

Modelling canine rabies dynamics in Arequipa, Peru

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Methods

All work has been done in R using the code contained in this R markdown file.

```
#Load libraries
suppressMessages(suppressWarnings(library(deSolve)))
suppressMessages(suppressWarnings(library(ggplot2)))
suppressMessages(suppressWarnings(library(dplyr)))
suppressMessages(suppressWarnings(library(stringr)))
suppressMessages(suppressWarnings(library(rgdal)))
suppressMessages(suppressWarnings(library(MASS)))
suppressMessages(suppressWarnings(library(leaflet)))
```

Data Data files will not be made publically available as they contain confidential information. The original files are accessible in the Castillo lab “Rabies” github repository. We will use two sources of data: 1. Rabies case reports 2. Longitudinal survey data

Rabies case reports come from collaboration from the Ministry of Health and from notes from the Zoonotic Disease Research Lab.

```
#Load rabies case data
df <- read.csv("~/Rabies/models/Data/RabiesCaseData_7May2020.csv") #Rabies case reports

#clean and format the case data
df <- df %>%
  rename(LabID = i..LabID) %>%
  mutate(
    Symptoms_date      = as.Date(Symptoms_date,      "%d/%m/%Y"),
    Complaint_date     = as.Date(Complaint_date,     "%d/%m/%Y"),
    Death_date         = as.Date(Death_date,         "%d/%m/%Y"),
    Obtained_date      = as.Date(Obtained_date,      "%d/%m/%Y"),
    Received_date      = as.Date(Received_date,      "%d/%m/%Y"),
    Result_date        = as.Date(Result_date,         "%d/%m/%Y"),
    ContainmentStart_date = as.Date(ContainmentStart_date, "%d/%m/%Y"),
    ContainmentOther_date = as.Date(ContainmentOther_date, "%d/%m/%Y"),
    MedicalAttention_date = as.Date(MedicalAttention_date, "%d/%m/%Y"),
    DateCaseBitten     = as.Date(DateCaseBitten,     "%d/%m/%Y"),
    NumDogsCaseBit     = as.numeric(as.character(NumDogsCaseBit)),
    Month              = as.numeric(as.character(Month)), #Format as number
    Years              = as.numeric(as.character(Years)), #Format as number
    Age                = Years*365.25 + Month*30.4375 #Calculate age in days
  )
```

```
## Warning: Problem with 'mutate()' input 'NumDogsCaseBit'.
## i NAs introduced by coercion
## i Input 'NumDogsCaseBit' is 'as.numeric(as.character(NumDogsCaseBit))'.
```

```
## Warning in mask$eval_all_mutate(dots[[i]]): NAs introduced by coercion
```

```
#Add on year labels
df$year <- 2020
df$year[1:19] <- 2015
df$year[20:79] <- 2016
df$year[80:129] <- 2017
df$year[130:165] <- 2018
df$year[166:204] <- 2019

#Read in the incidence table
rabies <- read.csv("~/Rabies/models/Data/Rabies_IncidenceTable.csv") #Rabies incidence table
```

Longitudinal survey data was collected from by the Castillo lab. For full methods, see Castillo, 2019. Briefly, in the weeks following the yearly mass dog vaccination campaign, trained surveyers went door to door conducting surveys in defined study areas in the Alta Sevre Alegro district of Arequipa. Surveyers would ascertain if people participated in the campaign and collect demographic data on both the respondent and their dogs. This analysis includes 4 years worth of survey data (2015-2019).

```
#read in 2016 and 2017 data
dogs1 <- read.csv("~/Rabies/rabia_ASA_encuesta_2017/resultados/dogs2016_2017_10Abr18.csv")

#Clean and format 2016 survey data
df_2016 <- subset(dogs1, !is.na(dogs1$EDAD_M16)) %>%
  dplyr::select(UNICODE, NOMBRE, SEXO, EDAD_A16, EDAD_M16, VACUNADO16, FECHA_VAC16, ACCESO_CALLE16) %>%
  rename(Unicdoe = UNICODE,
         Name = NOMBRE,
         Sex = SEXO,
         Years = EDAD_A16,
         Months = EDAD_M16,
         Vaccine = VACUNADO16,
         Date = FECHA_VAC16,
         Restriction = ACCESO_CALLE16) %>%
  mutate(Date= str_sub(Date, end=-6),
         Date= as.Date(Date, "%d/%m/%y"))

#Clean and format 2017 survey data
df_2017 <- subset(dogs1, !is.na(dogs1$EDAD_MESES17)) %>%
  dplyr::select(UNICODE, NOMBRE, SEXO, EDAD_ANIO17, EDAD_MESES17, ESTE_ANIO_VACUNARON17, FECHA17) %>%
  rename(Unicdoe = UNICODE,
         Name = NOMBRE,
         Sex = SEXO,
         Years = EDAD_ANIO17,
         Months = EDAD_MESES17,
         Vaccine = ESTE_ANIO_VACUNARON17,
         Date = FECHA17)

#2018 survey data
df_2018 <- read.csv("~/Rabies/rabia_ASA_encuesta_2018/resultados/PERRO_CLEAN_2018-08-31.csv")
```

```

df_2018 <-df_2018%>%
  dplyr::select(PERRO_UNICODE, PERRO_NOMBRE, PERRO_SEXO, PERRO_EDAD_ANIO,
                PERRO_EDAD_MES, PERRO_ESTE_ANIO_VACUNARON, PERRO_COMO_PERMANECE_CASA, PERRO_DATETIME) %>%
  rename(Unicode = PERRO_UNICODE,
         Name = PERRO_NOMBRE,
         Sex = PERRO_SEXO,
         Years = PERRO_EDAD_ANIO,
         Months = PERRO_EDAD_MES,
         Vaccine = PERRO_ESTE_ANIO_VACUNARON,
         Restriction = PERRO_COMO_PERMANECE_CASA,
         Date = PERRO_DATETIME) %>%
  mutate(Date = substr(as.character(Date), 1, 10))

#2019 survey data
df_2019 <- read.csv("~/Rabies/rabia_ASA_encuesta_2019/resultados/PERRO2019VANCAN_CLEAN_2019-12-10.csv")
df_2019 <-df_2019%>%
  dplyr::select(PERRO_UNICODE, PERRO_NOMBRE, PERRO_SEXO, PERRO_EDAD_ANIO,
                PERRO_EDAD_MES, PERRO_ESTE_ANIO_VACUNARON, PERRO_COMO_PERMANECE_CASA, PERRO_DATETIME) %>%
  rename(Unicode = PERRO_UNICODE,
         Name = PERRO_NOMBRE,
         Sex = PERRO_SEXO,
         Years = PERRO_EDAD_ANIO,
         Months = PERRO_EDAD_MES,
         Vaccine = PERRO_ESTE_ANIO_VACUNARON,
         Restriction = PERRO_COMO_PERMANECE_CASA,
         Date = PERRO_DATETIME) %>%
  mutate(Date = substr(as.character(Date), 1, 10),
         Months = as.numeric(as.character(Months)),
         Years = as.numeric(as.character(Years)))

```

```

## Warning: Problem with 'mutate()' input 'Months'.
## i NAs introduced by coercion
## i Input 'Months' is 'as.numeric(as.character(Months))'.

## Warning in mask$eval_all_mutate(dots[[i]]): NAs introduced by coercion

## Warning: Problem with 'mutate()' input 'Years'.
## i NAs introduced by coercion
## i Input 'Years' is 'as.numeric(as.character(Years))'.

## Warning in mask$eval_all_mutate(dots[[i]]): NAs introduced by coercion

```

Model framework We adapted a classic SEIR model to reflect the rabies system in Arequipa (Institute for Disease Modelling, 2020). We present an SEIV model that reflects the framework used to model the canine rabies disease system in Arequipa (Figure 1).

