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Subject :- Statistics DSE - I Regression Analysis

Assignment Topic :- Insurance cost prediction

Subject-in-charge :- Prof. Ashish Mhatre

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Problem Statement:-

Predicting insurance cost of an individual based on his/her age, sex, BMI, etc.

The dataset was downloaded from Kaggle. Here is the link to the dataset:- https://www.kaggle.com/mirichoi0218/insurance (Medical costs personal dataset).

Table of Content:

Describing the data: No. of rows, columns etc.

Looking for Missing Values.

EDA (Univariate and Bivariate analysis)

Feature engineering.

Feature Scaling.

Fitting an initial model.

Analysis of the fitted model (ANOVA).

Feature selection based on the initial fitted model.

Fitting the final multiple linear regression model.

Checking important assumptions: Residual analysis, Homoscedasticity, Autocorrelation, Multi-Collinearity analysis.

Real-time prediction from the model.

Bird's eye view of dataset

There are 1338 rows and 7 columns in the dataset. The below figure shows the datatypes of all the variables.

	age	sex	bmi	children	smoker	region	charges
0	19	female	27.900	0	yes	southwest	16884.92400
1	18	male	33.770	1	no	southeast	1725.55230
2	28	male	33.000	3	no	southeast	4449.46200
3	33	male	22.705	0	no	northwest	21984.47061
4	32	male	28.880	0	no	northwest	3866.85520

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 1338 entries, 0 to 1337
Data columns (total 7 columns):

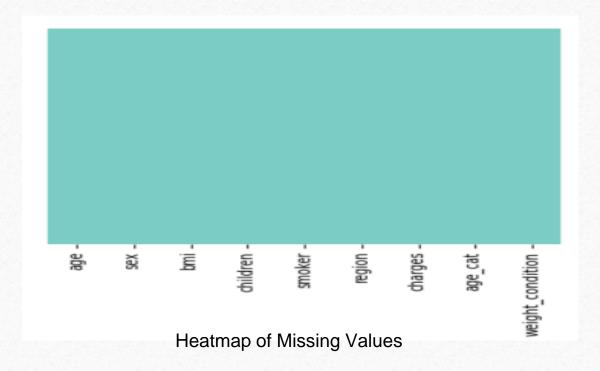
#	Column	Non-N	Null Count	Dtype				
0	age	1338	non-null	int64				
1	sex	1338	non-null	object				
2	bmi	1338	non-null	float64				
3	children	1338	non-null	int64				
4	smoker	1338	non-null	object				
5	region	1338	non-null	object				
6	charges	1338	non-null	float64				
dtyp	es: float6	4(2),	int64(2),	object(3)				
memory usage: 73.3+ KB								

Summary of numerical & categorical columns.

	age	bmi	children	charges
count	1338.000000	1338.000000	1338.000000	1338.000000
mean	39.207025	30.663397	1.094918	13270.422265
std	14.049960	6.098187	1.205493	12110.011237
min	18.000000	15.960000	0.000000	1121.873900
25%	27.000000	26.296250	0.000000	4740.287150
50%	39.000000	30.400000	1.000000	9382.033000
75%	51.000000	34.693750	2.000000	16639.912515
max	64.000000	53.130000	5.000000	63770.428010

	sex	smoker	region
count	1338	1338	1338
unique	2	2	4
top	male	no	southeast
freq	676	1064	364

Missing Value Analysis:



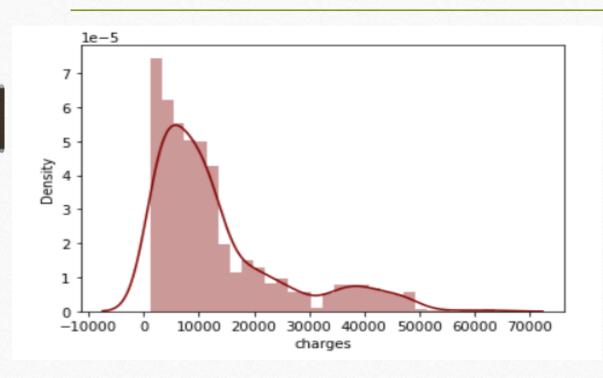
The above heatmap signifies absence of missing values.

```
df.isnull().sum()

age 0
sex 0
bmi 0
children 0
smoker 0
region 0
charges 0
dtype: int64
```

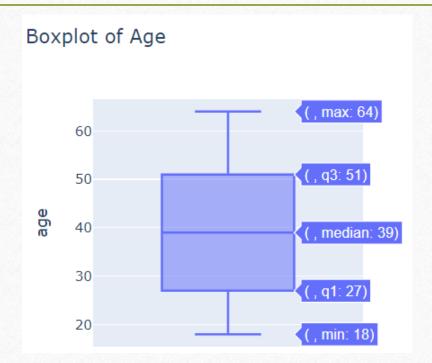
Exploratory Data Analysis (EDA)

Univariate Analysis:-



Plot of Charges

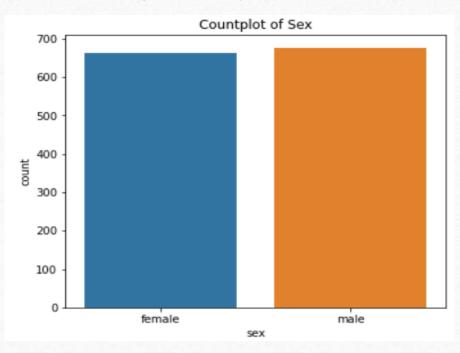
By just looking at the plot, we can figure out that "charges" which is our dependent variable has a right-skewed distribution with some extreme values of more than 60k.



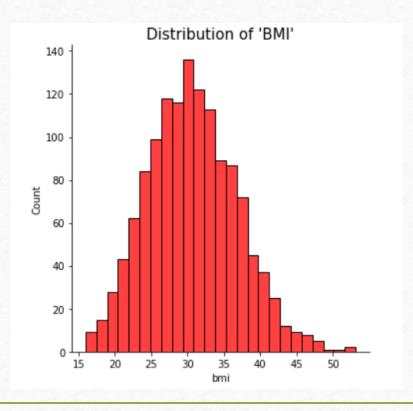
The figure on the right, shows the counts of male and female respondents in the dataset. The two classes are well balanced.

