

We can write this simply in matrix notation as

$$\frac{d}{dt} [N(t)] = [A(t)] [N(t)].$$

We can integrate this analytically as

$$[N(t)] = [N(0)] \exp \left\{ \int_0^t [A(t')] dt' \right\}.$$

We can make an assumption that we take the matrix inside the integrate at time t if it does not rapidly change. Therefore, the final equation is

$$[N(t)] = [N(0)] \exp \{ [A(t)] t \}.$$

The exponential term on the right hand side is known as the *matrix exponential*. There are many ways to approximate this. In this Fortran implementation we use a Pade approximation. The solution algorithm is presented in the next section. We can discretize the system for any time step, k , as

$$\boxed{[N^k] = [N^{k-1}] \exp \{ [A^k] \Delta t^{k-1} \} .}$$

The source code to the main point kinetics is listed in the Appendix.

Solving the Matrix Exponential - Pade Approximation

The theory for the approximation of the Pade Approximation presented here is summarized from *Nineteen Dubious Ways to Compute the Exponential of a Matrix, Twenty-Five Years Later*. The Pade approximation of an exponential, $\exp(A)$ is defined as

$$R_{pq}(A) = [D_{pq}(A)]^{-1} E_{pq}(A).$$

The numerator and denominator are defined by

$$E_{pq}(A) = \sum_{j=0}^q \frac{(p+q-j)! p!}{(p+q)! j! (p-j)!} A^j$$

and

$$D_{pq}(A) = \sum_{j=0}^q \frac{(p+q-j)! p!}{(p+q)! j! (p-j)!} (-A^j).$$

Before the Pade approximation is made, the method of *scaling and squaring* is used to avoid numerical roundoff error. To scale the exponential, it can be written as

$$\exp(A) = [\exp(A/m)]^m.$$

The criterion to choose a parameter like m is that

$$\|A/2^{e-1}\|_{\infty} \leq 1/2.$$

The integer value of e can be easily calculation and will be used at the end of the approximation to undo the scaling. After the matrix is scaled, the Pade approximation can be made. From above, the Pade approximation coefficients have numerous factorials and can be costly to compute. For example if we take this out to 4 terms and compute the diagonal approximate where, $p = q = 6$, we can see that it is

$$\sum_{j=0}^q \frac{(p+q-j)!p!}{(p+q)!j!(p-j)!} = 1 + \frac{11!6!}{12!5!} + \frac{10!6!}{12!2!4!} + \frac{9!6!}{12!3!3!} + \dots$$

We can simplify some of the factorials as

$$1 + \frac{6}{12} + \frac{6 \cdot 5}{12 \cdot 11 \cdot 2} + \frac{6 \cdot 5 \cdot 4}{12 \cdot 11 \cdot 10 \cdot 3 \cdot 2} + \dots$$

What we see from this is that each succeeding term has the terms of the previous value when greater than the second term. Thus, we can always factor out all of the preceeding coefficients,

$$1 + \frac{6}{12} + \left(\frac{6}{12}\right) \frac{5}{11 \cdot 2} + \left(\frac{6}{12}\right) \left(\frac{5}{11 \cdot 2}\right) \frac{4}{10 \cdot 3} + \dots$$

Therefore for every term, we will now the multiplication of the terms in parathesis from the previous coefficient. We just need to write an algorithm for the terms in fractions. We notice that starting from $j = 1$ term, the value of the numerator has to do with q . The numerator can always be computed as $num = q - j + 1$. The denominator is always made up of two terms. One of them is the term number, j . The other is just $2q - j + 1$. Therefore we can compute any Pade coefficient, c_j with the following algorithm:

$$c_j = c_{j-1} \frac{q - j + 1}{j \cdot (2q - j + 1)}, \quad j = 1, 2, \dots$$

Once the numerator, E_{qq} and denominator D_{qq} are computed the Pade approximation of them is just the division of the matrices. The last step is undo the scaling that was done at the beginning of the algorithm. This can be done with

