

Energy Transformer

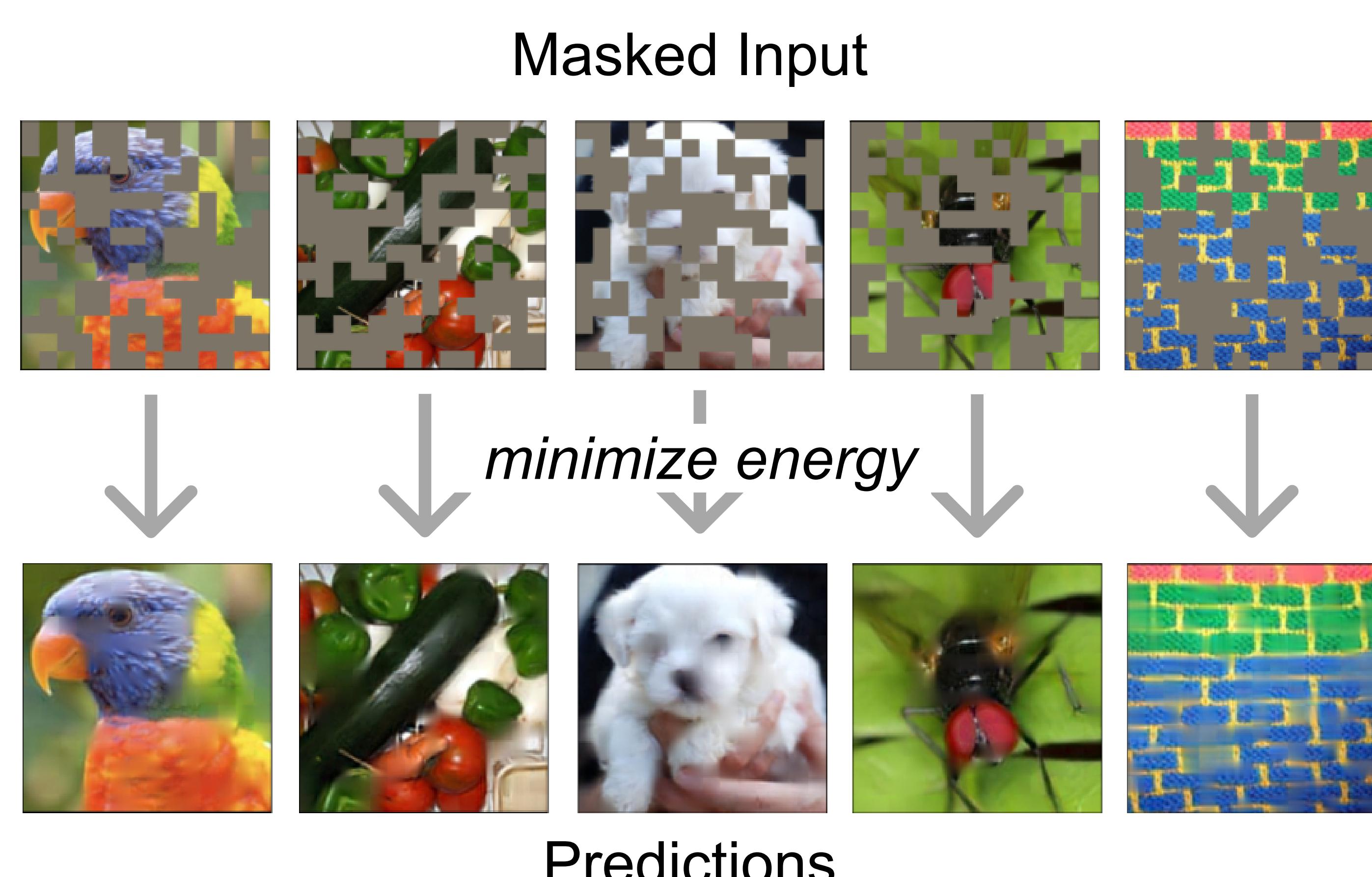
Benjamin Hoover* Yuchen Liang* Bao Pham* Rameswar Panda Hendrik Strobelt Polo Chau Mohammed J. Zaki Dmitry Krotov
*Authors contributed equally