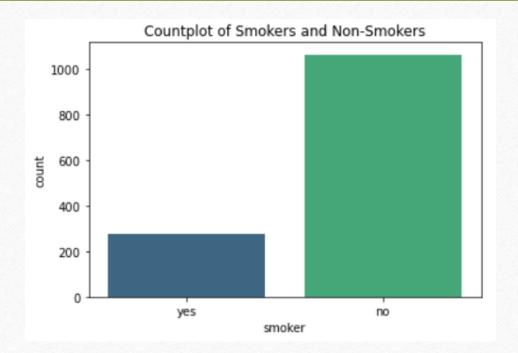
The figure on the left shows the boxplot of 'age'. Some important features are:-

- Max age is 64 yrs.
- Median age is 39 yrs.
- Min age is 18 yrs.
- Standard deviation of age is 14.15 yrs.

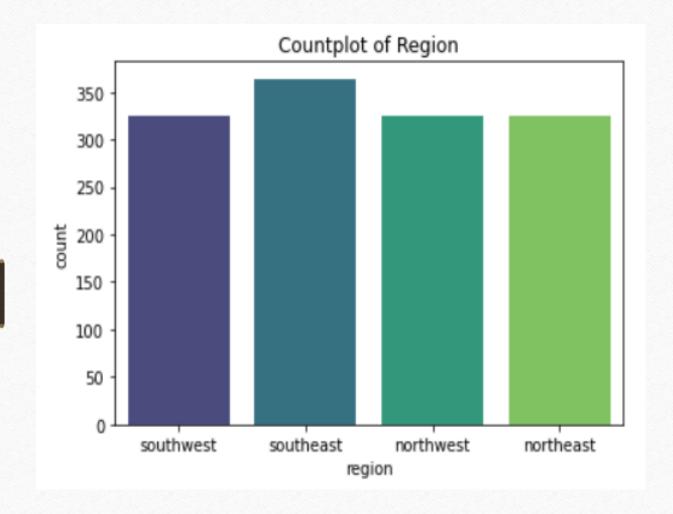


The figure on the right shows the count plot (Plot of counts) of smokers. There is a big imbalance among smokers and non-smokers in our dataset.





The figure on the left shows the distribution of 'BMI'. By looking at the plot it seems like 'BMI' is normally distributed with mean somewhere around 32.



```
df["region"].value_counts()
```

southeast 364 southwest 325 northwest 325 northeast 324

Name: region, dtype: int64

The counts for each class in the region column is almost the same, except for region southeast.

Creating additional variables from predefined variables:

Before moving onto the bivariate analysis, we will create some additional variables which will further help us in enhanced analysis.

Creating 2 new categorical features like 'weight_condition' and 'age_cat' from existing features like 'age' and 'bmi' with their respective code in python.

```
df["weight_condition"] = np.nan
lst = [df]

for col in lst:
    col.loc[col["bmi"] < 18.5, "weight_condition"] = "Underweight"
    col.loc[(col["bmi"] >= 18.5) & (col["bmi"] < 24.986), "weight_condition"] = "Normal Weight"
    col.loc[(col["bmi"] >= 25) & (col["bmi"] < 29.926), "weight_condition"] = "Overweight"
    col.loc[col["bmi"] >= 30, "weight_condition"] = "Obese"
```

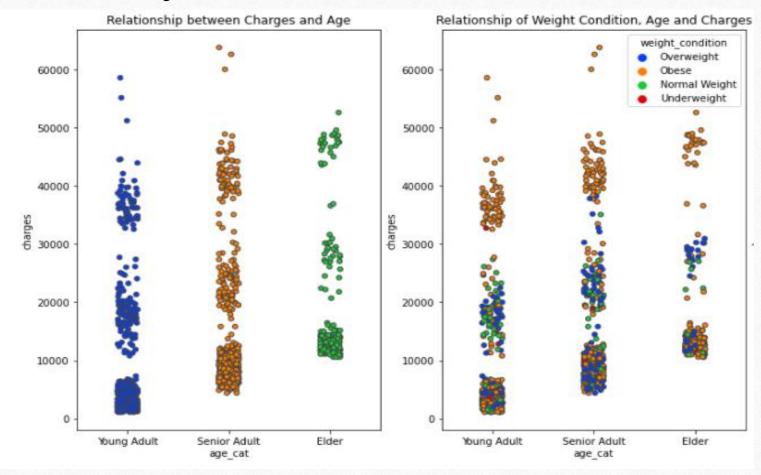
```
df['age_cat'] = np.nan
lst = [df]

for col in lst:
    col.loc[(col['age'] >= 18) & (col['age'] <= 35), 'age_cat'] = 'Young Adult'
    col.loc[(col['age'] > 35) & (col['age'] <= 55), 'age_cat'] = 'Senior Adult'
    col.loc[col['age'] > 55, 'age_cat'] = 'Elder'
```

