

UNIT-I (INTRODUCTION)

(1)

EVOLUTION OF FIBER OPTIC SYSTEMS

FIRST GENERATION

- # Operated at around 850 nm
- # Low loss transmission window of early silica fiber
- # GaAs-based optical sources, silicon photo detectors & MM fibers were used.
- # Repeater spacing around 10 km
- # Intermodal dispersion & fiber loss limited
- # The capacity of systems
- # Bit rate of 45 Mb/s

Second Generation

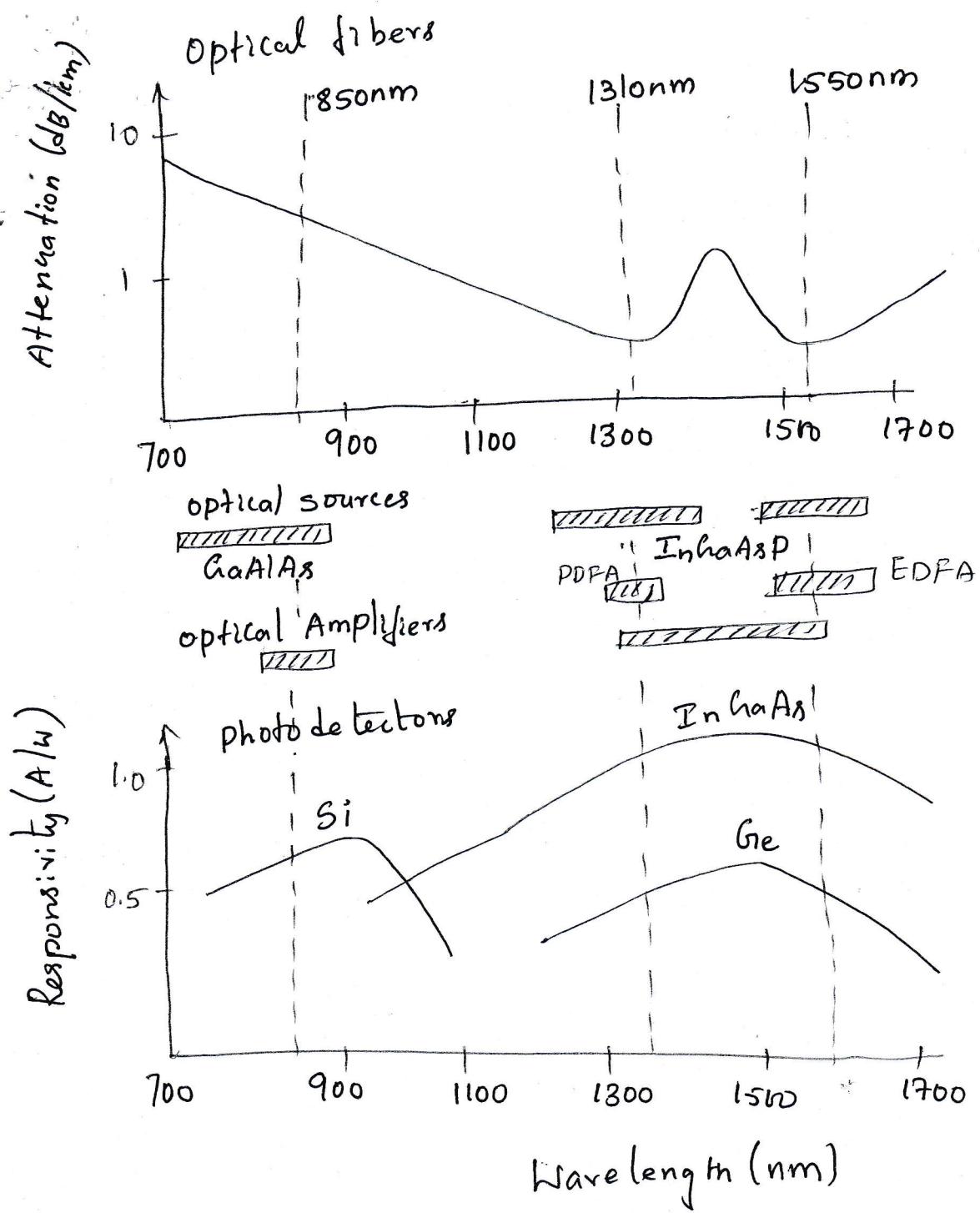
- # Operated at 1300 nm
- # Substantial increase in the repeaterless transmission distance for long-haul telephone link
- # Exhibit lower power loss & less signal dispersion at 1300 nm .
- # Bit rate, limited to below 100 Mb/s because of dispersion in MM fibers, this was overcome by SM fiber.
- # Bit rate of up to 1.7 Gb/s with a repeater spacing of about 20 km .

Third Generation

- # operated at 1550 nm
- # provide lowest attenuation, but std silica fibers have much larger signal dispersion at 1550 nm than at 1300 nm, dispersion problem was overcome by dispersion shifted fibers.
- # Bit rate of 2.5 Gb/s over 90 km repeaterless distances.
- # In 1996, advances in high quality lasers & Rx. allowed single-λ transmission rates of around 10Gb/s.

Fourth Generation

- # Make use of optical amplification for increasing repeater spacing and of WDM for increasing bit rate
- # WDM technique doubling the system capacity & led to operating at a bit rate of 10Gb/s (2001)
- # Fiber losses are compensated periodically using (EDFA) Erbium doped fiber amplifier spaced 60-80 km apart.



EDFA - Erbium doped fiber amplifier
operated at 1550nm

PDFA - praseodymium-doped fiber amplifier
operated at 1310 nm

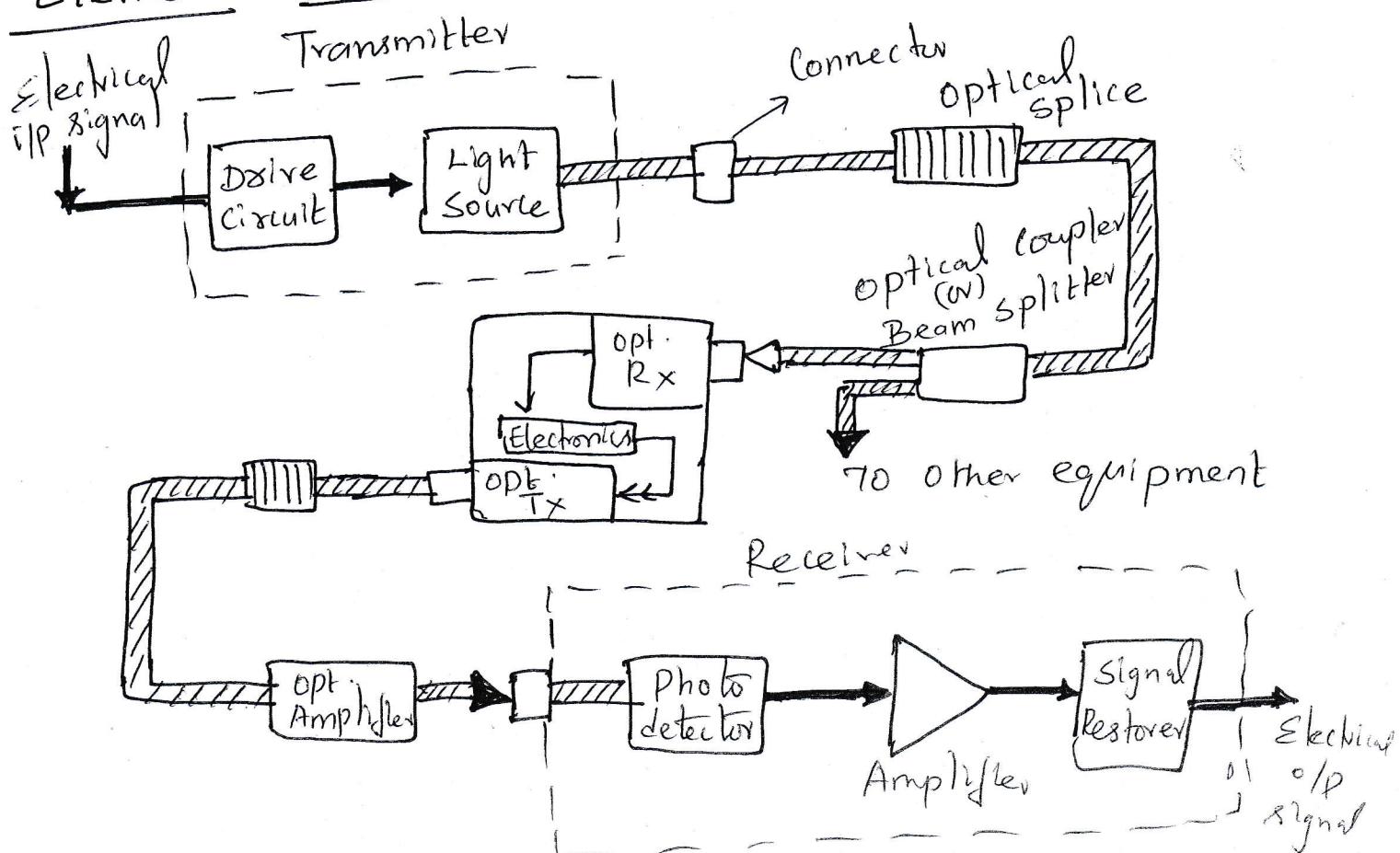
Fig:
Operating range of optical fiber systems & the characteristics of 4-key link components
(optical fiber, light source, photo detection & amplifier)