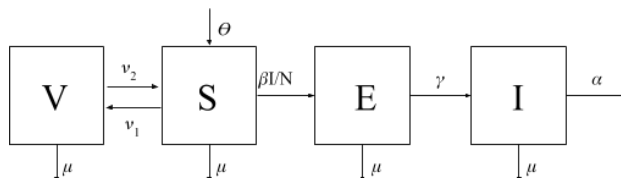


Figure 1: SEIV model framework for canine rabies system in Arequipa

In this model, the dog population is split into 4 compartments labeled “V”, “S”, “E”, and “I” corresponding to the following disease states: vaccinated, susceptible, exposed and infected. “N” is the total population ($S+E+I+V$). The arrows going between the compartments indicate flow of the population from one state to the other. For example, the arrow labeled “V1” indicates susceptibles moving from the susceptible compartment to the vaccinated compartment (by receiving the rabies vaccine). Different from classic SEIR models, there is no “R” or “recovered” population compartment because rabies is fatal once the dog is infected (World Health Organization, 2013). However, there is an effective rabies vaccine which confers immunity, so the “recovered” compartment is replaced with a “vaccinated” compartment. Parameters will be explained and calculated in full detail below.

From the model framework, we can write a system of ordinary differential equations describing the flow of the population in and out of each compartment.

$$dS/dt = \theta - \beta SI/N - \mu S - \nu_1 S + \nu_2 V$$

$$dE/dt = \beta SI/N - \gamma E - \mu E$$

$$dI/dt = \gamma E - \mu I - \alpha I$$

$$dV/dt = \nu_1 S - \nu_2 V - \mu V$$

Parameters The first step to simulating the rabies models is to define the parameters in the model framework (Figure 1). The rates of the population flow between compartments (defined by the parameters) are instantaneous and are equal to the inverse of the time spent in the compartments. We can use this relationship to calculate point estimates for the parameters.

Known parameters

Some parameters are known from the literature on rabies virus biology. The estimate of total dog population is from the Ministry of Health’s estimate (Red Arequipa Caylloma, 2019) is 264550.2646. The vaccine is labeled for 1 year (Castillo, 2019), so the instantaneous rate of dogs losing vaccination we conservatively set to $1/365$ (days^{-1}). γ , the rate of exposed dogs become infectious (the inverse of the latency period) is described in rabies biology literature and we will use the estimate given by Hampson, 2009: $1/50$ (days^{-1}). For simplicity we will set the initial vaccination coverage to be equal to 0, and immediately (day 1) of the model, introduce the first vaccination campaign.

```
DOG_POPN= 203183 #Peru Ministry of Health estimate
GAMMA= 1/22.3 #Hampson 2009
NU2 = 1/365 #vaccine label
ETA = 0 #initial vaccination coverage, setting to 0 for simplicity and will have first vancan on day 1
```

After known parameters are collected, unknown parameters are estimated based on the data from Arequipa.

μ (background death rate)

μ is the instantaneous per capita death rate of dogs not attributable to rabies. It can be estimated as the inverse of average age of dogs.

```
df_2019 <- df_2019 %>%
  mutate(Age = Years*365.25 + Months*30.4375)
#MU <- 1/t.test(df_2019$Age)$estimate[[1]] #Mean: 1099.203 [1063.346, 1135.060]
MU <- 1/1099.203
```

α (rabies death rate) α is the instantaneous per capita death rate of rabid dogs and can be calculated as the inverse of the time spent in the infectious compartment ($1/\text{infectious period}$).

```
df$Infectious <- df$Death_date - df$Symptoms_date
#ALPHA <- 1/t.test(df$Infectious)$estimate[[1]] #2.534247 [1.931721, 3.136772]
ALPHA <- 1/2.534247
```

ν_1 (vaccination coverage)

ν_1 is the instantaneous rate of immunity from vaccination. From our data we can calculate the coverage rates of dogs per year, and the day in which the majority of the vaccinations occurred. Additionally, based on pilot data shared from Sergio Recuenco we assume that 2014 and 2015 vaccine coverage was 48.98%. Finally we can transform coverage rates to instantaneous rates by using the equation: vaccination coverage = $1 - e^{-\nu_1 t}$, where $t = 1$ day.

```
# #2016
# plyr::count(df_2016$Vaccine) #0.6147823
# plyr::count(df_2016$Date) #Mode= June 12
#
# #2017
# plyr::count(df_2017$Vaccine) #0.4989594
# plyr::count(df_2017$Date) #Mode= September 22
#
# #2018
# plyr::count(df_2018$Vaccine) #0.5285256
# plyr::count(df_2018$Date) #Mode= August 6
#
# #2019
# plyr::count(df_2019$Vaccine) #0.5850053
# plyr::count(df_2019$Date) #Mode= October 24

#Build table
NU1 <- data.frame(year=c(2014, 2015, 2016,2017,2018,2019),
                  date=as.Date(c("2014-06-12", "2015-06-12", "2016-06-12", "2017-09-22", "2018-08-06", "2019-10-24"),
                  vax=c(0.4898, 0.4898, 0.6148, 0.4990, 0.5285, 0.5850))

NU1$inst <- -log(1-NU1$vax)
```

R_0 (basic reproductive number) and β (transmission coefficient)

R_0 is defined as the average number of secondary cases a primary case will infect in a totally susceptible population. An initial estimate of R_0 can be estimated by from survey data by the number of bites * the probability of rabies transmission (Hampson, 2009). Using the estimate of rabies transmission probability from Hampson, 2009 (0.49), and the number of dogs a rabid dog bites from rabies case report data in Arequipa. We can calculate a rough estimate of R_0 .

```
#Extract bite data
bites <- as.vector(na.omit(df$NumDogsCaseBit))
bites <- as.data.frame(bites)
colnames(bites) <- c("counts")

unnname((0.49*(t.test(bites$counts))$estimate[1]))
```

```
## [1] 1.366061
```

1.37 is a good starting estimate for R_0 . However, not all bite events are observed by owners/ public health officials, so what is recorded in the data will be an underestimate of R_0 . We can re-run the model increasing

the model of R_0 in small increments until we find the value of R_0 that gives the lowest sum squared of residuals. Doing this, we find an increased value of 1.44.

```
#fit to epidemic data by rerunning system in small increments and then calculate residuals
R_NAUGHT=1.44
```

R_0 is not used directly in the system of equations. However, it can be used to derive β . β is the transmission coefficient and is used to describe the infection rate (which is also based on the prevalence of rabies).

Using next generation matrix techniques (Diekman, 2010), β can be derived from the other parameters as:

$$\beta = R_0(\gamma + \mu)(\mu + \alpha)/\gamma$$

Deterministic Model With all parameters calculated, we can formulate the deterministic SEIV model so that R can solve it.