Energy Transformer (**E.T.**) is a novel architecture that is an **Energy-Based Model**, an **Associative Memory**, and a **Transformer**. Specifically, **E.T.** looks like a recurrent Transformer block that defines an attractor system (*an O.D.E. with guaranteed fixed points convergence*) that performs error correction via energy descent. **E.T.** shows excellent performance on MASKed image in-painting, graph anomaly detection, and graph classification.



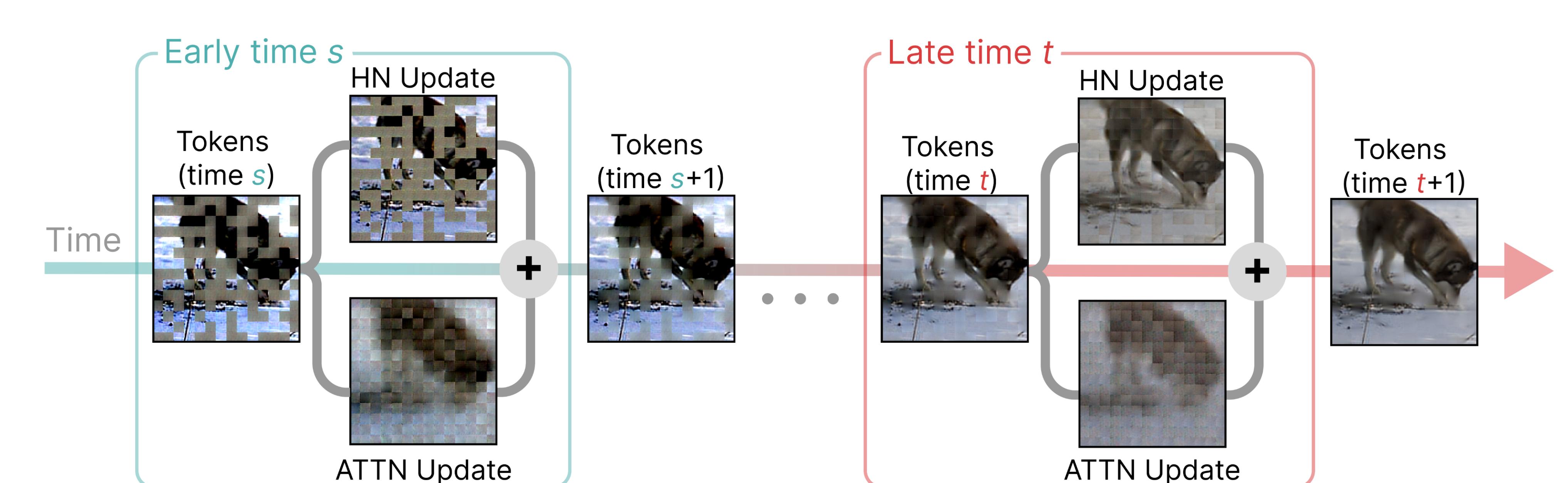
E.T. is Energy-Based Associative Memory

Minimizing energy (inference) performs error correction on corrupted data.