BASIC N/W INFORMATION RATES

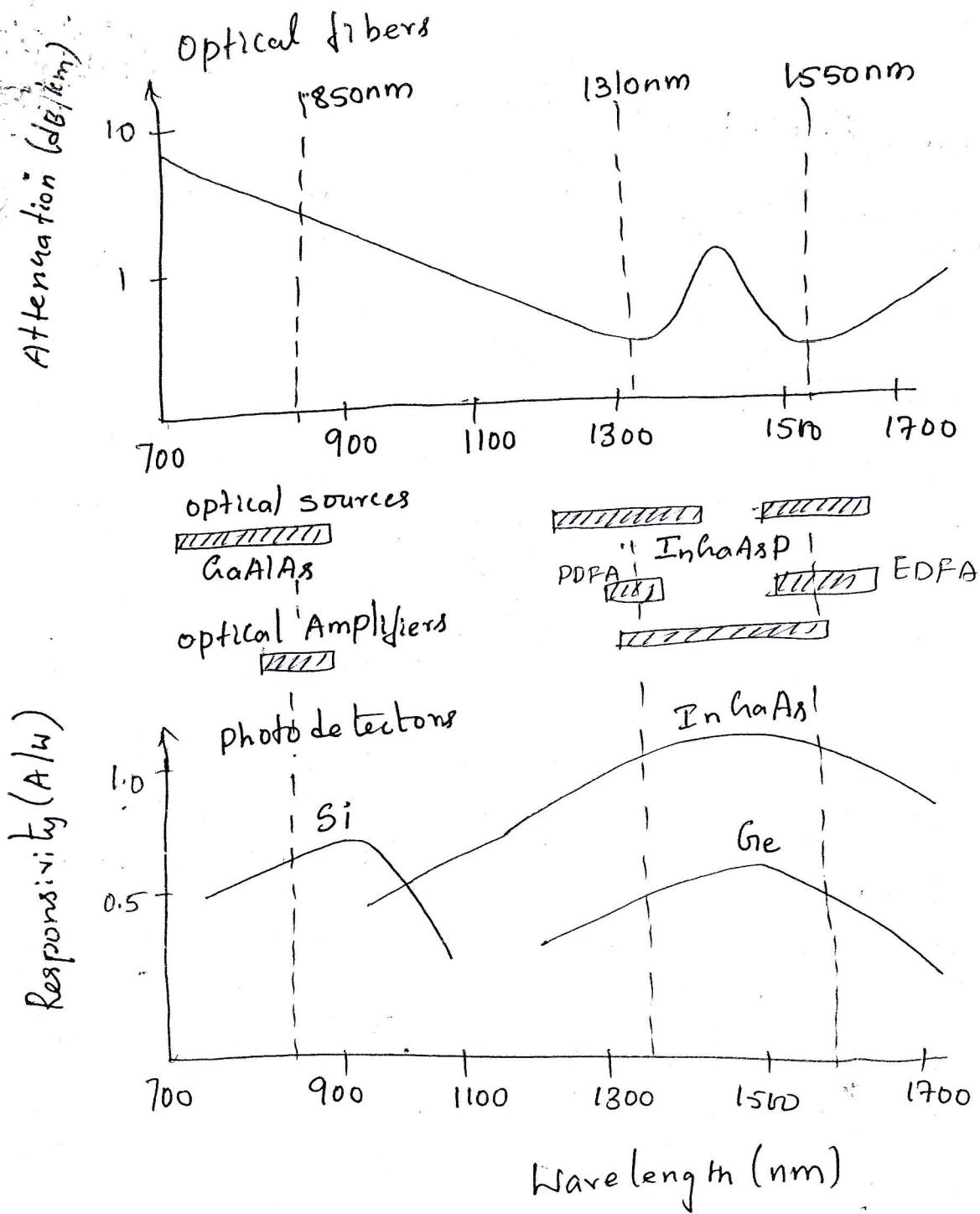
Type of Service

	Data rate
1. video on demand / interactive TV	1.5 - 6 Mb/s
2. Video games	1 - 2 Mb/s
3. Remote education	1.5 - 3 Mb/s
4. Electronic shopping	1.5 - 6 Mb/s
5. Data transfer for telecommuting	1 - 3 Mb/s
6. Video Conferencing	0.384 - 2 Mb/s
7. Voice (single channel)	64 kbit/s

Elements of an Optical fiber transmission link



(2)



EDFA - Erbium doped fiber amplifier
operated at 1550nm

PDFA - praseodymium-doped fiber amplifier
operated at 1310nm

Fig:

Operating range of optical fiber systems & the characteristics of 4-key link components
(optical fiber, light source, photo detection & amplifiers)

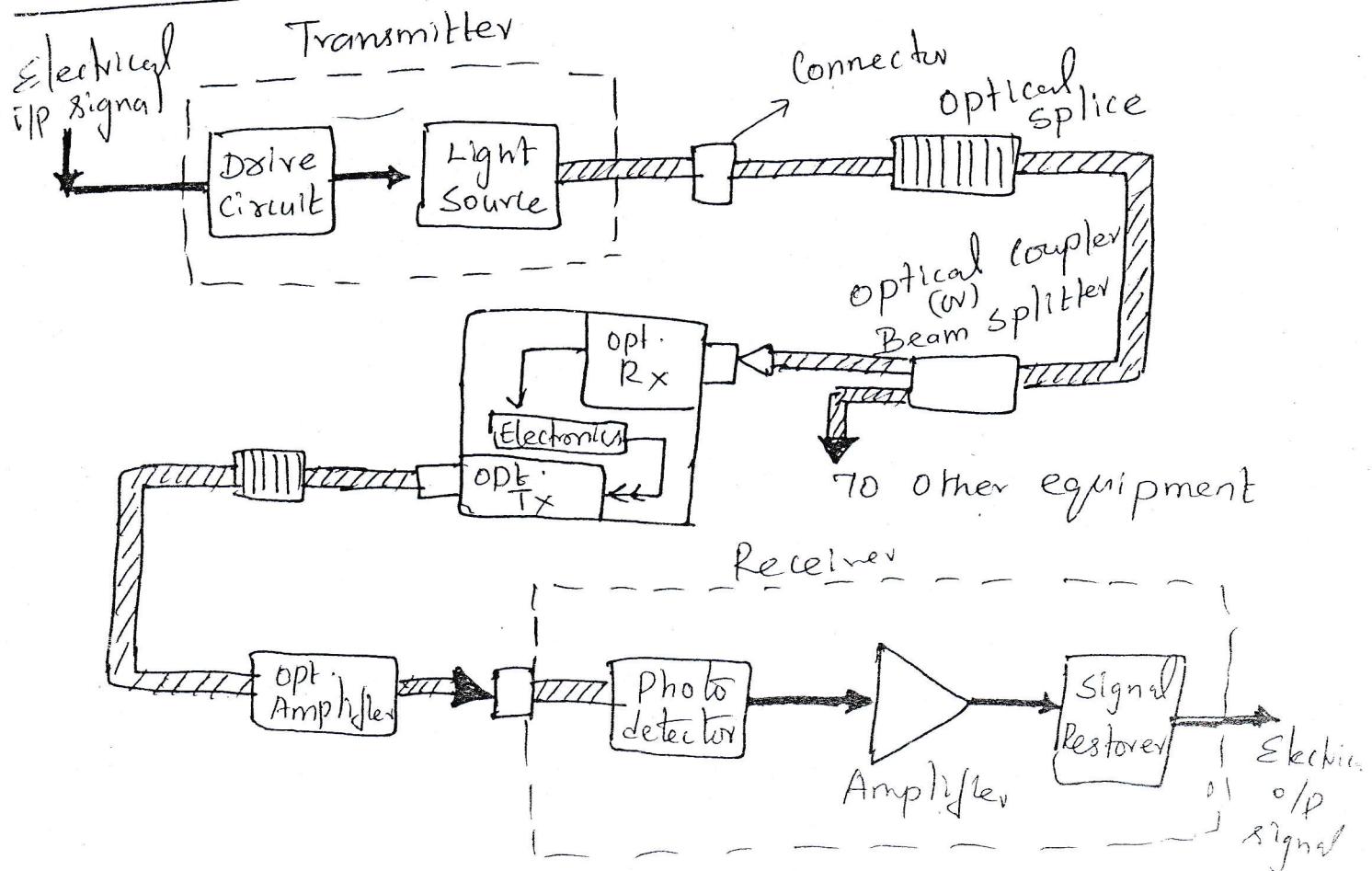
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Type of Service