First we save all parameters in a column that a can be inputted into a function.

```
#Parameters
params <- c(R0= R_NAUGHT, #Bite: 1.366061, #Age:2.487201
  m = MU, #mu (normal death rate)
  g = GAMMA, #gamma (latency rate)
  a = ALPHA, #alpha (death rate attributable to rabies)
  u = NU2, #1 yr vaccine
  eta= ETA, #initial vaccine coverage --- (have vancan start at d1)
  N =DOG_POPN, #2645.503, #Do we want this to be density (per km2) or total
  #rho = RHO, #Reporting rate
  d2= 1) #delta2, density dependency weight [1 (freq), 0 (dens)]
params["d"] <- 1/params["N"] + params["d2"]*((params["N"]-1)/params["N"]) #model type weight: frequency
params["beta"] <-params["R0"]*params["d"]*(params["g"]+params["m"])*(params["a"]+params["m"])/params["g"]
```

We then set initial conditions. Our assumption is that rabies was reintroduced into Arequipa through the transport of a dog that was exposed to rabies but had not yet become symptomatic.

```
#Initial conditions
init <- NULL # popn initial values
init["S"] <- (params["N"]-1)*(1-params["eta"])
init["E"] <- 1
init["I"] <- 0
init["R"] <- (params["N"]-1)*params["eta"]
init["H"] <- 0 #Accumulator variable
```

Because the vaccination campaign occurred yearly we want to “pulse” vaccinations each year corresponding to the vaccination campaign. Here we set up the time dependent series of vaccination pulses.

```
#Time dependent vaccination pulses for the yearly vaccination campaign
times <- seq(0, 2557, by = 1) #time series for model
signal <- data.frame(times = times, vax = rep(0, length(times))) #artificial time series

#specify vaccination coverage
signal$vax[1] <- NU1$inst[1] #2014-03-16 ***Earliest year we have data from
signal$vax[366] <- NU1$inst[2] #2015-03-16 ***Unreliable reports so using 2014 estimate
signal$vax[820] <- NU1$inst[3] #2016-06-12
signal$vax[1287] <- NU1$inst[4] #2017-09-22
```

```

signal$vax[1605] <- NU1$inst[5] #2018-08-06
signal$vax[2049] <- NU1$inst[6] #2019-10-24

input <- approxfun(signal)#Interpolating fx

```

Next we can construct a function that incorporates the time series, the initial condition and the parameters into the system of equations derived for the model frame work.

```

#deterministic model description
disease_dynamics <- function(times, state, params) {
  with(
    as.list(c(state, params)), {
      vax <- input(times)

      ##Equations (easy to read)
      dS <- (m*N + a*I) - beta*I*S/(d*N) - m*S -vax*S + u*R
      dE <- beta*S*I/(d*N) - g*E - m*E
      dI <- g*E -a*I - m*I
      dR <- vax*S - u*R - m*R
      dH <- beta*S*I/(d*N) #Accumulator variable- just a count of all cases moving into I
      return(list(c(dS, dE, dI, dR, dH), signal=vax))
    }
  )
}

```

Finally, we can use the deSolve package to solve the system of equations and get our results.

```

#Run model
out <- as.data.frame(ode(y = init, times = times, func = disease_dynamics, parms = params))
RESULTS<-data.frame(out$S, out$E, out$I, out$R, out$H) #results
RESULTS$date <-seq(as.Date("2014/03/16"), as.Date("2021/03/16"), "days")

#Convert model results to accumulated incidence
RESULTS <- RESULTS %>%
  mutate(diffH = out.H - lag(out.H))
RESULTS$diffH[is.na(RESULTS$diffH)] <- 0 #set dates don't have date for as 0 (I.e beginning and end)
RESULTS$Date <- seq(as.Date("2014/03/16"), as.Date("2021/03/16"), "days") #Create ref of days
rabies.stim <- data.table::setDT(RESULTS)[, .(Incidence = sum(diffH)), by = .(yr = data.table::year(Date))]
rabies$stim <- rabies.stim$Incidence #Match stim incidence with actual incidence df
rabies$stim_reports <- rabies$stim*params["rho"] #scale down stim reports by reporting percent

```

Changes caused by COVID 19 Determinic models can be used to answer many crucial questions. For instance we can examine the effect of COVID-19 control measures instituted in Peru on rabies dynamics. In March, 2020, much like the rest of the world, Peru instituted lock down, quarantine and work from home measures that disrupted rabies control activities.

To do so, we can re-initialize the initial conditions based on those when COVID-19 restrictions were started.

```

#Re initialize on March 16 (day of Peru lockdown)
init <- NULL # popn initial values
init["S"] <- RESULTS$out.S[RESULTS$Date == "2020-03-15"]
init["E"] <- RESULTS$out.E[RESULTS$Date == "2020-03-15"]

```



```

init["I"] <- RESULTS$out.I[RESULTS$Date == "2020-03-15"]
init["R"] <- RESULTS$out.R[RESULTS$Date == "2020-03-15"]
init["H"] <- RESULTS$out.H[RESULTS$Date == "2020-03-15"]

```

First we can examine the effect a cancelled (0% coverage) or reduced yearly mass vaccination campaign (58% coverage) versus an ideal coverage level (80%) on theoretical rabies cases over a year.

```

#set up pulse vax for a year
times <- seq(0, 365, by = 1) #time series for model

#Ideal vaccination coverage scenario
signal <- data.frame(times = times, vax = rep(0, length(times)))
signal$vax[223] <- -log(1-0.8000) #2020-10-24 ---> 80% coverage
input <- approxfun(signal)
out <- as.data.frame(ode(y = init, times = times, func = disease_dynamics, parms = params)) #Fun model
RESULTS2<-data.frame(out$S, out$E, out$I, out$R, out$H) #format results
RESULTS2 <- RESULTS2 %>%
  mutate(diffH = out.H - lag(out.H))
RESULTS2$diffH[is.na(RESULTS2$diffH)] <- 0
RESULTS2$Date <- seq(as.Date("2020/03/16"), as.Date("2021/03/16"), "days") #create day ref

#Sub-optimal vaccination coverage scenario
signal <- data.frame(times = times, vax = rep(0, length(times)))
signal$vax[223] <- -log(1-0.5800) #2020-10-24 ---> 48% coverage
input <- approxfun(signal)
out <- as.data.frame(ode(y = init, times = times, func = disease_dynamics, parms = params)) #Fun model
RESULTS3<-data.frame(out$S, out$E, out$I, out$R, out$H) #format results
RESULTS3 <- RESULTS3 %>%
  mutate(diffH = out.H - lag(out.H))
RESULTS3$diffH[is.na(RESULTS3$diffH)] <- 0
RESULTS3$Date <- seq(as.Date("2020/03/16"), as.Date("2021/03/16"), "days") #create day ref

#Total cancellation of vaccination campaign
signal <- data.frame(times = times, vax = rep(0, length(times)))
signal$vax[223] <- -log(1-0.0000) #2020-10-24 ---> 0% coverage
input <- approxfun(signal)
out <- as.data.frame(ode(y = init, times = times, func = disease_dynamics, parms = params)) #Fun model
RESULTS4<-data.frame(out$S, out$E, out$I, out$R, out$H) #format results
RESULTS4 <- RESULTS4 %>%
  mutate(diffH = out.H - lag(out.H))
RESULTS4$diffH[is.na(RESULTS4$diffH)] <- 0
RESULTS4$Date <- seq(as.Date("2020/03/16"), as.Date("2021/03/16"), "days") #create day ref

```

Next, we can repeat these scenarios but with the added change of decreased surveillance. In Arequipa, public health officials respond to reports of rabid dogs and eliminate suspect cases, decreases the survival time of rabid dogs and affecting the parameter, α . However, with COVID-19 restrictions, public health officials were not able to respond to reports of dogs acting rabies. This has the potential to increase the survival time of rabid dogs. Using the estimate of average length of survival of rabid dogs without intervention given by Hampson, 2009, we can set alpha to be the inverse of this estimate (3.7d) and re-run the simulation.


```

#set alpha based on increased survival time or rabid dogs
params["a"] <- 1/3.7

##Rerun scenarios
#Ideal vaccination coverage scenario
signal <- data.frame(times = times, vax = rep(0, length(times)))
signal$vax[223] <- -log(1-0.8000) #2020-10-24 ---> 80% coverage
input <- approxfun(signal)
out <- as.data.frame(ode(y = init, times = times, func = disease_dynamics, parms = params)) #Fun model
RESULTS5<-data.frame(out$S, out$E, out$I, out$R, out$H) #format results
RESULTS5 <- RESULTS5 %>%
  mutate(diffH = out.H - lag(out.H))
RESULTS5$diffH[is.na(RERESULTS5$diffH)] <- 0
RESULTS5$Date <- seq(as.Date("2020/03/16"), as.Date("2021/03/16"), "days") #create day ref

#Sub-optimal vaccination coverage scenario
signal <- data.frame(times = times, vax = rep(0, length(times)))
signal$vax[223] <- -log(1-0.5800) #2020-10-24 ---> 48% coverage
input <- approxfun(signal)
out <- as.data.frame(ode(y = init, times = times, func = disease_dynamics, parms = params)) #Fun model
RESULTS6<-data.frame(out$S, out$E, out$I, out$R, out$H) #format results
RESULTS6 <- RESULTS6 %>%
  mutate(diffH = out.H - lag(out.H))
RESULTS6$diffH[is.na(RERESULTS6$diffH)] <- 0
RESULTS6$Date <- seq(as.Date("2020/03/16"), as.Date("2021/03/16"), "days") #create day ref

#Total cancellation of vaccination campaign
signal <- data.frame(times = times, vax = rep(0, length(times)))
signal$vax[223] <- -log(1-0.0000) #2020-10-24 ---> 0% coverage
input <- approxfun(signal)
out <- as.data.frame(ode(y = init, times = times, func = disease_dynamics, parms = params)) #Fun model
RESULTS7<-data.frame(out$S, out$E, out$I, out$R, out$H) #format results
RESULTS7 <- RESULTS7 %>%
  mutate(diffH = out.H - lag(out.H))
RESULTS7$diffH[is.na(RERESULTS7$diffH)] <- 0
RESULTS7$Date <- seq(as.Date("2020/03/16"), as.Date("2021/03/16"), "days") #create day ref

