

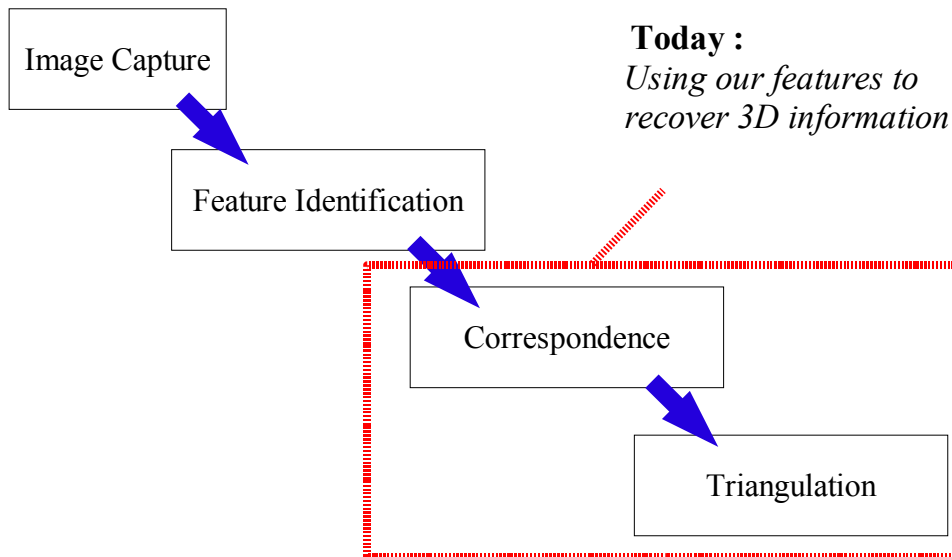
3D Recognition from stereo vision : correspondence & triangulation

Advanced Vision – Lecture 9

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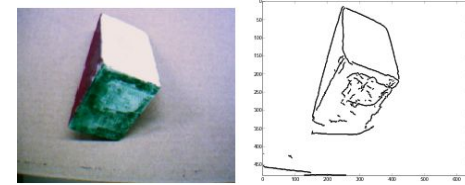
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Stereo Vision - Overview

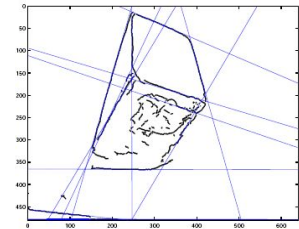


From Feature identification

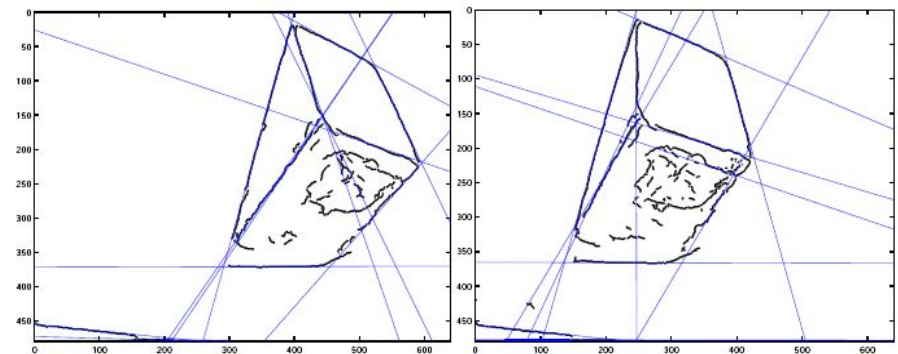
- Canny Edge Detection
 - Result: edge fragments



- RANSAC algorithm
 - parametric line descriptions that correspond to feature in image
 - N.B. infinite line model (i.e. vector direction)



RANSAC : line descriptions

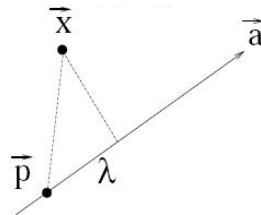


- RANSAC : Infinite unbounded lines – geometric description
 - point \vec{p} and direction \vec{a} - **position** (in 2D)
- For correspondence matching finite description useful
 - bounds on length - **shape**

Preprocessing : line segments

- **Requirement** : approx. start and end point of line segment.
- **Input** : geometric descriptions & set of points $\{\vec{x}_i\}$ for each segment identified by RANSAC.