$$\exp(A) \approx R_{qq}^s.$$

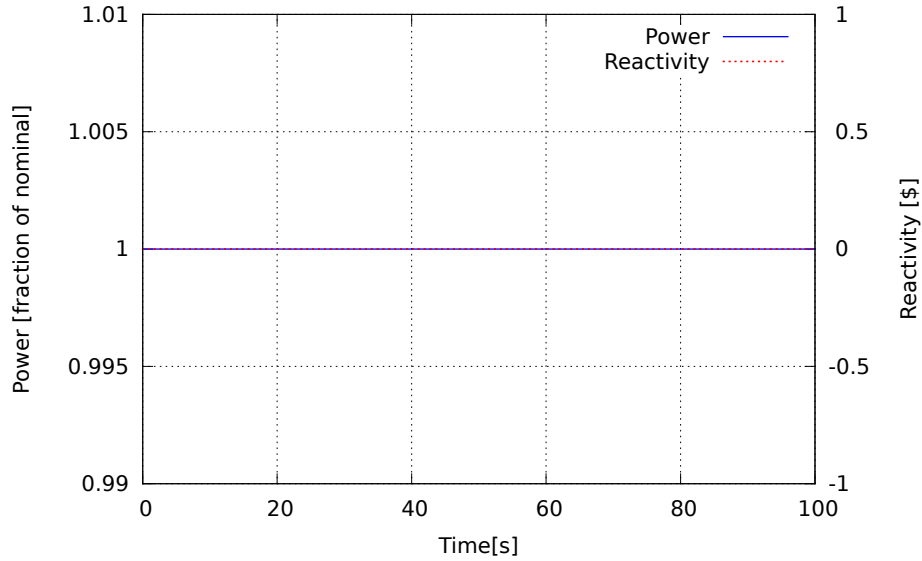
The algorithm of this method is presented below. The acutal Fortran source code written is available in the Appendix. For all complicated matrix operations, LAPACK routines were used.

Algorithm 1 Matrix Exponential - Pade Approximation with Squaring and Scaling

- 1: compute norm-inf of matrix, $\|A\|_\infty$
 - 2: get scaling parameter (s): determine e such that $norm = f \cdot 2^e$, $s = \max(0, e + 1)$
 - 3: initialize Pade numerator (E) and denominator (D) with a diagonal of ones (takes care of zeroth term)
 - 4: initialize Pade coefficient, $c = 1$
 - 5: **for** $j = 1, 2, 3, \dots, q$ **do**
 - 6: Compute Pade coefficient, $c = c * (q - j + 1) / (j * (2(q - j + 1)))$
 - 7: Perform matrix multiplication for A^j
 - 8: Compute numerator, $E = E + c * A^j$
 - 9: Compute denominator, $D = D(+/-)c * A^j$
 - 10: **end for**
 - 11: Compute approximate, $R = D^{-1}E$
 - 12: Undo scaling, $R = R^s$
-

Steady State Results

With any transient code, it is important to check that if the system starts in equilibrium and not perturbation is made to the system, the values do not change. This was simulated in the point kinetics code where a reactivity curve was input of all zeros. Therefore, we expect that the fractional power stays constant at zero. Below is a plot that shows the code can hold steady state.