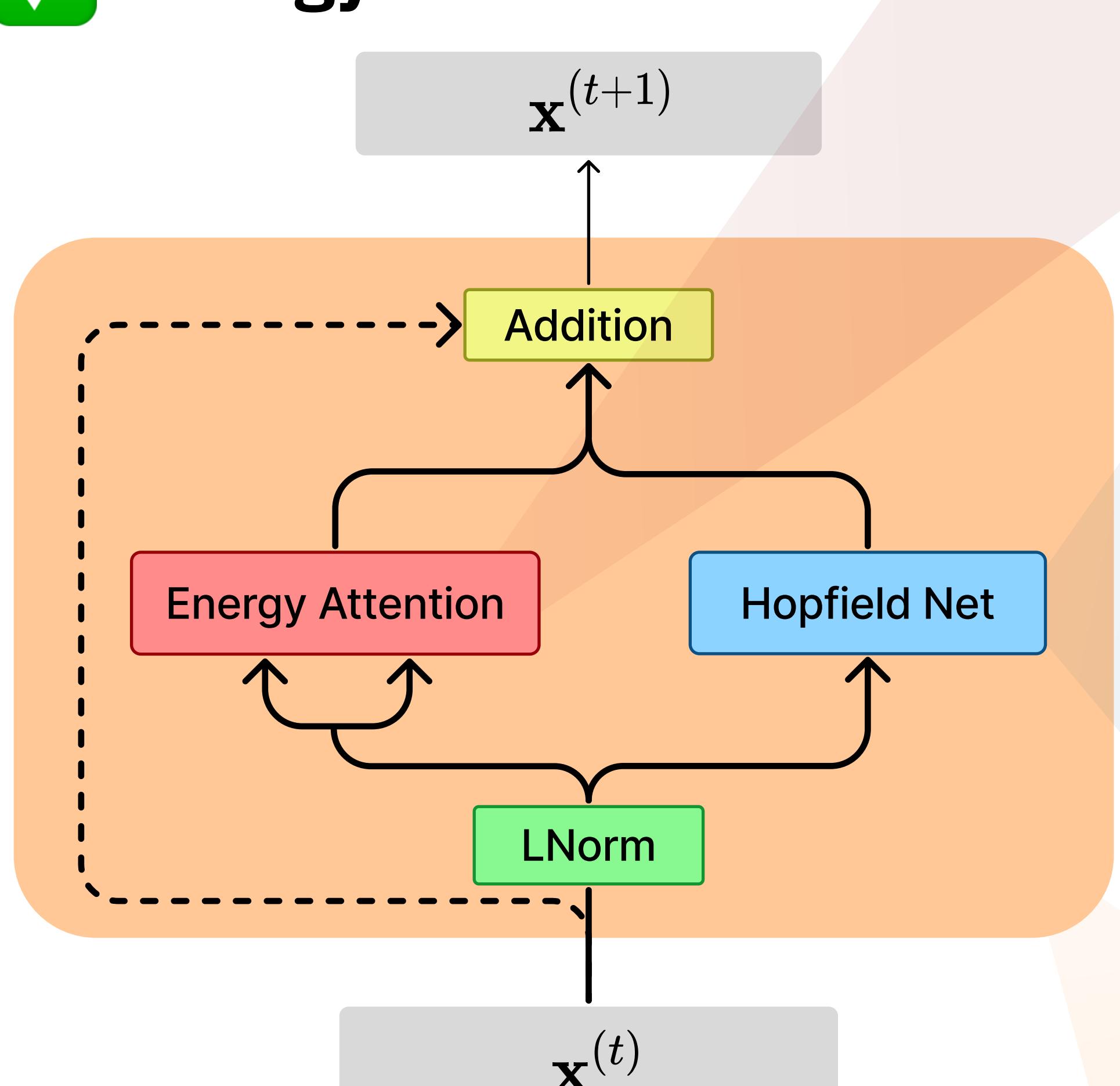
E.T. is Interpretable by Design

Visualize dynamic states (tokens and updates) at any time



E.T. is a Transformer

✓ Energy Transformer Block



Energy Attention makes Queries align with Keys in the latent space (and vice versa!)