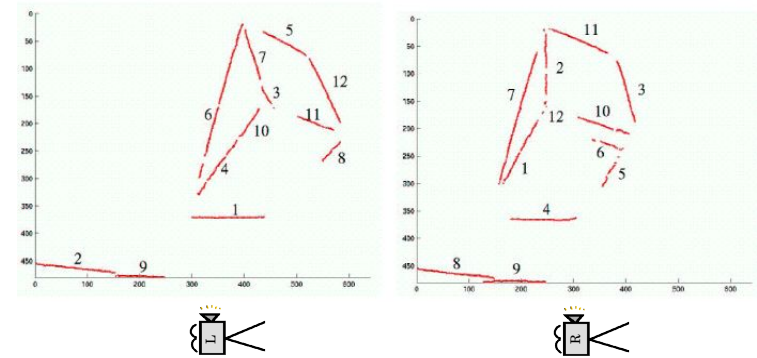
1. Project points $\{\vec{x}_i\}$ onto ideal line through point \vec{p} with direction \vec{a} : $\lambda_i = (\vec{x}_i - \vec{p}) \cdot \vec{a}$. Projected point is $\vec{p} + \lambda_i \vec{a}$



2. Remove projected points not having N neighbour points within D pixels distance - **outlier removal** (set N and D to be similar; e.g. 43 and 45)
3. Endpoints of line segment are now given by smallest / largest λ_i

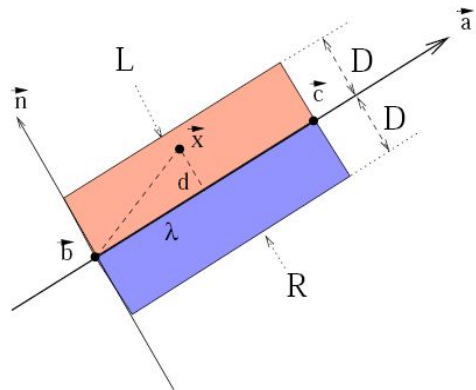
Preprocessing : line segments

- **Identified line segments**
 - geometric description (from RANSAC)
 - length description (from preprocessing)



Preprocessing : line description 1

- Given line segment endpoints \vec{b} and \vec{c} with direction $\vec{a} = (u, v)$



- Compute perpendicular : $\vec{n} = (-v, u)$
- Estimate midpoint : $\vec{m} = (\vec{b} + \vec{c}) / 2$
- Estimate length : $\|\vec{b} - \vec{c}\|$

(orientation)

(position)

(shape)

Preprocessing : line description 2

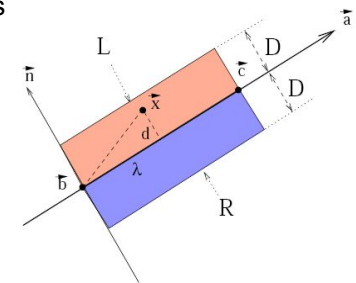
- Estimate edge contrast of line
 - consider area within distance D of line in regions L & R
 - Divide original images pixels into L/R regions

For any pixel \vec{x}

$$\text{If } 0 \leq (\vec{x} - \vec{b}) \cdot \vec{a} \leq \|\vec{b} - \vec{c}\|$$

$$\text{If } 0 < (\vec{x} - \vec{b}) \cdot \vec{n} \leq D, \text{ put } \vec{x} \text{ in L}$$

$$\text{If } -D \leq (\vec{x} - \vec{b}) \cdot \vec{n} < 0, \text{ put } \vec{x} \text{ in R}$$