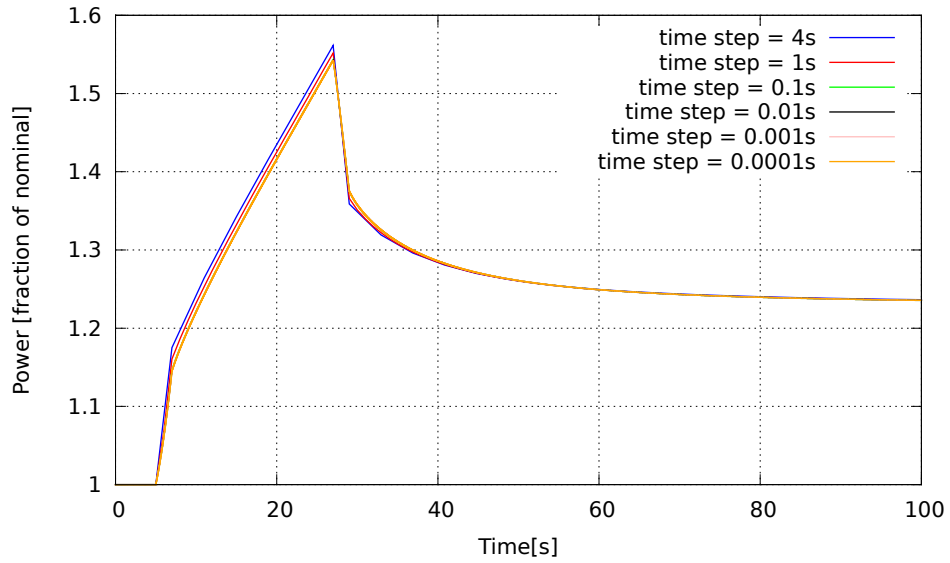


PART B

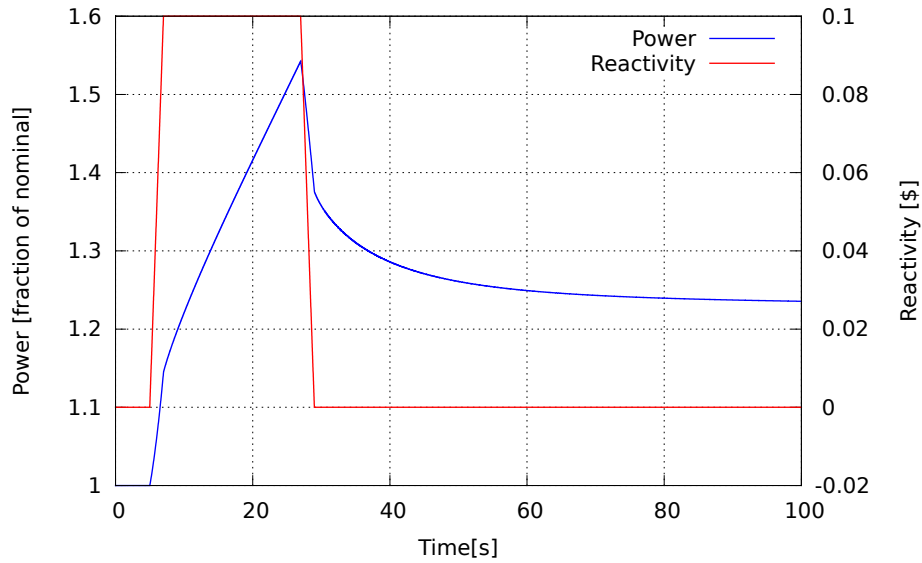
From the output of the code, the total value of beta and pnl is:

$$\beta = 0.006648 \quad \Lambda = 1.866 \times 10^{-5} \text{ s.}$$

The output of a point kinetics run can be viewed in the Appendix. The plot below shows fraction power vs. time during the transient for different time steps.



The plot above shows that once the time step becomes 0.1 seconds it very hard to visually see any differences. To be conservative we use a time step of 0.01 seconds. This time step is shown below with the corresponding reactivity input curve.



PART C

In this part we are tasked with writing an inverse point kinetics tool. In inverse kinetics, a power amplitude shape is used to determine a corresponding reactivity curve. We can start the derivation looking at the precursor balance equation for group i ,

$$\frac{d}{dt}C_i(t) = \frac{\beta_i}{\Lambda}T(t) - \lambda C_i(t).$$

Since we know the power dependence the equations are no longer coupled. We can solve this differential equation analytically as

$$\frac{d}{dt}C_i(t) + \lambda C_i(t) = \frac{\beta_i}{\Lambda}T(t).$$

The integrating factor is $\exp(\lambda_i t)$. Going through the analysis we can arrive at:

$$\exp(\lambda_i t) \frac{d}{dt}C_i(t) + \exp(\lambda_i t) \lambda C_i(t) = \exp(\lambda_i t) \frac{\beta_i}{\Lambda}T(t),$$

$$\frac{d}{dt}[\exp(\lambda_i t) C_i(t)] = \exp(\lambda_i t) \frac{\beta_i}{\Lambda}T(t),$$

$$\int \frac{d}{dt}[\exp(\lambda_i t) C_i(t)] dt = \int \exp(\lambda_i t) \frac{\beta_i}{\Lambda}T(t) dt,$$

$$\exp(\lambda_i t) C_i(t) = \frac{\beta_i}{\Lambda} \int \exp(\lambda_i t) T(t) dt.$$

In order to perform that integral on the right hand side the analytic shape of the power amplitude must be known. However, if the time step is small enough we can just pull it out of the integral as a constant and assume it is the average power of the time step. This is shown as

$$\exp(\lambda_i t) C_i(t) = \frac{\beta_i}{\Lambda} \bar{T} \int \exp(\lambda_i t) dt.$$

The general form of the equation is

$$\exp(\lambda_i t) C_i(t) = \frac{\beta_i}{\lambda_i \Lambda} \bar{T} \exp(\lambda_i t) + \tilde{C},$$

$$C_i(t) = \frac{\beta_i}{\lambda_i \Lambda} \bar{T} + \tilde{C} \exp(\lambda_i t).$$

The integration constant can be determine since we know from the initial power what the initial precursor concentration is. This constant can be evaluated as

$$C_i^0 = \frac{\beta_i}{\lambda_i \Lambda} \bar{T} + \tilde{C},$$

$$\tilde{C} = C_i^0 - \frac{\beta_i}{\lambda_i \Lambda} \bar{T}.$$

Substituting this back in to the general equation yields the final for of the precursor equation,

$$C_i(t) = \frac{\beta_i}{\lambda_i \Lambda} \bar{T} + \left(C_i^0 - \frac{\beta_i}{\lambda_i \Lambda} \bar{T} \right) \exp(\lambda_i t),$$

$$C_i(t) = C_i^0 \exp(\lambda_i t) + \frac{\beta_i}{\lambda_i \Lambda} \bar{T} [1 - \exp(\lambda_i t)].$$