Hopfield Network makes tokens look like memories

Energy Transformer minimizes the sum of these energies

$$E^{\text{ATT}} = -\frac{1}{\beta} \sum_h \sum_C \log \left(\sum_{B \neq C} \exp \left(\beta \sum_\alpha K_{\alpha h B} Q_{\alpha h C} \right) \right)$$

$$\begin{aligned} \text{Update: } -\frac{\partial E^{\text{ATT}}}{\partial g_{iA}} &= \sum_{C \neq A} \sum_\alpha W_{ci}^Q K_{\alpha C} \text{softmax}_C \left(\beta \sum_\gamma K_{\gamma C} Q_{\gamma A} \right) \\ &\quad + W_{ci}^K Q_{\alpha C} \text{softmax}_A \left(\beta \sum_\gamma K_{\gamma A} Q_{\gamma C} \right) \end{aligned}$$

$$E^{\text{HN}} = -\sum_{B=1}^N \sum_{\mu=1}^K G \left(\sum_{j=1}^D \xi_{\mu j} g_{jB} \right)$$

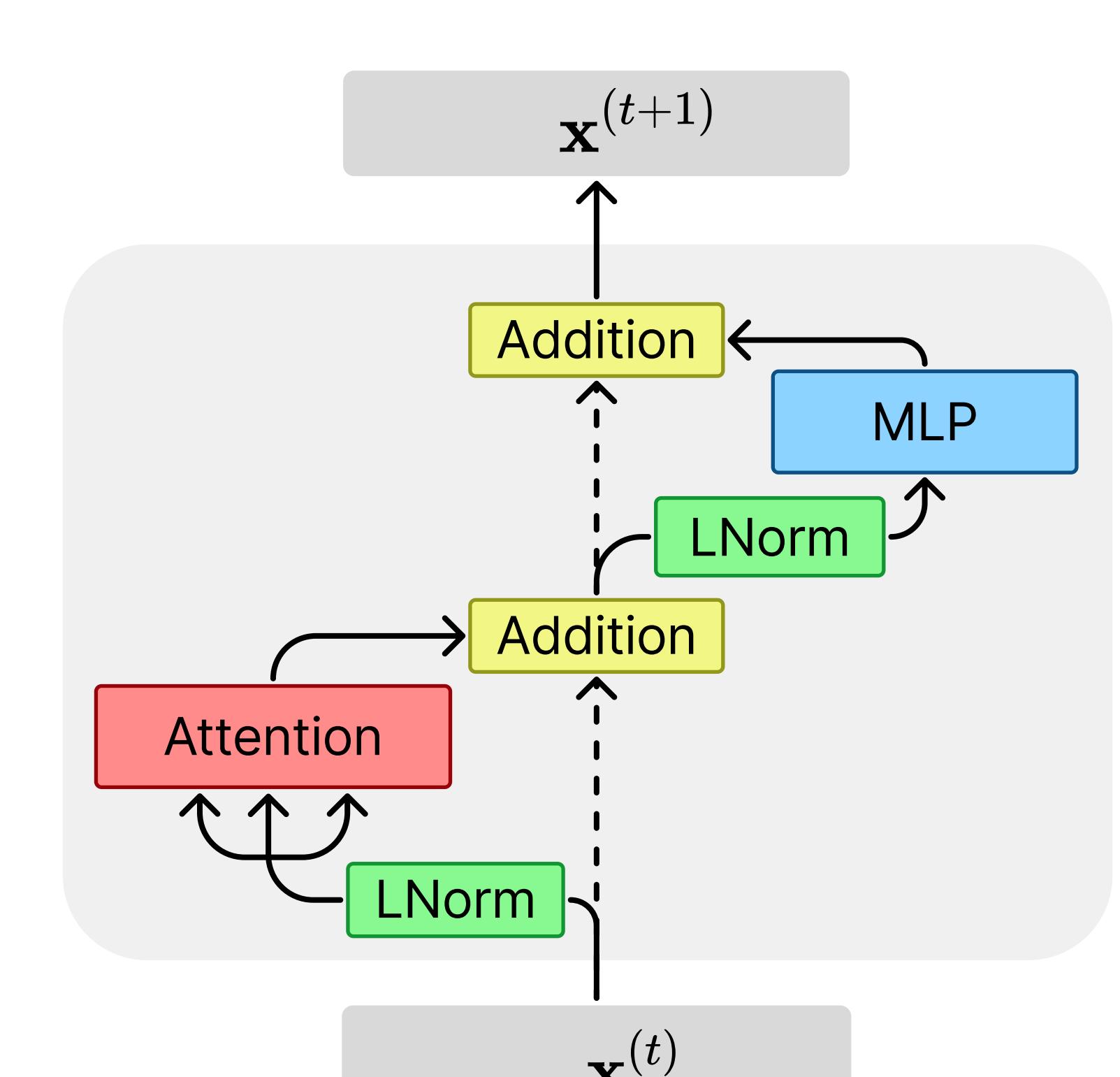
$$\text{Update: } -\frac{\partial E^{\text{HN}}}{\partial g_{iA}} = \sum_{\mu=1}^K \xi_{\mu i} G' \left(\sum_{j=1}^D \xi_{\mu j} g_{jA} \right)$$

