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# 1 Dr. Yielding's Questions

While HARL is indeed a subfield of MARL, the distinction between the two can often be unclear or inconsistently used in the literature. In the broadest sense, 'heterogeneous' may refer to any MARL scenario where the agents are not identical. However, using this broad definition risks diluting the practical significance of the term.

To provide a more useful distinction, HARL should be invoked when the heterogeneity of the agents is fundamental, essential, or definitional rather than merely incidental. This means the differences among agents are critical to their roles and interactions within the system, not just minor variations.

Prior to my literature review, I would have considered HARL to apply specifically to cases where agents are distinct from the outset, either in their capabilities (For action-space A,  $A_1 \neq A_2$ ) or their observation spaces  $(\mathcal{O}_1 \neq \mathcal{O}_2)$ . This intrinsic heterogeneity is evident in works like [1] (the Irish conference paper mentioned in Dr. Yielding's question) and implicitly reflected in [2] (OpenAI Five), even though they do not explicitly label their methods as HARL.

The most comprehensive source on HARL usage is Zhong et al. [3], whose work has greatly influenced my understanding. They focus on implementing algorithms that encourage the development of heterogeneous policies among agents. Their framework increases the likelihood of individual agents converging on distinct policies, which I term emergent heterogeneity.

In my prospectus, I also mention a suspicion that this approach might not entirely prevent agents from converging on policies that are functionally similar, thus lacking true diversity. However, this assertion remains an ancillary detail as it is not yet substantiated by empirical evidence.

Therefore, I propose distinguishing between intrinsic heterogeneity, where agents are fundamentally different before training, and emergent heterogeneity, where differences arise as a result of the learning process. In the cases where the heterogeneity of the agents falls below a level of functional relevance, and appears to be incidental, I argue that they should not be labeled as HARL. By maintaining these distinctions, we can more accurately categorize and understand the applications and implications of HARL and MARL.

Below, I apply these distinctions to the cases proposed:

- **1.1** HAA2C and HADDPG are among the numerous algorithms proposed by Zhong et al. [3]. While it seems reasonable that their algorithms could be applied to situations with intrinsic heterogeneity, their implementations and tests are applied to environments with agents that are functionally the same.
  - I intend to implement (at least a subset of) their algorithms to the extent that time allows. In doing so, I hope to either corroborate or contradict their results by comparing them to similar algorithms under different conditions. This exploration aims to identify any apparent advantages of these algorithms when applied to the experimental variables proposed for Contribution 1. These experimental variables represent smaller difficulties that we expect to face in Contributions 2 and 3.
- 1.2 (a) The scenario described in this part of the question is, perhaps unintuitively, more akin to single-agent than multi-agent reinforcement learning. This becomes clearer when considering a single agent acting as an 'overlord,' where the observation space is a combination of observations from all the individual agents. The actions taken by this overlord are combinations of actions chosen for each agent. Essentially, a single policy processes the combined observation and outputs the combined action.
  - (b) This example is a strong example of MARL, and because the agents utilize copies of a singular policy, this example is free from any of the types of heterogeneity described in the answer for question 1.1.
  - (c) The types of problems accurately described by the scenario provided in this part of the question appear to be a subset of MARL problems and a superset of HARL problems.
    - Many MARL algorithms allow the member policies to develop distinctly (e.g., [4]–[6]), but they are not optimized to facilitate the development of distinct policies.
    - Zhong et al. [3] formulate their series of HARL algorithms with optimizations intended to facilitate the development of distinct policies. One weakness of this formulation is that there is no guarantee that the multiple policies will not converge to a behaviorally indistinct set, similar to the concept of carcinization observed in evolutionary biology.
    - Thus, the resulting heterogeneity of the agents in these scenarios is not intrinsic but emergent. Whether the algorithm itself is labeled as MARL or HARL is distinguished by intent.
- **1.3** Referencing Centralized Training Decentralized Execution (CTDE) and Decentralized Training Decentralized Execution (DTDE) as employed by Li et al. in their FA2A paper [7], we see that CTDE is the most common format for Actor-Critic based MARL algorithms [4]–[8].
  - Li et al. [7] and Wen et al. [9] are the only papers I found that discuss the contrary implementation, DTDE. In both cases, the authors motivate DTDE with practical concerns, particularly the limitations of interagent communication in distributed systems. These considerations are important, but the relation to HARL remains the same as described in answer 1.2 (c).

# 2 Dr. Robbins' Questions

In addition to being included in the appendices of this exam, all code used to run the experiments is available on my github at https://github.com/bhosley/Specialty-Exam. It is written to be run on any ANT-Center VSCode server containers, but should work in a generic virtual environment. The specifications for the virtual machines used for this experiment are enumerated in table 1.

I recommended increasing the ratio of memory to CPU allocation for future experiments as the container was substantially closer to maximum utilization of memory than processing for the duration of the experiments run for this exam.

Setting	Value
Template	vscode-server
Image	reg.git.act3-ace.com/ace/
	hub/vscode-server:v0
Max CPUs	64
Req. CPUs	16
Memory	64 GB
GPU	None

**Table 1: Container Settings** 

The github readme has a short guide for setting up the virtual environment in the ANT-Center for easy replication. The answers for this section are drawn from the experiment running script, also provided in appendix A of this document.

2.1 The Deep Q-network (DQN) implementation [10], [11] implemented in the RLlib framework [12] was used for each of the answers in this section. The default results output is readable by tensorboard, but I chose to use the wandb (Weights and Balances) api as well.

To perform this baseline experiment we can call the default script (appendix A). We can accomplish a 5 replication test by setting --num-env-runners=5, however, this overrides the default of 10, so we have chosen not to use it and to keep the default. We use the

```
python dqn_exp.py --sweep --num-samples=30 --num-env-runners=10
```

#### Round 1 - Bad Results:

In the first round of Parameter sweeping, a large number of training runs failed to converge on reasonable results. This was somewhat surprising, and when examining the parameters there was no immediately obvious pattern. Adding the average number of steps per episode to the Comparison (fig. 1) shows consistently shorter episodes for poor performance. Further investigation showed that the observation space assigned to the environment from the RLlib registered lunar lander environment was significantly different from the

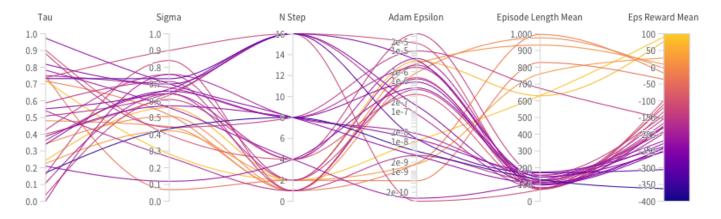


Figure 1: Lunar Lander Baseline Experiment 1 Hyperparameters

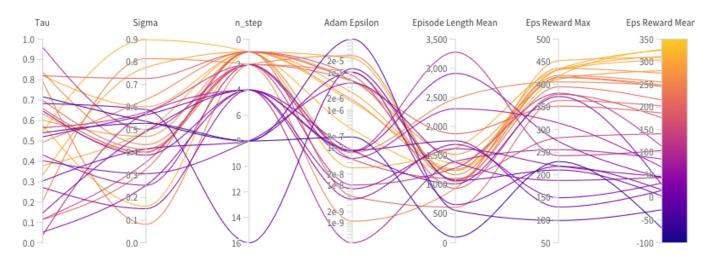


Figure 2: Lunar Lander Baseline Experiment 2 Hyperparameters



Figure 3: Baseline Experiment 2 Hyperparameter Importance

correct space. Further, manually registering the environment after importing it directly from the Farama maintained packages using Ray's environment registration function resulted in an outdated observation space, less prone to resulting in error, but still problematic.

Thus we gain two actionable insights. First, we adjust this experiment to use the custom Lunar Lander environment described in the next section, but set to one agent. Second, we identify an update that can be performed by a pull request to the maintainers of RLlib, a contribution to the open-source software I would like to attempt after the submission of this exam.

#### **Round 2 - Baseline Parameter Sweep:**

To evaluate the parameters of the sweep I elect to conduct a comparison with three different methods. I will use the same methods for the sweeps performed on the subsequent questions as well.

As above, the parallel coordinates graph provides a visual comparison of parameter values and a qualitative impression of the effects. Second, I use the wandb api Parameter importance and correlation graph, which provides an importance metric based on an algorithm from [13] that combines a tree-based regression and Spearman rank correlation; and the standard and Pearson correlation metric. Finally, for a more quantitative metric I produce an ANOVA table using second order interactions of the hyperparameters.

Figure 2 shows the parallel coordinates for this experiment's parameter sweep. Immediately this suggests that the n-step instances under-perform the single step instances. The factor importance (fig. 3) corroborates this. Finally, we execute the ANOVA in appendix C.1, and find that the  $\sigma$  parameter has a statistically significant effect on the final performance, particular as an interaction variable.

### **Multi-Agent Lunar Lander**

To modify the Lunar Lander environment to support multiple agents it appeared to be possible to simply duplicate all of the sections that referenced the lander in the original code. However, to achieve cleaner code, and behavior more consistent with Farama's PettingZoo environments, I elected to rewrite the environment to be more consistent with object oriented programming principles.

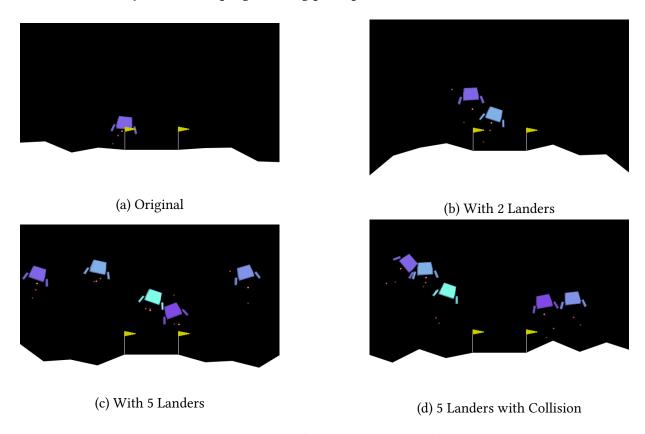


Figure 4: Multi-Agent Lunar Lander

This trivialized the retention of the environmental physics, and made it very easy for the new environment to comply with both the AEC (Agent Environment Cycle; or sequential) and parallel execution methods used in the PettingZoo API. Further, this made it much easier to retain the heuristic solution from the original environment. Figure 4 shows several screen shots from the resulting environment when rendered.

While an AEC version of this custom environment was constructed, it was not used for this exam. AEC iterates through the list of agents, allowing the agent to select an action and steps the environment with that action before moving to the next agent, in a manner similar to a board game. Such an implement doesn't necessarily contribute value to the multi agent Lunar Lander sim, and in fact, causes problems if the physics of the environment are not adjusted as the number of landers is increased. Using the heuristic as a measure, the AEC environment becomes unsolvable with 3 or more landers. The effect of their actions must be scaled to overcome the wait time between their turns, otherwise they simple crash, unable to overcome gravity.