Data rate

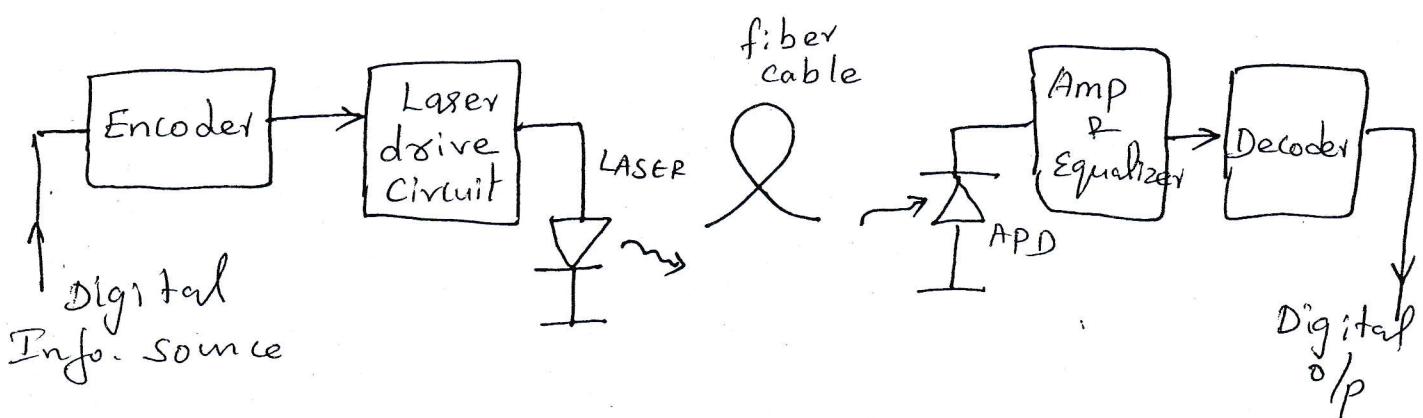
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Elements of an Optical fiber transmission link



(3)

Digital optical link using Semiconductor laser source & an avalanche photodiode (APD)



- * i/p digital signal from the information source is encoded for optical transmission.
- * Laser drive circuit directly modulates the intensity of the semiconductor laser with the encoded digital signal.
- * Digital optical signal is launched into the optical fiber cable.
- * APD detector is followed by a front-end amplifier & equalizer or filter to provide gain as well as linear signal processing and noise bandwidth reduction.
- * Finally, signal is decoded to give original digital information.

Advantages of Optical fiber Communication

i) Enormous potential Bandwidth:

The optical carrier freq in the range 10^{13} to 10^{16} Hz yields a far greater potential transmission BW than metallic cable systems.

(2) Small size & weight:

Optical fibers have very small diameters which hence, even when such fibers are covered with protective coatings, they are far smaller & much lighter than corresponding copper cables.

(3) Electrical Isolation

Optical fibers, fabricated from glass or plastic polymers, are electrical insulators & \therefore they don't exhibit earth loop & interface problems.

(4) Immunity to Interference & cross talk

Optical fibers form a dielectric waveguide and \therefore free from electromagnetic interference (EMI), Radio frequency interference (RFI) & unlike electrical conductors, cross talk is negligible, even when many fibers are cabled together.

(5) Signal security:

Light from optical fibers doesn't radiate significantly & ∴ they provide a high degree of signal security. This feature is attractive for military, banking and general data transmission applications.

(6) Low transmission loss

Optical fiber cables exhibit very low attenuation (or) transmission loss in comparison with copper conductors. They are fabricated with lower as low as 0.2 dB/km .

(7) Ruggedness & flexibility

Although protective coatings are essential, optical fibers may be manufactured with very high tensile strengths. Cable structures, have proved flexible, compact & extremely rugged.

(8) System Reliability & ease of maintenance

These features which reduces the requirement for intermediate repeaters or line amplifiers to boost the faded signal strength.

(9) Low cost:

The glass, provided optical fiber is made from sand - not a scarce resource. So in comparison with copper conductor

Principal Characteristics of an optical fiber
is its attenuation as a function of λ .

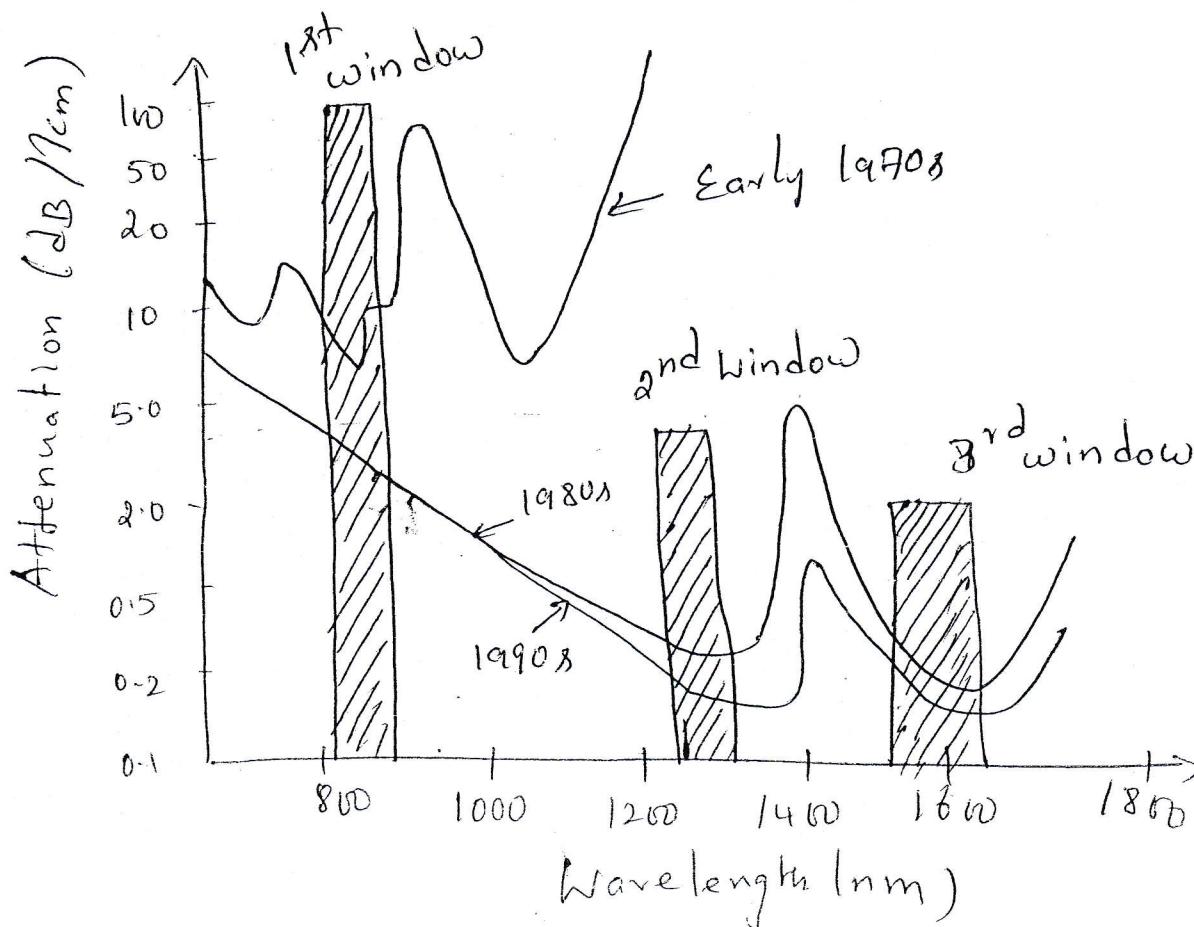
This is shown in figure.

First window: operated at $800 - 900 \text{ nm}$ λ band

Second Window (1310 nm) - operated at $1100 - 1600 \text{ nm}$ region.

Third Window, centred around 1550 nm

→ long-wavelength region
 $(1100 - 1600 \text{ nm})$



Optical fiber attenuation as a function
 λ .