$$E = E^{\text{ATT}} + E^{\text{HN}}$$

$$\text{Continuous update: } \tau \frac{dx_{iA}}{dt} = -\frac{\partial E}{\partial g_{iA}}$$

$$\text{Discrete update: } x_{iA}^{(t+1)} = x_{iA}^{(t)} - \alpha \left(\frac{\partial E^{\text{ATT}}}{\partial g_{iA}} + \frac{\partial E^{\text{HN}}}{\partial g_{iA}} \right)$$

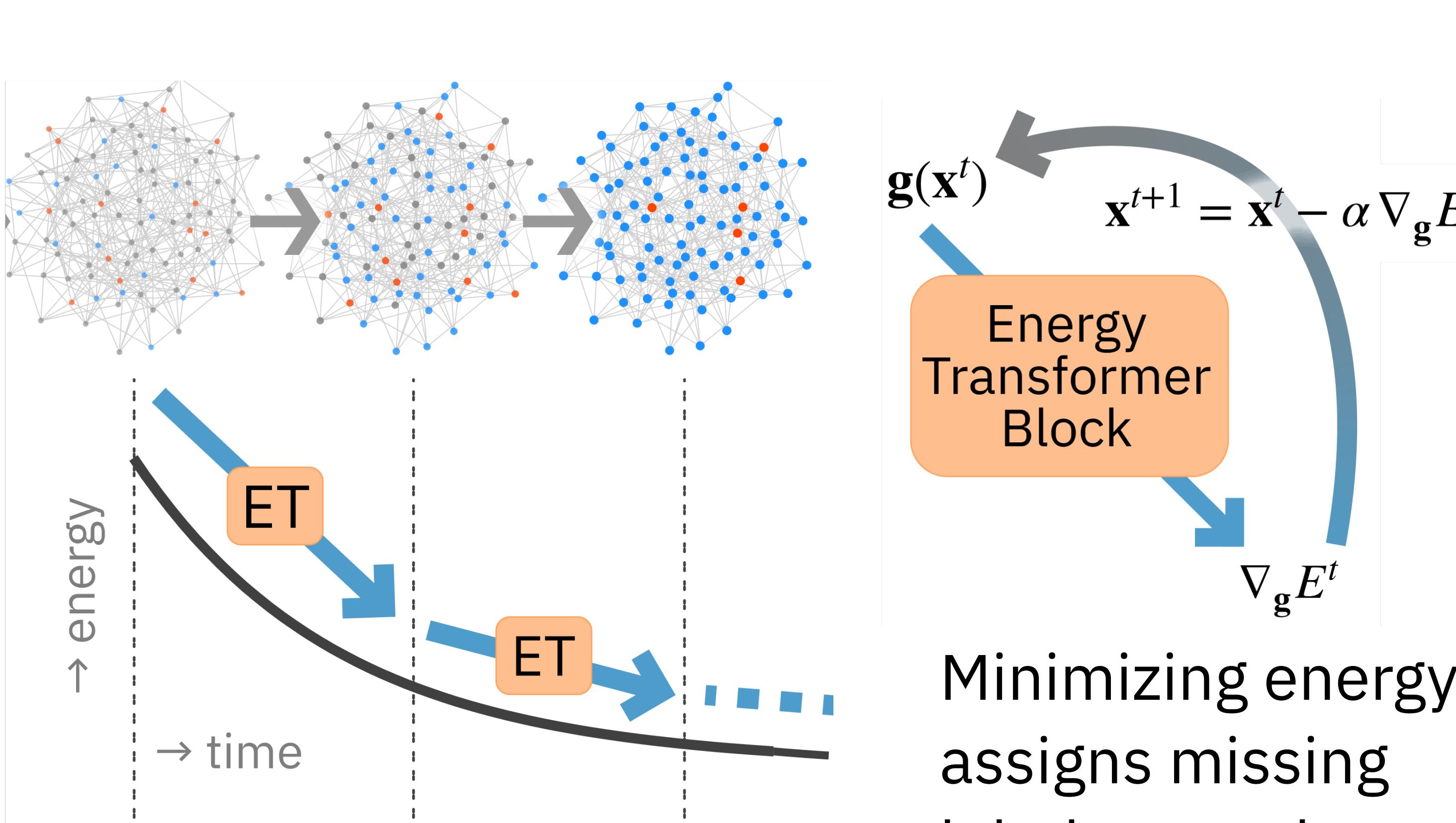
Standard Transformer Block



E.T. sets SOTA on Graphs

Node anomaly detection

Datasets	Split	Top Baseline Score	ET (Ours)
Macro-F1	1%	62.1 ± 1.3	63.0 ± 0.6 ▲0.9
	40%	71.0 ± 0.9	71.5 ± 0.1 ▲0.5
Amazon	1%	90.9 ± 0.7	89.3 ± 0.7 ▼0.7
	40%	92.2 ± 0.4	92.8 ± 0.3 ▲0.6
T-Finance	1%	84.8 ± 0.0	85.1 ± 1.0 ▲0.3
	40%	86.8 ± 0.0	88.2 ± 1.0 ▲1.4
T-Social	1%	75.9 ± 0.0	79.1 ± 0.7 ▲3.2