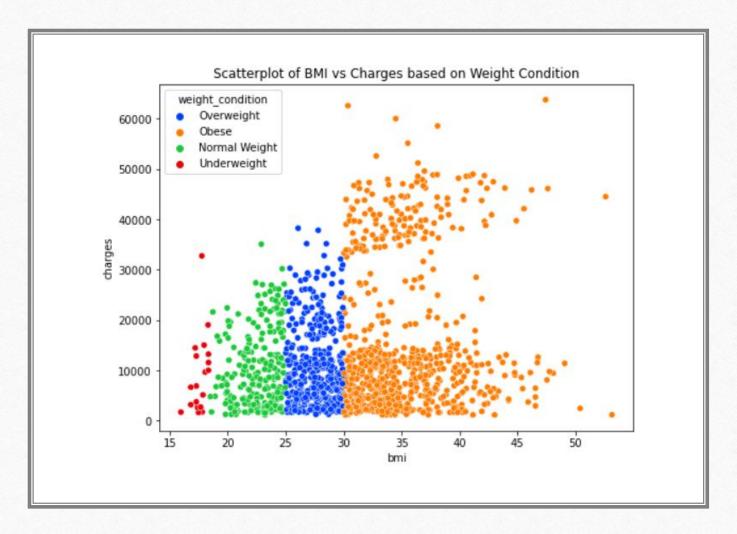
Visualizing the dataset with the new added variables:

	age	sex	bmi	children	smoker	region	charges	age_cat	weight_condition
0	19	female	27.900	0	yes	southwest	16884.92400	Young Adult	Overweight
1	18	male	33.770	1	no	southeast	1725.55230	Young Adult	Obese
2	28	male	33.000	3	no	southeast	4449.46200	Young Adult	Obese
3	33	male	22.705	0	no	northwest	21984.47061	Young Adult	Normal Weight
4	32	male	28.880	0	no	northwest	3866.85520	Young Adult	Overweight

Bivariate Analysis:

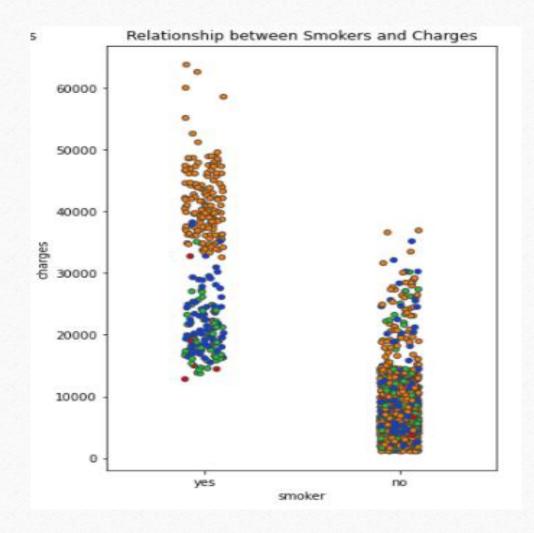


• From fig 1. we can observe that elder people have higher cost. Similarly in fig 2. it is clear that among all the age categories, obese people are paying much higher insurance costs then other weight conditions.



Relationship between 'Weight Conditions' and 'Charges'.

• The above plot confirms that, obese people pay much higher insurance cost then all the other categories.



Relationship between 'Smokers' and 'charges' paid.

• In the above figure, we can observe that smoker's in general are paying much higher insurance costs and non-smokers.

For further analysis, let's check the charges paid by an 'obese smoker' vs 'obese non-smoker'.

Deeper Look into Obese condition by Smoking status



The figure on the left suggests that, on an average the **median** insurance **cost paid** by an **obese smoker** is **30k more** than that of an **obese non-smoker**. That's great for an analysis!!

Feature Engineering:

Data Transformation:-

The table on the right shows the sample of our original dataset. We can figure out that the 'sex' and the "smoker" columns consists of **binary nominal object** type values. So, in this step we will convert these nominal values into **0s** and **1s**.

But why are we converting the 'text' or 'object' type values present in 'sex' and 'smoker' column into 0s and 1s?

	age	sex	bmi	children	hildren smoker region		charges	
0	19	female	27.900	0	yes	southwest	16884.92400	
1	18	male	33.770	1	no	southeast	1725.55230	
2	28	male	33.000	3	no	southeast	4449.46200	
3	33	male	22.705	0	no	northwest	21984.47061	
4	32	male	28.880	0	no	northwest	3866.85520	

The simple answer is: Our regression model cannot interpret text data. And since the data values present in this columns are of nominal type we will replace them with 0s and 1s.

Python code for transforming 'sex' and 'smoker' columns.

```
df["smoker"] = df["smoker"].replace({"yes":1, "no": 0})
df["sex"] = df["sex"].replace({"female": 0, "male": 1})
```

Let's take a look at the dataset after the transformation.

	age	sex	bmi	children	smoker	region	charges
0	19	0	27.900	0	1	southwest	16884.92400
1	18	1	33.770	1	0	southeast	1725.55230
2	28	1	33.000	3	0	southeast	4449.46200
3	33	1	22.705	0	0	northwest	21984.47061
4	32	1	28.880	0	0	northwest	3866.85520

One-hot Encoding the 'region' column:

We will now perform **One-hot Encoding** on the '**region**' column.

So, what is **One-hot Encoding**?

One hot encoding is a process by which categorical variables are converted into numeric form.

When we apply one-hot encoding to the 'region' column, we will get additional columns known as dummy variables of 0s and 1s for each distinct value in the 'region' column.

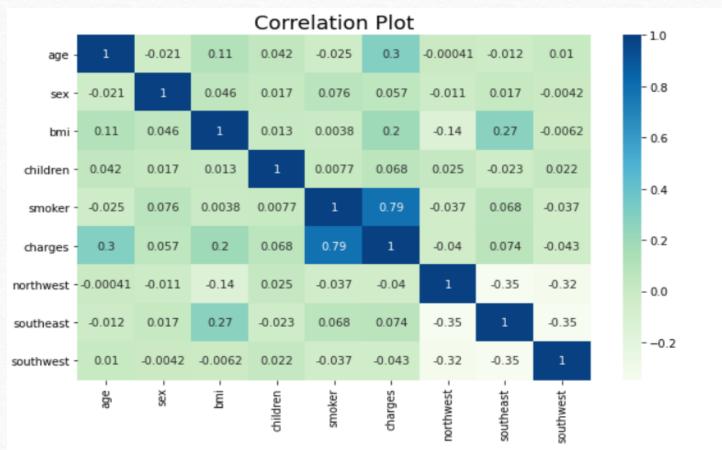
Notice that we miss a column for 'northeast' in our dataset. So, 'northeast' column was dropped from our analysis to avoid the famous concept of dummy variable trap.

df["region"].	value_counts()
southeast	364
northwest	325
southwest	325
northeast	324
Name: region,	, dtype: int64

	age	sex	bmi	children	smoker	charges	northwest	southeast	southwest
0	19	0	27.900	0	1	16884.92400	0	0	1
1	18	1	33.770	1	0	1725.55230	0	1	0
2	28	1	33.000	3	0	4449.46200	0	1	0
3	33	1	22.705	0	0	21984.47061	1	0	0
4	32	1	28.880	0	0	3866.85520	1	0	0

To know more about dummy variable trap refer this link: https://towardsdatascience.com/one-hot-encoding-multicollinearity-and-the-dummy-variable-trap-b5840be3c41a

Correlation Plot of Variables:



• As we can see that among all the numeric variables, 'smoker' variable has the most correlation with our dependent variable 'charges'.