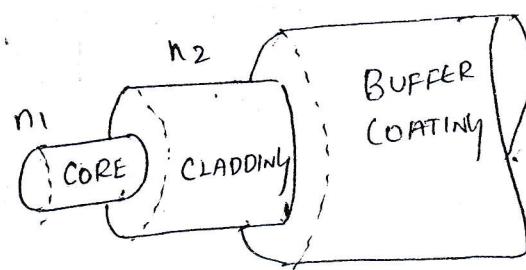
1st window

- short λ region
operated at 850nm
- Absorption by water molecule - low attenuation splice
- optical source - GaAlAs
- optical detector \rightarrow Si
- Loss = 3 dB/km

2nd window } 3rd window

- long λ region
- Reducing the concentration of OH^- ions & metallic impurities
- O band
- 1310nm
- loss: 0.5 dB/km
- zero dispersion for Si fiber
- opt. amplifier \rightarrow EDFA
- C band
- 1550nm
- 0.2 dB/km
- Non-zero dispersion
- Light source - InGaAsP
- photodetector - InGaAs

Basic Structure of optical fiber - It consists of 3 layers, core (inner), cladding (outer) & buffer coating layer



Core: Dielectric cylinder radius 'a'

- * Innermost layer, having ref. index n_1
- * light travels thro' axis of the core
- * Core material - glass
- * $n_1 > n_2$

(6)

Cladding:

- Thickness must be 2 times $> \lambda$ light to be guided
- provides strength to fiber
- Reduces scattering loss
- $n_2 < n_1$
- Cladding material - pure Si or plastic

Buffer Coating:

- Last layer, - protective layer
- provides strength to fibers
- It isolates or buffers the fiber from geometric irregularity, distortion & protect the fiber from drastic environmental changes.

RAY THEORY TRANSMISSION

Critical Angle: A fundamental optical parameter of a material is the refractive index (index of refraction). In free space light wave travels at a speed $c = 3 \times 10^8 \text{ m/s}$. The speed of light is related to frequency γ & wavelength λ by $c = \gamma \lambda$.

Refractive index: The ratio of speed of light in a vacuum to that in matter

$$n = \frac{c}{v}$$

$n = 1$	for air
$= 1.33$	for water
$= 1.5$	for glass
$= 2.42$	for diamond

Note:

Conditions for TIR to be satisfied

- (i) Light ray must pass thro' denser to rarer medium
- (ii) Incident angle ϕ_1 in denser medium must be greater than 90° (ϕ_c) critical angle of that medium

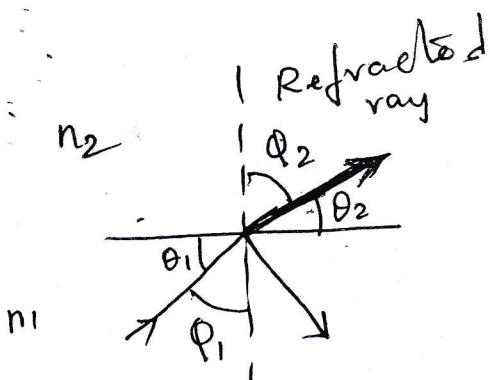
Angle of incidence ϕ_1 & angle of refraction ϕ_2 are related to each other & ref. indices of dielectric by Snell's law of refraction

$$n_1 \sin \phi_1 = n_2 \sin \phi_2$$

$$\frac{\sin \phi_1}{\sin \phi_2} = \frac{n_2}{n_1}$$

Three Cases:

- (i) $\phi_1 < \phi_c$, refracted into rarer medium it traverse along the interface so that $\phi_2 = 90^\circ$
- (ii) $\phi_1 = \phi_c$, totally reflected back into denser medium.
- (iii) $\phi_1 > \phi_c$,



$$n_1 > n_2$$

Where

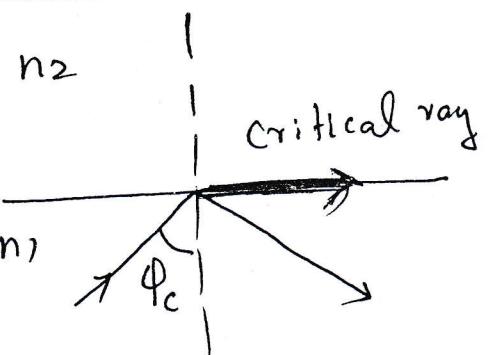
$$n_1 > n_2$$

$$\phi_i < \phi_c$$

ϕ_i - Angle of incidence

ϕ_2 - angle of refraction

\Rightarrow When $\phi_i < \phi_c$, it is refracted into the rarer medium.



$$n_1 > n_2$$

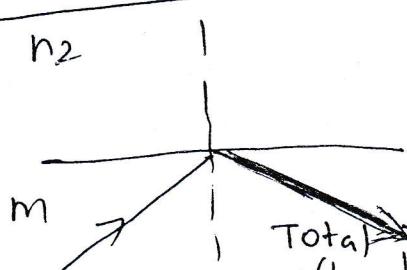
$$\phi_i = \phi_c$$

\Rightarrow When $\phi_i = \phi_c$, it traverses along the interface so that angle of refraction is 90°.

$$\therefore n_1 \sin \phi_i = n_2 \sin \phi_2$$

$$n_1 \sin \phi_c = n_2 \sin 90^\circ$$

$$\sin \phi_c = \frac{n_2}{n_1}$$



$$n_1 > n_2$$

$$\phi_i > \phi_c$$

\Rightarrow When $\phi_i > \phi_c$, it is totally reflected back into the denser medium itself with high efficiency. This is called TIR.

Critical Angle: The value of the incident angle at which the angle of refraction is 90°

Angle of incidence: The angle ϕ_i between the incident ray & the normal to the surface.

Aceptance Angle:

Maximum value of the angle of incidence at the entrance end of the fiber, at which angle of incidence at core-cladding interface is equal to critical angle of core medium

(or)

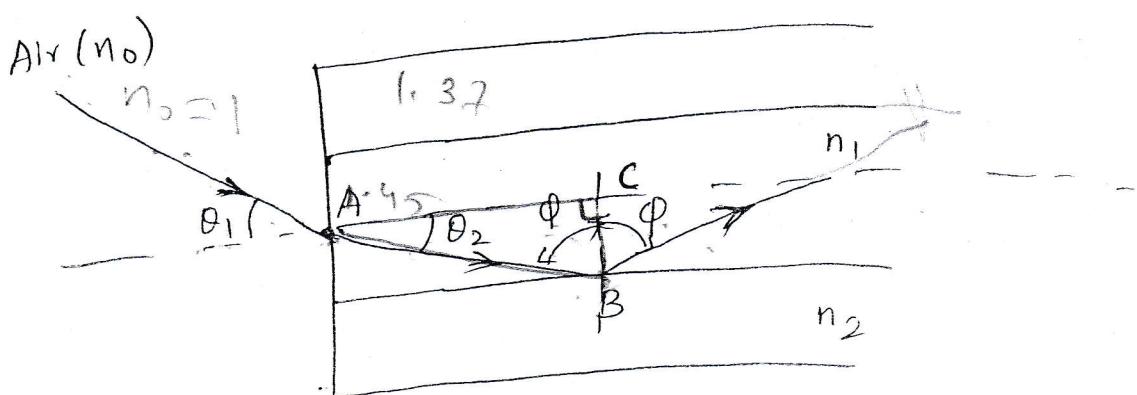
Angle at which the ray enters the fiber core.

$$\sin \phi_{\max} = \sqrt{n_1^2 - n_2^2} = NA$$

$$\phi_{\max} = \phi_A = \sin^{-1} NA$$

Numerical Aperture:

It is the light collecting power of the fiber. It is the measure of amount of light accepted by the fiber.



Ray Path for meridional ray launched into an optical fiber in air at an input angle less than acceptance angle for the fiber.

Relationship between NA & Acceptance angle

According to Snell's law, $n_0 \sin \theta_1 = n_1 \sin \theta_2$ (Meridional ray)

$$\frac{\sin \theta_1}{\sin \theta_2} = \frac{n_1}{n_0}$$

From the figure, consider right angled triangle ABC.

$$\phi = \frac{\pi}{2} - \theta_2$$

$$\theta_2 = \frac{\pi}{2} - \phi$$

Substitute θ_2 value in eqn (1)

$$n_0 \sin \theta_1 = n_1 \sin \left(\frac{\pi}{2} - \phi \right)$$

$$n_0 \sin \theta_1 = n_1 \cos \phi$$

$$\left\{ \begin{array}{l} \sin(90^\circ - \theta) \\ = \cos \theta \end{array} \right.$$

Using the trigonometrical relationship $\sin^2 \phi + \cos^2 \phi = 1$, we get

$$n_0 \sin \theta_1 = n_1 (1 - \sin^2 \phi)^{1/2}$$

$$\sin^2 \phi + \cos^2 \phi = 1 - \sin^2 \phi$$

$$\cos^2 \phi = 1 - \sin^2 \phi$$

By considering the limiting case of TIR, (ie)

$$\theta_1 = \phi_a \quad (\text{Acceptance angle})$$

$$\phi = \phi_c \quad (\text{Critical angle})$$

$$\& n_0 = 1$$

\therefore Eqn (4) becomes

$$n_0 \sin \phi_a = n_1 (1 - \sin^2 \phi_c)$$

$$\sin \phi_a = n_1 \sqrt{1 - \left(\frac{n_2}{n_1} \right)^2}$$

$$= n_1 \sqrt{\frac{n_1^2 - n_2^2}{n_1^2}}$$

$$\therefore \sin \phi_a = \sqrt{n_1^2 - n_2^2} = NA$$

$$\phi_a = \sin^{-1} \sqrt{n_1^2 - n_2^2}$$

Skew Rays

The rays that follows helical path around the fiber axis when they travel thro' the fiber & is transmitted without passing through the fiber axis.

