Coding

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6.18

Here we do a similar thing as in Example 6.3.2. The basic main effect model is:

$$\log \frac{\pi_{ij}}{\pi_{i1}} = \beta_{j0} + \beta_{j1}s_i + \beta_{j2}g_i + \beta_{j3}z_i^O + \beta_{j4}z_i^T + \beta_{j5}z_i^G$$

For j = 2, 3, 4, 5. Here the notation is the same as in Eample 6.3.2. And g_i is the gender for alligator i. Then we fit the model:

```
library("VGAM")
Alligators = read.table("Alligators2.txt", header = TRUE)
fit <- vglm(formula = cbind(y2,y3,y4,y5,y1) ~ size + gender + factor(lake),
            family = multinomial, data = Alligators)
summary(fit)
##
## Call:
## vglm(formula = cbind(y2, y3, y4, y5, y1) ~ size + gender + factor(lake),
       family = multinomial, data = Alligators)
##
##
## Pearson residuals:
                          Min
                                   1Q
                                        Median
                                                   3Q
                                                        Max
## log(mu[,1]/mu[,5]) -1.3218 -0.4611 0.01054 0.3810 1.866
## log(mu[,2]/mu[,5]) -0.7033 -0.5751 -0.35511 0.2610 2.064
## log(mu[,3]/mu[,5]) -1.1985 -0.5478 -0.22421 0.3678 3.478
## log(mu[,4]/mu[,5]) -1.6945 -0.2893 -0.10807 1.1236 1.367
##
## Coefficients:
##
                   Estimate Std. Error z value Pr(>|z|)
## (Intercept):1
                   -2.9477
                                0.6741 -4.373 1.23e-05 ***
## (Intercept):2
                    -1.7295
                                0.7928
                                       -2.182 0.02914 *
## (Intercept):3
                    -1.1266
                                0.6696 -1.682 0.09248 .
## (Intercept):4
                    -0.9547
                                0.5295
                                        -1.803
                                               0.07138 .
                                0.4112
                                         3.250 0.00116 **
## size:1
                    1.3363
## size:2
                    -0.5570
                                0.6466
                                        -0.861
                                               0.38898
                                        -1.120
## size:3
                    -0.7302
                                0.6523
                                               0.26292
## size:4
                     0.2906
                                0.4599
                                        0.632 0.52751
                                        -1.171 0.24180
## gender:1
                    -0.4630
                                0.3955
## gender:2
                                        -0.916 0.35978
                    -0.6276
                                0.6853
                    -0.6064
## gender:3
                                0.6888
                                        -0.880 0.37867
## gender:4
                    -0.2526
                                0.4663
                                        -0.542 0.58810
## factor(lake)2:1
                     2.6937
                                0.6693
                                         4.025 5.70e-05 ***
## factor(lake)2:2
                                         1.728 0.08393
                    1.4008
                                0.8105
                                1.1923 -0.944 0.34513
## factor(lake)2:3 -1.1256
```

```
## factor(lake)2:4
                    -0.7405
                                0.7421
                                         -0.998 0.31837
                                0.6874
                                          4.272 1.94e-05 ***
## factor(lake)3:1
                     2.9363
## factor(lake)3:2
                     1.9316
                                0.8253
                                          2.340
                                                0.01926 *
## factor(lake)3:3
                                          0.782
                                                0.43415
                     0.6617
                                0.8461
## factor(lake)3:4
                     0.7912
                                0.5879
                                          1.346
                                                0.17840
                                          2.857
## factor(lake)4:1
                     1.7805
                                0.6232
                                                 0.00428 **
                                         -0.947
## factor(lake)4:2
                    -1.1295
                                1.1928
                                                 0.34369
## factor(lake)4:3
                    -0.5753
                                0.7952
                                         -0.723
                                                 0.46943
## factor(lake)4:4
                    -0.7666
                                0.5686
                                        -1.348
                                                0.17756
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Number of linear predictors:
##
## Names of linear predictors:
  log(mu[,1]/mu[,5]), log(mu[,2]/mu[,5]), log(mu[,3]/mu[,5]), log(mu[,4]/mu[,5])
##
## Residual deviance: 50.2637 on 40 degrees of freedom
##
## Log-likelihood: -73.3221 on 40 degrees of freedom
##
## Number of iterations: 5
##
## No Hauck-Donner effect found in any of the estimates
##
## Reference group is level 5 of the response
```