This will be solved over a time step so that the above approximations are valid. The discretized equation then becomes

$$C_i^{k+1} = C_i^k \exp(\lambda_i dt^k) + \frac{\beta_i}{\lambda_i \Lambda} \bar{T}^k [1 - \exp(\lambda_i dt^k)] .$$

The power equation solved for reactivity is

$$\rho(t) = \frac{\Lambda}{T(t)} \frac{d}{dt} T(t) + \beta - \frac{\Lambda}{T(t)} \sum_i \lambda_i C_i(t) .$$

This can be discretized using a simple backward finite difference for the derivative so that

$$\rho^{k+1} = \frac{\Lambda}{T^{k+1}} \frac{T^{k+1} - T^k}{dt} + \beta - \frac{\Lambda}{T^{k+1}} \sum_i \lambda_i C_i^k .$$

These physics equation were implemented into a different Fortran code. The physics routines of the code can be viewed in the Appendix.

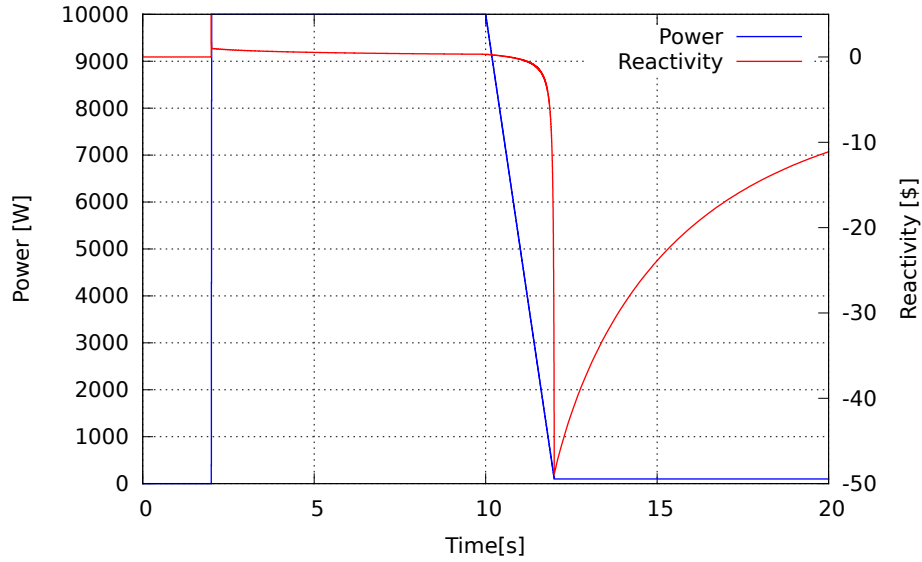
The given problem specifies a fixed power amplitude as a function of time as follows:

<i>Time</i> [s]	<i>Power</i> [W]
0	1
2	1
2.01	10000
10	10000
12	100
20	100

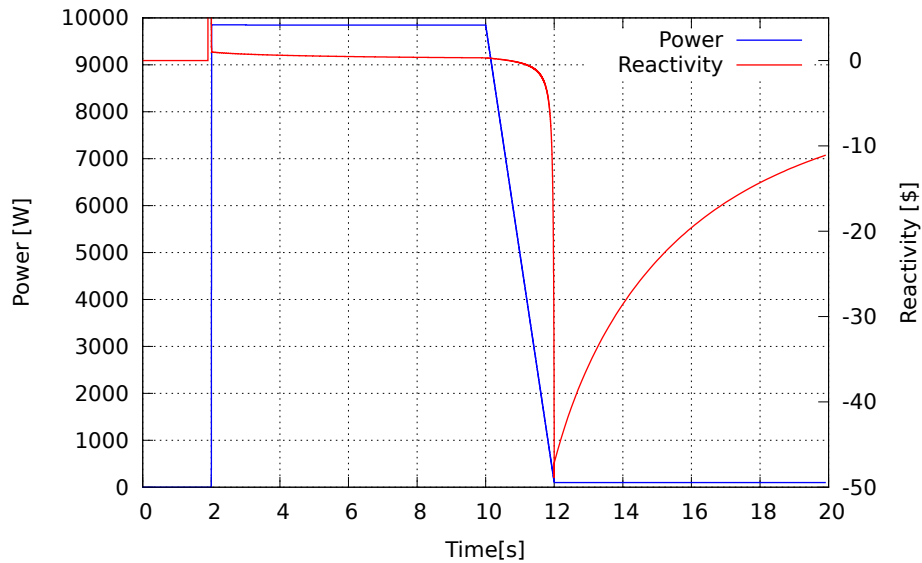
From running the code several times, we added the time step for each of these regions. To get the right shape after the reactivity insertion an extra time was put in to finer resolve the discretization:

<i>Time</i> [s]	<i>Power</i> [W]	<i>Time step</i> [s]
0	1	0.1
2	1	3×10^{-8}
2.01	10000	3×10^{-5}
3.0	10000	0.001
10	10000	0.0001
12	100	0.1
20	100	--

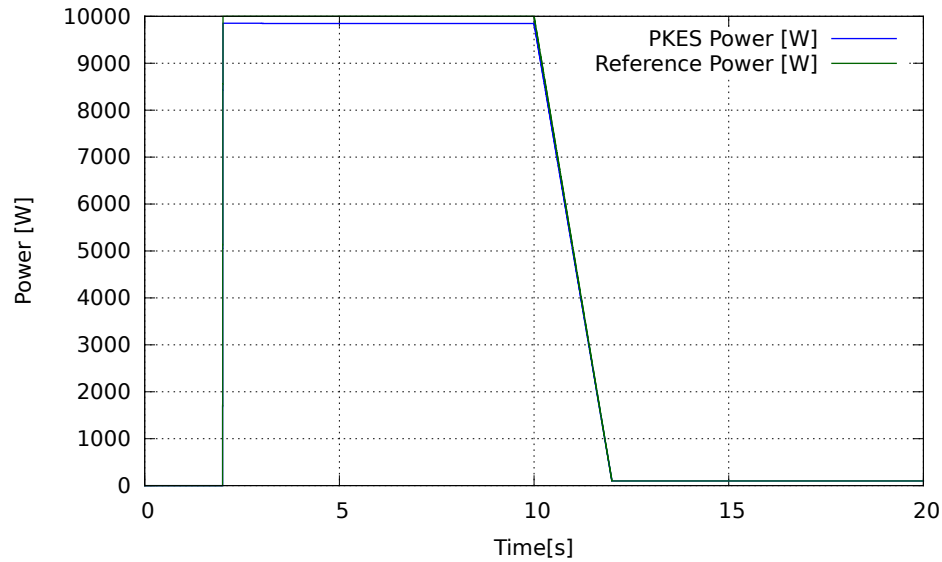
The input and output of the inverse point kinetics run is available in the Appendix. The resulting power and predicted reactivity curves are shown in the plot below.



Although the full scale of the reactivity can't be seen, the reactivity peaks at about **2700 dollars**! This is obviously ridiculous for an actual reactor system. We can then take this reactivity curve and run it in the point kinetics solver to see if the original power amplitude shape can be recovered. The input and output of this run can be viewed in the Appendix. Since the data can get large to port between the codes, a binary output file is written and can be read in by point kinetics code. The same power and reactivity plot is shown below except from the point kinetics solver.



We can see from this plot that the power doesn't quite get up to 10000 W. Other than that it matches the plot from inverse kinetics well. For comparison we plot it against the reference power from the problem statement below.



We miss the power prediction by about 1.5%. This is due to the approximations of the time derivative of the power. As we make the time steps infinitesimally small, the power should be in better agreement. This was the best prediction with the amount of time needed to run the code.

APPENDIX

Source Code

Point Kinetics Main Physics Solver

```

module physics

!-module options

    implicit none
    private
    public :: run_kinetics

contains

!=====
! RUN_KINETICS
!=====

    subroutine run_kinetics()

!-----external references

        use constants, only: NUM_PRECS

```

```

!   use expokit,      only: dense_pade
!   use global,       only: pke, restart
!   use output,       only: header
!   use solvers,      only: expm_pade

!——local variables

integer :: i ! loop counter
real(8) :: dt ! local time step

!——begin execution

! print header for run
call header("POINT KINETICS SIMULATION", level=1)

! set up coefficient matrix
call setup_coefmat()

! set up initial conditions
call set_init()

! begin loop through time steps
do i = 1, sum(pke % nt)

    ! print progress
    if (sum(pke%nt) > 100000 .and. restart) then
        if (mod(i,sum(pke%nt)/10000) == 0) write(*,*) 'On Time Step: ',i
    end if

    ! compute exponential matrix
    call set_reactivity(i,dt)

    ! solve matrix exponential
!   call dense_pade(pke % coef, NUM_PRECS + 1, dt, pke % expm) ! expokit
    call expm_pade(pke % coef, NUM_PRECS + 1, dt, pke % expm) ! my code

    ! get new vector
    pke % N(:,i+1) = matmul(pke % expm, pke % N(:,i))

end do

end subroutine run_kinetics

!=====
! SETUP_COEFMAT
!=====