It is not easy to visualize the skew ray paths in two dimensions, but it may be observed from figure (a) that the helical path traced thro' the fiber gives a change in direction of $\delta\gamma$ at each reflection where γ is the angle b/w projection of the ray in 2 dimension & radius of the fiber core at the pt. of reflection

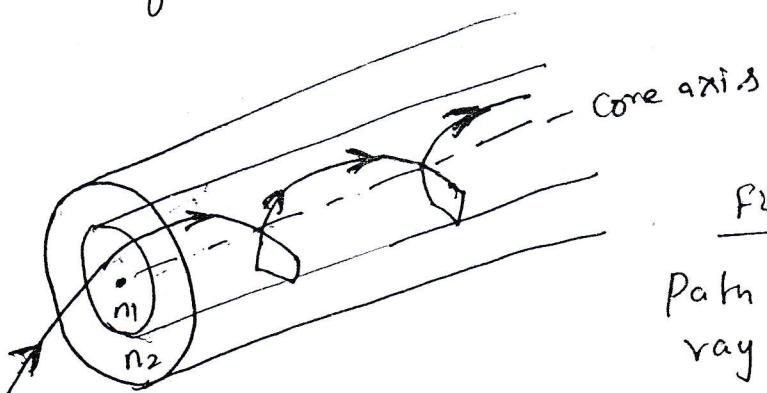
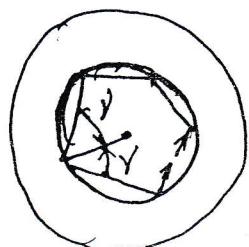


Figure (a) . Helical Path taken by skew ray in an opt. fiber

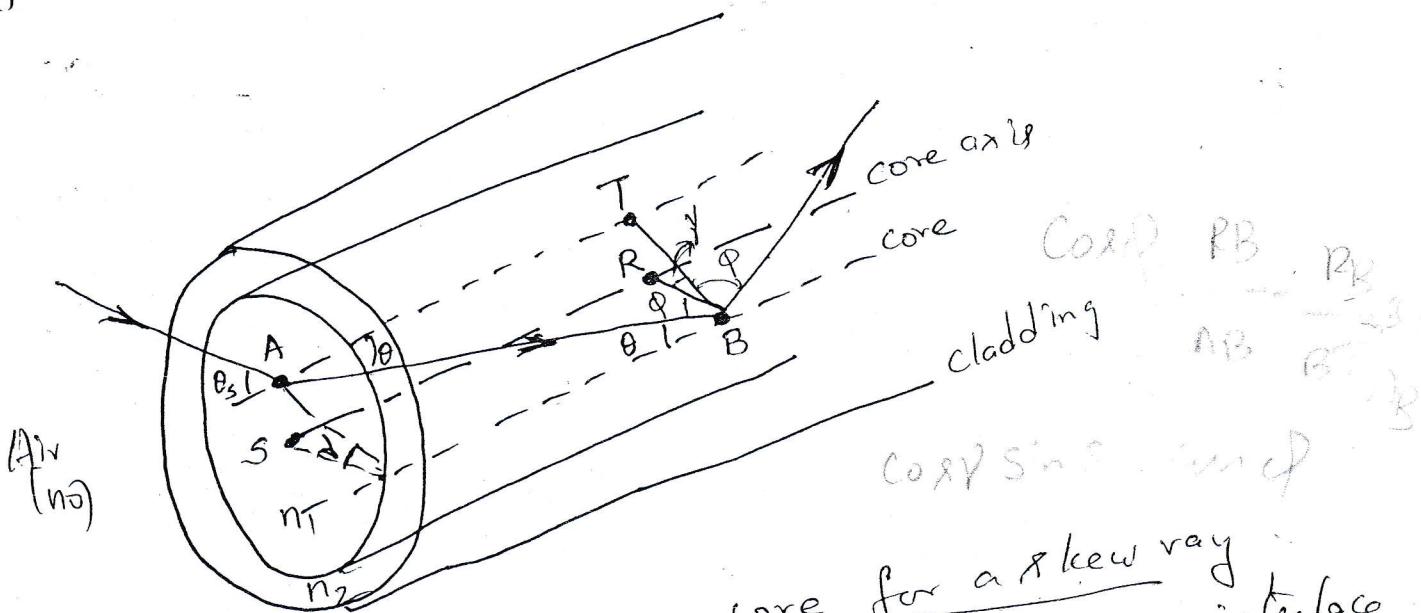


Cross-sectional view of fiber
(b)

Analysis of skew rays

Relationship b/w NA & acceptance angle for Skew rays

- * Skew ray is incident on the fiber core at the point A, at an angle θ_s to the normal at fiber end face.
- * The ray is refracted at air-core interface before travelling to point B in the same plane.
- * The angle of incidence & reflection at the point B are ϕ , $>$ than critical angle for core-cladding interface.



Ray path within fiber core for a skew ray incident at an angle θ_s to the normal at air-core interface.

- * As incident & reflected rays at the point B are in the same plane, this is simply $\cos\phi$.
- * However, if two 1^{st} plane thro' which ray path AB traversed are considered, then y is the angle b/w core radius & projection of ray on to a plane BRS normal to core axis θ is the angle b/w ray & a line AT 1^{st} to core axis

\therefore To resolve ray path AB relative to radius BR in these 2 1^{st} plane requires multiplication by $\cos\phi$ & $\sin\theta$.

Hence, reflection at point B at an angle ϕ is given by $\cos\phi \sin\theta = \cos\phi$ — (1)

Using trigonometric relation, $\sin^2\phi + \cos^2\phi = 1$, Eqn (1) becomes

$$\cos\phi \sin\theta = \cos\phi = (1 - \sin^2\phi)^{1/2}$$

By considering the limiting case of TIR,
 $\{\phi = \phi_c, \theta_a = \theta_{as}\}$

$$\begin{aligned} \therefore \cos\phi \sin\theta &\leq \cos\phi_c = (1 - \sin^2\phi_c)^{1/2} \\ &= \cos\phi \left(1 - \frac{n_2^2}{n_1^2}\right)^{1/2} \end{aligned}$$

Using Snell's law at point A, $n_2 \sin\theta_a = n_1 \sin\theta$. Where θ_a - max i/p axial angle for meridional ray.

(10)

$$\sin \theta_{as} = \frac{n_1}{n_0} \frac{\cos \phi_c}{\cos \psi}$$

$$= \frac{n_1}{n_0 \cos \psi} \left(1 - \frac{n_2^2}{n_1^2}\right)^{1/2}$$

Where θ_{as} = max ifp angle (or) acceptance angle
for skew rays.

* thus acceptance conditions for skew

rays are

$$n_0 \sin \theta_{as} \cos \psi = \sqrt{n_1^2 - n_2^2} = NA$$

for air, $n_0 = 1$ ∴

$$\therefore \sin \theta_{as} \cos \psi = NA$$

Problem:
An OI in air has an NA of 0.4 . Compare the
acceptance angle for meridional rays with that for
skew rays which change direction by 100° at each
reflection

for meridional rays,
 $\theta_a = \sin^{-1} NA = \sin^{-1}(0.4) = 23.6^\circ$

Solution
Skew rays change direction by 100° at each reflection
 $\therefore \nu = 50^\circ \therefore$ acceptance angle for skew rays is
 $\theta_{as} = \sin^{-1} \frac{NA}{\cos \nu} = \sin^{-1} \left(\frac{0.4}{\cos 50^\circ} \right) = 38.5^\circ$

Note: θ_{as} is about $15^\circ > \theta_a$

Mode Theory for optical propagation
(Refer OMP sheet) Refer book

Modes in a planar guide

- * planar guide is the simplest form of optical waveguide
- * Assume that it consists of a slab of dielectric with ref. index n_1 sandwiched b/w two regions of lower ref. index n_2 .
- * To obtain an improved model for optical propagation, it is necessary to consider the interference of plane wave components within this dielectric.
- * As the ref. index within the guide is n_1 , the optical λ is reduced to λ/n_1 , while the vacuum propagation constant is κ to $n_1 k_c$.
- * When θ is the angle b/w propagation vector & guide axis, plane wave is resolved into two component plane wave propagating in z & x dir.
 β_z & β_x (ie) $\beta_z = n_1 k \cos \theta$
 $\beta_{xc} = n_1 k \sin \theta$

Electromagnetic Mode Theory for Optical Propagation

Electromagnetic Wave:

In order to obtain an improved model for propagation of light in an optical fiber, EM wave theory must be considered.