The residual deviance 50.2637 with df = 40 doesn't give much evidence against our model, because the p value is not small:

```
1 - pchisq(50.2637,40)
```

[1] 0.1281848

Drop size or gender will cause a significant loss while no significant loss to drop gender. But dropping gender we will get the same result as in Example 6.3.2. Therefore here we accept our original model.

We have:

$$\log \frac{\hat{\pi}_{i2}}{\hat{\pi}_{i1}} = -2.9477 + 1.3363s_2 - 0.463g_2 + 2.6937z_2^O + 2.9363z_2^T + 1.7805z_2^G$$

For a given lake and gender, for small alligators the estimated odds that primary food choice was invertebrates instead of fish are $\exp(1.3363) = 3.8$ times the estimated odds for large alligators. The estimated effect is imprecise, as the Wald 95% con dence interval is $\exp(1.3363 \pm 1.96(0.4412)) = (1.602, 9.034)$. For a given lake and size, for gender = 0 alligators the estimated odds that primary food choice was invertebrates instead of fish are $\exp(0.463) = 1.5888$ times the estimated odds for gender=1 alligators. The estimated effect is also imprecise, as the Wald 95% con dence interval is $\exp(0.463 \pm 1.96(0.3955)) = (0.7318, 3.44933)$. The lake effects indicate that the estimated odds that the primary food choice was invertebrates instead of fish are relatively higher at lakes Ocklawaha, Trafford and George than they are at Lake Hancock.

7.31

a.

We fit the model like below:

$$\log \mu_i = \beta_0 + \beta_1 x_i$$

```
Homicide = read.table("Homicide.txt", header = TRUE)
fit.poi <- glm(count ~ race, family=poisson, data=Homicide)
summary(fit.poi)
##
## Call:
## glm(formula = count ~ race, family = poisson, data = Homicide)
## Deviance Residuals:
                      Median
                                    3Q
                                            Max
                 1Q
## -1.0218 -0.4295 -0.4295 -0.4295
                                         6.1874
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) -2.38321
                            0.09713 -24.54
                                              <2e-16 ***
                1.73314
                                              <2e-16 ***
## race
                            0.14657
                                      11.82
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for poisson family taken to be 1)
##
       Null deviance: 962.80 on 1307 degrees of freedom
## Residual deviance: 844.71 on 1306 degrees of freedom
## AIC: 1122
##
## Number of Fisher Scoring iterations: 6
Then the \hat{\beta} = 1.73314 means the estimated log ratio of mean for black and white people is 1.73314.
```

b.

Maybe the time interval to collect the response for each people is not fixed but rather a random variable. Then the Poisson assumption is inadequate.

Here we fit the corresponding negative binomial model:

```
library("MASS")
fit.nb <- glm.nb(count ~ race, data=Homicide)</pre>
summary(fit.nb)
##
## Call:
## glm.nb(formula = count ~ race, data = Homicide, init.theta = 0.2023119205,
       link = log)
##
## Deviance Residuals:
                      Median
##
       Min
                 1Q
                                    3Q
                                            Max
## -0.7184 -0.3899 -0.3899 -0.3899
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
```

```
## (Intercept) -2.3832
                           0.1172 -20.335 < 2e-16 ***
                 1.7331
                           0.2385
                                    7.268 3.66e-13 ***
## race
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
  (Dispersion parameter for Negative Binomial(0.2023) family taken to be 1)
##
##
##
       Null deviance: 471.57 on 1307 degrees of freedom
## Residual deviance: 412.60 on 1306 degrees of freedom
  AIC: 1001.8
##
  Number of Fisher Scoring iterations: 1
##
##
##
##
                 Theta:
                        0.2023
##
            Std. Err.:
                        0.0409
##
   2 x log-likelihood:
                        -995.7980
```

Here, the AIC for NB2 is much smaller than that for Poisson (1001.8 vs 1122). The much larger SE(0.2385 vs 0.14657) also the estimated NB2 dispersion parameter is 1/0.2023 = 4.943 is much larger than 1. We can notice that Poisson model had overdispersion.

c.