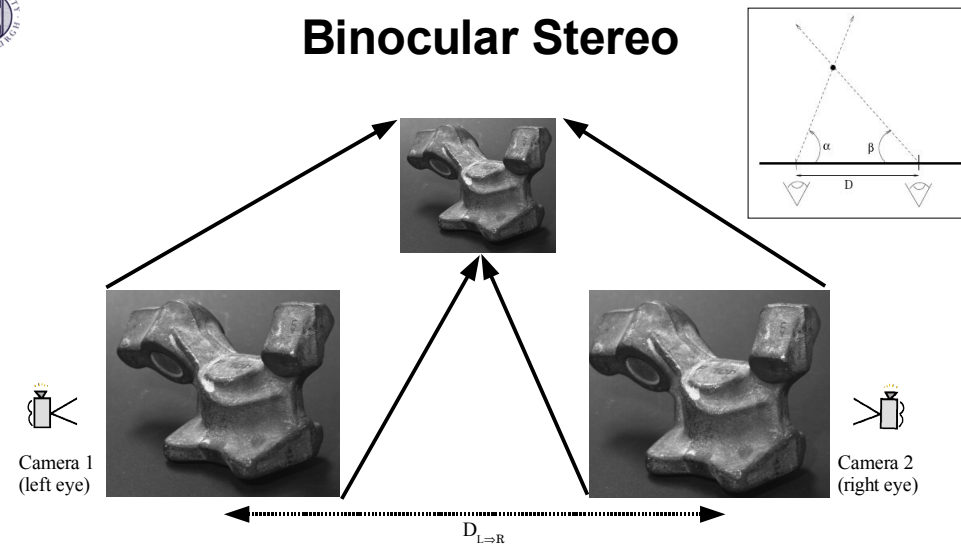
- Estimate contrast: $g = ((\text{average brightness of pixels in L}) - (\text{average brightness of pixels in R}))$
- **Overall final line description:**
 - direction \vec{a} , midpoint \vec{m} , length & contrast g

Corresponding Lines : Ground Truth

Edges	L dir	R dir	L len	R len	Edges	L mid	R mid	L con	R con
L1:R4	(0.00,-1.00)	(0.00,-1.00)	137	125	L1:R4	(370,369)	(364,242)	-91	-37
L5:R11	(0.45,0.89)	(0.38,0.93)	90	119	L5:R11	(55,477)	(40,309)	28	18
L6:R7	(0.96,-0.28)	(0.96,-0.29)	291	251	L6:R7	(158,355)	(181,194)	44	55
L7:R2	(0.95,0.32)	(1.00,0.00)	93	140	L7:R2	(74,416)	(90,246)	-117	-44
L8:R5	(0.70,-0.71)	(0.86,-0.50)	49	61	L8:R5	(250,567)	(278,371)	-66	-31
L10:R12	(0.81,-0.59)	(0.86,-0.52)	87	82	L10:R12	(208,402)	(205,221)	38	55
L11:R10	(-0.33,-0.94)	(-0.29,-0.96)	72	101	L11:R10	(199,536)	(195,358)	141	113
L12:R3	(0.89,0.45)	(0.96,0.28)	129	115	L12:R3	(140,554)	(132,400)	47	23

- Comparison of properties between lines that correspond in reality – **Ground Truth**
- But we need to find a correspondence automatically
 - we require **stereo correspondence**

Binocular Stereo



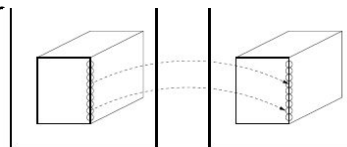
Key principle : triangulation between corresponding image features

Image Features - edges

- Correspondence = matching : but ... what to match ?