The parallel version of the environment was used for this exam, and required only one major assumption, centering around collisions between the landers. Lunar Lander uses the Box2D package to model the moon surface and lander. The most expedient method to address collisions using Box2D was to detect only contact with the lander's body. If any other object touches a lander's body it is considered a crash. As written, the Box2D contact detection does not distinguish between what the secondary object is, if the legs of the lander where included, contact with lunar surface would show as a crash. Thus I chose not to include the legs contact detection for collisions. The effective result is that if two lander's legs touch it is not treated as a crash, however, if one lander's legs touch another's body module it is treated as a crash and thus a failure.

In addition to being available on the associated github, the new environment code is included in appendix B

**2.2 Formulate a Markov Game:** The Markov game that represents the multi-agent version of this environment is an extension of the Markov Decision Process (MDP) that represents the original Lunar Lander environment. The formulation presented here will be used to describe the interactions in all of the questions that follow.

*Agent:* The agent is represented as a member of set of agents  $n \in N$ .

State Space: Let S be the state space. Then,  $S \equiv s^N$ , where

$$s = \begin{cases} x \in [-2.5, 2.5] & \text{Position of } n \text{ in } x \\ y \in [-2.5, 2.5] & \text{Position of } n \text{ in } y \\ \vec{x} \in [-10, 10] & \text{Velocity of } n \text{ in } x \\ \vec{y} \in [-10, 10] & \text{Velocity of } n \text{ in } y \\ \omega \in [-2\pi, 2\pi] & \text{Angle of } n \\ \vec{\omega} \in [-10, 10] & \text{Angular Velocity of } n \\ \mathbb{I}(\text{leg 1}) \in \{0, 1\} & \text{Leg on ground} \\ \mathbb{I}(\text{leg 2}) \in \{0, 1\} & \text{Leg on ground} \end{cases}$$

Action Space: Let A be the action space. Then,  $A \equiv a^N$ , where

$$a \in \begin{cases} 0 & \text{No-Op} \\ 1 & \text{Fire Left Engine} \\ 2 & \text{Fire Main Engine} \\ 3 & \text{Fire Right Engine} \end{cases}$$

Transition Probability: The transition probability for each agent n remains the same as the original environment,

$$P_n(s_{n,t+1}|s_{n,t},a_{n,t}) \cong \begin{cases} \text{Dispersion} \sim U(-1,1) \\ \text{Wind(Linear)} = \tanh(\sin(2kx) + \sin(\pi kx)) \\ \text{Wind(Rotate)} = \tanh(\sin(2kx) + \sin(\pi kx)) \end{cases}$$

Thus the transition probability for the game as a whole is

$$P(s_{t+1}|s_t, a_t) = \prod_{n \in N} P_n$$

Reward: The reward structure is similarly retained from the original Lunar Lander environment. Specifically, the reward at time t is defined as  $r(t) = \sum_{n \in \mathbb{N}} r_n(t)$  where

$$\begin{array}{ll} r_n(t) = & \\ & \pm 100 & \text{End-state, crash or land} \\ & + 10(s_{t,6} + s_{t,7}) & \text{leg(s) on ground} \\ & - a_n(t) \cdot [0, 0.03, 0.3, 0.03] & \text{thruster cost} \\ & - 100 \sqrt{s_n(t)_0^2 + s_n(t)_1^2} & \text{Distance} \\ & - 100 \sqrt{s_n(t)_2^2 + s_n(t)_3^2} & \text{Velocity} \\ & - 100 |\omega_n(t)| & \text{Tilt} \end{array}$$

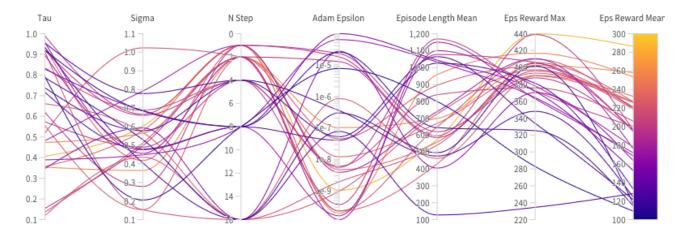


Figure 5: Single-agent Control Hyperparameter Sweep



Figure 6: Single-agent Control Hyperparameter Importance

**2.3 DQN Single-Agent Controller:** This problem was approached using a wrapper class around the custom multi-agent environment to translate the between the multi-agent environment and single-agent policy. The proxy single-agent state/observation was formed by simply concatenating the state vectors of each agent.

The modified action space for this problem is  $\mathcal{B} \equiv \mathcal{A}^N$ . To relate the two action spaces for this problem I use the function,

$$b = \sum a_n \times \dim(a)^n.$$

Then to translate the modified action into the agent-action vector necessary for the multi-agent environment I use the following function,

$$\mathbf{a} = \{b/\dim(a)^n \mod \dim(a)\}_{n \in N}$$

which relies on  $\dim(\mathcal{A}_n) = \dim(\mathcal{A}_m) \forall n, m \in \mathbb{N}$ , an assumption that I note as it is true for this problem, limits some generality. The policy can thus be represented as  $\pi(b|[s_n]_{n\in\mathbb{N}})$ .

Finally, the experiment can be replicated using the command:

$$\label{eq:python_dqn_exp.py} \ \text{--SA } \ \text{--sweep } \ \text{--num-samples} = 30 \ \text{--num-env-runners} = 10$$

Figure 5 shows the results of the parameter sweep for this experiment. It appears from this information that there are no clear patterns suggesting what the optimal values are for the hyperparameters. Next, we consult fig. 6. From these metrics we do see some indication that the  $\tau$  and n-step parameters may hold some importance for the final performance. And finally, the ANOVA table in appendix C.2, shows a statistical significance associated with the  $\sigma$  parameter.

I interpret the high statistical significance but extremely low correlation of the  $\sigma$  parameter to suggest that the mid-distribution value has a tendency to produce the best results. The superlative instance has a  $\sigma$  parameter near this 0.5, but overall, it appears that the algorithm is fairly resilient to Hyperparameter tuning.

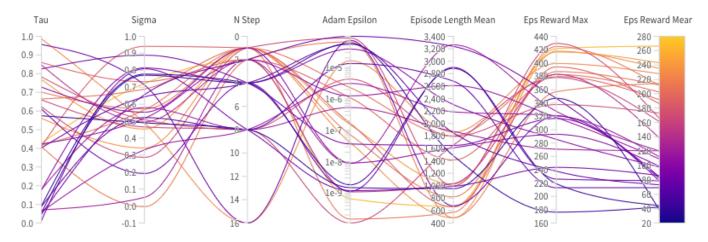


Figure 7: No Parameter Sharing Hyperparameter Sweep

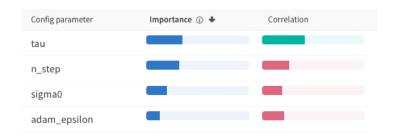


Figure 8: No Parameter Sharing Hyperparameter Importance

**2.4 NoPS - No Parameter Sharing:** This experiment uses a distinct policy for each agent,  $\pi_n(a_n|s_n)$ , and can be replicated using:

```
python \ src/dqn\_exp.py \ \hbox{--NoPS --sweep --num-samples} = 30 \ \hbox{--num-env-runners} = 10
```

The parameter sweep results for this experiment can be seen in fig. 7. There doesn't appear to be any extremely clear or significant patterns from this parallel comparison.

There are, however, several observations of interest that are not directly concerning the hyperparameters. First, is a generally poor performance for instances that produce longer average episode length. Second, unlike the parameter sharing control, this consistently converged on a result that produced a positive reward in every case. I attribute this partially to sample size, but also note that this result is consistent with have two separate policies; that in order for the final mean episode reward to be negative, both policies would have to converge to poor behavior. This may also explain the more even distribution of average returns between the instances of this experiment.

Next, fig. 8 shows the parameter importance metrics, which similarly suggests no strong relation between the Hyperparameter values and results, which is further corroborated in appendix C.3 which shows no statistically significant first or second order relationship between between the parameters and the final results. Finally, I present fig. 9 which shows the learning curves of the agents from 10 instances of this experiment. The resulting curves are consistent with pairs of agents that are learning differently.

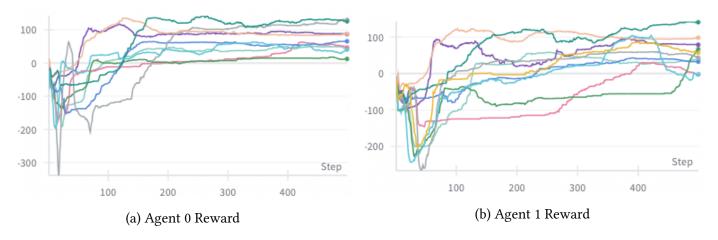


Figure 9: No-parameter Sharing Learning Curves, average reward × training iteration

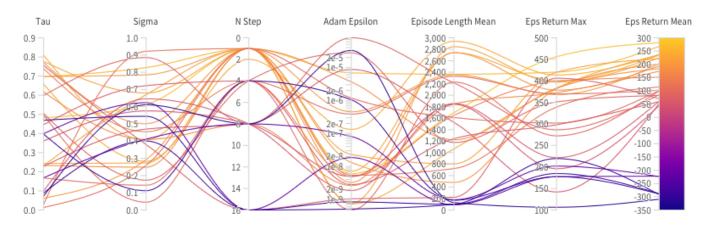


Figure 10: Full Parameter Sharing Hyperparameter Sweep

**2.5 FuPS - Full Parameter Sharing:** This experiment uses a shared policy for each agent,  $\pi(a_n|s_n)$ , and can be replicated using:

```
python \ src/dqn\_exp.py \ \text{--FuPS --sweep --num-samples} = 30 \ \text{--num-env-runners} = 10
```

The parameter sweep results for this experiment can be seen in fig. 10, once again it appears that there is a slightly higher performance result from a low or no n-step parameter. Further, when considering the additional compute required to execute the higher n instances, it is likely to be net negative. Figure 11 supports the high performance from lower n. Further, between the two figures, some support in favor of a  $\tau > 0.5$ . However, the ANOVA results (appendix C.4) suggest that these may not be statistically significant.



Figure 11: Full Parameter Sharing Hyperparameter Importance

#### 2.6 Results Comparisons:

Control	au	$\sigma$	N-Step	Adam- $\epsilon$
Single Agent	0.5	0.6	1	1e-5
NoPS	0.75	0.5	1	1e-7
FuPS	0.75	0.5	1	1e-8

Table 2: Hyperparameters used for control comparisons.