Here we are calculating the Wald 95% CI for β . We have:

For Poisson model:

```
print(exp(1.7331+0.14657*c(qnorm(0.025),qnorm(0.975))))
## [1] 4.245366 7.541129
For Negative Binomial model:
print(exp(1.7331+0.2385*c(qnorm(0.025),qnorm(0.975))))
```

```
## [1] 3.545391 9.029991
```

Since we have enough evidence that Poisson GLM have an overdispersion, we rather believe the larger interval for $\hat{\beta}$. Also the AIC shows that NB GLM is a better model, so we choose (3.5,9.0) to be our CI.

overdispersion

The only thing we need to do is to estimate the overdispersion term σ^2 for $var(Y_i) = \sigma^2 \mu_i$.

We have:

```
n = length(Homicide$0bs)
p = 1
sigma_2 = 1 / (n-p) * sum((Homicide$count - fitted(fit.poi))^2 / fitted(fit.poi))
sigma_2
```

```
## [1] 1.744356
```

Therefore the ture estimate variance for $\hat{\beta}$ is 0.14657 * 1.744356 = 0.2556703. So the CI is print(exp(1.7331+0.2556703*c(qnorm(0.025),qnorm(0.975))))

```
## [1] 3.428063 9.339050
```

10.

(i)

For the question one, if the books are consistent, than they follow the main effect model as:

$$\log \mu_{i} = \beta_{0} + \beta_{1}b_{i}^{SI} + \beta_{2}b_{i}^{SS} + \eta_{1}w_{i}^{an} + \eta_{2}w_{i}^{that} + \eta_{3}w_{i}^{this} + \eta_{4}w_{i}^{with} + \eta_{5}w_{i}^{without}$$

Here μ_i is the mean count for i^{th} data. $b_i^{()}, w_i^{()}$ are the flag for book and word. If this model holds, then the relative appearence (ratio of mean) for each word is $\eta_i - \eta_j$ ($\eta_0 = 0$ for word a) which does not influenced by the book flag β_i . So the books are consistent. Therefore we compare this model with the full model to make the decision.

```
library(tidyverse)
Jane = read_csv("Ex0205.csv")
Jane_herself = Jane %>% filter(Book != "SanditonII")
fit.jane11.full = glm(Count ~ Book:Word, family=poisson, data=Jane_herself)
fit.jane11.homo = glm(Count ~ factor(Book) + factor(Word),
                      family=poisson, data=Jane_herself)
summary(fit.jane11.homo)
##
## Call:
  glm(formula = Count ~ factor(Book) + factor(Word), family = poisson,
       data = Jane_herself)
##
##
##
  Deviance Residuals:
        Min
                   1Q
                         Median
                                       3Q
                                                Max
  -1.71399
                        0.00187
            -0.48124
                                  0.49657
                                            1.55116
##
## Coefficients:
##
                                 Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                  5.23521
                                             0.05995 87.331 < 2e-16 ***
## factor(Book)SanditonI
                                 -0.77851
                                             0.08499
                                                      -9.160
                                                              < 2e-16 ***
## factor(Book)Sense&Sensibility -0.15985
                                             0.07028
                                                      -2.274
                                                                0.0229 *
## factor(Word)an
                                 -1.94591
                                             0.13577 -14.333
                                                              < 2e-16 ***
## factor(Word)that
                                 -0.60921
                                             0.08088 -7.532 4.98e-14 ***
## factor(Word)this
                                 -1.61870
                                             0.11803 - 13.714
                                                              < 2e-16 ***
## factor(Word)with
                                 -0.99164
                                             0.09228 -10.746
                                                              < 2e-16 ***
## factor(Word)without
                                 -2.43546
                                             0.16917 -14.396 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
  (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 709.289
                               on 17 degrees of freedom
## Residual deviance: 12.587
                               on 10 degrees of freedom
## AIC: 127.34
##
## Number of Fisher Scoring iterations: 4
```