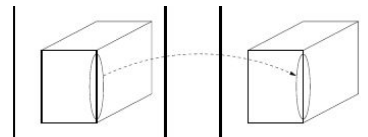
- **Edge Fragments** from edge detector

- numerous, noisy, limited description



- **Edge Lines** from RANSAC (post-processed edge fragments)

- larger structures, less noise, rich description

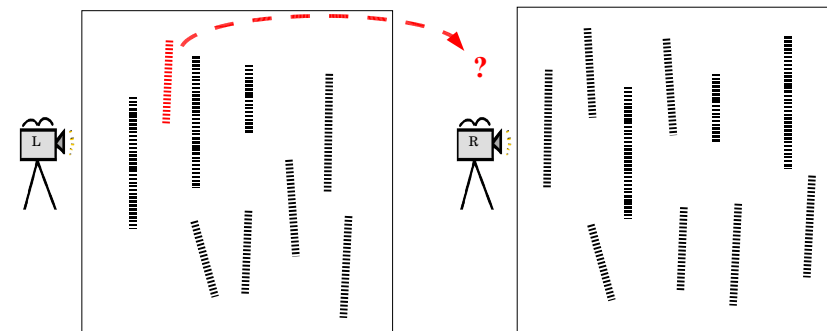


- Which ?

- Lines : few and larger (easier) but harder to obtain and less dependable (noise, occlusion) – **used here**
- Fragments : thought to be used by human visual system

Stereo Correspondence Problem

Q: For a given feature in the left, what is the correct correspondence?



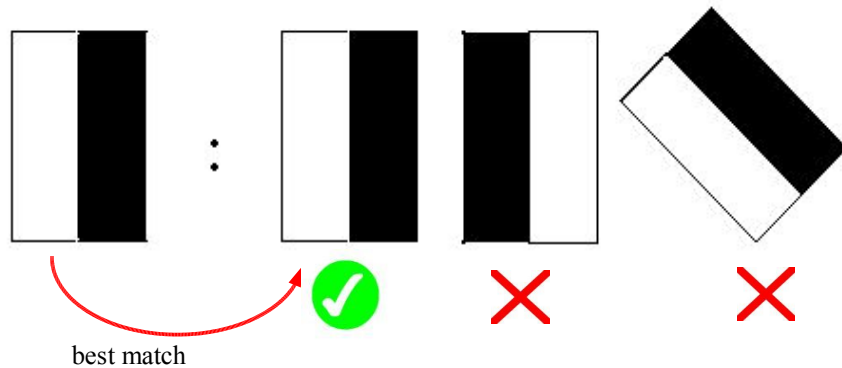
- Different pairing result in different 3D results
 - inconsistent correspondence = inconsistent 3D (!)
 - Key problem in all stereo vision approaches



Correspondence : Matching Constraints (local)

• Orientation

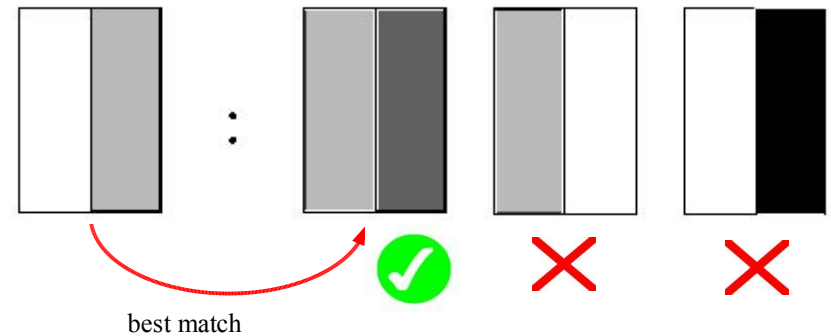
- edge direction \vec{a}



Correspondence : Matching Constraints (local)

