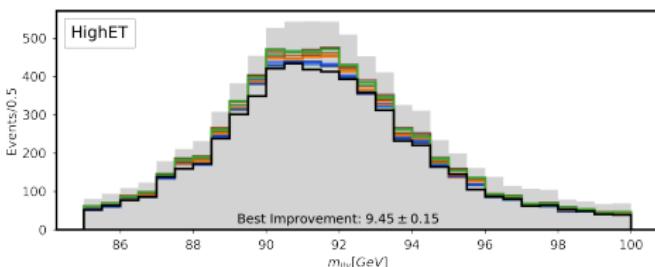
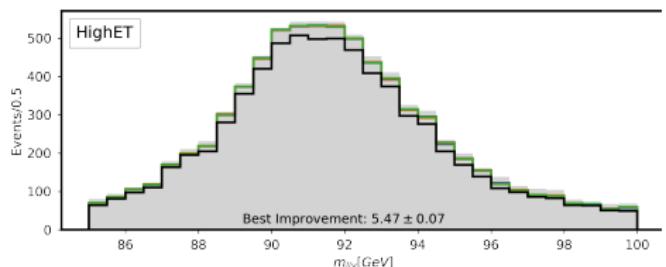
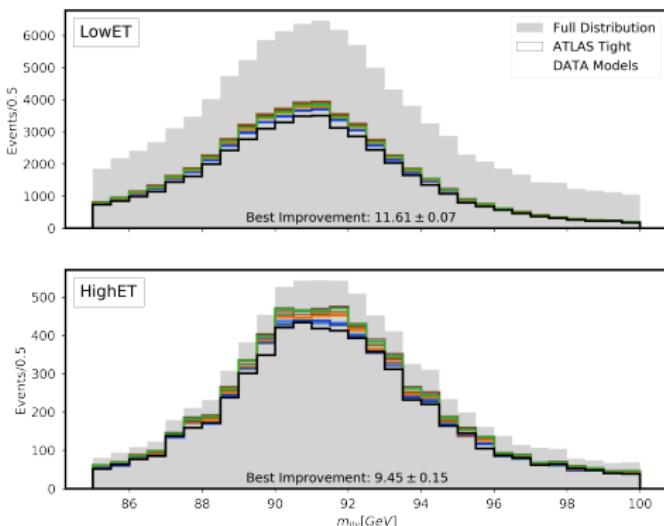
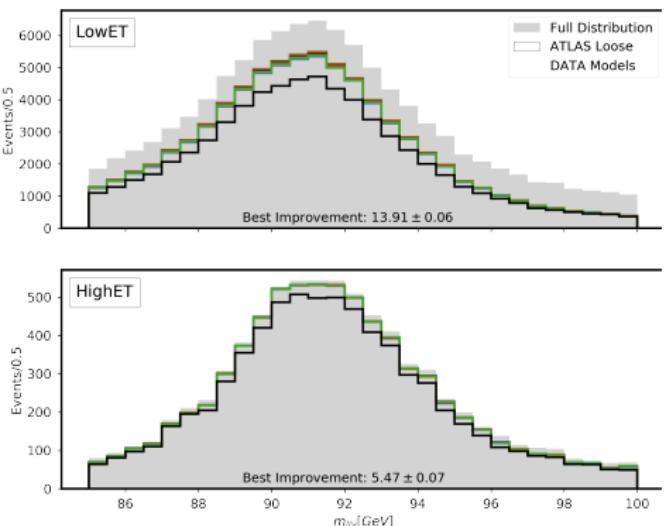
Results in DATA



Split DATA $Z \rightarrow \ell\ell\gamma$ evaluation of DATA models at low pileup ($\langle \mu \rangle < 50$) and high pileup ($\langle \mu \rangle > 50$). Compared to the Loose (left) and tight (right) working point.



Results in DATA



Split DATA $Z \rightarrow \ell\ell\gamma$ evaluation of DATA models at low E_T ($E_T < 30\text{GeV}$) and high E_T ($E_T > 30\text{GeV}$). Compared to the Loose (left) and tight (right) working point.



Event Reconstruction



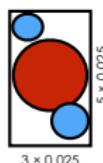
The ATLAS Experiment

Event Reconstruction is done in several steps.

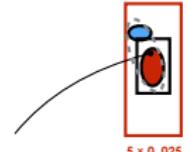
Hits in the Inner Detector are clustered into tracks and deposits in the calorimeter are clustered into clusters.

Photon and Electron Reconstruction has its foundation is these ID tracks and ECAL clusters.

All e^\pm, γ :
Add all clusters within 3×5 window around seed cluster.

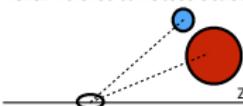


Electrons only:
Seed, secondary cluster
match the same track.

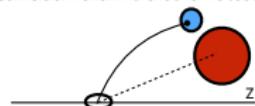


Converted photons only:

Add topo-clusters that have the **same conversion vertex** matched as the seed cluster.