Then we find that the AIC for main effect model is less than that of full model (127.34 vs 134.76). Also the residul devience for main effect model is 12.587 with df=10, which has a p value of 0.2476881, no significant loss. So we may choose the main effect model, which means that the books are consistent.

For the question two, we also compare the main effect model:

```
\log \mu_{i} = \beta_{0} + \beta_{1} o_{i} + \eta_{1} w_{i}^{an} + \eta_{2} w_{i}^{that} + \eta_{3} w_{i}^{this} + \eta_{4} w_{i}^{with} + \eta_{5} w_{i}^{without}
```

with the full model, where here the o_i is the flag for whether the book is written by Jane. Then we have:

```
Jane compare = Jane %>%
                mutate(Original = (Book != "SanditonII"))
fit.jane12.full <- glm(Count ~ Original:Word,
                       family = poisson, data = Jane_compare)
fit.jane12.homo <- glm(Count ~ factor(Original) + factor(Word),</pre>
                       family = poisson, data = Jane_compare)
summary(fit.jane12.full)
##
## Call:
## glm(formula = Count ~ Original:Word, family = poisson, data = Jane_compare)
## Deviance Residuals:
      Min
                 1Q
                      Median
                                   3Q
                                           Max
                               1.1977
## -5.2455 -0.7782
                      0.0000
                                        3.2897
##
## Coefficients: (1 not defined because of singularities)
##
                             Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                               2.5390
                                          0.1622 15.651 < 2e-16 ***
## OriginalFALSE:Worda
                               1.8799
                                          0.1959
                                                   9.598 < 2e-16 ***
## OriginalTRUE:Worda
                               2.4355
                                          0.1692 14.396 < 2e-16 ***
## OriginalFALSE:Wordan
                               0.8283
                                          0.2466
                                                   3.359 0.000781 ***
## OriginalTRUE:Wordan
                               0.4895
                                          0.2060
                                                   2.376 0.017492 *
## OriginalFALSE:Wordthat
                               0.5521
                                          0.2679
                                                   2.061 0.039329 *
## OriginalTRUE:Wordthat
                                          0.1748 10.448 < 2e-16 ***
                              1.8262
                                                   0.554 0.579253
## OriginalFALSE:Wordthis
                               0.1691
                                          0.3049
## OriginalTRUE:Wordthis
                               0.8168
                                          0.1948
                                                   4.193 2.75e-05 ***
## OriginalFALSE:Wordwith
                              1.2222
                                          0.2226
                                                   5.490 4.03e-08 ***
## OriginalTRUE:Wordwith
                               1.4438
                                          0.1804
                                                   8.006 1.19e-15 ***
                                                  -2.193 0.028319 *
## OriginalFALSE:Wordwithout -1.1527
                                          0.5257
## OriginalTRUE:Wordwithout
                                   NA
                                              NA
                                                      NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for poisson family taken to be 1)
##
       Null deviance: 878.86 on 23 degrees of freedom
## Residual deviance: 108.60 on 12 degrees of freedom
## AIC: 261.19
##
## Number of Fisher Scoring iterations: 4
summary(fit.jane12.homo)
##
## Call:
## glm(formula = Count ~ factor(Original) + factor(Word), family = poisson,
##
       data = Jane_compare)
##
## Deviance Residuals:
```

```
Median
##
                 10
                                   30
                                           Max
## -4.5646
                      0.0266
           -1.5535
                               1.7490
                                        3.6245
##
## Coefficients:
##
                        Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                         4.42531
                                    0.07882 56.148 < 2e-16 ***
## factor(Original)TRUE
                        0.54789
                                    0.07801
                                              7.023 2.16e-12 ***
## factor(Word)an
                        -1.73718
                                    0.11368 -15.281
                                                     < 2e-16 ***
## factor(Word)that
                        -0.69508
                                    0.07622
                                            -9.119
                                                     < 2e-16 ***
## factor(Word)this
                        -1.63292
                                    0.10879 - 15.010
                                                     < 2e-16 ***
## factor(Word)with
                        -0.92992
                                    0.08268 -11.247
                                                     < 2e-16 ***
                                    0.16045 -15.646 < 2e-16 ***
## factor(Word)without
                       -2.51037
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
                                     degrees of freedom
##
       Null deviance: 878.86 on 23
## Residual deviance: 140.34 on 17 degrees of freedom
## AIC: 282.92
##
## Number of Fisher Scoring iterations: 4
```