Feature Scaling:

Feature scaling is a very important step in which all the features(columns) in the dataset are brought under a common scale. The methods for scaling down the features include Standardization and Normalization.

Here, we will be perform standardization to scale our features.

$$x_{scaled} = rac{x-mean}{sd}$$

The data after standardization is as follows:

age	bmi	children	regionsoutheast	regionsouthwest	sex	charges	smoker1	regionnorthwest
1 -1.4409320 -0.44	192692 -0.	90824684	-0.6080396	1.7604578	0	16884.924	0	0
2 -1.5121637 0.53	316712 -0.	07957262	1.6433959	-0.5676079	1	1725.552	1	0
3 -0.7998469 0.40	029959 1.	57777583	1.6433959	-0.5676079	1	4449.462	1	0
4 -0.4436884 -1.33	174097 -0.	90824684	-0.6080396	-0.5676079	1	21984.471	1	1
5 -0.5149201 -0.28	355006 -0.	90824684	-0.6080396	-0.5676079	1	3866.855	1	1
6 -0.5861518 -0.83	102285 -0.	90824684	1.6433959	-0.5676079	0	3756.622	1	0

Splitting the data into test and train datasets:

We have randomly assigned 70% of total data for fitting the model and 30% data for testing the model performance. First few columns of the train dataset after split are as follows: (Note here Y_train = Charges)

1		age	sex	bmi	children	smoker1	regionnorthwest	regionsoutheast	regionsouthwest	Y_train
	1	19	0	27.90	0	0	0	0	1	16884.924
J	5	32	1	28.88	0	1	1	0	0	3866.855
	6	31	0	25.74	0	1	0	1	0	3756.622
	8	37	0	27.74	3	1	1	0	0	7281.506
	9	37	1	29.83	2	1	0	0	0	6406.411
	10	60	0	25.84	0	1	1	0	0	28923.137

Fitting the model (Feature selection):

We are now starting with the Forward selection method. Here we input the null model and the algorithm gives us the best model.

This is done using step() function in R. The function uses AIC (Akaike's Information Criterion) to find the best model. The lower the AIC, the better the model.

 $AIC = DEVIANCE + 2 \times NO. OF PARAMETERS$

Iteration 1:

Start: AIC=17629.54

```
Y_train ~ 1
          Df Sum of Sq RSS AIC Pr(>Chi)
+ smoker1 1 8.5499e+10 5.3179e+10 16733 < 2.2e-16 ***
+ age 1 1.3029e+10 1.2565e+11 17539 < 2.2e-16 ***
+ bmi 1 3.9900e+09 1.3469e+11 17604 1.694e-07 ***
+ sex 1 1.0544e+09 1.3762e+11 17624 0.00749 **
+ regse 1 7.8783e+08 1.3789e+11 17626 0.02086 *
+ children 1 5.6340e+08 1.3811e+11 17628 0.05081 .
                      1.3868e+11 17630
<none>
+ regsw 1 2.8410e+08 1.3839e+11 17630 0.16568
+ regnw 1 2.8410e+08 1.3839e+11 17630 0.16568
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Step: AIC=16733.43
Y_train ~ smoker1
```

Iteration 2:

```
Df Sum of Sq RSS AIC Pr(>Chi)
+ age 1 1.3948e+10 3.9231e+10 16450 < 2.2e-16 ***
+ bmi 1 4.4836e+09 4.8696e+10 16653 < 2.2e-16 ***
+ children 1 5.5945e+08 5.2620e+10 16726 0.001644 **
                       5.3179e+10 16733
<none>
+ sex 1 6.5741e+07 5.3114e+10 16734 0.281663
+ regse 1 5.1250e+07 5.3128e+10 16735 0.341861
+ regsw 1 3.8734e+06 5.3175e+10 16735 0.793902
           1 3.8734e+06 5.3175e+10 16735 0.793902
+ regnw
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Step: AIC=16450.4
Y_train ~ smoker1 + age
```

Iteration 3:

```
Df Sum of Sq RSS AIC Pr(>Chi)
+ bmi 1 3323095509 3.5908e+10 16370 < 2.2e-16 ***
+ children 1 347464834 3.8884e+10 16444 0.003887 **
+ regse 1 50809832 3.9181e+10 16451 0.270477
+ age:smoker1 1 40303537 3.9191e+10 16451 0.326406
+ regsw 1 12485695 3.9219e+10 16452 0.584978
+ regnw 1 12485695 3.9219e+10 16452 0.584978
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Step: AIC=16369.47
Y_train ~ smoker1 + age + bmi
```

Iteration 4:

```
Df Sum of Sq RSS AIC Pr(>Chi)
+ bmi:smoker1 1 1.2870e+10 2.3039e+10 15956 < 2.2e-16 ***
+ children 1 3.2112e+08 3.5587e+10 16363 0.003717 **
                         3.5908e+10 16370
<none>
+ regse 1 7.2967e+07 3.5835e+10 16370 0.167413
+ age:smoker1 1 5.7221e+07 3.5851e+10 16370 0.221546
+ sex 1 3.4455e+07 3.5874e+10 16371 0.342914
+ regsw 1 5.3447e+06 3.5903e+10 16371 0.708803
+ regnw 1 5.3447e+06 3.5903e+10 16371 0.708803
+ age:bmi 1 2.3961e+05 3.5908e+10 16372 0.936975
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Step: AIC=15955.63
Y_train ~ smoker1 + age + bmi + smoker1:bmi
```