For the comparison I ran 10 instances of each algorithm using the parameters in table 2, which were values near those of the superlative performers in the previous sections. Some consideration was given to the default values of the DQN implementation. It may be noted that Mnih et al. [11] intended for their algorithm to be resilient and require minimal adjustments. The results seen in the previous sections seem to fit that intent, with exception to certain more extreme settings.

Figure 12 shows learning curve aggregates for each of the evaluated algorithms. From these results we see that the single-agent consistently under-performing the other algorithms, particularly, that after 250 episodes every instance's average was below the average of every instance of the other algorithms. Additionally, the variance in the average performance of the single-agent control algorithm was significantly greater than the other two algorithms. I attribute both of these observations to the larger action space and reduced ability to explore when using this control method.

Figure 13 shows a measure of performance of the algorithms from the perspective of computational requirements. The CPU utilization for the single-agent control was by far the most consistent of the three, where the full-parameter sharing was generally higher while occasionally dropping to a utilization similar to the single-agent control. No-parameter sharing appears to have spent equal time between these two values. It is unclear from the experiments conducted for this exam why this would be the case. I would have expected that the NoPS instance would have a generally higher utilization than the others.

The memory utilization is about the same for each algorithm (fig. 14). Given that the algorithms use the same deep network architecture for their value functions, it reasonably follows that the memory usage would be similar, with small differences by the nature of the non-sharing networks are two separate networks it would not be surprising for those instances to have greater memory use, which appears to be the case by a small margin.

This same graph highlights perhaps the most significant advantage of the single agent control, which was an execution time almost half as long as the others. While this was not an advantage that I had considered prior to the experiment it seems that it would follow that the single agent controller uses the DQN once per step for each action and afterwards updates one network, where as the others would have to do so twice.

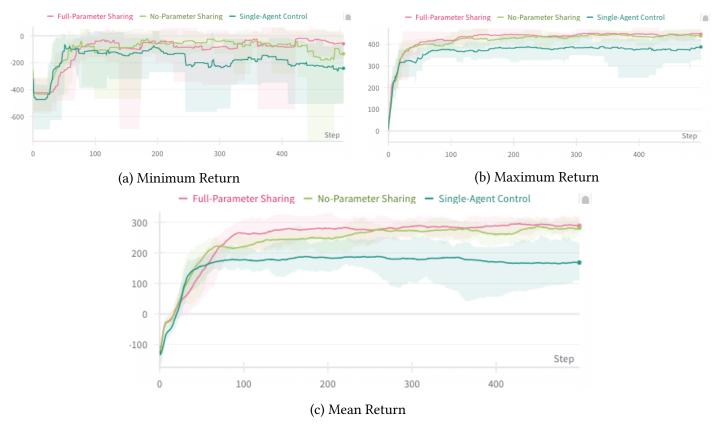


Figure 12: Returns by Episodes



Figure 13: CPU Utilization



Figure 14: Memory Usage (MB)

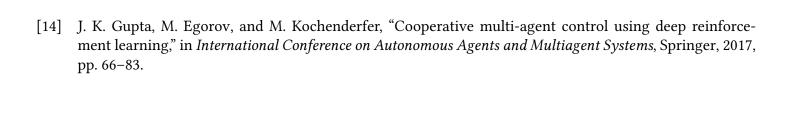
Base Algorithm MARL HARL Action Space PPO MAPPO HAPPO DQN

# 3 Dr. Cox's Questions

- **3.1** I concur with the probable necessity of narrowing the scope of contribution one, particularly to maintain the feasibility of the proposed timeline.
  - (a) **Cooperative Tasks:** The SISL (Stanford Intelligent Systems Laboratory) environments are presented by Gupta et. al. in [14]. Two of the task in particular I believe to be usable, *Pursuit* and *Waterworld*. The latter of the two can be instantiated as a cooperate-competitive task. *Multiwalker* may be included, but that will be determined by whether or no I am able to get the task to function as expected with different numbers of walkers from the default 3. The two former environments are known to operate with a wide range of numbers of agents.
    - The MPE (Multi Particle Environment) is simple and has a variety of available tasks. However, among the manufacturer included tasks, *Simple Spread* is probably the only one suitable for the proposed evaluated. *Simple Spread* is a task that is essentially a zone-coverage/task-assignment type problem.
  - (b) **Competitive Tasks:** To maintain a greater focus on the adaptability and cooperation aspect of agent-groups I believe that it would be best to omit any pure competitive tasks. However, I intend to include cooperative-competitive tasks. As an example of this, let us take *Water World*; when the task is set such that a single agent can complete ('consume the food') it becomes a pure competitive environment, however, increasing that value is intended to produce emergent cooperation as the goal requires n agents to simultaneously activate the goal.
  - (c) Algorithms:
  - (d) Environments:
  - (e) League:

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## **A** Experiment Running Script

```
"""Script for Dr. Robbins Questions
  Establishing a baseline implementation of Single Agent Lunar Lander
  with a DQN.
  See: https://gymnasium.farama.org/environments/box2d/lunar lander/
  for more details on the environment.
  How to run this script
  `python [script_name].py`
  For debugging, use the following additional command line options
12
  `--no-tune --num-env-runners=0`
13
14
  For logging to your WandB account, use:
   `--wandb-key=[your WandB API key] --wandb-project=[some project name]
16
  --wandb-run-name=[optional: WandB run name (within the defined project)]`
18
   11 11 11
20
  import numpy as np
21
  from gymnasium import Wrapper, spaces
  from argparse import ArgumentParser
23
  from ray import tune
  from ray.rllib.core.rl_module.rl_module import SingleAgentRLModuleSpec
  from ray.rllib.core.rl_module.marl_module import MultiAgentRLModuleSpec
  from ray.rllib.env.wrappers.pettingzoo_env import ParallelPettingZooEnv
  from ray.rllib.utils.test utils import (add rllib example script args,
29
                                            run_rllib_example_script_experiment)
  from ray.tune.registry import get_trainable_cls, register_env
31
  import multi_lander
33
35
  parser = add_rllib_example_script_args(
       ArgumentParser(conflict_handler='resolve'), # Resolve for num_agents
37
       default_reward=600.0,
       default_iters=500, #100, #200
39
       default_timesteps=1000000, #10000, #100000
  )
41
  parser.add_argument(
42
       "--control",
43
       type=str,
44
       choices=["Baseline", "SA", "NoPS", "FuPS"],
       default="Baseline",
       help="The controller method."
47
       "'Baseline': Original Lunar Lander with single agent and lander"
48
       "`SA`: A single agent controls all of the landers."
       "'NoPS': No parameter sharing between the agents."
50
       "'FuPS': Full parameter sharing between the agents.",
  )
52
  parser.add_argument(
53
       "--SA", action="store_true",
54
       help="`SA`: Creates a single agent for controlling all of the agents.",
55
  )
56
  parser.add_argument(
57
       "--NoPS", action="store_true",
```

```
help="'NoPS': No parameter sharing between the agents.",
59
   )
   parser.add_argument(
61
       "--FuPS", action="store_true",
62
       help="`FuPS`: Full parameter sharing between the agents.",
63
64
   parser.add_argument(
65
       "--num-agents", type=int, default=2,
       help="The number of agents",
68
   parser.add_argument(
69
       "--sweep", action="store_true",
70
       help="Perform a parameter sweep instead of using tune",
71
72
73
74
   class CustomWrapper(ParallelPettingZooEnv):
75
       """Wraps a Parallel Petting Zoo Environment for RLlib
76
       This wrapper is necessary to interface with rllib's workers.
       There is a problem caused when the one agent terminates before
       the other, which seems to pass inconsistent length episode
80
       trajectories to the rollout worker(s).
81
       It also adds the necessary `__all__` key to the done dictionaries.
       11 11 11
       def step(self, action_dict) -> tuple:
           obs, rew, terminateds, truncateds, info = self.par_env.step(action_dict)
           active = [a_id for a_id, term in terminateds.items() if term==False]
           obs_s = {a_id: obs.get(a_id) for a_id in active}
           rew_s = {a_id: rew.get(a_id) for a_id in active}
           terminateds = {a_id: terminateds.get(a_id) for a_id in active}
           truncateds = {a_id: truncateds.get(a_id) for a_id in active}
           terminateds["__all__"] = all(terminateds.values())
95
           truncateds["__all__"] = all(truncateds.values())
           return obs_s, rew_s, terminateds, truncateds, info
   # Registry is necessary for functional passing later.
99
   register_env("ma-lander", lambda : CustomWrapper(multi_lander.Parallel_Env()))
100
101
102
   class SingleAgentWrapper(Wrapper):
103
       """Wraps a parallel multi-agent environment for single-agent control.
104
105
        *It is currently limited to agents with discrete action spaces and
106
       box observation spaces with identical lengths.
107
108
       This will wrap environments with an arbitrary number of agents,
       however, the action space scales exponentially by the number of
110
       agents and is likely to be the limiting factor for performance.
       11 11 11
112
       def __init__(self, *args):
113
           super().__init__(*args)
114
           # Concat all action spaces into a single action space
115
           self.action_space = spaces.Discrete(np.prod())
116
                                 [list(self.env.action_spaces.values())[i].n
117
                                 for i in range(len(self.env.observation_spaces))]))
118
```

```
self._act_n = list(self.env.action_spaces.values())[0].n
119
            # Concat all obs spaces into a single obs space
            low, high = [],[]
121
            for i in range(len(self.env.observation_spaces)):
122
                low.extend(list(self.env.observation_spaces.values())[i].low)
123
                high.extend(list(self.env.observation_spaces.values())[i].high)
124
            self.observation_space = spaces.Box(np.array(low), np.array(high))
125
126
       def observe(self) -> tuple:
            # Concat all obs values into a single obs tuple
128
            #return sum(self.env.observe().values(),[]) # By monoid
129
            return np.array(list(self.env.observe().values())).flatten()
130
131
       def observation(self) -> tuple:
132
            return self.observe()
133
134
       def reset(self,*, seed:int | None=None, options:dict | None=None) -> tuple:
            self.env.reset(seed=seed, options=options)
136
            return self.observe(), {}
138
       def step(self, action:int) -> tuple:
            action\_list = \{a: int(action/(self.\_act\_n^{**}i))\%self.\_act\_n
140
                             for i,a in enumerate(self.agents)}
141
            obss, rews, terminations, _, _ = self.env.step(action_list)
142
            obs = self.observe()
143
            # Calculate reward, but drop terminated agent, else get exploding values
144
            reward = sum(np.array(rews.values()) *
145
                          np.invert(list(terminations.values())))
            term = (self.env.game_over or all(terminations.values()))
147
            if (term or np.any(obs < self.observation_space.low) or</pre>
148
                         np.any(obs > self.observation_space.high)):
149
                term = True
                obs = np.clip(obs, self.observation_space.low,
151
                               self.observation_space.high)
152
            return obs, reward, term, False, {}
153
   # Registry is necessary for functional passing later.
155
   register_env("sa-lander",
156
       lambda _: SingleAgentWrapper(multi_lander.Parallel_Env()))
157
158
159
   if name == " main ":
160
       args = parser.parse_args()
161
162
       # Shared config settings for all experiments
163
       base_config = (
164
            get_trainable_cls("DQN")
165
            .get default config()
166
            .framework('torch')
167
       )
168
       # Set config for experiment if using Single Agent Control
170
       if args.control == 'NoPS' or args.SA:
171
            config = (
172
                base_config
                .environment(
174
                     "sa-lander",
175
                     env_config={"num_landers": args.num_agents}
176
                )
177
            )
178
```

```
# Set config for experiment if using No-Parameter Sharing
elif args.control == 'NoPS' or args.NoPS:
    policies = {"lander_" + str(i) for i in range(args.num_agents)}
    config = (
        base_config
        .multi_agent(
            policies=policies, # 1:1 map from AgentID to ModuleID.
            policy_mapping_fn=(lambda aid, *args, **kwargs: aid),
        )
        .rl_module(
            rl_module_spec=MultiAgentRLModuleSpec(
               module_specs={p:SingleAgentRLModuleSpec() for p in policies},
            ),
        )
        .environment(
            "ma-lander",
            env_config={"num_landers": args.num_agents}
    )
# Set config for experiment if using Full-Parameter Sharing
elif args.control == 'FuPS' or args.FuPS:
    config = (
        base_config
        .multi_agent(
            policies={"p0"}, # All agents map to the same policy.
            policy_mapping_fn=(lambda aid, *args, **kwargs: "p0"),
        )
        .rl_module(
            rl_module_spec=MultiAgentRLModuleSpec(
                module_specs={"p0": SingleAgentRLModuleSpec()},
            ),
        )
        .environment(
            "ma-lander"
            env_config={"num_landers": args.num_agents}
        )
# Default, original lunar lander with one agent and lander
else:
    config = (
    base_config
    .environment(
        # env="lunar-lander"
        "ma-lander"
        env_config={"num_landers": 1}
    )
)
# Parameter sweep settings
if args.sweep:
    param_space = {
        "adam_epsilon": tune.loguniform(1e-4, 1e-10), # 1e-8
        "sigma0": tune.randn(0.5, 0.2), # 0.5
        "n_step": tune.choice([2^{**}i \text{ for } i \text{ in } range(5)]), # 1
        # Update the target by \t * policy + (1-\t au) * target_policy.
        "tau": tune.uniform(0.0,1.0), # 1.0,
        \#epsilon = [(0, 1.0), (10000, 0.05)]
                                                 [(step, epsilon), ...]
        # -> 1.0 at beginning, decreases to 0.05 over 10k steps
    config = config.training(**param_space)
```

