Advanced Statistical Methods Homework 5

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Overview

1 Q1A: Issues/mistakes with cross-validation

- Q1B: Issues/mistakes with bootstrap?
- 3 Q2: Hastie and Tibshirani Summary

Issues/mistakes with cross-validation

 K-fold cross validation biases toward increased prediction error.

```
Test data

Training data

Iteration 2

Iteration 3

Iteration k

All data
```



Issues/mistakes with cross-validation

- K-fold cross validation biases toward increased prediction error.
- Filtering data before placing into validation groups can cause problems with fitting;
 over-fitting to 0% training error.

```
Iteration 2

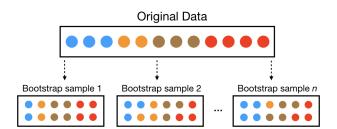
Iteration 3

Iteration k

Iteration k
```

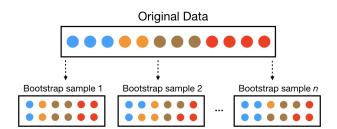
Issues/mistakes with bootstrap

• Datasets possess significant overlap.



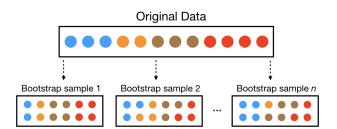
Issues/mistakes with bootstrap

- Datasets possess significant overlap.
- Severely underestimates the prediction error.



Issues/mistakes with bootstrap

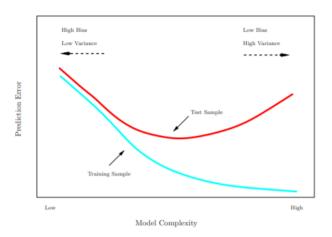
- Datasets possess significant overlap.
- Severely underestimates the prediction error.
- May be improved if validated with samples that did not end up in any of the bootstrap samples.



Hastie and Tibshirani Lecture: Resampling Methods

Testing the accuracy of our model.

The goal is to minimize testing error:



Hastie and Tibshirani Lecture: Resampling Methods

Possible approaches:

- Validation Set Random splitting of data to provide a set for testing error.
- K-fold Cross Validation Splitting data into K parts, using one as the validation set, and the other K-1 as training sets. Afterward select the model that provided the lowest test error.
 - Bootstrap Multiple data sets produced from the original by sampling from the original with some data replaced with random selections from the original data-set.

Hastie and Tibshirani Lecture: Permutation v. Bootstrapping

Bootstrap

Sample from estimated population

Permutation

Sample from estimated null distribution

Hastie and Tibshirani Lecture: Permutation v. Bootstrapping

Bootstrap

- Sample from estimated population
- Great for estimating population stats

Permutation

- Sample from estimated null distribution
- Is simpler and generally performs just as well as bootstrap

Hastie and Tibshirani Lecture: Permutation v. Bootstrapping

Bootstrap

- Sample from estimated population
- Great for estimating population stats
- Great for testing certain null hypotheses

Permutation

- Sample from estimated null distribution
- Is simpler and generally performs just as well as bootstrap
- More practical with modern computing