Iteration 5:

```
Df Sum of Sq RSS AIC Pr(>Chi)
+ children 1 325557794 2.2713e+10 15944 0.0002605 ***
+ regsw 1 71211280 2.2967e+10 15955 0.0885404 .
+ regnw 1 71211280 2.2967e+10 15955 0.0885404 .
+ regse 1 50526622 2.2988e+10 15956 0.1514863
+ age:smoker1 1 3052970 2.3036e+10 15958 0.7245495
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Step: AIC=15944.3
Y_train ~ smoker1 + age + bmi + children + smoker1:bmi
```

Iteration 6:

```
Df Sum of Sq RSS AIC Pr(>Chi)
               1 78146805 2.2635e+10 15943 0.07233 .
+ regsw
           1 78146805 2.2635e+10 15943 0.07233 .
+ regnw
        2.2713e+10 15944
1 40454868 2.2673e+10 15945 0.19620
1 29114196 2.2684e+10 15945 0.27295
<none>
+ regse
+ sex
+ children:smoker1 1
                    28928687 2.2684e+10 15945 0.27449
+ bmi:children 1 8507260 2.2705e+10 15946 0.55353
+ age:children 1 874655 2.2712e+10 15946 0.84934
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Step: AIC=15943.07
Y_train ~ smoker1 + age + bmi + children + regsw + smoker1:bmi
```

Iteration 7:

```
Df Sum of Sq RSS AIC Pr(>Chi)
                   1 101527450 2.2533e+10 15941 0.04013 *
+ regse
                               2.2635e+10 15943
<none>
                   1 29764438 2.2605e+10 15944 0.26683
+ sex
+ children:regsw 1 28518887 2.2606e+10 15944 0.27709
+ children:smoker1 1 27892448 2.2607e+10 15944 0.28243
                      10489755 2.2624e+10 15945 0.50987
+ age:regsw
+ bmi:children
                   1 7170385 2.2628e+10 15945 0.58585
                   1 6572518 2.2628e+10 15945 0.60191
+ age:bmi
                   1 5167902 2.2630e+10 15945 0.64368
+ smoker1:regsw
               1 984450 2.2634e+10 15945 0.84001
1 962621 2.2634e+10 15945 0.84177
+ age:children
+ age:smoker1
+ bmi:regsw
                        654972 2.2634e+10 15945 0.86921
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Step: AIC=15940.86
Y_train ~ smoker1 + age + bmi + children + regsw + regse + smoker1:bmi
```

Iteration 8:

```
Df Sum of Sq RSS AIC Pr(>Chi)
+ bmi:regse
                   1 181270123 2.2352e+10 15935 0.005941 **
                               2.2533e+10 15941
<none>
                   1 29308194 2.2504e+10 15942 0.269457
+ sex
+ children:smoker1 1 28141042 2.2505e+10 15942 0.279213
+ children:regsw
                   1 27437676 2.2506e+10 15942 0.285308
+ age:regsw
                   1 9739684 2.2524e+10 15942 0.524472
+ bmi:children
                   1 7851472 2.2526e+10 15942 0.567702
+ age:regse
                       6997314 2.2526e+10 15943 0.589572
+ age:bmi
                       5879388 2.2527e+10 15943 0.620965
+ smoker1:regse
                       4508316 2.2529e+10 15943 0.665016
+ smoker1:regsw
                       3229953 2.2530e+10 15943 0.713994
+ children:regse
                      2328935 2.2531e+10 15943 0.755645
                   1 2234683 2.2531e+10 15943 0.760486
+ age:smoker1
+ age:children 1 618474 2.2533e+10 15943 0.872590
                  1 447684 2.2533e+10 15943 0.891473
+ bmi:regsw
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Step: AIC=15935.29
Y_train ~ smoker1 + age + bmi + children + regsw + regse + smoker1:bmi +
   bmi:regse
```

Iteration 9:

```
Df Sum of Sq RSS AIC Pr(>Chi)
                               2.2352e+10 15935
<none>
+ bmi:regsw
                   1 41446914 2.2311e+10 15936
                                                  0.1873
+ children:regsw
                   1 30998796 2.2321e+10 15936
                                                  0.2541
+ children:smoker1
                   1 25920055 2.2326e+10 15936
                                                  0.2971
                   1 23936621 2.2328e+10 15936
                                                  0.3164
+ sex
                   1 11367385 2.2341e+10 15937
                                                  0.4899
+ age:regse
                   1 8493392 2.2344e+10 15937
+ smoker1:regse
                                                  0.5507
+ bmi:children
                       8196278 2.2344e+10 15937
                                                  0.5577
+ age:bmi
                       7746389 2.2344e+10 15937
                                                  0.5687
                       6663113 2.2345e+10 15937
                                                  0.5971
+ age:regsw
+ smoker1:regsw
                       2080678 2.2350e+10 15937
                                                  0.7677
                   1
+ children:regse
                       1527444 2.2351e+10 15937
                                                  0.8002
                   1 861691 2.2351e+10 15937
+ age:smoker1
                                                  0.8493
+ age:children
                        366124 2.2352e+10 15937
                                                  0.9014
call:
lm(formula = Y_train ~ smoker1 + age + bmi + children + regsw +
    regse + smoker1:bmi + bmi:regse, data = dat_full)
```

Final model using forward selection:

```
call:
lm(formula = Y_train ~ smoker1 + age + bmi + children + regsw +
    regse + smoker1:bmi + bmi:regse, data = dat_full)
```

-955.7

Coefficients:

-9184.6

```
(Intercept)
                                                     children
                smoker1
                                             bmi
                                age
                                                                    regsw
                                                                                 regse
   32693.3
           -23757.8
                             3776.0
                                          9572.3
                                                        589.8
                                                                  -1032.8
                                                                                -628.3
smoker1:bmi
              bmi:regse
```

Backward elimination method in R:

```
lm(Y_train ~ smoker1 + age + bmi + children + regsw +
    regse + smoker1:bmi + bmi:regse + age:bmi + smoker1:children
    + bmi:children,data = dat_full)
```

Iteration 1:

```
Start: AIC=15939.4
Y_train ~ smoker1 + age + bmi + children + regsw + regse + smoker1:bmi +
   bmi:regse + age:bmi + smoker1:children + bmi:children
                Df Sum of Sq RSS AIC Pr(>Chi)
- age:bmi 1 8.8102e+06 2.2316e+10 15938 0.543006
- bmi:children 1 1.1185e+07 2.2318e+10 15938 0.493129
- smoker1:children 1 2.8368e+07 2.2335e+10 15939 0.275161
2.2307e+10 15939
<none>
- smoker1:bmi 1 1.3026e+10 3.5333e+10 16368 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Step: AIC=15937.77
Y_train ~ smoker1 + age + bmi + children + regsw + regse + smoker1:bmi +
   bmi:regse + smoker1:children + bmi:children
```

Iteration 2:

```
Df Sum of Sq RSS AIC Pr(>Chi)
- bmi:children 1 1.0325e+07 2.2326e+10 15936 0.510302
- smoker1:children 1 2.8049e+07 2.2344e+10 15937 0.277968
                           2.2316e+10 15938
<none>
1 1.2958e+10 3.5274e+10 16365 < 2.2e-16 ***
- age
- smoker1:bmi 1 1.3018e+10 3.5333e+10 16366 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Step: AIC=15936.2
Y_train ~ smoker1 + age + bmi + children + regsw + regse + smoker1:bmi +
   bmi:regse + smoker1:children
```

Iteration 3:

```
Df Sum of Sq RSS AIC Pr(>Chi)
- smoker1:children 1 2.5920e+07 2.2352e+10 15935 0.297092
                              2.2326e+10 15936
<none>
           1 1.5719e+08 2.2483e+10 15941 0.010348 *
regsw
- bmi:regse 1 1.7905e+08 2.2505e+10 15942 0.006223 **
            1 1.2949e+10 3.5275e+10 16363 < 2.2e-16 ***
- age
- smoker1:bmi 1 1.3051e+10 3.5377e+10 16366 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Step: AIC=15935.29
Y_train ~ smoker1 + age + bmi + children + regsw + regse + smoker1:bmi +
   bmi:regse
```

Iteration 4:

```
Df Sum of Sq RSS AIC Pr(>Chi)
                          2.2352e+10 15935
<none>
         1 1.5855e+08 2.2511e+10 15940 0.0100679 *
- regsw
- bmi:regse 1 1.8127e+08 2.2533e+10 15941 0.0059407 **
- children 1 3.1551e+08 2.2668e+10 15946 0.0002901 ***
      1 1.2929e+10 3.5281e+10 16361 < 2.2e-16 ***
- age
- smoker1:bmi 1 1.3038e+10 3.5390e+10 16364 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
call:
lm(formula = Y_train ~ smoker1 + age + bmi + children + regsw +
   regse + smoker1:bmi + bmi:regse, data = dat_full)
```

Final model using Backward Elimination:

```
lm(formula = Y_train ~ smoker1 + age + bmi + children + regsw +
    regse + smoker1:bmi + bmi:regse, data = dat_full)
coefficients:
(Intercept)
                 smoker1
                                                bmi
                                                        children
                                  age
                                                                        regsw
                                                                                      regse
                -23757.8
                               3776.0
                                             9572.3
    32693.3
                                                           589.8
                                                                      -1032.8
                                                                                     -628.3
smoker1:bmi
               bmi:regse
    -9184.6
                  -955.7
```

Analyzing the variables suggested by the function:

The model has suggested the following variables to be significant:

- Smoking status.
- Age
- BMI
- No. of children
- If region of residence was south west.
- If region of residence was south east.
- Interaction effect between smoking status and BMI
- Interaction effect between region of residence being south east and BMI

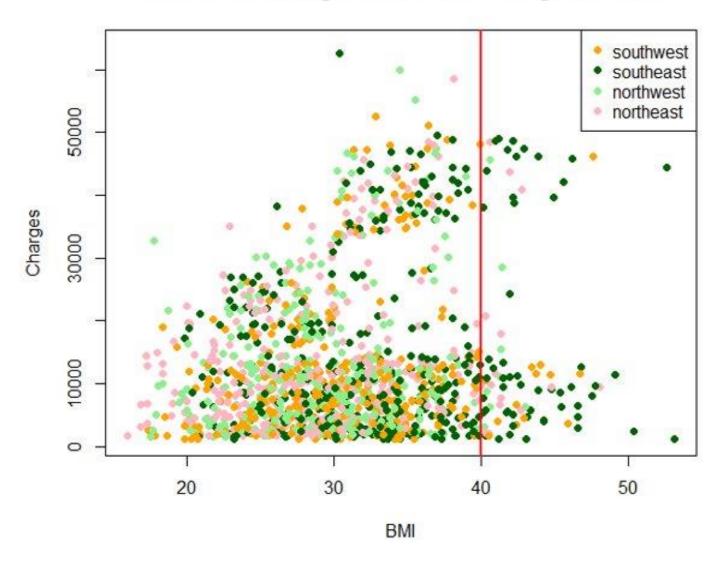
From the variables suggested, we know that interaction between smoking status and BMI of an individual is indeed significant. In other words, higher BMI i.e. higher weight and smoking habit lead to a significant increase in charges of insurance, as compared to a higher weight and absence of smoking habit.

Further, let's analyze whether the other variables suggested by the function are significant or not.

We'll start with the interaction term between BMI and region south east.