The basis for the study of electromagnetic wave propagation is provided by Maxwell's equation. For a medium with zero conductivity these vector relationships may be written in terms of E , H , D & B as curl equations.

$$\nabla \times E = -\frac{\partial B}{\partial t} \quad \text{--- (1)}$$

$$\nabla \times H = \frac{\partial D}{\partial t} \quad \text{--- (2)}$$

Divergence conditions:

$$\nabla \cdot D = 0 \quad (\text{no free charges}) \quad \text{--- (3)}$$

$$\nabla \cdot B = 0 \quad (\text{no free poles}) \quad \text{--- (4)}$$

Where ∇ is a vector operator

The four field vectors are related by the relations,

$$D = \epsilon E \quad \text{--- (5)}$$

$$B = \mu H$$

Where ϵ is the dielectric permittivity

μ is the magnetic permeability of the medium

Substituting for D & B & taking curl of (1) & (2) eqn

$$\nabla \times (\nabla \times E) = -\mu \epsilon \frac{\partial^2 E}{\partial t^2} \quad \text{--- (6)}$$

$$\nabla \times (\nabla \times H) = -\mu \epsilon \frac{\partial^2 H}{\partial t^2} \quad \text{--- (7)}$$

Then using the divergence condition of eqn (3) & (4) with the vector identity:

$$\nabla \times (\nabla \times \mathbf{y}) = \nabla(\nabla \cdot \mathbf{y}) - \nabla^2 \mathbf{y}$$

& we obtain the nondispersive wave eqn.

$$\nabla^2 E = \mu \epsilon \frac{\partial^2 E}{\partial t^2} \quad \text{--- (8)}$$

$$\nabla^2 H = \mu \epsilon \frac{\partial^2 H}{\partial t^2} \quad \text{--- (9)}$$

Where ∇^2 is the Laplacian operator.

For rectangular cartesian & cylindrical polar coordinates, the above wave eqn. hold for each component of the field vector, H component satisfying the scalar wave equation:

$$\nabla^2 \psi = \frac{1}{V_p^2} \frac{\partial^2 \psi}{\partial t^2} \quad \text{--- (10)}$$

Where ψ may represent a component of E or H field & V_p is the phase velocity (or velocity of propagation of a point of constant phase in the wave) in the dielectric medium.

$$\therefore V_p = \frac{1}{\sqrt{\mu \epsilon}} = \frac{1}{\sqrt{\mu_r \mu_0 \epsilon_r \epsilon_0}} \quad \text{--- (11)}$$

Where μ_r & ϵ_r are the relative permeability & Permittivity for the dielectric medium & μ_0 & ϵ_0 are the permeability & permittivity of free space. The velocity of light in free space c is

$$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}} \quad \text{--- (12)}$$

Formation of a mode in a planar dielectric guide

(11)

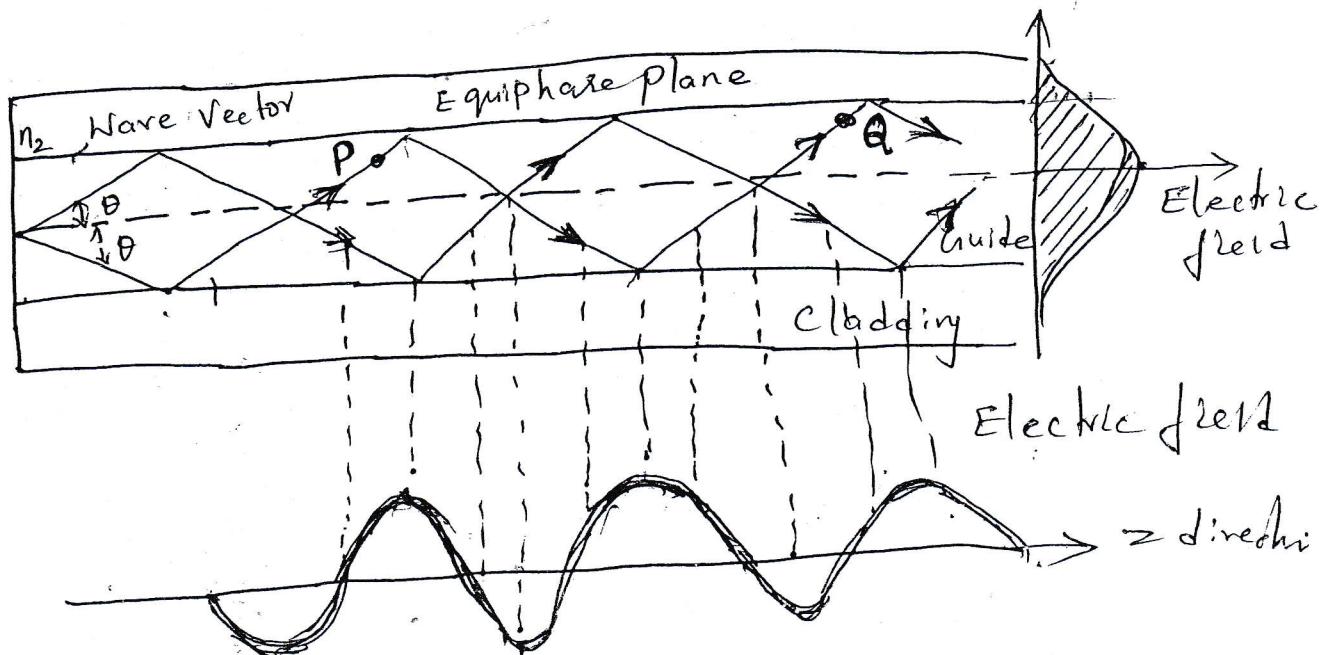
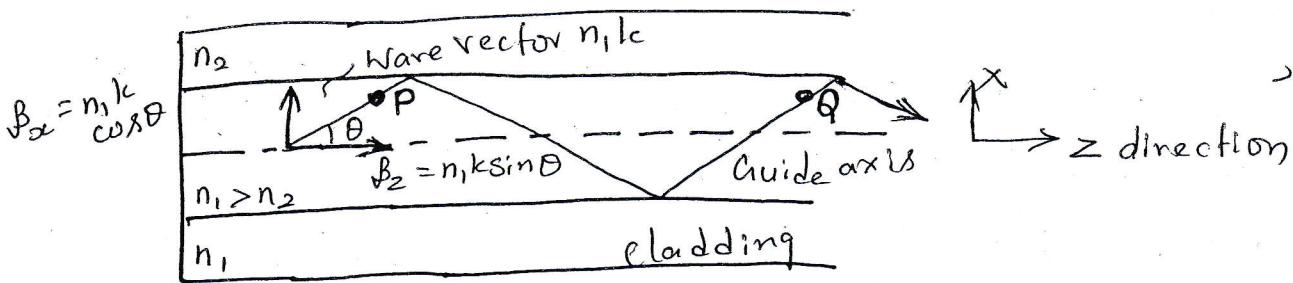
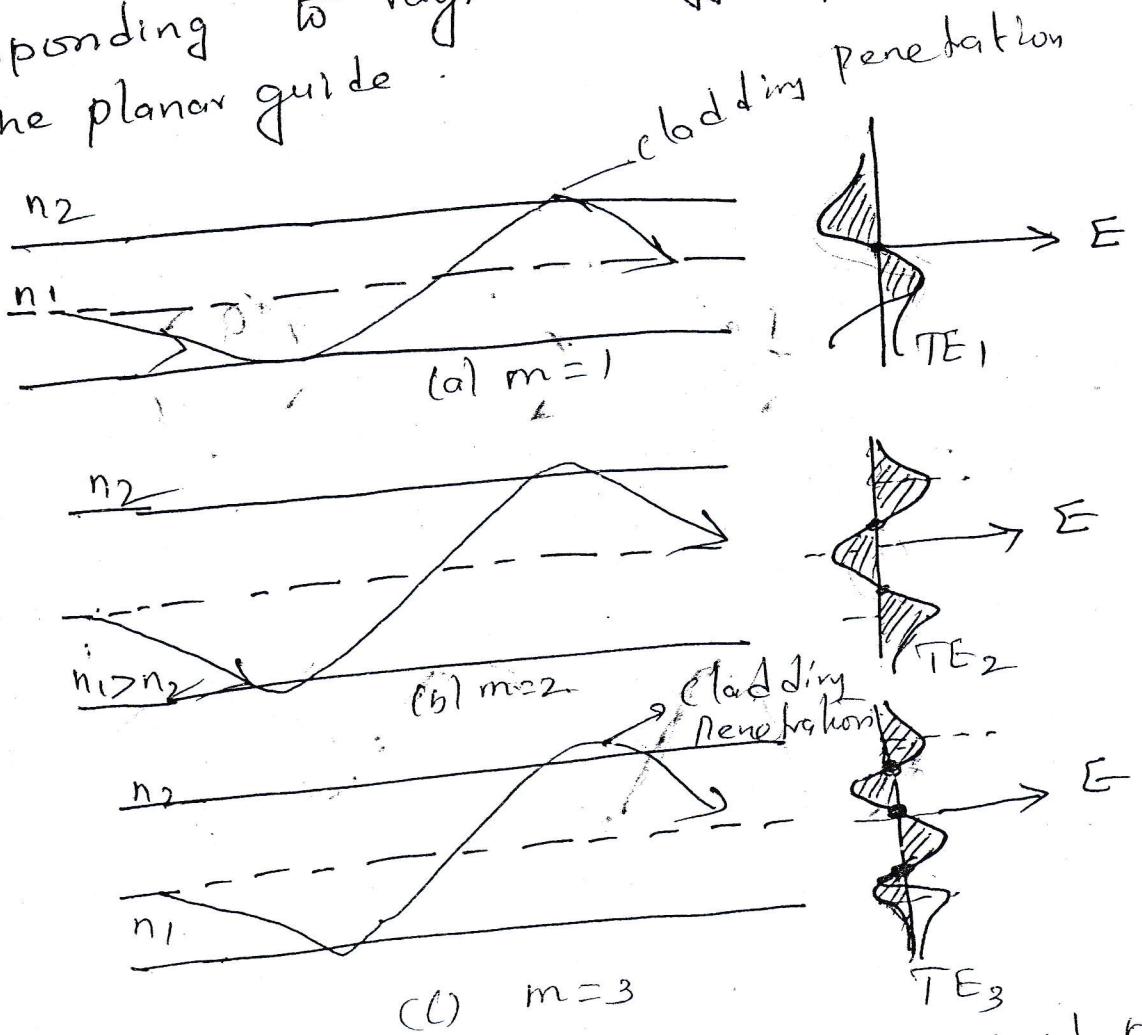