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```
# Use Param sweep, not tune
#args.no_tune = True

# Call experiment runner
run_rllib_example_script_experiment(config, args)
```

# **B** Multi-Agent Lunar Lander

```
import math
  from typing import TYPE_CHECKING, Optional
  import numpy as np
  import gymnasium as gym
  from gymnasium import spaces, logger
  from gymnasium.error import DependencyNotInstalled
  from gymnasium.utils import EzPickle
  from pettingzoo import AECEnv
  from pettingzoo.utils import agent_selector
12
  try:
13
       import Box2D
14
       from Box2D.b2 import (
15
           circleShape,
16
           contactListener,
           edgeShape,
           fixtureDef,
           polygonShape,
           revoluteJointDef,
21
       )
   except ImportError as e:
23
       raise DependencyNotInstalled(
           'Box2D is not installed, you can install it by run `pip install swig` '
25
           + 'followed by `pip install "gymnasium[box2d]"`'
       ) from e
27
  if TYPE_CHECKING:
29
       import pygame
31
  FPS = 50
  SCALE = 30.0 # affects how fast the game is, forces should be adjusted as well
  MAIN\_ENGINE\_POWER = 13.0
  SIDE\_ENGINE\_POWER = 0.6
35
  INITIAL_RANDOM = 1000.0 # Set 1500 to make game harder
37
  LANDER_POLY = [(-14, +17), (-17, 0), (-17, -10), (+17, -10), (+17, 0), (+14, +17)]
  LEG_AWAY = 20
  LEG_DOWN = 18
  LEG_W, LEG_H = 2, 8
  LEG_SPRING_TORQUE = 40
  SIDE ENGINE HEIGHT = 14
  SIDE\_ENGINE\_AWAY = 12
  MAIN_ENGINE_Y_LOCATION = 4 # The Y loc of the main engine on the lander body.
  VIEWPORT_W = 600
  VIEWPORT_H = 400
50
51
  class ContactDetector(contactListener):
53
       def __init__(self, env):
54
           contactListener.__init__(self)
55
           self.env = env
       def BeginContact(self, contact):
```

```
for lander in self.env.landers:
59
                if (
                    lander == contact.fixtureA.body
61
                    or lander == contact.fixtureB.body
                ):
                    self.env.game_over = True
           for leg in self.env.legs:
                if leg in [contact.fixtureA.body, contact.fixtureB.body]:
                    leg.ground_contact = True
       def EndContact(self, contact):
            for leg in self.env.legs:
                if leg in [contact.fixtureA.body, contact.fixtureB.body]:
                    leg.ground_contact = False
72
73
74
   class SequentialEnv(AECEnv, EzPickle):
       r"""
76
       This is a rewrite of the Farama foundation Lunar Lander environment from:
           https://gymnasium.farama.org/environments/box2d/lunar_lander/
       Adapted for a AEC type petting zoo environment.
       The action space and physics remain the same.
80
       metadata = {
            "render_modes": ["human", "rgb_array"],
            "name": "multi_lander_v0",
            "is_parallelizable": True,
            "render_fps": FPS,
       }
       def init (
                self,
                render_mode: Optional[str] = None,
                continuous: bool = False,
                gravity: float = -10.0,
                enable_wind: bool = False,
                wind_power: float = 15.0,
95
                turbulence_power: float = 1.5,
                num_landers: int = 2,
                *args, **kwargs
       ):
           EzPickle.__init__(
100
                self,
                render_mode,
102
                continuous,
103
                gravity,
104
                enable_wind,
                wind power,
106
                turbulence_power,
107
                *args, **kwargs
108
            )
           AECEnv.__init__(self)
110
           self.render mode = render mode
           self.np_random = np.random
112
            # Value Checkers
114
            assert (-12.0 < gravity and gravity < 0.0
115
                ), f"gravity (current value: {gravity}) must be between -12 and 0"
116
           self.gravity = gravity
117
```

```
if 0.0 > wind_power or wind_power > 20.0:
    logger.warn(
        "wind_power value is recommended to be between 0.0 and 20.0, " +
        f"(current value: {wind_power})"
    )
self.wind_power = wind_power
if 0.0 > turbulence power or turbulence power > 2.0:
    logger.warn(
        "turbulence power value is recommended to be between 0.0 and " +
        f"2.0, (current value: {turbulence_power})"
    )
# These are bounds for position realistically the environment
# should have ended long before we reach more than 50% outside
low = np.array(
    -2.5, -2.5,
                                # x,y coordinates
        -10.0, -10.0,
                                # x,y velocity bounds is 5x rated speed
        -2 * math.pi, -10.0,
                                # Angle, Angular Velocity
        -0.0, -0.0,
                                # L,R Leg not on ground
    ]).astype(np.float32)
high = np.array(
    2.5, 5.0, # 2.5,
                                # x, y coordinates
        10.0, 10.0,
                                # x,y velocity bounds is 5x rated speed
        2 * math.pi, 10.0,
                                # Angle, Angular Velocity
        1.0, 1.0,
                                # L,R Leg on ground
    ]).astype(np.float32)
# Environmental Variables
self.turbulence power = turbulence power
self.enable_wind = enable_wind
self.screen: pygame.Surface = None
self.clock = None
self.isopen = True
self.world = Box2D.b2World(gravity=(0, gravity))
self.moon = None
self.particles = []
self.landers = []
self.legs = []
self.prev_reward = None
self.continuous = continuous
# Agents
self.possible_agents = ["lander_" + str(i) for i in range(num_landers)]
self.agents = self.possible_agents[:]
self.agent_name_mapping = dict(zip(self.agents,
                                   list(range(self.num agents))))
self._agent_selector = agent_selector(self.agents)
# Spaces
self.observation_spaces = dict(zip(self.agents,
                            [spaces.Box(low, high)]*self.num_agents))
if self.continuous:
    # Action is two floats [main engine, left-right engines].
    # Main engine: -1..0 off, 0..+1 throttle from 50% to 100% power.
    #
                    Engine can't work with less than 50% power.
    # Left-right:
                   -1.0..-0.5 fire left engine, +0.5..+1.0 fire right
    #
                    engine, -0.5..0.5 off
    self._action_space = spaces.Box(-1, +1, (2,), dtype=np.float32)
```

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```
else:
        # No-op, fire left engine, main engine, right engine
        self._action_space = spaces.Discrete(4)
    self.action_spaces = dict(zip(self.agents,
                                   [self._action_space]*self.num_agents))
def observation_space(self, agent):
    return self.observation_spaces[agent]
def action_space(self, agent):
    return self.action_spaces[agent]
def convert_to_dict(self, list_of_list):
    return dict(zip(self.agents, list of list))
def close(self):
    if self.screen is not None:
        import pygame
        pygame.display.quit()
        pygame.quit()
        pygame.QUIT
        self.isopen = False
def create_landers(self):
    landers = []
    for n in range(self.num_agents):
        lander: Box2D.b2Body = self.world.CreateDynamicBody(
            position=((n+1)/(self.num_agents+1) * VIEWPORT_W / SCALE,
                      VIEWPORT_H / SCALE),
            angle=0.0,
            fixtures=fixtureDef(
                shape=polygonShape(
                    vertices=[(x/SCALE, y/SCALE) for x, y in LANDER_POLY]),
                density=5.0,
                friction=0.1,
                categoryBits=0x0010,
                \#maskBits=0x001.
                                  # uncomment for : collide only with ground
                restitution=0.0,
            ),
                # 0.99 bouncy
        )
        lander.color1 = ((128), (102+75*(n))\%255, (230))
        lander.color2 = ((77), (77), (128))
        landers.append(lander)
    self.landers = landers
    legs = []
    for n,lander in enumerate(self.landers):
        for i in [-1, +1]:
            leg = self.world.CreateDynamicBody(
                position=(lander.position[0] - i * LEG_AWAY / SCALE,
                          lander.position[1]),
                angle=(i * 0.05),
                fixtures=fixtureDef(
                    shape=polygonShape(box=(LEG_W / SCALE, LEG_H / SCALE)),
                    density=1.0,
                    restitution=0.0,
                    categoryBits=0x0020,
                    \#maskBits=0x001,
                ),
            )
```