Now the residual deviance is 140.34-108.6=31.74 with df=17-12=5. So the p value is 6.688744e-06, there is a significant difference between the style of Jane and the ghost writer.

For question three, the model is the same as in question two. But the data for Jane here only contains Santiton!

```
SantitonI:
Jane_s12 = Jane \%
            filter(Book=="SanditonI" | Book=="SanditonII")
fit.jane13.full <- glm(Count ~ factor(Book):factor(Word),</pre>
                        family = poisson, data = Jane_s12)
fit.jane13.homo <- glm(Count ~ factor(Book) + factor(Word),</pre>
                        family = poisson, data = Jane_s12)
summary(fit.jane13.homo)
##
## Call:
  glm(formula = Count ~ factor(Book) + factor(Word), family = poisson,
       data = Jane s12)
##
## Deviance Residuals:
##
          1
                    2
                               3
                                         4
                                                    5
                                                              6
##
    0.77745
             -2.26305
                       -0.05810
                                   1.24308
                                            -1.39358
                                                        1.02240 -0.81138
##
          8
                    9
                                        11
                              10
                                   1.31126
##
    1.95671
              0.05868 -1.36807
                                            -1.19731
##
## Coefficients:
##
                           Estimate Std. Error z value Pr(>|z|)
                                       0.08873 51.131 < 2e-16 ***
## (Intercept)
                            4.53675
## factor(Book)SanditonII -0.03015
                                       0.10026 -0.301
                                                           0.764
## factor(Word)an
                           -1.52606
                                       0.17445 -8.748 < 2e-16 ***
## factor(Word)that
                                                -7.602 2.91e-14 ***
                           -1.13740
                                       0.14961
## factor(Word)this
                           -1.81374
                                       0.19690 -9.212 < 2e-16 ***
## factor(Word)with
                           -0.95226
                                       0.13971 -6.816 9.37e-12 ***
```

We get a residual deviance of 19.777 with df=5, therefore a p value of 0.001376036, still a significant loss. So the ghost writer didn't follow the style in SanditonI.

(ii)

For the first question, we build the Multinormal model like this:

$$\log \frac{\pi_{ij}}{\pi_{i1}} = \beta_{0j} + \beta_{1j}b_i^{SI} + \beta_{2j}b_i^{SS}$$

Where π_{ij} is the probability for j^{th} word in i^{th} data, $b_i^{()}$ are the flags for book name

Then we fit the model:

Call:

```
## vglm(formula = cbind(an, that, this, with, without, a) ~ factor(Book),
##
       family = multinomial, data = Jane_herself_2)
##
##
## Coefficients:
                                    Estimate Std. Error z value Pr(>|z|)
##
## (Intercept):1
                                   -1.967650
                                               0.209375 -9.398 < 2e-16 ***
## (Intercept):2
                                   -0.571786
                                               0.122066 -4.684 2.81e-06 ***
## (Intercept):3
                                   -1.562185
                                               0.176117 -8.870 < 2e-16 ***
## (Intercept):4
                                   -0.921682
                                               0.137440 -6.706 2.00e-11 ***
                                   -2.923162
                                               0.324617 -9.005 < 2e-16 ***
## (Intercept):5
## factor(Book)SanditonI:1
                                   -0.249575
                                               0.380326 -0.656
                                                                  0.5117
## factor(Book)SanditonI:2
                                   -0.432416
                                               0.227658 - 1.899
                                                                  0.0575 .
## factor(Book)SanditonI:3
                                   -0.344885
                                               0.328002 -1.051
                                                                  0.2930
## factor(Book)SanditonI:4
                                   -0.361234
                                               0.253979 - 1.422
                                                                  0.1549
## factor(Book)SanditonI:5
                                    0.610626
                                               0.463980
                                                                  0.1882
                                                          1.316
## factor(Book)Sense&Sensibility:1 0.196093
                                               0.301066
                                                          0.651
                                                                  0.5148
## factor(Book)Sense&Sensibility:2 0.124649
                                               0.179837
                                                          0.693
                                                                  0.4882
## factor(Book)Sense&Sensibility:3 0.037488
                                               0.262812
                                                          0.143
                                                                  0.8866
```

```
## factor(Book)Sense&Sensibility:4 0.008786
                                              0.206499
                                                                 0.9661
                                                         0.043
## factor(Book)Sense&Sensibility:5 0.823101
                                              0.409554
                                                                 0.0445 *
                                                         2.010
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Number of linear predictors: 5
##
## Names of linear predictors:
## log(mu[,1]/mu[,6]), log(mu[,2]/mu[,6]), log(mu[,3]/mu[,6]), log(mu[,4]/mu[,6]), log(mu[,5]/mu[,6])
## Residual deviance: -6.628e-14 on 0 degrees of freedom
##
## Log-likelihood: -37.9598 on 0 degrees of freedom
##
## Number of iterations: 4
## Warning: Hauck-Donner effect detected in the following estimate(s):
  '(Intercept):5'
## Reference group is level 6 of the response
```

We notice that the estimate $\hat{\beta}_{1j}$ and $\hat{\beta}_{2j}$ are mostly not significant away from zero(see the p value), which means for many words the ratio of odds between different book is not significant away from one. Therefore we can regard a consistence between Jane's writing.

For the second question, we build model like this:

$$\log \frac{\pi_{ij}}{\pi_{i1}} = \beta_{0j} + \beta_{1j}o_i$$

Where o_i is the flag for i^{th} whether or not belong to Jane.