Fig (b)

- * When the total phase change after two successive reflections at the upper & lower interfaces (b/w P & Q) is $2m\pi$ radians, where m is an integer, then constructive interference occurs & a standing wave is obtained in x direction (This is in Fig (b))
- * E is max. at the centre of guide decaying towards zero at the boundary b/w guide & cladding
- * The stable field distribution in x -direction with only a periodic z dependence is known as a Mode.

* To visualize the dominant modes propagating in the z -direction, we consider plane waves corresponding to rays at diff. specific angles in the planar guide.



Ray Propagation & corresponding TE field patterns of 3 lower order modes ($m=1, 2, 3$) in the planar dielectric guide

- * When light is described as an EM wave it consists of a periodically varying E & H which are oriented at right angles to each other.
- * When $E_z = 0$ & magnetic field is in direction of propagation, modes are said to be transverse Electric (TE) when a component of E field is in dir. of propagation & $H_z = 0$, modes are called transverse magnetic (TM) & $E_z = 0$, TEM waves exist (Rarely found in optical fibers).

Phase vector

Overview of Modes:

- * Order 0 mode is equal to the no. of field zeros across the guide

Low-order Modes: Fields are tightly concentrated near the centre of the slab (axis of), with little penetration into the cladding region. - Bounded

Higher-order modes: Fields are distributed more towards the edges of the guide & penetrate further into the cladding region. - Radiation modes

* Leaky modes: Boundary b/w bounded & radiation modes, which is defined by some cut-off condition. (e)

$$n_2 k < \beta < n_1 k \quad \text{for modes guided inside the core}$$

- * There leaky modes are only partially confined to the core region & attenuate by continuously radiating their power out of the core as they propagate along the fiber. This radiation out of the waveguide results from a quantum mechanical phenomenon known as Tunnel Effect.

Phase velocity :

The velocity of propagation of a point of constant phase in the wave. In the case of plane waves these constant phase points form a surface called Wavefront. Hence the points of constant phase in a wave front travel at a phase velocity such that

$$V_p = \frac{\omega}{\beta}$$

Where ω - angular frequency of the wave
 β - phase / propagation constant

Group velocity

velocity of wave packet which is formed by a sum of plane wave component of diff. frequencies such that

$$V_g = \frac{d\omega}{d\beta}$$

Cylindrical fiber

Mode:

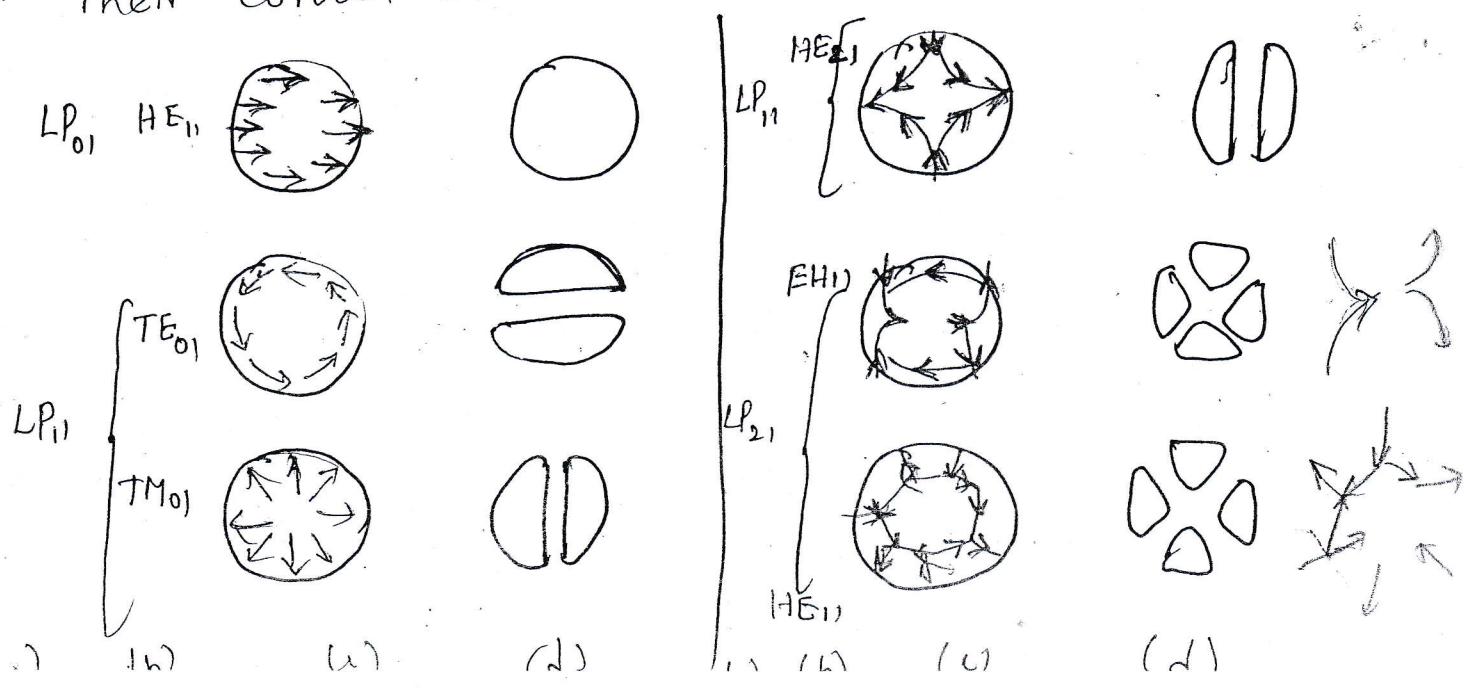
- * For cylindrical waveguide, we refer to TE_{lm} & TM_{lm} modes. These modes correspond to meridional rays travelling within the fiber.
- * However, hybrid modes where $E_2 \neq 0$ also occur within the cylindrical waveguide. These modes result from skew ray propagation within the fiber are designated as HE_{lm} & EH_{lm} depending upon whether the components of H or E make the larger contribution to transverse field (axis)
- * Thus exact description of modal fields in a step index fiber proves complicated. Therefore the analysis may be simplified when the fibers satisfy the weakly guided approximation where $\Delta \ll 1$.
- * In fact $\Delta < 3\%$. for optical fiber communication
- * For weakly guided structures, the approximate solution for HE , EH , TE & TM modes may be given by two linearly polarized Components (LP)
- * There LP modes are not exact modes of the fiber. except for fundamental (lowest order mode) fiber. as Δ is very small in weakly guiding fiber
- * However, as Δ is very small in weakly guiding fiber HE - EH modes are said to be degenerate.

* Relationship b/w traditional HE, EH, TE & TM mode designations & LP_{lm} mode designations are given as

Linearly Polarized	Exact
LP ₀₁	HE ₁₁
LP ₁₁	HE ₂₁ , TE ₀₁ , TM ₀₁
LP ₂₁	HE ₃₁ , EH ₁₁
LP ₀₂	HE ₁₂
LP ₃₁	HE ₄₁ , EH ₂₁
LP ₁₂	HE ₂₂ , TE ₀₂ , TM ₀₂
LP _{lm}	HE _{2m} , TE _{0m} , TM _{0m}

Correspondence b/w lower order in LP modes & traditional exact modes from which they are formed

- * The mode subscript l & m are related to electric field intensity profile for a particular LP mode
- * Electric field intensity profiles for the lowest three LP modes, together with E distribution of their constituent exact modes are shown below.