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```
leg.ground_contact = False
239
                     leg.color1 = ((128), (102+75*(n))\%255, (230))
                     leg.color2 = ((77), (77), (128))
241
                     rjd = revoluteJointDef(
242
                         bodyA=lander,
243
                         bodyB=leg,
244
                         localAnchorA=(0, 0),
245
                         localAnchorB=(i * LEG_AWAY / SCALE, LEG_DOWN / SCALE),
246
                         enableMotor=True,
                         enableLimit=True,
248
                         maxMotorTorque=LEG_SPRING_TORQUE,
249
                         motorSpeed=+0.3 * i, # low enough not to jump into the sky
250
                     )
251
                     if i == -1:
252
                         rjd.lowerAngle = (
253
                             +0.9 - 0.5
254
                         ) # Valid angle of travel for the legs
                         rjd.upperAngle = +0.9
256
                     else:
                         rjd.lowerAngle = -0.9
258
                         rjd.upperAngle = -0.9 + 0.5
                     leg.joint = self.world.CreateJoint(rjd)
260
                     legs.append(leg)
261
            self.legs = legs
263
       def _create_particle(self, mass, x, y, ttl):
264
            p = self.world.CreateDynamicBody(
265
                position=(x, y),
                angle=0.0,
267
                fixtures=fixtureDef(
268
                     shape=circleShape(radius=2 / SCALE, pos=(0, 0)),
269
                     density=mass,
                     friction=0.1,
271
                     categoryBits=0x0100,
                    maskBits=0x001, # collide only with ground
273
                     restitution=0.3,
                ),
275
            )
            p.tt1 = tt1
277
            self.particles.append(p)
            self._clean_particles(False)
279
            return p
       def _clean_particles(self, all_particle):
282
            while self.particles and (all_particle or self.particles[0].ttl < 0):
283
                self.world.DestroyBody(self.particles.pop(0))
284
       def render(self):
287
            if self.render mode is None:
288
                assert self.spec is not None
                gym.logger.warn(
290
                     "You are calling render method without specifying render mode."
                     "You can specify the render mode at initialization, "
292
                     f'e.g. gym.make("{self.spec.id}", render_mode="rgb_array")')
                return
294
            try:
                import pygame
                from pygame import gfxdraw
298
```

```
except ImportError as e:
    raise DependencyNotInstalled(
        'pygame is not installed, run `pip install "gymnasium[box2d]"`'
    ) from e
if self.screen is None and self.render_mode == "human":
    pygame.init()
    pygame.display.init()
    self.screen = pygame.display.set_mode((VIEWPORT_W, VIEWPORT_H))
if self.clock is None:
    self.clock = pygame.time.Clock()
self.surf = pygame.Surface((VIEWPORT_W, VIEWPORT_H))
pygame.transform.scale(self.surf, (SCALE, SCALE))
pygame.draw.rect(self.surf, (255, 255, 255), self.surf.get_rect())
for obj in self.particles:
    obj.ttl = 0.15
    obj.color1 = (
        int(max(0.2, 0.15 + obj.ttl) * 255),
        int(max(0.2, 0.5 * obj.ttl) * 255),
        int(max(0.2, 0.5 * obj.tt1) * 255),
    )
    obj.color2 = (
        int(max(0.2, 0.15 + obj.tt1) * 255),
        int(max(0.2, 0.5 * obj.tt1) * 255),
        int(max(0.2, 0.5 * obj.tt1) * 255),
    )
self._clean_particles(False)
for p in self.sky_polys:
    scaled_poly = []
    for coord in p:
        scaled_poly.append((coord[0] * SCALE, coord[1] * SCALE))
    pygame.draw.polygon(self.surf, (0, 0, 0), scaled_poly)
    gfxdraw.aapolygon(self.surf, scaled_poly, (0, 0, 0))
for obj in self.particles + self.drawlist:
    for f in obj.fixtures:
        trans = f.body.transform
        if type(f.shape) is circleShape:
            pygame.draw.circle(
                self.surf,
                color=obj.color1,
                center=trans * f.shape.pos * SCALE,
                radius=f.shape.radius * SCALE,
            pygame.draw.circle(
                self.surf,
                color=obj.color2,
                center=trans * f.shape.pos * SCALE,
                radius=f.shape.radius * SCALE,
            )
        else:
            path = [trans * v * SCALE for v in f.shape.vertices]
            pygame.draw.polygon(self.surf,color=obj.color1,points=path)
            gfxdraw.aapolygon(self.surf, path, obj.color1)
            pygame.draw.aalines(
                self.surf, color=obj.color2, points=path, closed=True)
```

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```
359
                     for x in [self.helipad_x1, self.helipad_x2]:
                         x = x * SCALE
361
                         flagy1 = self.helipad_y * SCALE
362
                         flagy2 = flagy1 + 50
363
                         pygame.draw.line(
364
                              self.surf,
365
                              color=(255, 255, 255),
366
                              start_pos=(x, flagy1),
                              end_pos=(x, flagy2),
368
                              width=1,
369
                         )
370
                         pygame.draw.polygon(
371
                              self.surf,
372
                              color=(204, 204, 0),
373
                              points=[
374
                                  (x, flagy2),
                                  (x, flagy2 - 10),
376
                                  (x + 25, flagy2 - 5),
                              ],
378
                         )
                         gfxdraw.aapolygon(
380
                              self.surf,
381
                              [(x, flagy2), (x, flagy2 - 10), (x + 25, flagy2 - 5)],
382
                              (204, 204, 0),
383
                         )
384
385
            self.surf = pygame.transform.flip(self.surf, False, True)
387
            if self.render_mode == "human":
388
                assert self.screen is not None
389
                self.screen.blit(self.surf, (0, 0))
                pygame.event.pump()
391
                self.clock.tick(self.metadata["render_fps"])
                pygame.display.flip()
393
            elif self.render_mode == "rgb_array":
                return np.transpose(
395
                     np.array(pygame.surfarray.pixels3d(self.surf)), axes=(1, 0, 2)
                )
        # End Render()
399
        def _destroy(self):
            if not self.moon:
                return
402
            self.world.contactListener = None
403
            self._clean_particles(True)
404
            self.world.DestroyBody(self.moon)
            self.moon = None
406
            for lander in self.landers:
407
                self.world.DestroyBody(lander)
408
                lander = None
            for i in range(len(self.legs)):
410
                self.world.DestroyBody(self.legs[i])
412
        def reset(self,*,seed: Optional[int] = None,options: Optional[dict] = None):
414
415
            self._destroy()
            # Issue: https://github.com/Farama-Foundation/Gymnasium/issues/728
416
            # self._destroy() is not enough to clean(reset), workaround is
417
            # to create a totally new world for self.reset()
418
```

```
self.world = Box2D.b2World(gravity=(0, self.gravity))
self.world.contactListener_keepref = ContactDetector(self)
self.world.contactListener = self.world.contactListener_keepref
self.game over = False
self.prev_shaping = [None]*self.num_agents
W = VIEWPORT_W / SCALE
H = VIEWPORT_H / SCALE
# Create Terrain
CHUNKS = 11
height = self.np_random.uniform(0, H / 2, size=(CHUNKS + 1,))
chunk_x = [W / (CHUNKS - 1) * i for i in range(CHUNKS)]
self.helipad_x1 = chunk_x[CHUNKS // 2 - 1]
self.helipad_x2 = chunk_x[CHUNKS // 2 + 1]
self.helipad_y = H / 4
height[CHUNKS // 2 - 2] = self.helipad_y
height[CHUNKS // 2 - 1] = self.helipad_y
height[CHUNKS // 2 + 0] = self.helipad_y
height[CHUNKS // 2 + 1] = self.helipad_y
height[CHUNKS // 2 + 2] = self.helipad_y
smooth_y = [
    0.33 * (height[i - 1] + height[i + 0] + height[i + 1])
    for i in range(CHUNKS)
]
self.moon = self.world.CreateStaticBody(
    shapes=edgeShape(vertices=[(0, 0), (W, 0)])
self.sky_polys = []
for i in range(CHUNKS - 1):
    p1 = (chunk_x[i], smooth_y[i])
    p2 = (chunk_x[i + 1], smooth_y[i + 1])
    self.moon.CreateEdgeFixture(vertices=[p1,p2],density=0,friction=0.1)
    self.sky_polys.append([p1, p2, (p2[0], H), (p1[0], H)])
self.moon.color1 = (0.0, 0.0, 0.0)
self.moon.color2 = (0.0, 0.0, 0.0)
if self.enable_wind: # Initialize wind pattern based on index
    self.wind_idx = self.np_random.integers(-9999, 9999)
    self.torque_idx = self.np_random.integers(-9999, 9999)
self.create_landers()
for lander in self.landers:
    lander.ApplyForceToCenter(
    (
        self.np_random.uniform(-INITIAL_RANDOM, INITIAL_RANDOM),
        self.np_random.uniform(-INITIAL_RANDOM, INITIAL_RANDOM),
    ),
    True,
)
self.drawlist = self.legs + self.landers
if self.render_mode == "human": self.render()
self.agents = self.possible_agents[:]
self._agent_selector = agent_selector(self.agents)
self.agent_selection = self._agent_selector.next()
self.rewards = {agent: 0 for agent in self.agents}
```