```

Next we can run simulations for 5 years to assess the relative impact of these disruptions. We will assume that the “normal” vaccination coverage for Arequipa is 58% and that the normal survival time of rabid dogs (after symptom onset) is 2.5 days.

```

#####
#Scenario 0: No disruption (counterfactual)
#####
#Set up time series params
times <- seq(0, 365*5+1, by = 1) #time series for model (5yrs)
params["a"] <- 1/2.5
signal <- data.frame(times = times, vax = rep(0, length(times)))
signal$vax[197] <- -log(1-0.58) #2020-09-28 ---> 58% coverage
signal$vax[562] <- -log(1-0.58) #2021-09-28 ---> 58% coverage
signal$vax[927] <- -log(1-0.58) #2022-09-28 ---> 58% coverage
signal$vax[1292] <- -log(1-0.58) #2023-09-28 ---> 58% coverage

```

```

signal$vax[1658] <- -log(1-0.58) #2024-09-28 ---> 58% coverage
input <- approxfun(signal)

#Run model
out <- as.data.frame(ode(y = init, times = times, func = disease_dynamics, parms = params)) #Fun model
RESULTS.A<-data.frame(out$S, out$E, out$I, out$R, out$H) #format results
RESULTS.A <- RESULTS.A %>%
  mutate(diffH = out.H - lag(out.H))
RESULTS.A$diffH[is.na(RESULTS.A$diffH)] <- 0
RESULTS.A$Date<-seq(as.Date("2020/03/16"), as.Date("2025/03/16"), "days") #create day ref

#####
#Scenario 3: 3 yr disruption(ST=3.7d, vax coverage = 12.3%)
#####
#Part 1: disruption time period (1 yr)
times <- seq(0, 365*3, by = 1) #time series for model (3yr)
params["a"] <- 1/3.7 #Survival time increased
signal <- data.frame(times = times, vax = rep(0, length(times)))
signal$vax[197] <- -log(1-0.123) #2020-09-28 ---> 12.3% coverage
signal$vax[562] <- -log(1-0.123) #2021-09-28 ---> 12.3% coverage
signal$vax[927] <- -log(1-0.123) #2022-09-28 ---> 12.3% coverage
input <- approxfun(signal)
out <- as.data.frame(ode(y = init, times = times, func = disease_dynamics, parms = params)) #Fun model
RESULTS.B<-data.frame(out$S, out$E, out$I, out$R, out$H) #format results
RESULTS.B <- RESULTS.B %>%
  mutate(diffH = out.H - lag(out.H))
RESULTS.B$diffH[is.na(RESULTS.B$diffH)] <- 0
RESULTS.B$Date <- seq(as.Date("2020/03/16"), as.Date("2023/03/16"), "days") #create day ref

#Part 2: Normal control activities resume
init3 <- NULL # popn initial values
init3["S"] <- RESULTS.B$out.S[RESULTS.B$Date == "2023-03-15"]
init3["E"] <- RESULTS.B$out.E[RESULTS.B$Date == "2023-03-15"]
init3["I"] <- RESULTS.B$out.I[RESULTS.B$Date == "2023-03-15"]
init3["R"] <- RESULTS.B$out.R[RESULTS.B$Date == "2023-03-15"]
init3["H"] <- RESULTS.B$out.H[RESULTS.B$Date == "2023-03-15"]

times <- seq(0, 365*2+1, by = 1) #time series for model (5-3yr)
params["a"] <- 1/2.5 #Survival time increased
signal <- data.frame(times = times, vax = rep(0, length(times)))
signal$vax[197] <- -log(1-0.58) #2023-09-28 ---> 58% coverage
signal$vax[563] <- -log(1-0.58) #2024-09-28 ---> 58% coverage
input <- approxfun(signal)
out <- as.data.frame(ode(y = init3, times = times, func = disease_dynamics, parms = params)) #Fun model
RESULTS.B2<-data.frame(out$S, out$E, out$I, out$R, out$H) #format results
RESULTS.B2 <- RESULTS.B2 %>%
  mutate(diffH = out.H - lag(out.H))
RESULTS.B2$diffH[is.na(RESULTS.B2$diffH)] <- 0
RESULTS.B2$Date <- seq(as.Date("2023/03/15"), as.Date("2025/03/15"), "days") #create day ref

RESULTS.B1 <- RESULTS.B %>%
  filter(Date < as.Date("2023-03-15"))

```

```

RESULTS.B <- rbind(RESULTS.B1, RESULTS.B2)

#####
#Scenario 2: 2 yr disruption(ST=3.7d, vax coverage = 12.3%)
#####

#Part 2: Normal control activities resume
init2 <- NULL # popn initial values
init2["S"] <- RESULTS.B$out.S[RESULTS.B$Date == "2022-03-15"]
init2["E"] <- RESULTS.B$out.E[RESULTS.B$Date == "2022-03-15"]
init2["I"] <- RESULTS.B$out.I[RESULTS.B$Date == "2022-03-15"]
init2["R"] <- RESULTS.B$out.R[RESULTS.B$Date == "2022-03-15"]
init2["H"] <- RESULTS.B$out.H[RESULTS.B$Date == "2022-03-15"]

times <- seq(0, 365*3+1, by = 1) #time series for model
params["a"] <- 1/2.5 #Survival time increased
signal <- data.frame(times = times, vax = rep(0, length(times)))
signal$vax[197] <- -log(1-0.58) #2022-09-28 ----> 58% coverage
signal$vax[562] <- -log(1-0.58) #2023-09-28 ----> 58% coverage
signal$vax[928] <- -log(1-0.58) #2024-09-28 ----> 58% coverage

input <- approxfun(signal)
out <- as.data.frame(ode(y = init2, times = times, func = disease_dynamics, parms = params)) #Fun model
RESULTS.C2<-data.frame(out$S, out$E, out$I, out$R, out$H) #format results
RESULTS.C2 <- RESULTS.C2 %>%
  mutate(diffH = out.H - lag(out.H))
RESULTS.C2$diffH[is.na(RESULTS.C2$diffH)] <- 0
RESULTS.C2$Date <- seq(as.Date("2022/03/15"), as.Date("2025/03/15"), "days") #create day ref

RESULTS.C1 <- RESULTS.B %>%
  filter(Date < as.Date("2022-03-15"))

RESULTS.C <- rbind(RESULTS.C1, RESULTS.C2)

#####
#Scenario 1: 1 yr disruption(ST=3.7d, vax coverage = 12.3%)
#####

#Part 2: Normal control activities resume
init1 <- NULL # popn initial values
init1["S"] <- RESULTS.B$out.S[RESULTS.B$Date == "2021-03-15"]
init1["E"] <- RESULTS.B$out.E[RESULTS.B$Date == "2021-03-15"]
init1["I"] <- RESULTS.B$out.I[RESULTS.B$Date == "2021-03-15"]
init1["R"] <- RESULTS.B$out.R[RESULTS.B$Date == "2021-03-15"]
init1["H"] <- RESULTS.B$out.H[RESULTS.B$Date == "2021-03-15"]

times <- seq(0, 365*4+1, by = 1) #time series for model
params["a"] <- 1/2.5 #Survival time increased
signal <- data.frame(times = times, vax = rep(0, length(times)))
signal$vax[197] <- -log(1-0.58) #2021-09-28 ----> 58% coverage
signal$vax[562] <- -log(1-0.58) #2022-09-28 ----> 58% coverage
signal$vax[927] <- -log(1-0.58) #2023-09-28 ----> 58% coverage
signal$vax[1293] <- -log(1-0.58) #2024-09-28 ----> 58% coverage
input <- approxfun(signal)