From this plot, we can see that, after BMI = 40, there are more individuals from region south east as compared to other regions.

Plot of BMI vs Charges with a factor of region included



P(Person being from south east | Large BMI)

$$= \frac{P(Large\ BMI\ | Person\ being\ from\ south\ east) * P(Person\ being\ from\ south\ east)}{P(Large\ BMI)}$$

This can be caused due to 3 reasons:

- The no. of people sampled from region southeast was a bit higher as compared to other regions.
- The BMI of individuals of southeast is higher on average as compared to other regions.
- Both the above reasons.
- But, on analyzing we have found that,

Region	Mean (BMI)	Median (BMI)
Southeast	33.33	33.35
Southwest	30.3	30.6
Northeast	28.88	29.17
Northwest	28.88	29.20

- Thus, we can observe that, the mean & median BMI is almost same for all regions. This means, our second reason and third reasons are eliminated. Thus, in reality we are getting bmi:region southeast as significant just because we have a higher no. of people from there.
- Thus, interaction effect isn't significant. Hence, we have removed that interaction from our model now.

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept)
            32641.7
                         394.3 82.775 < 2e-16 ***
smoker1
           -23788.8
                         396.3 -60.032 < 2e-16 ***
                         163.4 23.239 < 2e-16 ***
             3796.7
age
bmi
             9206.2
                         355.4 25.907 < 2e-16 ***
children
              592.9
                         163.5
                                3.626 0.000304 ***
             -820.6
                         401.1 -2.046 0.041046 *
regse
             -966.0
                         403.2 -2.396 0.016783 *
regsw
                         396.0 -23.115 < 2e-16 ***
smoker1:bmi
            -9152.9
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

ANOVA (For individual significance)

From this we can observe that, region SE and SW here are not that significant.

Logically, if we think about this, we understand that we should include these coefficients in the model, only when they have some significant impact on charges, as compared to other regions. But, on analyzing, we found that all regions have almost equal chance of paying higher charges. So, why include region SW and SE in our model?

So, we do not add the variables region SE and region SW in our model. Thus, our final model is then as follows:

Coefficients:

(Intercept) age bmi children smoker1 bmi:smoker1 32172.7 3797.7 9083.1 598.5 -23772.6 -9109.3

Summary of the fitted model & Individual significance.

```
Coefficients:
          Estimate Std. Error t value Pr(>|t|)
(Intercept) 32172.7
                      352.0 91.394 < 2e-16 ***
age
                      163.8 23.184 < 2e-16 ***
      3797.7
bmi
                      352.8 25.745 < 2e-16 ***
      9083.1
children 598.5 163.8 3.653 0.000274 ***
smoker1 -23772.6 396.1 -60.016 < 2e-16 ***
bmi:smoker1 -9109.3 396.5 -22.972 < 2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 4939 on 931 degrees of freedom
Multiple R-squared: 0.8362, Adjusted R-squared: 0.8353
F-statistic: 950.7 on 5 and 931 DF, p-value: < 2.2e-16
```

ANOVA (For overall significance)

Residual standard error: 4939 on 931 degrees of freedom Multiple R-squared: 0.8362, Adjusted R-squared: 0.8353 F-statistic: 950.7 on 5 and 931 DF, p-value: < 2.2e-16

The last part of the summary for the model has been pasted above.

For testing the overall significance of our model:

Null: All variables have no significant linear relationship with the dependent variable charges.

Alternative: At least 1 variable has a significant linear relationship with the dependent variable charges.

From above output, we can see that, the p-value is very low indeed. Thus, we can reject our null hypothesis and may conclude that our model is overall significant at 5% level of significance.

Checking the assumptions of Classical Linear Regression Model:

Following assumptions will be checked in the subsequent slides:

- Error distribution for the fitted model.
- Auto-correlation between residuals.
- Homoscedasticity of residuals.
- Multicollinearity between independent variables.

Error distribution:

Checking if residuals follow a normal distribution. For checking the error distribution, calculating the errors first.

Errors = Y observed - Y fitted

We've used the test data, consisting 30% of total data for calculating the fitted values. Then using these fitted values, residuals have been calculated. First few residuals and standardized residuals calculated are as follows:

Residuals

559.29259

-830.04859

-71.03779

-1704.33387

-2055.11799

-1375.14516

Std_residuals

1 -2.870054e-06

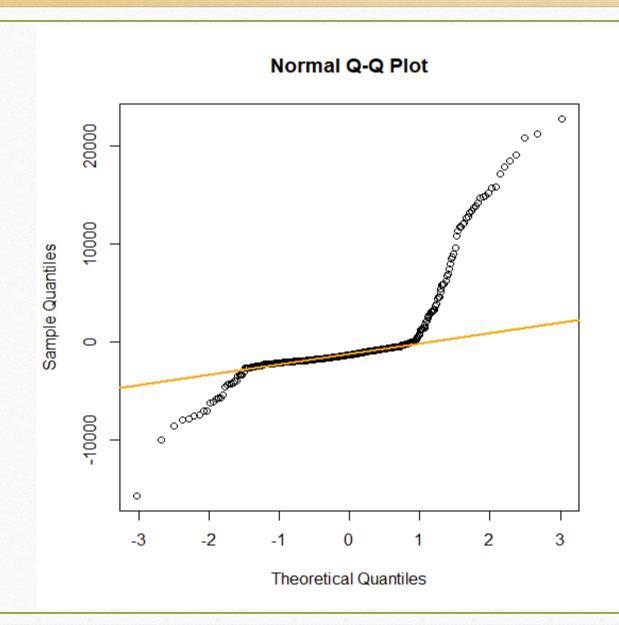
2 -9.636259e-07

3 -1.918516e-06

4 -7.400922e-06

5 -7.923663e-06

6 -6.400994e-06



From this plot we can see the distribution of residuals is heavy tailed i.e. it has fatter tails as compared to normal distribution. Thus, our regression model is violating one of the assumptions of CLRM.