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```
self._cumulative_rewards = {agent: 0 for agent in self.agents}
    self.terminations = {agent: False for agent in self.agents}
    self.truncations = {agent: False for agent in self.agents}
    self.infos = {agent: {} for agent in self.agents}
    return self.observe(), None
# End reset()
def observe(self, agent=None):
    if not agent : agent = self.agent_selection
    id = self.agent_name_mapping[agent]
    lander = self.landers[id]
    pos = lander.position
    vel = lander.linearVelocity
    observation = [
        (pos.x - VIEWPORT_W/SCALE/2) / (VIEWPORT_W/SCALE/2),
        (pos.y - (self.helipad_y + LEG_DOWN/SCALE)) / (VIEWPORT_H/SCALE/2),
        vel.x * (VIEWPORT_W/SCALE/2) / FPS,
        vel.y * (VIEWPORT_H/SCALE/2) / FPS,
        lander.angle,
        20.0 * lander.angularVelocity / FPS,
        1.0 if self.legs[id*2+0].ground_contact else 0.0,
        1.0 if self.legs[id*2+1].ground_contact else 0.0,
    assert len(observation) == 8
    return observation
def latest_reward_state(self, agent, state):
    reward = 0
    id = self.agent_name_mapping[agent]
    shaping = (
        -100 * np.sqrt(state[0] * state[0] + state[1] * state[1])
        - 100 * np.sqrt(state[2] * state[2] + state[3] * state[3])
        - 100 * abs(state[4])
        + 10 * state[6] + 10 * state[7]
        # And ten points for legs contact, the idea is if you
        # lose contact again after landing, you get negative reward
    if self.prev_shaping[id] is not None:
        reward = shaping - self.prev_shaping[id]
    self.prev_shaping[id] = shaping
    return reward
def step(self, action):
    assert self.landers is not None, "You forgot to call reset()"
    if (
        self.terminations[self.agent_selection]
        or self.truncations[self.agent_selection]
    ):
        # If one agent has terminated this accepts a None action,
        # which otherwise errors, handles stepping to the next agent
        obs = self.observe(self.agent selection)
        self.agent_selection = self._agent_selector.next()
        return obs, 0, True, False, {}
    # Update wind and apply to the lander
    if self.enable wind and not any([1.ground_contact for 1 in self.legs]):
        # the function used for wind is tanh(sin(2 k x) + sin(pi k x)),
```

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```
# which is proven to never be periodic, k = 0.01
539
                wind mag = (
                    math.tanh(
541
                         math.sin(0.02 * self.wind_idx)
542
                         + (math.sin(math.pi * 0.01 * self.wind_idx))
543
                     ) * self.wind_power
544
                )
545
                self.wind_idx += 1
546
                for lander in self.landers:
548
                     lander.ApplyForceToCenter(
549
                         (wind_mag, 0.0),
550
                         True,
551
                     )
552
553
                # the function used for torque is tanh(sin(2 k x) + sin(pi k x)),
554
                # which is proven to never be periodic, k = 0.01
                torque_mag = (
556
                    math.tanh(
                         math.sin(0.02 * self.torque_idx)
558
                         + (math.sin(math.pi * 0.01 * self.torque_idx))
                     ) * self.turbulence_power
560
                )
561
                self.torque_idx += 1
563
                for lander in self.landers:
564
                     lander.ApplyTorque(
565
                         torque_mag,
                         True,
567
                     )
568
569
            # For current agent:
            agent = self.agent selection
571
            lander = self.landers[self.agent_name_mapping[agent]]
            # Check action validity
573
            if self.continuous:
                action = np.clip(action, -1, +1).astype(np.float64)
575
            else:
                assert self.action_spaces[agent].contains(
577
                     action), f"{action!r} ({type(action)}) invalid "
579
            # Tip is the (X and Y) components of the rotation of the lander.
            tip = (math.sin(lander.angle), math.cos(lander.angle))
582
            # Side is the (-Y and X) components of the rotation of the lander.
583
            side = (-tip[1], tip[0])
584
            # Generate two random numbers between -1/SCALE and 1/SCALE.
586
            dispersion = [self.np_random.uniform(-1.0,+1.0)/SCALE for _ in range(2)]
587
588
            m_power = 0.0
            if (self.continuous and action[0] > 0.0) or (
590
                not self.continuous and action == 2
            ):
592
                # Main engine
                if self.continuous:
594
                    m_power = (np.clip(action[0], 0.0, 1.0) + 1.0) * 0.5 # 0.5.1.0
                     assert m_power >= 0.5 and m_power <= 1.0
596
                else:
597
                    m_power = 1.0
598
```

```
# 4 is move a bit downwards, +-2 for randomness
    # The components of the impulse to be applied by the main engine.
    ox = (
        tip[0] * (MAIN_ENGINE_Y_LOCATION / SCALE + 2 * dispersion[0])
        + side[0] * dispersion[1]
    )
    oy = (
        -tip[1] * (MAIN_ENGINE_Y_LOCATION / SCALE + 2 * dispersion[0])
        - side[1] * dispersion[1]
    impulse_pos = (lander.position[0] + ox, lander.position[1] + oy)
    if self.render_mode is not None:
        # particles are just a decoration, with no physics impact,
        # so don't add them when not rendering
        p = self._create_particle(
            3.5, # 3.5 is here to make particle speed adequate
            impulse_pos[0],
            impulse_pos[1],
            m_power,
        )
        p.ApplyLinearImpulse(
                ox * MAIN ENGINE POWER * m power,
                oy * MAIN_ENGINE_POWER * m_power,
            impulse_pos,
            True,
    lander.ApplyLinearImpulse(
        (-ox * MAIN ENGINE POWER * m power,
         -oy * MAIN_ENGINE_POWER * m_power),
        impulse_pos,
        True,
    )
s_power = 0.0
if (self.continuous and np.abs(action[1]) > 0.5) or (
    not self.continuous and action in [1, 3]
):
    # Orientation/Side engines
    if self.continuous:
        direction = np.sign(action[1])
        s_power = np.clip(np.abs(action[1]), 0.5, 1.0)
        assert s_power >= 0.5 and s_power <= 1.0
    else:
        # action = 1 is left, action = 3 is right
        direction = action - 2
        s_power = 1.0
    # The components of the impulse to be applied by the side engines.
    ox = tip[0] * dispersion[0] + side[0] * (
        3 * dispersion[1] + direction * SIDE_ENGINE_AWAY / SCALE
    )
    oy = -tip[1] * dispersion[0] - side[1] * (
        3 * dispersion[1] + direction * SIDE_ENGINE_AWAY / SCALE
    )
    # The constant 17 is presumably meant to be SIDE ENGINE HEIGHT.
    # However, SIDE_ENGINE_HEIGHT is defined as 14, causing the
```

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```
# position of the thrust on the body of the lander to change,
659
                # depending on the orientation of the lander. This results in
                # an orientation dependent torque being applied to the lander.
661
662
                impulse_pos = (
663
                     lander.position[0] + ox - tip[0] * 17 / SCALE,
664
                     lander.position[1] + oy + tip[1] * SIDE_ENGINE_HEIGHT / SCALE,
665
666
                if self.render_mode is not None:
                     # particles are just decoration, with no impact on the physics,
668
                     # so don't add them when not rendering
669
                    p = self._create_particle(0.7, impulse_pos[0],
670
                                                 impulse_pos[1], s_power)
                     p.ApplyLinearImpulse(
672
                         (ox * SIDE_ENGINE_POWER * s_power,
673
                          oy * SIDE_ENGINE_POWER * s_power,),
674
                         impulse_pos,
                         True,
676
                     )
                lander.ApplyLinearImpulse(
678
                     (-ox '
                           * SIDE_ENGINE_POWER * s_power,
                      -oy * SIDE_ENGINE_POWER * s_power),
680
                     impulse_pos,
681
                     True,
                )
683
684
            # Update Positions
685
            self.world.Step(1.0 / FPS, 6 * 30, 2 * 30)
687
            observation = self.observe(agent)
688
            reward = self.latest reward state(agent, observation)
689
            reward -= m_power * 0.30 # Deduct cost of fuel
            reward -= s_power * 0.03 # Deduct cost of fuel
691
            if self.game_over or abs(observation[0]) >= 1.0:
693
                self.terminations[self.agent_selection] = True
                reward = -100
695
            if not lander.awake:
                self.terminations[self.agent_selection] = True
                reward = +100
            terminated = self.terminations[self.agent_selection]
699
700
            self.rewards[agent] = reward
701
            self._accumulate_rewards()
702
703
            self.agent_selection = self._agent_selector.next()
704
            if self.render mode == "human":
706
                self.render()
707
            # truncation=False as the time limit is handled by the `TimeLimit`
708
            return observation, reward, terminated, False, {}
710
711
   class Parallel Env(SequentialEnv):
712
       def observe(self):
713
            obs_list = []
714
            for i, lander in enumerate(self.landers):
715
                pos = lander.position
716
                vel = lander.linearVelocity
717
                obs = [
718
```

```
(pos.x - VIEWPORT_W/SCALE/2) / (VIEWPORT_W/SCALE/2),
            (pos.y - (self.helipad_y + LEG_DOWN/SCALE)) / (VIEWPORT_H/SCALE/2),
            vel.x *
                    (VIEWPORT_W/SCALE/2) / FPS,
            vel.y * (VIEWPORT_H/SCALE/2) / FPS,
            lander.angle,
            20.0 * lander.angularVelocity / FPS,
            1.0 if self.legs[i*2+0].ground_contact else 0.0,
            1.0 if self.legs[i*2+1].ground_contact else 0.0,
        ]
        assert len(obs) == 8
        obs_list.append(obs)
    return dict(zip(self.possible_agents,obs_list))
def last(self):
   return self.observe()
def step(self, action_list):
    self._clear_rewards()
    assert self.landers is not None, "You forgot to call reset()"
    # Update wind and apply to the lander
    if self.enable_wind and not any([1.ground_contact for 1 in self.legs]):
        # the function used for wind is tanh(sin(2 k x) + sin(pi k x)),
        # which is proven to never be periodic, k = 0.01
        wind_mag = (
            math.tanh(
                math.sin(0.02 * self.wind_idx)
                + (math.sin(math.pi * 0.01 * self.wind_idx))
            ) * self.wind_power
        )
        self.wind idx += 1
        for lander in self.landers:
            lander.ApplyForceToCenter(
                (wind_mag, 0.0),
                True,
        # the function used for torque is tanh(sin(2 k x) + sin(pi k x)),
        # which is proven to never be periodic, k = 0.01
        torque_mag = (
            math.tanh(
                math.sin(0.02 * self.torque_idx)
                + (math.sin(math.pi * 0.01 * self.torque_idx))
            ) * self.turbulence_power
        )
        self.torque_idx += 1
        for lander in self.landers:
            lander.ApplyTorque(
                torque_mag,
                True,
            )
    #for agent in self.agents:
    for agent, action in action_list.items():
        # For current agent:
        lander = self.landers[self.agent_name_mapping[agent]]
        # Check action validity
        if self.continuous:
            action = np.clip(action, -1, +1).astype(np.float64)
```

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```
else:
    assert self.action_spaces[agent].contains(
        action), f"{action!r} ({type(action)}) invalid "
# Tip is the (X and Y) components of the rotation of the lander.
tip = (math.sin(lander.angle), math.cos(lander.angle))
# Side is the (-Y and X) components of the rotation of the lander.
side = (-tip[1], tip[0])
# Generate two random numbers between -1/SCALE and 1/SCALE.
dispersion = [self.np_random.uniform(-1.0,+1.0)/SCALE for _ in range(2)]
m power = 0.0
if (self.continuous and action[0] > 0.0) or (
    not self.continuous and action == 2
):
    # Main engine
    if self.continuous:
        m_power = (np.clip(action[0], 0.0, 1.0) + 1.0) * 0.5 # 0.5..1.0
        assert m_power >= 0.5 and m_power <= 1.0
    else:
        m_power = 1.0
    # 4 is move a bit downwards, +-2 for randomness
    # The components of the impulse to be applied by the main engine.
    ox = (
        tip[0] * (MAIN_ENGINE_Y_LOCATION / SCALE + 2 * dispersion[0])
        + side[0] * dispersion[1]
    )
    ov = (
        -tip[1] * (MAIN_ENGINE_Y_LOCATION / SCALE + 2 * dispersion[0])
        - side[1] * dispersion[1]
    impulse_pos = (lander.position[0] + ox, lander.position[1] + oy)
    if self.render mode is not None:
        # particles are just a decoration, with no physics impact,
        # so don't add them when not rendering
        p = self._create_particle(
            3.5, # 3.5 is here to make particle speed adequate
            impulse_pos[0],
            impulse_pos[1],
            m_power,
        )
        p.ApplyLinearImpulse(
                ox * MAIN_ENGINE_POWER * m_power,
                oy * MAIN_ENGINE_POWER * m_power,
            impulse_pos,
            True,
    lander.ApplyLinearImpulse(
        (-ox * MAIN ENGINE POWER * m power,
        -oy * MAIN ENGINE POWER * m power),
        impulse_pos,
        True,
    )
s_power = 0.0
```