```

```

out <- as.data.frame(ode(y = init1, times = times, func = disease_dynamics, parms = params)) #Fun model
RESULTS.D2<-data.frame(out$S, out$E, out$I, out$R, out$H) #format results
RESULTS.D2 <- RESULTS.D2 %>%
  mutate(diffH = out.H - lag(out.H))
RESULTS.D2$diffH[is.na(RESULTS.D2$diffH)] <- 0
RESULTS.D2$Date <- seq(as.Date("2021/03/15"), as.Date("2025/03/15"), "days") #create day ref

RESULTS.D1 <- RESULTS.B %>%
  filter(Date < as.Date("2021-03-15"))

RESULTS.D <- rbind(RESULTS.D1, RESULTS.D2)

```

Results

Epidemiologic data exploration Since 2015 to March, 2020 (when surveillance was suspended due to COVID restrictions), 214 cases of rabies were reported to the Peru Ministry of Health (Figure 2). The distribution of cases over time can be viewed in Figure 2, and mapped out in Figure 3. Parameters were calculated to parameterize the model framework (Figure 1) and are displayed in Table 1 except for ν_2 which varied per year displayed in Table 2.

```

#Epi curve
fig2 <- ggplot() +
  theme_classic()+
  geom_col(data = rabies, aes(x=month, y=reports))+
  scale_x_discrete(breaks=seq(0, max(rabies$month)+1, 1),
    limits=seq(0, max(rabies$month)+1, 4))+
  scale_y_discrete(breaks=seq(0, max(rabies$reports)+1, 1),
    limits=seq(0, max(rabies$reports)+1, 1))+
  xlab("Month") + ylab("New rabies cases")+
  ggtitle("Arequipa rabies epi curve")

```

```

## Warning: Continuous limits supplied to discrete scale.
## Did you mean 'limits = factor(...)' or 'scale*_continuous()' ?

## Warning: Continuous limits supplied to discrete scale.
## Did you mean 'limits = factor(...)' or 'scale*_continuous()' ?

```

```
fig2
```

Table 1: Table 1: Estimated parameters

Parameter	Estimate
θ	$\mu \cdot N + a \cdot I$
β	0.581080381190508
μ	0.000909750064364817
γ	0.0448430493273543
α	0.394594528473349
ν_2	0.00273972602739726

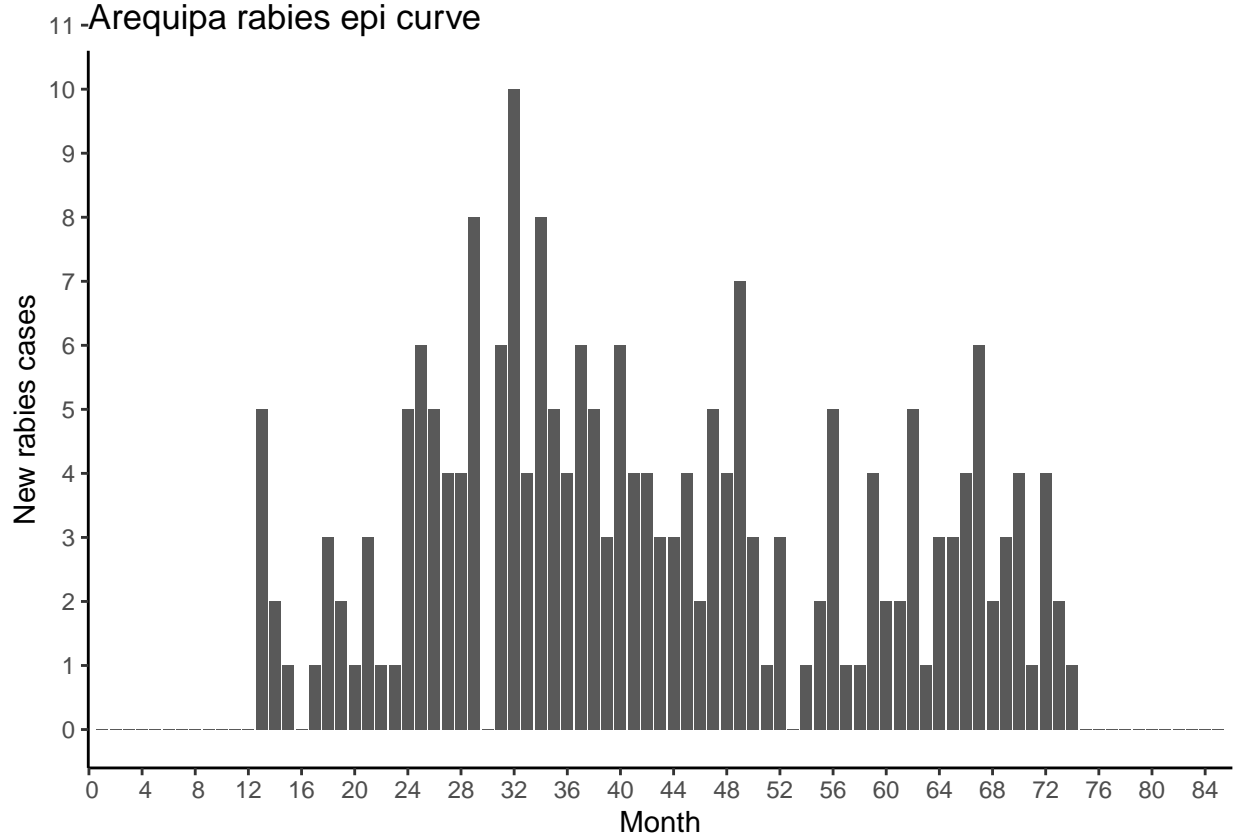


Figure 2: Epidemiologic curve of reported canine rabies incidence

```

params.table <- data.frame(
  Parameter= c("$\\theta$", "$\\beta$", "$\\mu$", "$\\gamma$", "$\\alpha$", "$\\nu_2$"),
  Estimate= c("mu*N + a*I", unname(params["beta"]), MU, GAMMA, ALPHA, NU2))

params.table %>%
  kableExtra::kbl(caption = "Table 1: Estimated parameters")%>%
  kableExtra::kable_styling()

NU1 %>%
  rename(Year = year, Date=date, Coverage=vax, Rate=inst)%>%
  kableExtra::kbl(caption = "Table 2: Estimated vaccination rates per year")%>%
  kableExtra::kable_styling()

```

Table 2: Table 2: Estimated vaccination rates per year

Year	Date	Coverage	Rate
2014	2014-06-12	0.4898	0.6729525
2015	2015-06-12	0.4898	0.6729525
2016	2016-06-12	0.6148	0.9539926
2017	2017-09-22	0.4990	0.6911492
2018	2018-08-06	0.5285	0.7518362
2019	2019-10-02	0.5850	0.8794768