• Colour

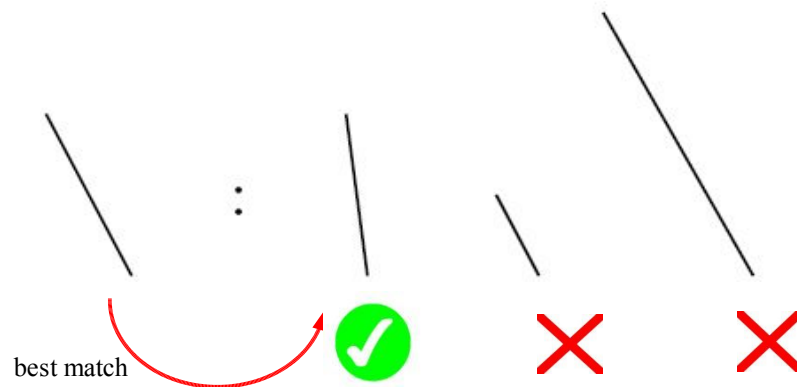
- edge contrast g
(nearly the same across the edge, find closest match)



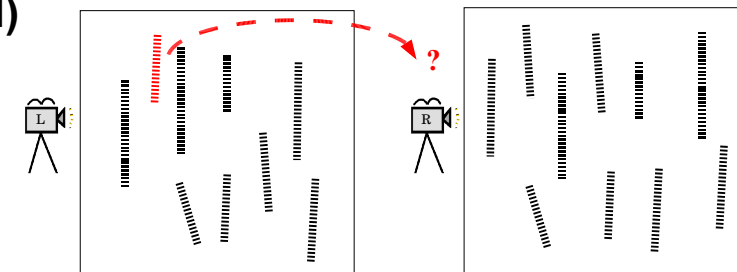
Correspondence : Matching Constraints (local)

• Shape

- edge length



Correspondence : Matching Constraints (global)



• Smoothness

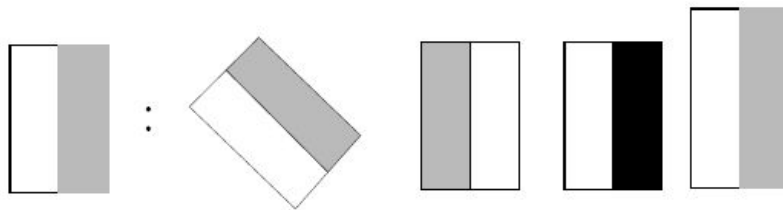
- matched features have consistent depth to neighbours

• Uniqueness

- one to one, left to right, correspondence
 - 0 : no match (due to occlusion in one image)
 - 1 : normal 1-to-1 matching
 - 2+ : difficult cases (wires, vines, etc. from coincidental)

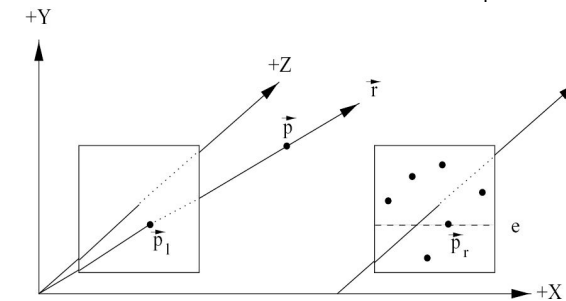
Lecture Problem

- Which stereo correspondence constraint would you use to reject these matches ?



Correspondence : Epipolar Geometry

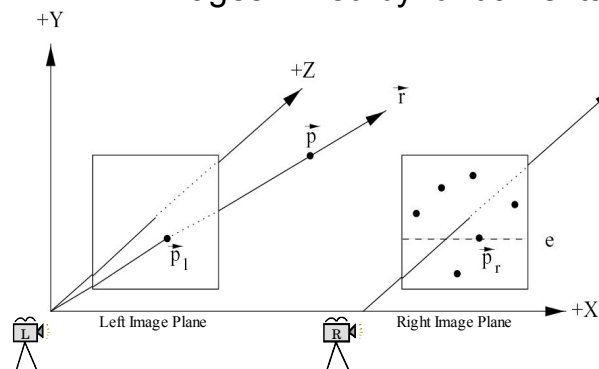
- Feature \vec{p}_l in the left image lies on a ray \vec{r} in space
- \vec{r} projects to an epipolar line e in the right image
 - along which the matching feature \vec{p}_r must lie



- If the images are “rectified”, then epipolar line is the image row
 - i.e. cameras (or images via post-processing) both perfectly axis aligned

Correspondence : Epipolar Geometry

- Constraining L->R Correspondence
 - reduces 2D search to 1D
 - images linked by fundamental matrix, F .

