

Set up an analysis of variance table for the following two-way design results: per acre production data for three varieties of wheat. Also state whether variety difference are significant at 5% level (Given that  $F_{2,6}=5.14$  and  $F_{3,6}=4.76$ )

Per acre production data

Plot of land	Variety of wheat		
	A	B	C
1	6	5	5
2	7	5	4
3	3	3	3
4	8	7	4

Solution:

	A	B	C	Total
1	6	5	5	36
2	7	5	4	16
3	3	3	3	9
4	8	7	4	19
Total	24	20	16	60

$A^2$	$B^2$	$C^2$	
36	25	25	
49	25	16	
9	9	9	
64	49	16	
158	108	66	$332 = \sum X^2$

I. Sum of all observations

$$T = 24 + 20 + 16 = 60$$

$$n = \sum n_i = 4 + 4 + 4 = 12$$

$$\text{Corrector factor} = (T)^2/n = (60)^2/12 = 300$$

II. Total SS

$$\sum X^2 - (T)^2/n = 332 - 300 = 32$$

III. SS between columns

$$\sum(T_j)^2/n_j - (T)^2/n = (24)^2 + (20)^2 + (16)^2/4 - 300 = 308 - 300 = 8$$

IV. SS between rows

$$\sum(T_i)^2/n_i - (T)^2/n = (16)^2 + (16)^2 + (9)^2 + (19)^2/3 - 300 = 318 - 300 = 18$$

V. SS residual = Total SS - (SS between columns + SS between rows)

$$32 - (8 + 18) = 32 - 26 = 6$$

VI.

Source Of Variance	Sum Of Sqaures	Degree Of Freedom	Mean Sqaure Value(MS)	F-ratio Value
Between Columns	8	c-1= (3-1)=2	SSB(columns)/ c-1=8/2=4	MSC(column)/MSR=4/1= 4<5.14 (F2,6)
Between Rows	18	r-1= (4-1)=3	SSB(rows)/ r-1=18/3=6	MSR(rows)/MSR=6/1= 6>4.76 (F3,6)
Residual or error	6	(c-1)(r-1) =(3)(2)=6	SSresidual/ (c-1)(r-1)= 6/6=1	
Total	32			

From the ANOVA we conclude that the variety of wheat of F(2,6) is insignificant as the calculated ratio 4 is less than 5.14.

Whereas, the variety of wheat of F(3,6) is significant as the calculated ratio 6 is greater than 4.76.