Deterministic model results Results from the deterministic model stimulation show an almost cyclical variation in the susceptible and vaccinated populations (Figure 4). This is actually introduced from the vaccination campaign. The vaccination campaign will increase the number of vaccinated in one pulse, and these numbers will slowly decline as immunity is lost and is the population turns over. The infected and exposed populations appear to be at 0 (Figure 4), but this is only do to the massive scale of the entire population. When looking at just the infected population (Figure 5), the cyclic variations corresponding to the rise in vaccination with the yearly campaigns are apparent.

```
#plot whole system dynamics
Pal1 <- c('Susceptible' = 'gold',
  'Exposed' = 'orange1',
  'Infectious' = 'red3',
  'Vaccinated' = 'dodgerblue3')

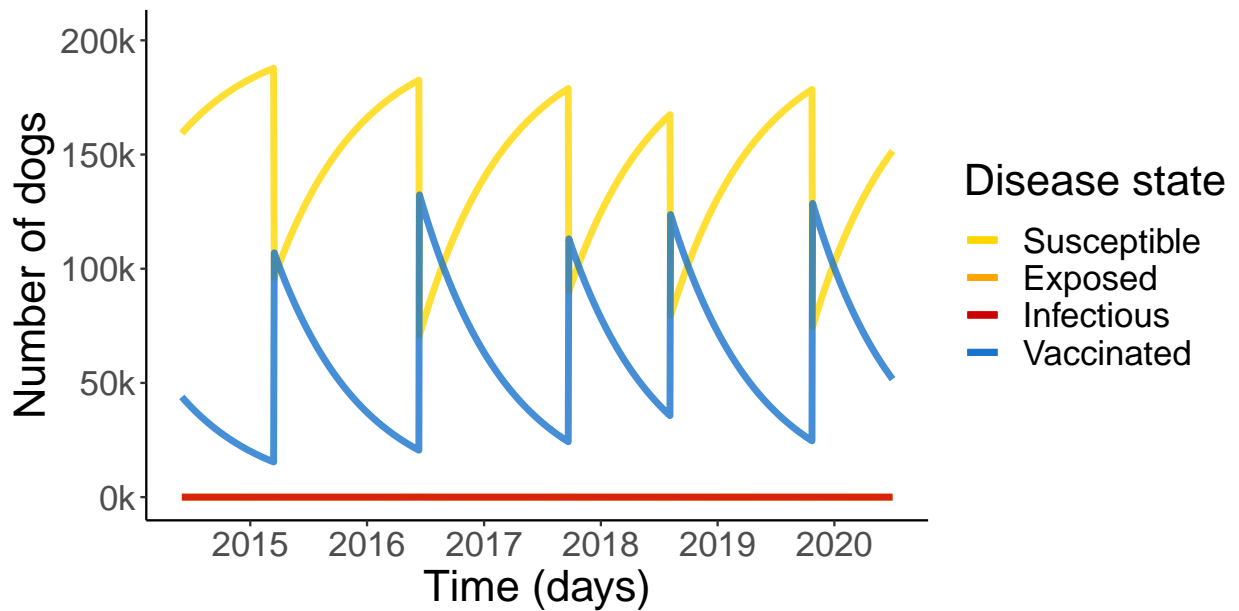
fig4 <- ggplot()+
  theme_classic()+ #white background w/ out grid
  geom_line(data=RESULTS, aes(x=date, y=out.S, color="Susceptible"), size=1.5, alpha=0.8)+
  geom_line(data=RESULTS, aes(x=date, y=out.E, color="Exposed"), size=1.5, alpha=0.8)+
  geom_line(data=RESULTS, aes(x=date, y=out.I, color="Infectious"), size=1.5, alpha=0.8)+
  geom_line(data=RESULTS, aes(x=date, y=out.R, color="Vaccinated"), size =1.5, alpha=0.8)+
  scale_y_continuous(labels = function(l) {
    trans = 1 / 1000
    paste0(trans, "k")
  })+
  # ggtitle("Deterministic model") + #title label
  scale_color_manual(values = Pal1, name= "Disease state", breaks=c("Susceptible","Exposed","Infectious",
  scale_x_date(date_breaks= "1 year", date_labels="%Y", limits=c(as.Date("2014-06-01", "%Y-%m-%d"), a
  theme(text = element_text(size=20),
    axis.text.x = element_text(size=16))+
  labs(y= "Number of dogs", x = "Time (days)") #axis labels
fig4
```

```
## Warning: Removed 335 row(s) containing missing values (geom_path).
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## Warning: Removed 335 row(s) containing missing values (geom_path).
```



```
fig4b <- ggplot()+
  theme_classic()+ #white background w/ out grid
  # geom_line(data=RESULTS, aes(x=date, y=out.S, color="Susceptible"), size=1.5, alpha=0.8)+
  geom_line(data=RESULTS, aes(x=date, y=out.E, color="Exposed"), size=1.5, alpha=0.8)+
  geom_line(data=RESULTS, aes(x=date, y=out.I, color="Infectious"), size=1.5, alpha=0.8)+
  #geom_line(data=RESULTS, aes(x=date, y=out.R, color="Vaccinated"), size=1.5, alpha=0.8)+
  # ggtitle("Deterministic model") + #title label
  scale_color_manual(values = Pal1, name= "Disease state", breaks=c("Susceptible","Exposed","Infectious",
  scale_x_date(date_breaks= "1 year", date_labels="%Y", limits=c(as.Date("2014-06-01", "%Y-%m-%d"), as.Date("2020-06-01", "%Y-%m-%d")),
  theme(text = element_text(size=20),
    axis.text.x = element_text(size=16))+
  labs(y= "Number of dogs", x = "Time (days)") #axis labels
fig4b
```

```
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```

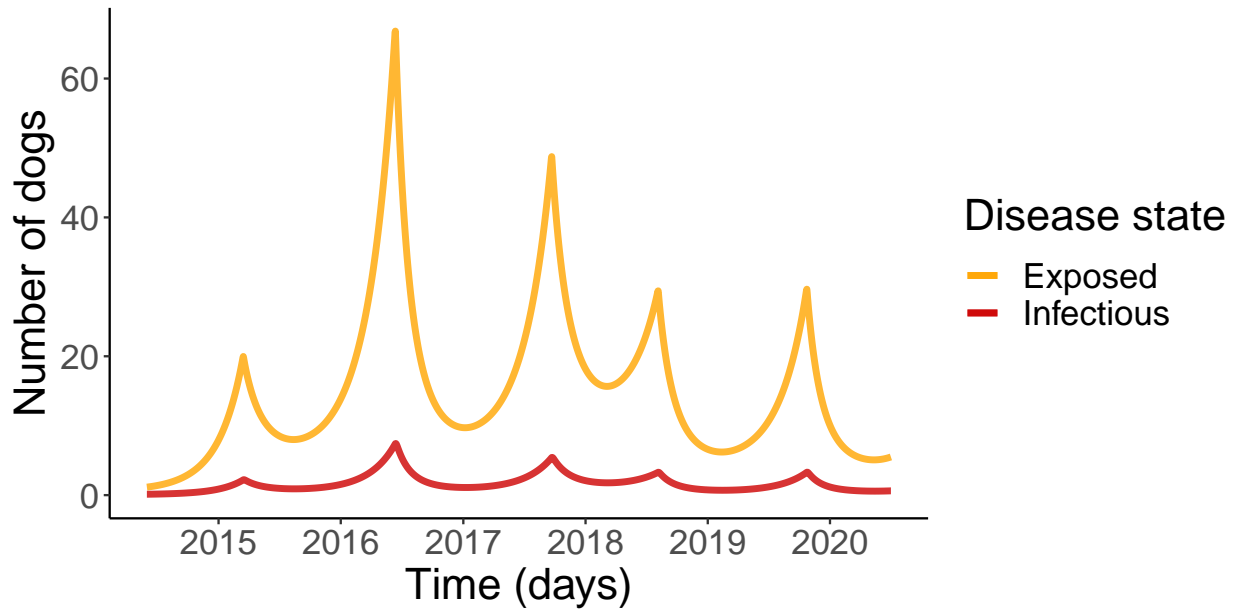



Figure 4: Simulated population dynamics from deterministic rabies model

When comparing reported cases to simulated cases assuming a 10% reporting rate, the fit seems reasonable (Figure 5). Variations can be explained by uncertainty with case reporting: rabies worldwide is underreported, especially in dogs (World Health Organization, 2013), and by population heterogeneity.