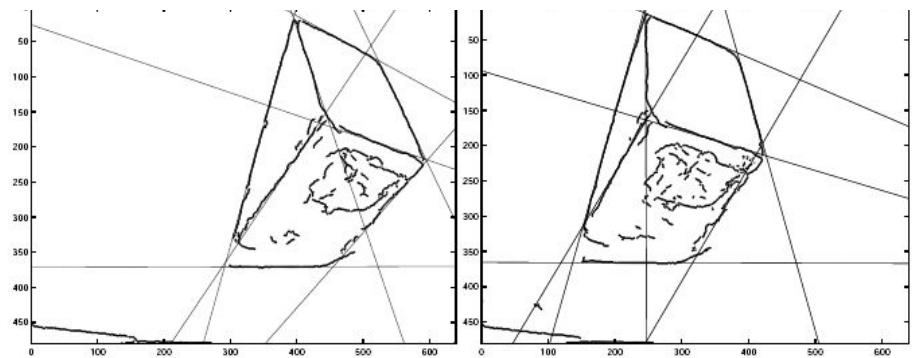


- For matched points $\vec{p}_l F \vec{p}_r = 0$.
- F generally derived from prior calibration routine (with pre-known target).
- Points are homogeneous
- F is 3x3

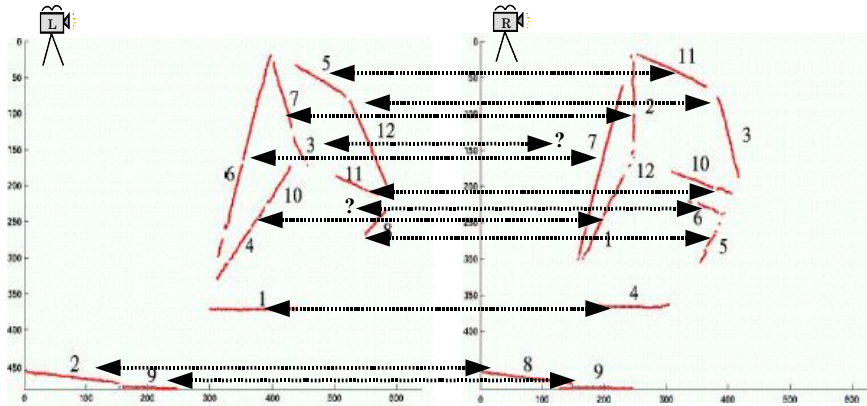
- Match for point \vec{p}_l on ray \vec{r} (left) must lie on epipolar line e (right).



Stereo Matching Results



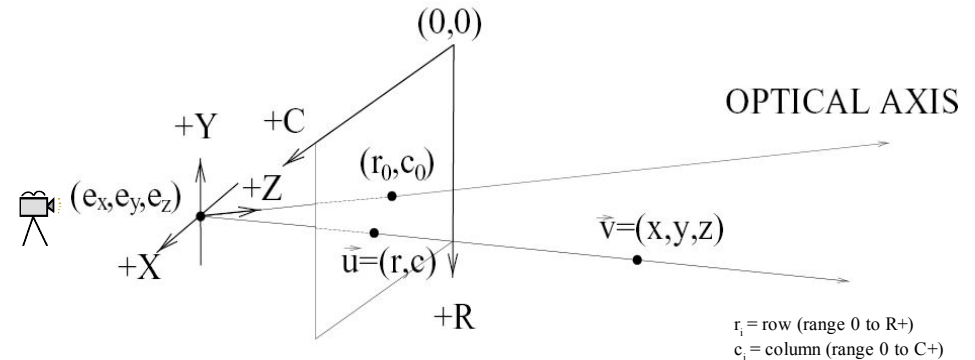
Stereo Matching Results



- Maximally consistent set of correspondences
- Based on local, global and epipolar constraint (interpretation tree or similar, wildcard matches)