	40%	83.9 ± 0.0	83.5 ± 0.4 ▼0.4
AUC	1%	75.4 ± 0.9	73.2 ± 0.8 ▼2.2
	40%	84.0 ± 0.9	84.9 ± 0.3 ▲0.9
Amazon	1%	90.4 ± 2.0	91.9 ± 1.0 ▲1.5
	40%	98.0 ± 0.4	97.3 ± 0.4 ▼0.7
T-Finance	1%	91.1 ± 0.0	92.8 ± 1.1 ▲1.7
	40%	94.3 ± 0.0	95.0 ± 3.0 ▲0.7
T-Social	1%	88.0 ± 0.0	91.9 ± 0.6 ▲3.9
	40%	95.2 ± 0.0	93.9 ± 0.2 ▼1.3



Rensselaer

IBM Research

GT Georgia Tech

Graph Classification

Datasets	Top Baseline Score	ET (Ours)
PROTEINS	84.9 ± 1.6	90.3 ± 5.4 ▲5.4
NCI1	87.5 ± 0.5	90.1 ± 0.1 ▲2.6
NCI109	87.4 ± 0.3	90.5 ± 0.1 ▲3.1
DD	95.7 ± 1.9	95.9 ± 0.8 ▲0.2
ENZYMES	78.4 ± 0.6	99.8 ± 0.0 ▲21.4
MUTAG	100.0 ± 0.0	96.6 ± 0.2 ▼3.4
MUTAGENICITY	82.2 ± 0.6	98.7 ± 0.1 ▲16.5
FRANKENSTEIN	78.9 ± 0.3	99.8 ± 0.1 ▲20.9