```
#Plot of incidence real vs stim
fig5 <- ggplot()+
  theme_classic()+ #white background w/ out grid
  geom_col(data = rabies, aes(x=month, y=reports, fill="Reported rabies cases", alpha="Reported rabies cases"),
  geom_col(data = rabies, aes(x=month, y=.1*stim_reports, fill="Simulated cases reported", alpha="Simulated cases reported"),
  ggtitle("Rabies cases") + #title label
  #scale_x_date(date_breaks= "2 months", date_labels="%Y", limits=c(as.Date("2014-03-16", "%Y"), as.Date("2020-03-16", "%Y")))
  scale_fill_manual(values = c(
    'Reported rabies cases' = 'red',
    'Simulated cases reported' = 'blue'),
    name= "Reported cases") +
  scale_alpha_manual(values = c(
    'Reported rabies cases' = 0.5,
    'Simulated cases reported' = 0.5),
    name= "Reported cases") +
  labs(y= "Number of reports", x = "Time (month)") #axis labels
fig5
```

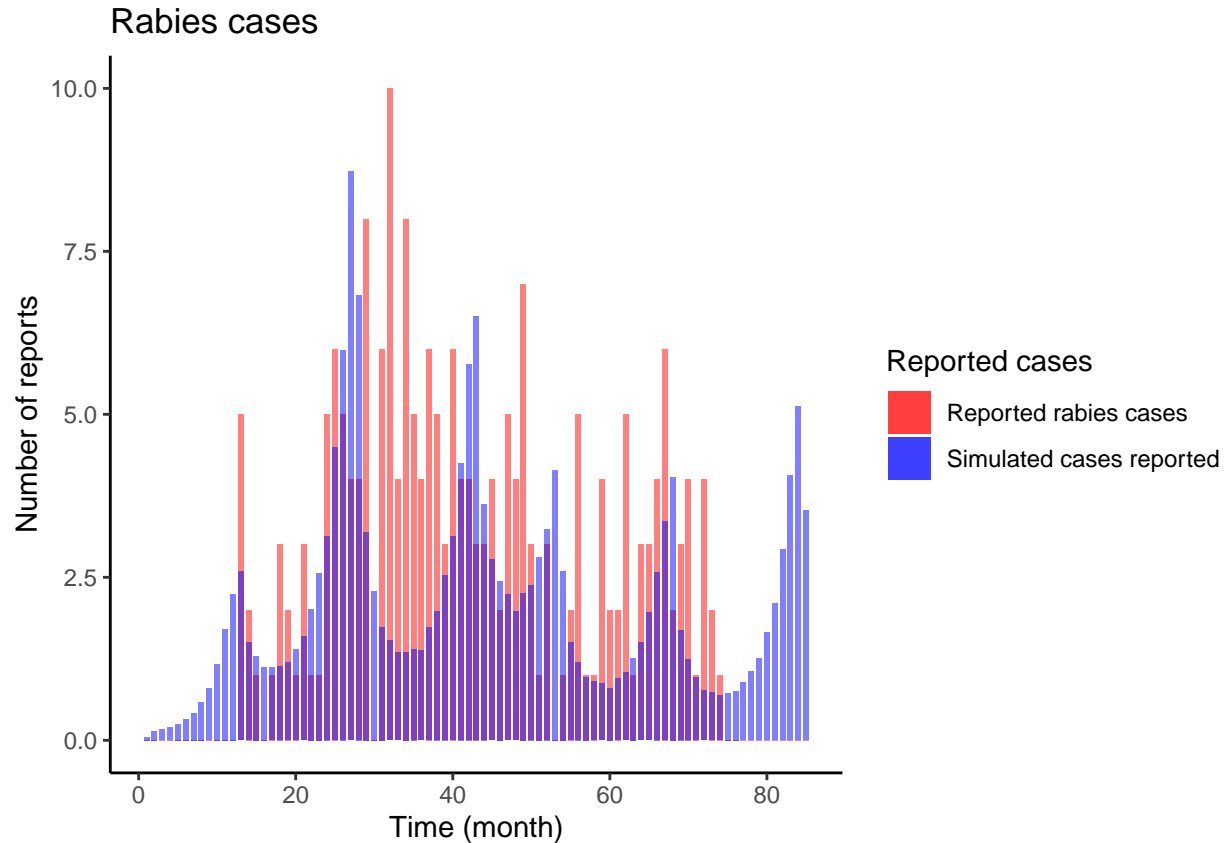


Figure 5: Observed versus simulated rabies case incidence

COVID 19 changes Due to restrictions instituted in Peru to control SARS-CoV-2 spread, there has been decreased vaccination and delayed vaccination campaigns. When investigating scenarios of how these measures effect rabies dynamics, we see a range of possibilities over a year depending on the scenario (Figure 6). When control activities are able to maintain the normal survival time (ST) of rabid dogs at 2.5 days, there are less overall cases than an increased ST of 3.7 days (Figure 6). Similarly, the higher the level of vaccination coverage, the lower the overall rabies cases over the year. In the best case scenario where control activities maintain a normal ST and vaccination coverage is optimal, canine rabies is nearly eliminated in a year (Figure 6), while in the worst case scenario with an increased ST and no vaccination coverage, rabies cases grow exponentially (Figure 6). Though it is now December and these predictions begin in March, there is still very little surveillance and subsequent case reports to be able to validate these predictions.

```
#Plot
COVID_plots <- function(RESULTS, title) {
  p.sub <-< ggplot()+
    theme_classic()+ #white background w/ out grid
    geom_line(data=RESULTS, aes(x=Date, y=out.E, color="Exposed"), size=1.5, alpha=0.8)+
    geom_line(data=RESULTS, aes(x=Date, y=out.I, color="Infectious"), size=1.5, alpha=0.8)+
    ggtitle(title) + #title label
    theme(axis.text.x = element_text(angle = 45, hjust=1))+
    scale_color_manual(values = Pal1, name= "Disease state") +
    labs(y= "Number of dogs", x = "Time (days)") #axis labels
}

COVID_plots(RESULTS2, "Optimal vax, normal ST"); C1 <- p.sub
```

```

COVID_plots(RESULTS3, "Sub-optimal vax, normal ST"); C2 <- p.sub
COVID_plots(RESULTS4, "No vax, normal ST"); C3 <- p.sub
COVID_plots(RESULTS5, "Optimal vax, incr ST"); C4 <- p.sub
COVID_plots(RESULTS6, "Sub-optimal vaX, incr ST"); C5 <- p.sub
COVID_plots(RESULTS7, "No vax, incr ST"); C6 <- p.sub

```