```

```

subroutine setup_coefmat()

!——external references

  use constants,  only: beta, NUM_PRECS, lambda, pnl
  use global,     only: pke

!——local variables

  integer :: i ! loop counter

!——begin execution

  ! set up coefficient matrix manually for time 0
  pke % coef(1,1) = (pke % rho(1)*sum(beta) - sum(beta))/pnl

  ! begin loop around rest of matrix
  do i = 2, NUM_PRECS + 1

    ! set row 1
    pke % coef(1,i) = lambda(i - 1)

    ! set diagonal
    pke % coef(i,i) = -lambda(i - 1)

    ! set column 1
    pke % coef(i,1) = beta(i-1) / pnl

  end do

end subroutine setup_coefmat

=====
! SET_INIT
=====

subroutine set_init()

!——external references

  use constants,  only: ONE, beta, lambda, pnl, NUM_PRECS
  use global,     only: pke

!——local variables

  integer :: i ! loop counter

```

```

!——begin execution

! set power at 1.0
pke % N(1,1) = ONE

! loop through precursors
do i = 1, NUM_PRECS

    ! set initial value
    pke % N(i+1,1) = beta(i)/(pnl*lambda(i)) * pke % N(1,1)

end do

end subroutine set_init

=====
! SET_REACTIVITY
=====

subroutine set_reactivity(i,dt)

!——external references

use constants,    only: beta, pnl
use global,       only: pke

!——arguments

integer :: i    ! current time step
real(8) :: dt   ! current dt

!——local variables

integer :: idx ! interpolation index

!——begin execution

! check if index should be moved in input vectors
if (i > sum(pke % nt(1:pke % idx))) pke % idx = pke % idx + 1
idx = pke % idx

! compute current time
dt = pke % dt(idx)
pke % time(i+1) = pke % time(i) + dt

! interpolate on reactivity
pke % react(i) = pke % rho(idx) + ((pke % rho(idx+1) - pke % rho(idx)) / &

```

```

                                (pke % t(idx + 1) - pke % t(idx))) * &
                                (pke % time(i+1) - pke % t(idx))

! set values in coefficient matrix
pke % coef(1,1) = (pke % react(i)*sum(beta) - sum(beta))/pnl

end subroutine set_reactivity

end module physics

```

Inverse Point Kinetics Main Physics Solver

```

module physics

!—module options

implicit none
private
public :: run_invkinetics

contains

!=====
! RUN_INVKINETICS
!=====

subroutine run_invkinetics()

!—external references

use constants,    only: NUM_PRECS, pnl, beta, lambda
use global,       only: ipke, total_time
use output,       only: header

!—local variables

integer :: i          ! loop counter
real(8) :: dt         ! local time step
real(8) :: avgpower   ! avg. power between timesteps

!—begin execution

! print header for run
call header("INVERSE POINT KINETICS SIMULATION", level=1)

! set initial precursors
ipke % N(1,1) = ipke % power(1)

```

```

ipke % N(2:NUM_PRECS+1,1) = beta/(pnl*lambda) * ipke % N(1,1)

! begin loop through time steps
do i = 1, sum(ipke % nt)

    ! compute exponential matrix
    call set_power(i,dt)

    ! compute average power
    avgpwr = (ipke % N(1,i) + ipke % N(1,i+1)) / 2.0_8

    ! solve for precursors
    ipke % N(2:NUM_PRECS+1,i+1) = ipke % N(2:NUM_PRECS+1,i)*exp(-lambda*dt) +&
    beta/(lambda*pnl)*(avgpwr - avgpwr*exp(-lambda*dt))

    ! solve for reactivity
    ipke % react(i+1) = pnl/(ipke % N(1,i+1)) *                                &
    ((ipke % N(1,i+1) - ipke % N(1,i))/dt) +                                &
    sum(beta) - pnl/ipke % N(1,i+1) *                                        &
    sum(lambda*ipke % N(2:NUM_PRECS+1,i+1))

    ! change to dollars
    ipke % react(i+1) = ipke % react(i+1)/sum(beta)

end do

end subroutine run_invkinetics

```

```

! SET_POWER

```

```

subroutine set_power(i,dt)

!——external references

    use constants,    only: beta, pnl
    use global,       only: ipke

!——arguments

    integer :: i    ! current time step
    real(8) :: dt   ! current dt

!——local variables

    integer :: idx ! interpolation index

```

```

!——begin execution

! check if index should be moved in input vectors
if (i > sum(ipke % nt(1:ipke % idx))) ipke % idx = ipke % idx + 1
idx = ipke % idx

! compute current time
dt = ipke % dt(idx)
ipke % time(i+1) = ipke % time(i) + dt

! interpolate on power
ipke % N(1,i+1) = ((ipke % power(idx+1) - ipke % power(idx)) / &
                  (ipke % t(idx + 1) - ipke % t(idx))) * &
                  (ipke % time(i+1) - ipke % t(idx)) + &
                  ipke % power(idx)

end subroutine set_power

end module physics