Add topo-clusters with a **track match** that is **part of the conversion vertex** matched to the seed cluster.



Theory



Collider Physics

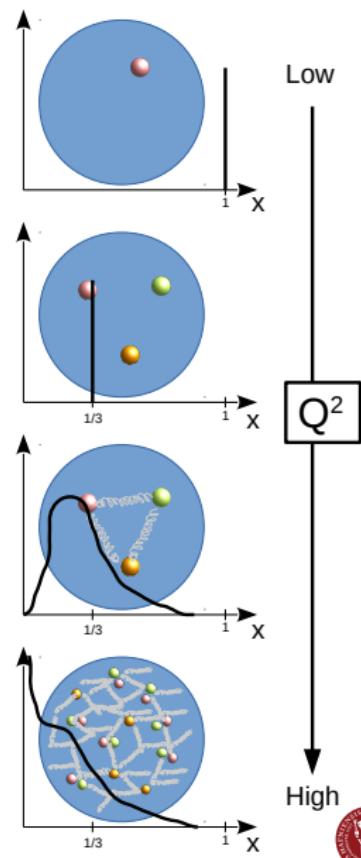
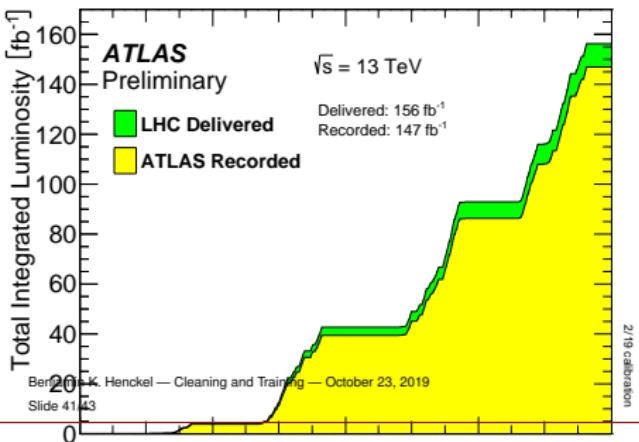
Natural units: $\hbar = c = 1$. Masses, energies, momenta in eV and lengths and times in eV^{-1} .

$$1\text{eV} = 1.602 \times 10^{-19}\text{J.}$$

Coordinate system using the azimuthal angle ϕ and

$$\text{rapidity } y = \frac{1}{2} \ln \left[\frac{E + p_z}{E - p_z} \right] \xrightarrow{m=0} \eta = -\ln(\tan(\theta/2))$$

Luminosity is a direct measure of your ability to probe interesting physics



Luminosity

The formula introducing luminosity³

$$\frac{d\sigma}{d\Omega} = \frac{1}{I_b \rho dx} \frac{dL\sigma}{d\Omega}$$

where I_b is the current of beam particles, ρ is the density of the target, dx is the target thickness and L is the luminosity. It describes the effective cross section of interaction and is measured in barns ($1\text{ barn} = 10^{-24}\text{ cm}^2$), it has the dimension of area.

$$\frac{N_{\text{events}}}{s} = L\sigma \quad , \quad L = \frac{n_{\text{bunches}} N_1 N_2 f_{\text{rev}}}{A}$$

Where $N_{1(2)}$ is the number of events in the corresponding bunch, A is the overlapping area of the two bunches colliding head on, and f_{rev} is the frequency of revolution.

³Hansen, 2015, Particle Detectors and Accelerators Lecture Notes



Production Cross Section

The QCD master formula⁴ for production cross sections at LHC, based on the QCD factorization theorem.

$$\sigma = \sum_{a,b=q,g} \int_0^1 dx_a dx_b f_a(x_a, \mu^2) f_b(x_b, \mu^2) \\ \times \frac{1}{2\hat{s}} \int_{cuts} \prod_{i=1,n} \frac{d^3 p_i}{2E_i(2\pi)^3} (2\pi)^4 \delta^{(4)}(p_a + p_b - \sum_i p_i) \sum_i |\bar{M}^{ab \rightarrow 1, \dots, n}|^2$$

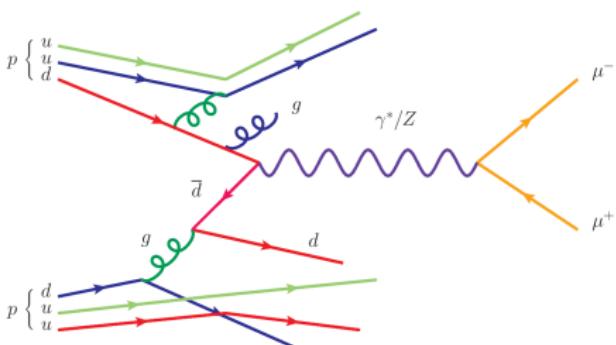


Figure from: <https://www.quantumdiaries.org/2015/05/18/dy-resummation/>

⁴Thomson, 2013, Modern Particle Physics