Then we fit the model:

```
Jane_compare_2 = Jane %>%
                mutate(Original = (Book != "SanditonII")) %>%
                spread(Word, Count)
fit.jane22 <- vglm(formula = cbind(an,that,this,with,without,a) ~ Original,</pre>
            family = multinomial, data = Jane_compare_2)
summary(fit.jane22)
##
   vglm(formula = cbind(an, that, this, with, without, a) ~ Original,
##
       family = multinomial, data = Jane_compare_2)
##
##
## Pearson residuals:
     log(mu[,1]/mu[,6]) log(mu[,2]/mu[,6]) log(mu[,3]/mu[,6])
##
             -1.113e-01
                                  3.593e-01
## 1
                                                      3.476e-01
## 2
             -6.924e-01
                                 -1.873e+00
                                                     -8.495e-01
             -1.542e-16
                                                      7.619e-16
## 3
                                  9.135e-16
## 4
              6.287e-01
                                  9.858e-01
                                                      2.470e-01
     log(mu[,4]/mu[,6]) log(mu[,5]/mu[,6])
## 1
              5.860e-01
                                 -1.549e+00
## 2
             -1.103e+00
                                  6.159e-01
## 3
             -1.995e-16
                                 -3.643e-17
```

```
## 4
              1.747e-01
                                 1.226e+00
##
## Coefficients:
##
                  Estimate Std. Error z value Pr(>|z|)
## (Intercept):1
                 -1.05154
                              0.21571
                                      -4.875 1.09e-06 ***
## (Intercept):2 -1.32780
                              0.23980 -5.537 3.07e-08 ***
## (Intercept):3
                 -1.71079
                              0.28056 -6.098 1.08e-09 ***
## (Intercept):4
                 -0.65764
                              0.18789
                                       -3.500 0.000465 ***
## (Intercept):5
                 -3.03255
                              0.51191
                                       -5.924 3.14e-09 ***
## OriginalTRUE:1 -0.89437
                              0.25488
                                      -3.509 0.000450 ***
## OriginalTRUE:2 0.71859
                              0.25307
                                        2.839 0.004519 **
## OriginalTRUE:3 0.09209
                              0.30438
                                        0.303 0.762225
## OriginalTRUE:4 -0.33400
                              0.20933
                                      -1.596 0.110587
## OriginalTRUE:5 0.59709
                              0.53914
                                       1.107 0.268082
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Number of linear predictors: 5
##
## Names of linear predictors:
## log(mu[,1]/mu[,6]), log(mu[,2]/mu[,6]), log(mu[,3]/mu[,6]), log(mu[,4]/mu[,6]), log(mu[,5]/mu[,6])
## Residual deviance: 12.5873 on 10 degrees of freedom
##
## Log-likelihood: -55.6109 on 10 degrees of freedom
##
## Number of iterations: 4
##
## Warning: Hauck-Donner effect detected in the following estimate(s):
## '(Intercept):5'
##
## Reference group is level 6 of the response
```

Here we can see some significant value for β_{1j} (see the p value). For this result we can say that compared to the ghost writer Jane used less an and more that (the estimated odds ratio for an and that between two writer based on a is $\exp(-0.89437)=0.4089$ and $\exp(0.71859)=2.05154$), and no significant difference for other words (based on the odds). Therefore we can say that the ghost writer didn't strictly follow Jane's pattern.

For the third question, the model is same as in second question, but now Jane's data only contains the book SanditonI We fit the model.

```
## (Intercept):1
                     -2.2172
                                 0.3175 -6.983 2.88e-12 ***
## (Intercept):2
                     -1.0042
                                        -5.226 1.74e-07 ***
                                 0.1922
                     -1.9071
                                         -6.892 5.50e-12 ***
## (Intercept):3
                                 0.2767
                     -1.2829
## (Intercept):4
                                 0.2136
                                         -6.007 1.89e-09 ***
## (Intercept):5
                     -2.3125
                                 0.3315
                                         -6.976 3.04e-12 ***
                                 0.3839
                                                0.00239 **
## BookSanditonII:1
                     1.1657
                                          3.037
## BookSanditonII:2
                    -0.3236
                                 0.3073
                                         -1.053
                                                 0.29232
## BookSanditonII:3
                     0.1963
                                 0.3941
                                          0.498
                                                 0.61842
## BookSanditonII:4
                     0.6253
                                 0.2845
                                          2.198
                                                0.02794 *
## BookSanditonII:5 -0.7200
                                 0.6099 -1.181 0.23777
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Number of linear predictors:
##
## Names of linear predictors:
## log(mu[,1]/mu[,6]), log(mu[,2]/mu[,6]), log(mu[,3]/mu[,6]), log(mu[,4]/mu[,6]), log(mu[,5]/mu[,6])
## Residual deviance: -3.297e-14 on 0 degrees of freedom
## Log-likelihood: -22.8086 on 0 degrees of freedom
##
## Number of iterations: 7
##
## No Hauck-Donner effect found in any of the estimates
## Reference group is level 6 of the response
```

The result is similar to question 2. We can see some significant value for β_{1j} (see the p value). We can say that compared to the SanditonI, the ghost writer used more an and more with (the estimated odds ratio for an and with between two writer based on a is $\exp(1.1657)=3.208$ and $\exp(0.6253)=1.8688$), and no significant difference for other words (based on the odds). Therefore we can say this ghost writer's work is not good.