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```
if (self.continuous and np.abs(action[1]) > 0.5) or (
        not self.continuous and action in [1, 3]
    ):
        # Orientation/Side engines
        if self.continuous:
            direction = np.sign(action[1])
            s_{power} = np.clip(np.abs(action[1]), 0.5, 1.0)
            assert s_power >= 0.5 and s_power <= 1.0
        else:
            # action = 1 is left, action = 3 is right
            direction = action - 2
            s_power = 1.0
        # The components of the impulse to be applied by the side engines.
        ox = tip[0] * dispersion[0] + side[0] * (
            3 * dispersion[1] + direction * SIDE_ENGINE_AWAY / SCALE
        )
        oy = -tip[1] * dispersion[0] - side[1] * (
            3 * dispersion[1] + direction * SIDE_ENGINE_AWAY / SCALE
        )
        # The constant 17 is presumably meant to be SIDE_ENGINE_HEIGHT.
        # However, SIDE_ENGINE_HEIGHT is defined as 14, causing the
        # position of the thrust on the body of the lander to change,
        # depending on the orientation of the lander. This results in
        # an orientation dependent torque being applied to the lander.
        impulse_pos = (
            lander.position[0] + ox - tip[0] * 17 / SCALE,
            lander.position[1] + oy + tip[1] * SIDE_ENGINE_HEIGHT / SCALE,
        if self.render_mode is not None:
            # particles are just decoration, with no impact on the physics,
            # so don't add them when not rendering
            p = self._create_particle(0.7, impulse_pos[0],
                                    impulse_pos[1], s_power)
            p.ApplyLinearImpulse(
                (ox * SIDE_ENGINE_POWER * s_power,
                oy * SIDE_ENGINE_POWER * s_power,),
                impulse_pos,
                True,
            )
        lander.ApplyLinearImpulse(
            (-ox * SIDE_ENGINE_POWER * s_power,
            -oy * SIDE_ENGINE_POWER * s_power),
            impulse_pos,
            True,
        self.rewards[agent] -= m_power * 0.30 # Deduct cost of fuel
        self.rewards[agent] -= s_power * 0.03 # Deduct cost of fuel
""" End Agent Loop """
# Update Positions
self.world.Step(1.0 / FPS, 6 * 30, 2 * 30)
obs_list = self.observe()
for agent in self.agents:
    obs = obs_list[agent]
    lander = self.landers[self.agent_name_mapping[agent]]
```

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```
self.rewards[agent] += self.latest_reward_state(agent, obs)
899
                if self.game_over or abs(obs[0]) >= 1.0:
                     self.terminations[agent] = True
901
                     self.rewards[agent] -= 100
902
                if not lander.awake:
903
                     self.terminations[agent] = True
                     self.rewards[agent] += 100
905
906
            self._accumulate_rewards()
908
            if self.render_mode == "human":
909
                self.render()
910
            # truncation=False as the time limit is handled by the `TimeLimit`
911
            return obs_list, self.rewards, self.terminations, self.truncations, {}
912
913
914
   def heuristic(env, s):
915
        11 11 11
916
        The heuristic for
        1. Testing
918
        2. Demonstration rollout.
920
        Args:
921
            env: The environment
922
            s (list): The state. Attributes:
923
                s[0] is the horizontal coordinate
924
                s[1] is the vertical coordinate
925
                s[2] is the horizontal speed
                s[3] is the vertical speed
927
                s[4] is the angle
928
                s[5] is the angular speed
929
                s[6] 1 if first leg has contact, else 0
                s[7] 1 if second leg has contact, else 0
931
932
        Returns:
933
             a: The heuristic to be fed into the step function defined above to
                determine the next step and reward.
935
        11 11 11
937
        angle_targ = s[0] * 0.5 + s[2] * 1.0 # angle should point towards center
        if angle_targ > 0.4:
939
            angle targ = 0.4 # more than 0.4 radians (22 degrees) is bad
940
        if angle_targ < -0.4:</pre>
941
            angle_targ = -0.4
942
        hover\_targ = 0.55 * np.abs(
943
944
           # target y should be proportional to horizontal offset
946
        angle_todo = (angle_targ - s[4]) * 0.5 - (s[5]) * 1.0
947
        hover\_todo = (hover\_targ - s[1]) * 0.5 - (s[3]) * 0.5
948
        if s[6] or s[7]: # legs have contact
950
            angle\_todo = 0
            hover_todo = (
952
                -(s[3]) * 0.5
               # override to reduce fall speed, that's all we need after contact
954
        if env.unwrapped.continuous:
956
            a = np.array([hover_todo * 20 - 1, -angle_todo * 20])
957
            a = np.clip(a, -1, +1)
958
```

```
else:
959
             \mathbf{a} = 0
             if hover todo > np.abs(angle todo) and hover todo > 0.05:
961
962
             elif angle_todo < -0.05:</pre>
963
                 a = 3
964
             elif angle_todo > +0.05:
965
                 a = 1
        return a
968
    def demo_heuristic_lander(env, reps=1, seed=None, render=False):
969
        total_reward = 0
970
        steps = 0
971
        for _ in range(reps):
972
            s = env.reset(seed=seed)
973
            while True:
974
                 s = env.last()[0]
                 a = heuristic(env, s)
976
                 s, r, terminated, truncated, info = env.step(a)
                 total reward += r
978
                 if render:
980
                     still_open = env.render()
981
                      if still_open is False:
                          break
984
                 if steps % 20 == 0 or terminated or truncated:
985
                     print("observations:", " ".join([f"\{x:+0.2f\}" for x in s]))
                     print(f"step {steps} total_reward {total_reward:+0.2f}")
987
                     print(env.terminations.values())
988
                 steps += 1
989
                 # if terminated or truncated:
                 if all(env.terminations.values()):
991
                     break
        if render:
993
             env.close()
        return total reward
995
    def demo_parallel_heuristic(env, reps=1, seed=None, render=False):
997
        total_reward = 0
        steps = 0
999
        for <u>in</u> range(reps):
1000
              = env.reset(seed=seed)
1001
             obs = env.last()
1002
             while True:
1003
                 actions = {agent: heuristic(env, obs[agent]) for agent in env.agents}
1004
                 obs, r, terminateds, truncateds, info = env.step(actions)
1005
                 total reward += sum(r.values())
1006
1007
                 if render:
1008
                      still_open = env.render()
                      if still_open is False:
1010
                          break
1012
                 if steps % 20 == 0 or all(terminateds) or all(truncateds):
                      for agent in env.agents:
1014
                          print(f"{agent} observations:", " ".join([f"{x:+0.2f}]" for x in obs[ag
1015
                     print(f"step {steps} total_reward {total_reward:+0.2f}")
1016
                     print(env.terminations.values())
1017
                 steps += 1
1018
```

```
# if terminated or truncated:
1019
                 if all(env.terminations.values()):
                     break
1021
        if render:
1022
            env.close()
1023
        return total_reward
1024
1025
    def parallel_env(**kwargs):
1026
        return Parallel_Env(**kwargs)
1027
1028
    def sequential_env(**kwargs):
1029
        return SequentialEnv(**kwargs)
1030
1031
    def env(**kwargs):
1032
        return Parallel_Env(**kwargs)
1033
1034
    if __name__ == "__main__":
1035
        import argparse
1036
        parser = argparse.ArgumentParser(description=
1037
                                             'A multi-agent version of Lunar Lander')
1038
        parser.add_argument('-s', '--sequential', action="store_true",
                              help='Iterate as AEC environment')
1040
        parser.add_argument('-n', '--num_landers', type=int, default=2,
1041
                              help='number of landers')
1042
        parser.add_argument('-d', '--demo_iters', type=int, default=1,
1043
                              help='number of landers')
1044
        args = parser.parse_args()
1045
        if args.sequential:
1047
             _env = sequential_env(render_mode="human", num_landers=args.num_landers)
1048
            demo heuristic lander( env, reps=args.demo iters, render=True)
1049
        else:
1050
             _env = parallel_env(render_mode="human", num_landers=args.num_landers)
1051
            demo_parallel_heuristic(_env, reps=args.demo_iters, render=True)
```

# **ANOVA Tables**

### **C.1** Baseline Lander

OLS	Regression	Results
-----	------------	---------

Dep. Variable: Model: Method: Date: Time: No. Observations: Df Residuals: Df Model:	Least Squ Mon, 22 Jul 22:3	2024 33:51 30 10	Adj. F-st Prob	uared: R-squared: atistic: (F-statistic) Likelihood:	:	0.966 0.902 15.12 5.46e-05 -131.47 302.9 331.0	
Covariance Type:	nonro				======		=======
	coef	std	err	t	P>   t	[0.025	0.975]
Intercept	70.1409	135.9	922	0.516	0.617	-232.712	372.994
tau	-5.201e+07	2.25e-	⊦07	-2.313	0.043	-1.02e+08	-1.9e+06
sigma	33.4494	24.0	068	1.390	0.195	-20.178	87.077
n_step	844.5087	373.8	352	2.259	0.047	11.515	1677.502
adam_eps	891.1404	278.9	946	3.195	0.010	269.611	1512.670
ep_len_mean	-0.0763	0.3	129	-0.589	0.569	-0.365	0.212
tau_pow_2	1020.8171	418.	234	2.441	0.035	88.934	1952.700
tau_sigma	2.216e+06	1.12e-	⊦06	1.981	0.076	-2.76e+05	4.71e+06
tau_n_step	1.156e+07	7.5e-		1.542	0.154	-5.15e+06	2.83e+07
tau_adam_eps	4.7e+07	2.06e-	⊦07	2.283	0.046	1.12e+06	9.29e+07
tau_ep_len_mean	3824.1099	8513.8		0.449	0.663	-1.51e+04	2.28e+04
sigma_pow_2	5.0039		93	4.580	0.001	2.569	7.438
sigma_n_step	-158.6486	39.8		-3.986	0.003	-247.337	-69.960
sigma_adam_eps	-66.9395	34.4		-1.945	0.080	-143.629	9.750
sigma_ep_len_mean	-0.0181		800	-2.187	0.054	-0.037	0.000
n_step_pow_2	-37.5373	228.9		-0.164	0.873	-547.650	472.576
n_step_adam_eps	-1089.7884	257.		-4.238	0.002	-1662.686	-516.891
n_step_ep_len_mean	-0.0624		116	-0.539	0.602	-0.320	0.195
adam_eps_pow_2	-123.4370	238.4		-0.518	0.616	-654.745	407.871
adam_eps_ep_len_mean			71	-0.740	0.476	-0.211	0.106
ep_len_mean_pow_2	3.182e-05	2.77e	-05	1.150	0.277	-2.98e-05	9.35e-05

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=======================================	=========		=========
Omnibus:	5.720	Durbin-Watson:	1.321
Prob(Omnibus):	0.057	Jarque-Bera (JB):	4.528
Skew:	-0.944	Prob(JB):	0.104
Kurtosis:	3.246	Cond. No.	6.21e+16
=======================================		=======================================	=========

#### Notes:

<sup>[1]</sup> Standard Errors assume that the covariance matrix of the errors is correctly specified. [2] The smallest eigenvalue is 8.67e-20. This might indicate that there are strong multicollinearity problems or that the design matrix is singular.