Triangulation : Image Projection

- Projection of object point $\vec{v} = (x, y, z, 1)'$ onto image plane, image point $\vec{u}_i = (r_i, c_i, 1)'$. (3D world to 2D image)
- $\lambda \vec{u}_i = P_i \vec{v}$ (λ = homogeneous scaling factor)
 - where P_i = camera projection matrix for $i \in \{L, R\}$



r_i = row (range 0 to R+)
 c_i = column (range 0 to C+)

Triangulation: Projection Matrix

- $P_i = K_i R_i [I | -\vec{e}_i]$, $i \in \{L, R\}$

- R_i : camera orientation
- $\vec{e}_i = (e_{xi}, e_{yi}, e_{zi})$: camera centre (in world)

$$K_i = \begin{bmatrix} f_i m_{ri} & s_i & r_{0i} \\ 0 & f_i m_{ci} & c_{0i} \\ 0 & 0 & 1 \end{bmatrix}$$

- f_i = camera focal length (mm)
- m_{ri}, m_{ci} = row/column pixel/mm scale
- r_{0i}, c_{0i} = optical axis / image plane intersection
- s_i = skew factor

Lab Cameras (example)

$$R_L = R_R = I$$

$$\vec{e}_L = (0, 0, 0) \quad \vec{e}_R = (D_{L \rightarrow R}, 0, 0)$$

(camera separation of d)

$$K_L = K_R$$

(L and R = identical camera(s))

$$f_i m_{ci} = f_i m_{ri} = 832.5$$

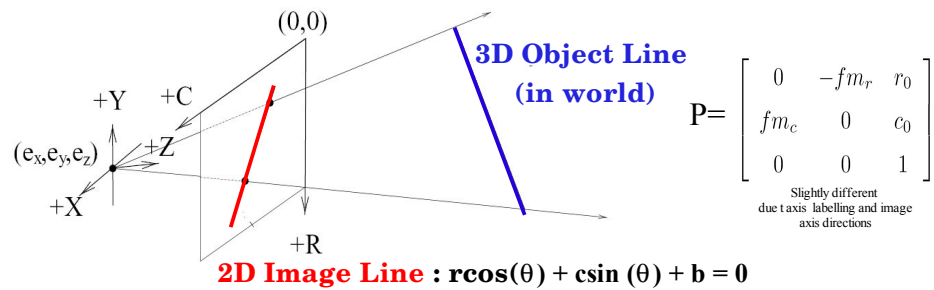
$$r_{0i}, c_{0i} = (\text{height}/2, \text{width}/2)$$

$$s_i = 0 \quad (\text{typical for CCD})$$

Triangulation : 3D line calculation

- **Aim** : recovery of 3D line position
- **Assume** : line successfully matched in L & R images
- Two key stages
 1. **Compute 3D plane** that goes through 2D line in image and camera origin (for both L and R cameras)
 2. **Compute intersection of these two 3D planes** from two cameras
 - intersection of two 3D planes = 3D line

Triangulation – Step 1: Find 3D planes



- Find 3D plane for each image L and R : $\vec{n} \cdot (x, y, z)' + d = 0$

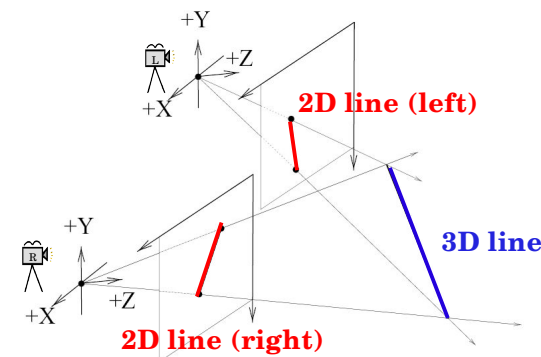
– $(\lambda r, \lambda c, \lambda)' = P(x, y, z, 1)'$ from projection relation. Solving we get:

$$r = -f m_r \frac{y - e_y}{z - e_z} + r_0 \quad c = f m_c \frac{x - e_x}{z - e_z} + c_0$$