Autocorrelation:

Our assumption was that there is no autocorrelation between the residuals.

Checking whether that assumption holds true. This is an important assumption, since presence of autocorrelation makes our OLS estimation invalid. We would have to use WLS (Weighted Least Squares) method in that case.

We've used Durbin Watson test in R, to check whether autocorrelation exists. The code and output for same is as follows:

```
> #H0 : No correlation among residuals.
> #vs H1 :Residuals are auto correlated.
>
> durbinWatsonTest(result3)
  lag Autocorrelation D-W Statistic p-value
      1     -0.01610781     2.029453     0.634
  Alternative hypothesis: rho != 0
> #We cannot reject H0, thus the residuals aren't correlated.
```

Homoscedasticity:

Checking if errors have equal variance.

To do this, we will first plot residuals vs Fitted values. Secondly, we will also formally test this using Breusch-Pagan-Godfrey test (BPG test).

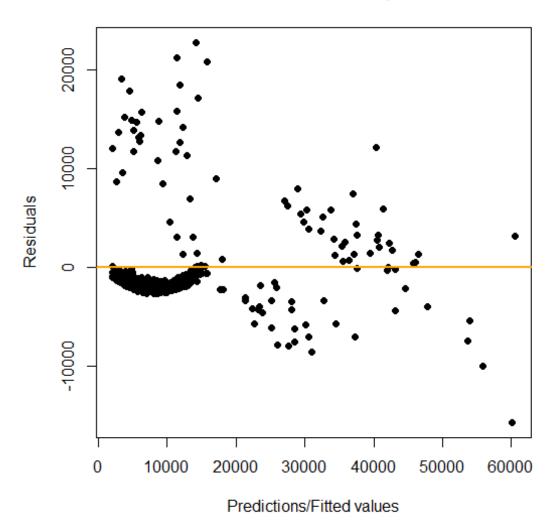
The plot of Residuals vs Fitted values is as given in the right.

From this we have 2 conclusions:

- For some part of residuals, it seems that the response variable is non-linearly correlated with the independent variables.
- And for the remaining part, the residuals have a negative correlation with fitted values. This implies, there is some variable outside our dataset, which has some significant relationship with the response variable 'Charges'.

Thus, now it becomes difficult to judge homoscedasticity using this plot. Thus, we go for an alternative way to check this, i.e. to use the BPG test.

Residuals vs Fitted plot



Now, we formally checked this homoscedasticity using BPG test, the output is as follows:

> bptest(result3)

studentized Breusch-Pagan test

data: result3

BP = 5.2133, df = 5, p-value = 0.3904

The null hypothesis in this case was that homoscedasticity is present, alternative being homoscedasticity is absent.

Thus, we conclude that since the p-value is not significant, we can't reject null. And hence, the residuals have equal variances.

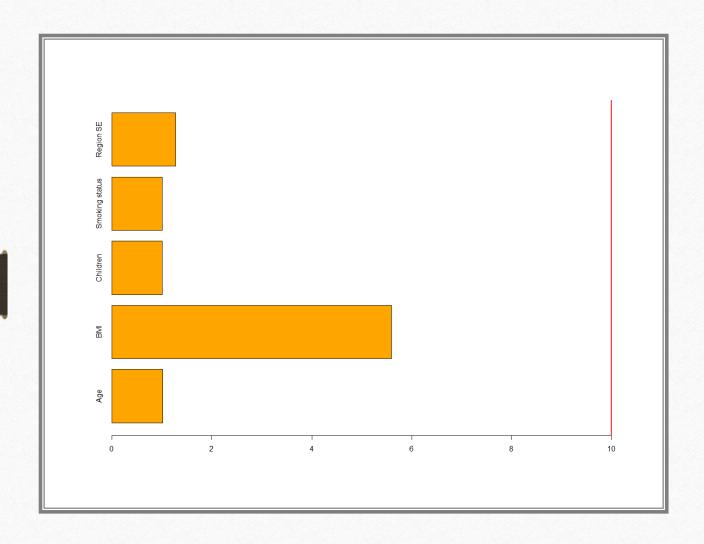
Multicollinearity:

Checking if the independent variables have any correlation between them.

To check this, we had already plotted a heatmap of all the variables in our data. From that, we could see that there was not much correlation between any 2 independent variables. To formally check this, we use the Variance Inflation Factor (VIF). The output for the same has been pasted below.

Each value can be examined for understanding whether the corresponding independent variable is highly correlated with other variables or not.

```
car::vif(result3)
age bmi children smoker1 bmi:smoker1
1.008840 4.801857 1.001975 1.000593 4.801303
```



To easily understand and better represent whether the VIF for our independent variables is larger than a value of 10 or not, we've drawn this bar plot.

Real-Time Prediction from the model

error
2064
3324
1917
1944
2144
13134
2132
1769
2046
3334

Conclusions:

- We had taken secondary data for predicting medical insurance costs of individuals based on their various features.
- We had equal no. of male and female respondents in our dataset.
- Charges have a right skewed distribution.
- BMI has an almost normal distribution.
- There are more non-smokers in our dataset as compared to smokers.
- The smoking status, is most correlated with our dependent variable.
- As age increases, the charges for medical insurance increase too.
- As BMI increases, the charges for medical insurance increase too.
- Medical insurance cost for smokers was higher as compared to non-smokers.
- Medical insurance costs for obese smokers were significantly higher than obese non-smokers.
- We arrived at the same model using both Forward selection & Backward elimination method.
- The adjusted R squared for our fitted model was about 84%.
- The assumption of error distribution being normal was violated by our model.
- While the assumptions of Homoscedasticity, absence of autocorrelation and multicollinearity were satisfied.

Bibliography:

- https://www.kaggle.com/
- https://www.r-bloggers.com/
- http://www.sthda.com/
- https://www.statology.org/
- https://stackoverflow.com/
- https://www.geeksforgeeks.org/
- https://towardsdatascience.com/
- https://en.wikipedia.org/

Thank you.