#### **C.2 Single-Agent Control**

OLS	Regression	Resul	lts
-----	------------	-------	-----

=======================================	=============		=========
Dep. Variable:	Score	R-squared:	0.868
Model:	OLS	Adj. R-squared:	0.616
Method:	Least Squares	F-statistic:	3.449
Date:	Tue, 23 Jul 2024	Prob (F-statistic):	0.0247
Time:	22:13:46	Log-Likelihood:	-123.07
No. Observations:	30	AIC:	286.1
Df Residuals:	10	BIC:	314.2
Df Model:	19		
Covariance Type:	nonrobust		
=======================================	=======================================		=======================================

eovariance type:						
	coef	std e	rr t	P>   t	[0.025	0.975]
Intercept	415.8797	180.2	10 2.308	0.044	14.346	817.413
tau	1.001e+04	1.98e+	0.005	0.996	-4.39e+06	4.41e+06
sigma	-62.7730	18.2	-3.437	0.006	-103.473	-22.073
n_step	-168.8124	259.8	77 -0.650	0.531	-747.856	410.231
adam_eps	87.5099	200.5	0.436	0.672	-359.336	534.356
ep_len_mean	0.1006	0.2	0.413	0.688	-0.442	0.643
tau_pow_2	311.4753	314.5	16 0.990	0.345	-389.377	1012.328
tau_sigma	-2.468e+04	2.05e+	05 -0.121	0.906	-4.81e+05	4.31e+05
tau_n_step	9.437e+06	6.03e+	1.566	0.148	-3.99e+06	2.29e+07
tau_adam_eps	-4.769e+06	3.13e+	06 -1.522	0.159	-1.18e+07	2.21e+06
tau_ep_len_mean	-2349.7876	2023.1	41 -1.161	0.272	-6857.627	2158.052
sigma_pow_2	2.4038	0.5	99 4.012	0.002	1.069	3.739
sigma_n_step	1.2135	10.1	17 0.120	0.907	-21.329	23.756
sigma_adam_eps	8.5121	5.9	1.439	0.181	-4.665	21.689
sigma_ep_len_mean	0.0263	0.0	10 2.674	0.023	0.004	0.048
n_step_pow_2	53.2984	129.9	63 0.410	0.690	-236.278	342.875
n_step_adam_eps	231.7169	252.9	0.916	0.381	-331.855	795.289
n_step_ep_len_mean	-0.0407	0.2	-0.180	0.861	-0.545	0.464
adam_eps_pow_2	-126.2286	110.2	-1.145	0.279	-371.888	119.430
adam_eps_ep_len_mean	-0.1330	0.1	12 -1.188	0.262	-0.383	0.116
ep_len_mean_pow_2	-8.01e-06	0.0	-0.056	0.957	-0.000	0.000
Omnibus:	=======	8.754	ourbin-Watson	======== :	 1.550	: )
Prob(Omnibus):			Jarque-Bera (		7.490	)
Skew:			Prob(JB):	•	0.0236	•
Kurtosis:			Cond. No.		5.78e+15	5

\_\_\_\_\_\_

<sup>[1]</sup> Standard Errors assume that the covariance matrix of the errors is correctly specified.

<sup>[2]</sup> The smallest eigenvalue is 4.72e-19. This might indicate that there are strong multicollinearity problems or that the design matrix is singular.

# C.3 No Parameter Sharing

OLS	Regression	Resul	lts
-----	------------	-------	-----

=======================================	==============	:======================================	=========
Dep. Variable:	Score	R-squared:	0.864
Model:	OLS	Adj. R-squared:	0.605
Method:	Least Squares	F-statistic:	3.339
Date:	Tue, 23 Jul 2024	Prob (F-statistic):	0.0276
Time:	12:14:05	Log-Likelihood:	-138.94
No. Observations:	30	AIC:	317.9
Df Residuals:	10	BIC:	345.9
Df Model:	19		
Covariance Type:	nonrobust		
===========	=======================================		=======================================

	Type: Hom					
	coef	std err	t	P>   t	[0.025	0.975]
Intercept	425.0804	244.891	1.736	0.113	-120.571	970.732
tau	-2.892e+06	2.95e+06	-0.980	0.350	-9.47e+06	3.68e+06
sigma	-13.7033	25.615	-0.535	0.604	-70.776	43.370
n_step	-60.6324	363.894	-0.167	0.871	-871.440	750.175
adam_eps	-101.7131	477.938	-0.213	0.836	-1166.626	963.200
ep_len_mean	0.0414	0.187	0.222	0.829	-0.375	0.458
tau_pow_2	-73.8498	253.375	-0.291	0.777	-638.404	490.704
tau_sigma	-9.58e+04	2.43e+05	-0.394	0.702	-6.37e+05	4.45e+05
tau_n_step	-1.973e+06	4.24e+06	-0.465	0.652	-1.14e+07	7.47e+06
tau_adam_eps	3.361e+06	3.01e+06	1.117	0.290	-3.34e+06	1.01e+07
tau_ep_len_mean	1460.5816	946.981	1.542	0.154	-649.424	3570.587
sigma_pow_2	0.4027	1.422	0.283	0.783	-2.765	3.571
sigma_n_step	-17.9749	30.768	-0.584	0.572	-86.530	50.580
sigma_adam_eps	20.5071	19.299	1.063	0.313	-22.494	63.508
sigma_ep_len_mean	0.0005	0.006	0.087	0.933	-0.012	0.013
n_step_pow_2	5.5271	268.271	0.021	0.984	-592.218	603.273
n_step_adam_eps	100.0307	249.637	0.401	0.697	-456.195	656.256
n_step_ep_len_mean	-0.0024	0.080	-0.030	0.977	-0.180	0.175
adam_eps_pow_2	46.3900	267.727	0.173	0.866	-550.143	642.923
adam_eps_ep_len_mean	-0.0622	0.095	-0.654	0.528	-0.274	0.150
ep_len_mean_pow_2	-2.231e-05	3.99e-05	-0.560	0.588	-0.000	6.65e-05
Omnibus:						
			- />			

			=========
Omnibus:	2.859	Durbin-Watson:	1.983
Prob(Omnibus):	0.239	Jarque-Bera (JB):	1.678
Skew:	-0.548	Prob(JB):	0.432
Kurtosis:	3.378	Cond. No.	1.63e+16

#### Notes:

<sup>[1]</sup> Standard Errors assume that the covariance matrix of the errors is correctly specified.

<sup>[2]</sup> The smallest eigenvalue is 2.28e-18. This might indicate that there are strong multicollinearity problems or that the design matrix is singular.

# **C.4** Full Parameter Sharing

lts

Score	R-squared:	0.953						
OLS	Adj. R-squared:	0.840						
Least Squares	F-statistic:	8.450						
Tue, 23 Jul 2024	Prob (F-statistic):	0.00219						
12:16:56	Log-Likelihood:	-128.54						
28	AIC:	297.1						
8	BIC:	323.7						
19								
nonrobust								
	OLS Least Squares Tue, 23 Jul 2024 12:16:56 28 8	OLS Adj. R-squared: Least Squares F-statistic: Tue, 23 Jul 2024 Prob (F-statistic): 12:16:56 Log-Likelihood: 28 AIC: 8 BIC: 19						

	coef	std err	t	P>   t	[0.025	0.975]
Intercept	175.2457	162.159	1.081	0.311	-198.692	549.184
tau	186.4124	296.485	0.629	0.511	-497.284	870.109
sigma	1043.0267	402.067	2.594	0.032	115.859	1970.194
-	2.574e+06	9.38e+06	0.274	0.032	-1.91e+07	2.42e+07
n_step	-95.1023	52.882	-1.798	0.791	-1.916+07	26.843
adam_eps				0.110	-217.048	
ep_len_mean	-0.0065	0.113	-0.057			0.253
tau_pow_2	190.7520	308.769	0.618	0.554	-521.270	902.774
tau_sigma	287.9223	339.789	0.847	0.421	-495.633	1071.478
tau_n_step	2.957e+07	2.43e+07	1.215	0.259	-2.65e+07	8.57e+07
tau_adam_eps	-11.6668	25.878	-0.451	0.664	-71.341	48.008
tau_ep_len_mean	-0.1573	0.138	-1.140	0.287	-0.476	0.161
sigma_pow_2	-723.8557	329.556	-2.196	0.059	-1483.814	36.103
sigma_n_step	1.668e+07	1.05e+07	1.592	0.150	-7.48e+06	4.08e+07
sigma_adam_eps	-64.5262	24.704	-2.612	0.031	-121.494	-7.559
sigma_ep_len_mean	-0.1967	0.106	-1.850	0.101	-0.442	0.048
n_step_pow_2	6058.0985	5450.747	1.111	0.299	-6511.346	1.86e+04
n_step_adam_eps	-1.209e+06	1.3e+06	-0.933	0.378	-4.2e+06	1.78e+06
n_step_ep_len_mean	-1.043e+04	6264.673	-1.665	0.135	-2.49e+04	4018.744
adam_eps_pow_2	5.8045	2.667	2.176	0.061	-0.346	11.955
adam_eps_ep_len_mean	0.0344	0.019	1.799	0.110	-0.010	0.078
ep_len_mean_pow_2	1.923e-05	3.59e-05	0.535	0.607	-6.36e-05	0.000
Omnibus:	=======	1.813 Dur	======== bin-Watson:	:======	2.036	
Prob(Omnibus):			que-Bera (JB):		1.473	
Skew:			b(JB):		0.479	
Kurtosis:		2.725 Con	d. No.		1.20e+17	
=======================================		========				

<sup>[1]</sup> Standard Errors assume that the covariance matrix of the errors is correctly specified. [2] The smallest eigenvalue is 3.25e-20. This might indicate that there are strong multicollinearity problems or that the design matrix is singular.