– **3D plane** : $\vec{n} = (f m_c \sin(\theta), -f m_r \cos(\theta), r_0 \cos(\theta) + c_0 \sin(\theta) + b)'$

$$d = -\vec{n}' \cdot (e_x, e_y, e_z)'$$

Triangulation – Step 2: Planar Intersection



Two 3D Planes :

- LEFT : $\vec{n}_L \cdot (x, y, z)' + d_L = 0$
- RIGHT : $\vec{n}_R \cdot (x, y, z)' + d_R = 0$

Intersection of two 3D planes gives a 3D line

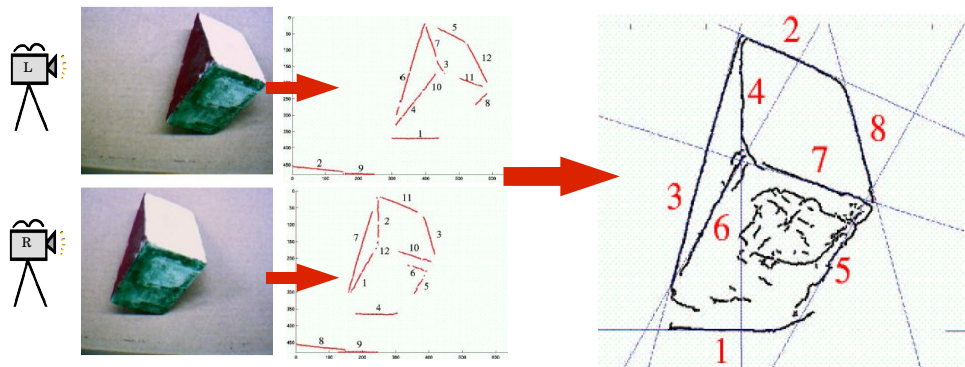
- 3D line defined as : direction \vec{v} , point \vec{a}**

$$\vec{v} = \vec{n}_L \times \vec{n}_R \quad (\text{cross product of planar normals})$$

$$\text{let : } M = [\vec{v}, \vec{n}_L, \vec{n}_R]' \quad (3 \times 3 \text{ matrix}) \quad \vec{b} = [0, -d_L, -d_R]' \quad (3D \text{ point})$$

$$\vec{a} = M^{-1} \vec{b} \quad (\text{point on line closest to origin})$$

Projected Stereo Line Positions



- 3D awareness of our lines as : vector \vec{v} & point \vec{a}
 - defined in \mathbb{R}^3

Correspondence Between Lines

Lines in 3D space

Number	Pairs	direction	point
1	L1:R4	(-0.82, 0.08, -0.56)	(9.1, 2.0, -13.0)
2	L5:R11	(0.61, -0.06, 0.78)	(-125.3, 98.6, 107.1)
3	L6:R7	(-0.28, -0.95, -0.03)	(0.9, -10.6, 294.4)
4	L7:R2	(0.07, -0.62, -0.77)	(48.3, -97.0, 82.9)
5	L8:R5	(-0.18, -0.45, 0.87)	(114.8, 91.8, 72.1)
6	L10:R12	(-0.50, -0.73, 0.44)	(71.5, 77.0, 208.8)
7	L11:R10	(0.79, -0.20, 0.57)	(-98.4, 57.2, 154.6)
8	L12:R3	(0.11, -0.69, -0.70)	(110.4, -123.6, 140.1)

- each line represented by point / vector



Summary

- **Feature Identification**
 - Last lecture : Canny Edge Detection & RANSAC
- **Feature pre-processing**
 - extract extended position/shape/colour description
- **Stereo Correspondence**
 - local and global **matching constraints**
 - **epipolar geometry**
- **Triangulation**
 - intersection of 3D planes \rightarrow 3D line

Next lecture : recognition