```

ggpubr::ggarrange(C1, C4, C2, C5, C3, C6, nrow = 3, ncol=2)

```

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```

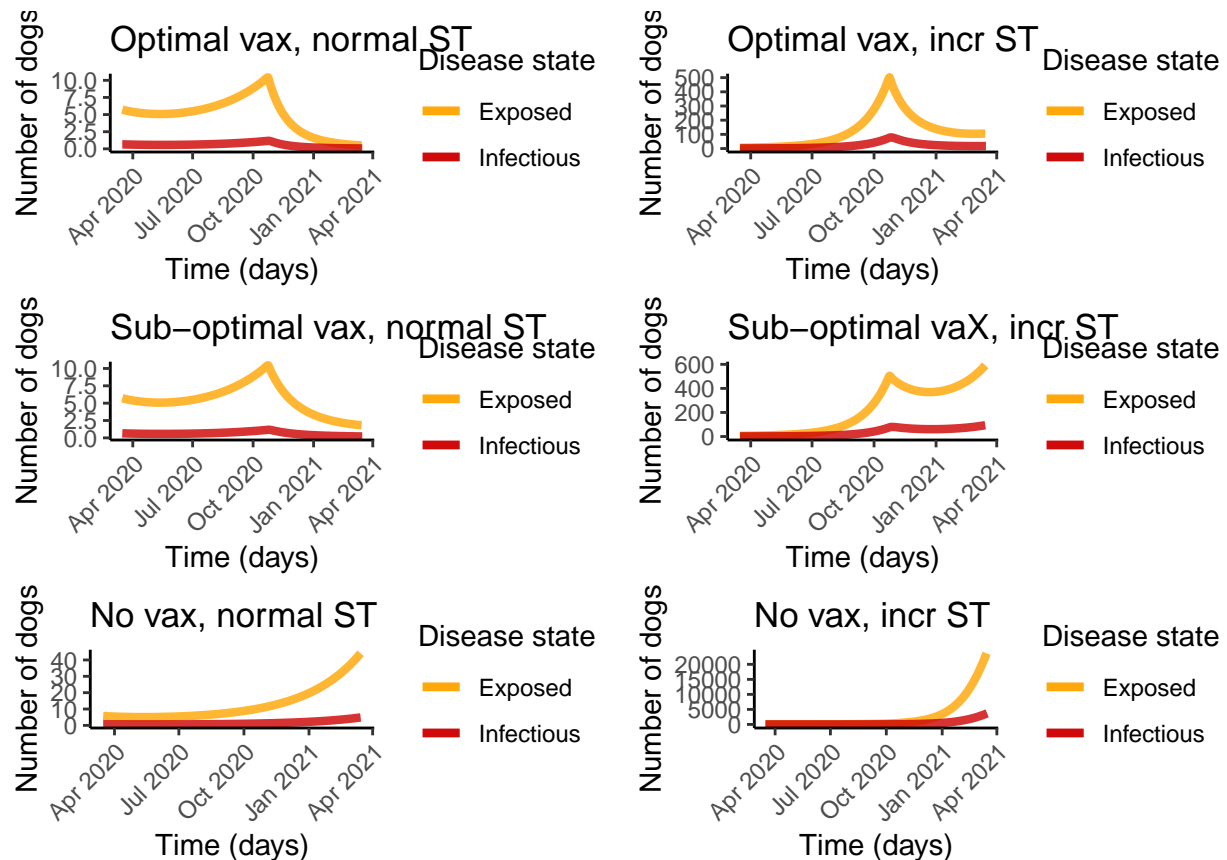


Figure 6: Simulated rabies cases for different COVID scenarios

To look at the intermediate term effects of COVID 19, we ran 5 year simulations for different scenarios:

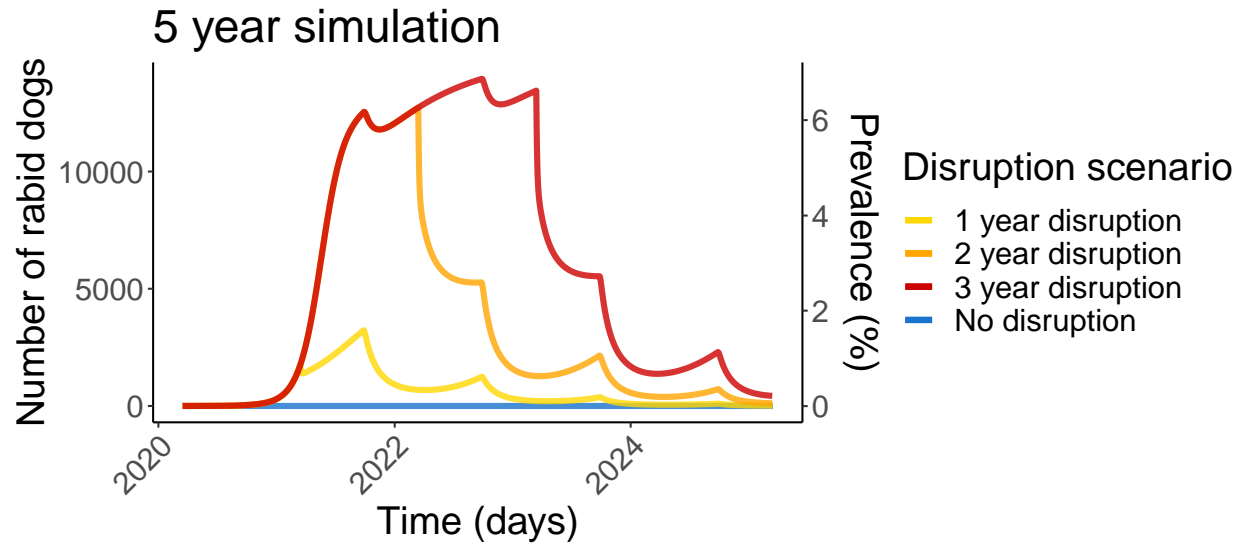
1. **Counterfactual- no disruptions**, maintained 2.5 day average survival time of rabid dogs and achieved yearly vaccination coverage of 58%
2. **1 year disruption: From March 2020-March 2021**, survival time of rabid dogs increased to 3.7d and yearly vaccination campaign reached coverage of 12.3%, before returning to pre-pandemic normal (2.5 day average survival time of rabid dogs and achieved yearly vaccination coverage of 58%)
3. **2 year disruption: From March 2020-March 2022**, survival time of rabid dogs increased to 3.7d and yearly vaccination campaign reached coverage of 12.3%, before returning to pre-pandemic normal (2.5 day average survival time of rabid dogs and achieved yearly vaccination coverage of 58%)
4. **3 year disruption: From March 2020-March 2023**, survival time of rabid dogs increased to 3.7d and yearly vaccination campaign reached coverage of 12.3%, before returning to pre-pandemic normal (2.5 day average survival time of rabid dogs and achieved yearly vaccination coverage of 58%)

```
Pal2 <- c('1 year disruption' = 'gold',
         '2 year disruption' = 'orange1',
         '3 year disruption' = 'red3',
         'No disruption' = 'dodgerblue3')
fig6 <- ggplot()+
  theme_classic()+ #white background w/ out grid
  geom_line(data=RESULTS.A, aes(x=Date, y=out.I, color="No disruption"), size=1.5, alpha=0.8)+
  geom_line(data=RESULTS.D, aes(x=Date, y=out.I, color="1 year disruption"), size=1.5, alpha=0.8)+
  geom_line(data=RESULTS.C, aes(x=Date, y=out.I, color="2 year disruption"), size=1.5, alpha=0.8)+
  geom_line(data=RESULTS.B, aes(x=Date, y=out.I, color="3 year disruption"), size=1.5, alpha=0.8)+
  ggtitle("5 year simulation") + #title label
  scale_color_manual(values = Pal2, name= "Disruption scenario") +
  scale_y_continuous(name="Number of rabid dogs",
                    sec.axis = sec_axis(trans=~.*100/params["N"], name="Prevalence (%)"))+
  theme(axis.text.x = element_text(angle = 45, hjust=1, size=16),
        text = element_text(size=20),
        axis.title.y.right = element_text(vjust=2))+
  labs(x = "Time (days)") #axis labels

fig6
```

```
## Warning: Removed 1 row(s) containing missing values (geom_path).
```

```
## Warning: Removed 1 row(s) containing missing values (geom_path).
```



References

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