```

Matrix Exponential Solver - Pade Approximation

```

module solvers

!—module options

implicit none
private
public :: expm_pade

contains

!=====
! EXPM_PADE
!=====

subroutine expm_pade(A,N,dt,EXPM)

!——external references

use constants,    only: ZERO, ONE
use math,         only: norm_inf, ilog2

!——arguments

integer :: N          ! dimension of square matrix

```

```

real(8) :: A(N,N)      ! the coefficient matrix
real(8) :: dt          ! the time step
real(8) :: EXPM(N,N)   ! output matrix

!——local variables

integer :: ex          ! this is the integer exponent that goes into th scaling
integer :: s           ! this is the scaling parameter
integer :: i           ! loop counter
integer :: j           ! Pade order counter
integer :: q           ! Pade approximation order
integer :: info        ! did LAPACK work?
integer, allocatable :: IPIV(:) ! pivot elements from LU factorization
real(8) :: norm        ! the norm of the coefficient matrix for scaling
real(8) :: c           ! Pade coefficient
real(8) :: shift       ! -1 or +1 and a function of J for D term
real(8), allocatable :: At(:, :) ! the exponential being approximated
real(8), allocatable :: X(:, :)  ! accumulates multiplication of A
real(8), allocatable :: Xt(:, :) ! temporary matrix for X
real(8), allocatable :: E(:, :)  ! numerator of Pade
real(8), allocatable :: D(:, :)  ! denominator of Pade

!——begin execution

! allocate temporary matrices
allocate(At(N,N))
allocate(X(N,N))
allocate(Xt(N,N))
allocate(E(N,N))
allocate(D(N,N))
allocate(IPIV(N))

! set matrix
At = A

! get matrix to be approximated in exponential
At = At * dt

! compute norm for scaling
norm = norm_inf(At, N)

! compute integer exponent of formula norm = f*2**(ex)
ex = ilog2(norm)

! determine scaling parameter
s = max(0, ex+1)

```



```

! scale matrix by scaling parameter
At = At / (2**s)

! begin pade approximation for numerator and denominator of rational fun.
! Pade order 6, diagonal approximates
q = 6

! can easily set j=0 and j=1 parts right away
! begin loop to set the A^0 terms in each E and D, not this is a diag of ones
E = ZERO
D = ZERO
do i=1,N
    E(i,i) = ONE
    D(i,i) = ONE
end do
c = ONE
c = 0.5_8      ! this is j=1 Pade coefficient (need to do this before loop)
E = E + c*At ! accumulate in sum
D = D - c*At ! accumulate in sum

! begin rest of pade loop
X = At          ! set A to X, X will accumulated the A^j in the Pade eq.
shift = ONE ! for order 2 term, the shift for denominator is +1
do j = 2,q

    ! compute Pade coefficient
    c = c * dble(q-j+1) / dble(j*(2*q-j+1))

    ! multiply A^(j-1) by LAPACK ROUTINE
    call DGEMM('N','N',N,N,N,ONE,At,N,X,N,ZERO,Xt,N)

    ! move temporary to actual
    X = Xt

    ! accumulate into numerator and denominator
    E = E + c*X
    D = D + shift*c*X
    shift = -ONE

end do

! compute rational function (E is R after the next two lines)
call DGETRF(N,N,D,N,IPIV,info) ! LU factorization of D, LAPACK
call DGETRS('N',N,N,D,N,IPIV,E,N,info) ! solves E = D^-1*E, LAPACK

! perform squaring
do i = 1,s

```

```

    call DGEMM('N','N',N,N,N,ONE,E,N,E,N,ZERO,Xt,N) ! does E*E LAPACK
    E = Xt
end do

! set output matrix
EXPM = E ! E is really R, didnt want to make a separate matrix

! deallocate temporary matrices
deallocate(At)
deallocate(X)
deallocate(Xt)
deallocate(E)
deallocate(D)
deallocate(IPIV)

end subroutine expm_pade

end module solvers

```

Part B Runs

Point Kinetics Input

```

<?xml version="1.0" encoding="UTF-8"?>
<input>

  <!-- Reactivity Shape -->
  <reactivity>
    <time> 0.0 5.0 7.0 27.0 29.0 100.0 </time>
    <rho> 0.0 0.0 0.1 0.1 0.0 0.0 </rho>
    <timestep> .01 .01 .01 .01 .01 </timestep>
  </reactivity>

</input>

