

# Official CUSUM Report

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## 1 Overview

This report summarizes the version of **CUSUM (cumulative sum)** used in the Intraday-Volatility-Monitor (IVM) project. CUSUM detects small standard deviation, persistent shifts in a process mean over time.

For our purposes, we will use CUSUM to look at the standard deviation, this will allow us to detect changes in movement without requiring a stable mean. This makes the approach more suitable for minute-by-minute trading environments.

## 2 The Use of CUSUM In The IVM

In the IVM project, CUSUM is applied to detect persistent directional movement in intraday price changes. Rather than computing deviations from a fixed expected mean, we evaluate each new price update relative to the previous minute.

Let

$$r = r_t - r_{t-1}$$

represent the most recent return difference, and let  $\varepsilon$  represent a volatility-scaled tolerance based on recent standard deviation estimates.

We then compute:

$$S_+ = \max\{0, r + \varepsilon\}$$

$$S_- = \max\{0, -(r + \varepsilon)\}$$

These act as accumulating evidence measures for upward and downward movement (these are sets of numbers that will keep growing in size). A detection event (alarm) occurs when the sum of these sets exceed our choice of threshold,  $h$ :

$$S_+ + S_- \geq h \Rightarrow \text{alarm}$$

and if

$$S_+ + S_- < h \Rightarrow \text{no alarm}$$

This allows our system to detect consistent directional movement that exceeds what we want to call 'normal volatility', even when the mean price level is drifting intraday.

### 3 Required Inputs

To run the intraday CUSUM algorithm, the following inputs are required:

- 1-minute trade data (price and timestamp)
- recent return difference  $r$
- standard deviation estimate  $\varepsilon$  (volatility scaling factor)
- threshold  $h$  controlling sensitivity
- rolling 1-minute sampling

Unlike traditional CUSUM, no global mean  $\mu_0$  is required—the method adapts purely to relative movement (standard deviation).

### 4 Expected Outputs

The IVM CUSUM system will produce:

- positive and negative cumulative signals  $S_+, S_-$
- detection events when  $S_+ + S_- \geq h$

- timestamps and magnitude of detected moves
- direction of movement (positive or negative). These will be shown as charts of the changes in positive and negative volatility.

These outputs support real-time monitoring of intraday volatility shifts and trading opportunities.

## 5 Implementation (Pseudo-Code)

*To be completed...*

*Placeholder for algorithmic implementation and pseudo-code.*

## 6 Issues and Limitations

When applying this CUSUM approach to high-frequency intraday data, the following issues may arise:

1. Non-stationarity: volatility and price structure evolve throughout the day.
2. Noise sensitivity: rapid micro-price movements may trigger partial accumulations.
3. Threshold selection:  $h$  must balance false alarms vs. slow detection.
4. Lag: evidence must accumulate before triggering.
5. Computation: rolling minute-by-minute updates must remain efficient.

## 7 Conclusion

CUSUM provides an effective real-time detection mechanism for intraday directional volatility patterns. By basing the calculation on standard deviation, the implementation aligns with the dynamic nature of high-frequency trading.

Once we tune it correctly (by selecting an appropriate  $h$ ), the method can highlight meaningful movements while filtering out normal market noise, strengthening the IVM team's ability to detect emerging intraday anomalies as soon as possible.