```

Point Kinetics Output

```

-----/-----/-----/-----/-----/-----/-----/-----/-----/-----/
/_____/ \ /_____/ \ /_____/ \ /_____/ \ /_____/ \ /_____/ \ /_____/ \ /_____/ \
\::: \ \::: \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \
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```

Developed At: Massachusetts Institute of Technology
Version: 0.1
Git SHA1: 029eecfb04ec8c268d2584929167b6a17c1af2fc
Date/Time: 2012-09-15 11:33:19

=====
=====> INITIALIZATION <=====
=====

Reading settings XML file...

INPUT SUMMARY

Number of time steps: 10000

Time (s)	Rho (\$)
0.000E+00	0.000E+00
5.000E+00	0.000E+00
7.000E+00	1.000E-01
2.700E+01	1.000E-01
2.900E+01	0.000E+00
1.000E+02	0.000E+00

PHYSICS SUMMARY

Number of Precursor Groups: 8

beta	lambda
2.180E-04	1.247E-02
1.023E-03	2.829E-02
6.050E-04	4.252E-02
1.310E-03	1.330E-01
2.200E-03	2.925E-01
6.000E-04	6.665E-01
5.400E-04	1.635E+00
1.520E-04	3.555E+00

Total Delayed Neutron Fraction 0.006648

Prompt Neutron Lifetime [s]: 1.866E-05

```
=====
=====>      POINT KINETICS SIMULATION      <=====
=====
```

Plotting results with GNUPLOT...

SIMULATION SUMMARY

Total simulation time = 6.9000E-01 seconds

Simulation Finished.

Part C Runs

Inverse Point Kinetics Input

```
<?xml version="1.0" encoding="UTF-8"?>
<input>

  <!-- Power Shape -->
  <time>   0.0 2.0 2.01   3.0      10.0   12.0  20.0   </time>
  <power>  1.0 1.0 10000.0 10000.0 10000.0 100.0 100.0   </power>
  <timestep> 0.1 3e-8 3e-5 1e-3 1e-4 0.1 </timestep>

</input>
```

Inverse Point Kinetics Output

```

  -- .-- -- .----- .-----
  | | | \ | | \ \ / / | _ \ | | / / | -----|
  | | | \ | | \ \ / / |_____| |_) | | " / | |__
  | | | . ' | | \ / / |_____| ___/ | < | __| | |
  | | | \ | | \ \ / / | | | | . \ | |_____|
  |__| |__| \__| \__/_/ | _| |__| \__| |_____|
```

Developed At: Massachusetts Institute of Technology
 Version: 0.1
 Git SHA1: 6ad3e02a086a0c13c2b75274e997addef77cc7e7
 Date/Time: 2012-09-15 12:04:56

```
=====
=====>      INITIALIZATION      <=====
=====
```

Reading settings XML file...

INPUT SUMMARY

Number of time steps: 393433

Time (s)	Rho (\$)
0.000E+00	1.000E+00
2.000E+00	1.000E+00
2.010E+00	1.000E+04
3.000E+00	1.000E+04
1.000E+01	1.000E+04
1.200E+01	1.000E+02
2.000E+01	1.000E+02

PHYSICS SUMMARY

Number of Precursor Groups: 8

beta	lambda
2.180E-04	1.247E-02
1.023E-03	2.829E-02
6.050E-04	4.252E-02
1.310E-03	1.330E-01
2.200E-03	2.925E-01
6.000E-04	6.665E-01
5.400E-04	1.635E+00
1.520E-04	3.555E+00

=====

=====> INVERSE POINT KINETICS SIMULATION <=====

=====

Plotting results with GNUPLOT...

SIMULATION SUMMARY

Total simulation time = 2.4000E-01 seconds

Simulation Finished.

Point Kinetics Input

```
<?xml version="1.0" encoding="UTF-8"?>
<input>
```

```
<restart> .TRUE. </restart>
```

Point Kinetics Output

[illegible]

```
Developed At:  Massachusetts Institute of Technology
Version:      0.1
Git SHA1:     029eecfb04ec8c268d2584929167b6a17c1af2fc
Date/Time:    2012-09-15 12:06:35
```

```
=====
=====>      INITIALIZATION      <=====
=====
```

Reading settings XML file...

INPUT SUMMARY

Number of time steps: 393433

Restarted from inverse kinetics...

PHYSICS SUMMARY

Number of Precursor Groups: 8

beta	lambda
2.180E-04	1.247E-02
1.023E-03	2.829E-02
6.050E-04	4.252E-02
1.310E-03	1.330E-01
2.200E-03	2.925E-01
6.000E-04	6.665E-01
5.400E-04	1.635E+00
1.520E-04	3.555E+00

Total Delayed Neutron Fraction 0.006648

Prompt Neutron Lifetime [s]: 1.866E-05

```

=====
=====>          POINT KINETICS SIMULATION          <=====
=====

```

Plotting results with GNUPLOT...

SIMULATION SUMMARY

Total simulation time = 4.8745E+02 seconds

Simulation Finished.