* for the cylindrical homogeneous core waveguide under the weak guidance conditions, the scalar wave equation can be written in the form:

$$\frac{d^2\psi}{dr^2} + \frac{1}{r} \frac{d\psi}{dr} + \frac{1}{r^2} \frac{d^2\psi}{d\phi^2} + (n_1^2 k^2 - \beta^2) \psi = 0 \quad \text{--- (1)}$$

Where ψ is the field ($E \text{ or } H$),

n_1 - ref. index of the fiber core

k - propagation constant for light in a vacuum

r, ϕ - cylindrical co-ordinates.

* The propagation constant of guided modes lie in the range: $n_2 k < \beta < n_1 k$ (2)

Where n_2 - ref. index of fiber cladding.

* Solutions of the wave equation for cylindrical fiber are separable, having the form:

$$\psi = E(r) \left\{ \frac{\cos(l\phi)}{\sin(l\phi)} \exp(iwt - \beta z) \right\} \quad \text{--- (3)}$$

Where ψ - dominant transverse E component

Periodic dependence on ϕ following $\cos(l\phi)$ or $\sin(l\phi)$ gives a mode of radial order l . Hence the fiber supports a finite no. of guided modes of the form of above equation.

* Introducing the solution given by eqn(3) into (1) results in a differential equation of the form

$$\frac{d^2 E}{dr^2} + \frac{1}{r} \frac{dE}{dr} + \left[(n_1 k^2 - \beta^2) - \frac{l^2}{r^2} \right] E = 0 \quad (4)$$

* For a step index fiber with a constant refractive index core, eqn(4) is a Bessel differential equation & the solutions are cylinder functions.

* In the core region, the solution are Bessel functions denoted by J_l . & in cladding region, the solution are modified Bessel functions denoted by k_l . These modified Bessel functions decay exponentially with respect to r .

* Electric field may be given by

$$E(r) = G J_l(Ur) \quad \text{for } R < 1 \text{ (core)} \\ = G J_l(U) \frac{k_l(Nr)}{K_l(W)} \quad R > 1 \text{ (cladding)}$$

Where G is the amplitude coefficient

$R = r/a$ is the normalized radial coordinate

a - radius of fiber core.

U & W - Eigen values in core & cladding respectively

denoted as $U = a(n_1^2 k^2 - \beta^2)^{1/2}$

$$W = a(\beta^2 - n_2^2 k^2)^{1/2}$$

$$V = (U^2 + W^2)^{1/2} = ka(n_1^2 - n_2^2)^{1/2}$$

1. An optical fiber in air has an numerical aperture (NA) ≈ 0.4 . Find acceptance angle? light collecting efficiency of fiber

$$\theta_a = n_0 \sin^{-1} NA$$

for air

$$\theta_a = \sin^{-1}(0.4) = 23.6^\circ$$

Q Let medium 1 be glass
medium 2 be water.
For an angle of incidence of 30° determine angle of refraction.

$$n_1 (\text{glass}) = 1.5$$

$$n_2 (\text{water}) = 1.33$$

$$\text{Angle of incidence } = \phi_1 = 30^\circ$$

using Snell's law, $n_1 \sin \phi_1 = n_2 \sin \phi_2$

$$\sin \phi_2 = \frac{n_1}{n_2} \sin \phi_1$$

$$= \frac{1.5}{1.33} \sin 30^\circ$$

$$\sin \phi_2 = 0.56 \quad = (1.128)(0.5)$$

$$\phi_2 \leq \sin^{-1}(0.56) = 34.05^\circ$$

(3) A silica optical fiber with
Core ref. index of $1.50^{(n_1)}$ and a
cladding refractive index of $1.47 (n_2)$

Determine

(i) critical angle

(ii) Numerical Aperture

(iii) Acceptance angle.

(i) Critical angle is

$$\phi_c = \sin^{-1} \frac{n_2}{n_1}$$

$$= \sin^{-1} \left(\frac{1.47}{1.50} \right)$$

$$= \sin^{-1} (0.98) = 78.5^\circ$$

(ii) NA

$$= \sqrt{(n_1^2 - n_2^2)}$$

$$= \sqrt{(1.50)^2 - (1.47)^2}$$

$$= \sqrt{0.09} = 0.3$$

$$= \sqrt{(2.25 - 2.16)}$$

(iii) Acceptance angle $\theta_a = \sin^{-1}(NA)$

$$= \sin^{-1}(0.3)$$

$$\theta_a = 17.46^\circ$$

Comparison

Parameters

Step Index Fiber

Data rate

Coupling efficiency

Ray path

Index variation

Numerical Aperture

Material used

Pulse spreading

Attenuation of light

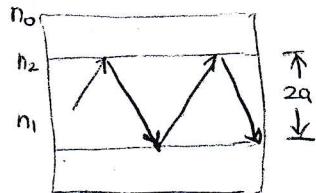
9. Typical light source

Applications

Step Index Fiber

Slow

Coupling efficiency with fiber is higher
By total internal reflection



$$\Delta = \frac{n_1 - n_2}{n_1}$$

NA remains same

Plastic or glass is preferred

Pulse spreading by fiber length is more

Less typically 0.34 dB/km at 1.3 μm

LED

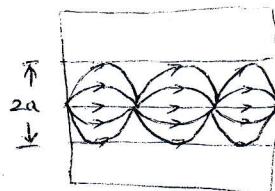
Subscriber local network communication

Graded Index Fiber

Higher

Lower coupling efficiency.

Light ray travels in oscillatory fashion



$$\Delta = \frac{n_1^2 - n_2^2}{2n_1 n_2}$$

Changes continuously with distance from fiber axis

Glasses is preferred.

Pulse spreading is less

More 0.6 to 1 dB/km at 1.3 μm

LED, Laser

Local and wide area networks.

Step index

diameter of core \approx about

50 - 200 μm \rightarrow multimode fiber.

8 - 10 μm \rightarrow single mode fiber.

Light rays propagating through it are in form of meridional rays which will cross the fiber axis during every reflection at the core-cladding boundary & are propagating in a zig-zag manner.

2. Signal distortion \rightarrow more in multimode step index fibers since the rays reflected at high angles or the higher order modes travel a greater distance than the rays reflected at low angles or the lower order modes, to reach the exit end of the fiber. So high angle rays arrive later than the low angle rays \therefore signal pulses are broadened & distortion takes place. Not distortion in single mode step index fiber.

4. BW \rightarrow 50 MHz-km \rightarrow multimode step index fiber

$> 1 \text{ GHz} \rightarrow$ single mode step index

5. Attenuation more \rightarrow multimode step index fiber

less \rightarrow single mode step index

more \rightarrow multimode fiber

Graded index

Diameter of core

- 50 μm (multimode).

2. Light rays propagating through it is in the form of skew rays (or) helical rays which will not cross the fiber axis at any time & rays are propagating around the fiber axis in helical or spiral manner.

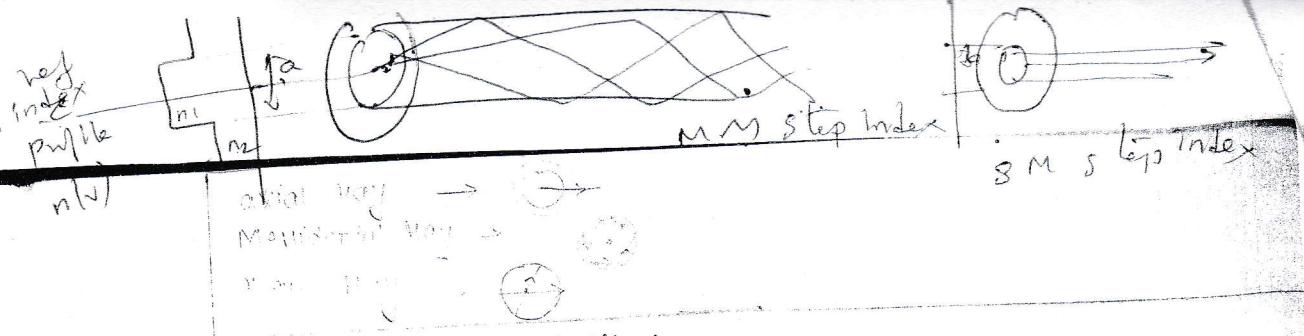
3. Signal distortion low \rightarrow

self focusing effect. Light rays travel at different speeds in different parts of the fiber as the refractive index varies throughout the fiber. As a result light rays near outer edge travel faster than light rays near the centre of the core. In effect light rays are continuously refocussed as they travel down the fiber & almost all rays reach the exit end of fiber at the same time due to helical path of light propagation.

4. BW \rightarrow 200 MHz-km - 600 MHz-km

5. Attenuation - less

6. Numerical aperture \rightarrow less



MULTINODE STEP INDEX :

- centre core layer has large light to fiber aperture end.
- allows more light to enter the cable.
- Light rays strike the core cladding interface and propagate down the core in zig-zag fashion.
- do not take same amount of time to travel along the length of the fiber.

MULTIMODE GRADATED INDEX :

- Light propagates through refraction constantly reflected and result in continuous bending of light rays.
- Light enters at many different angles.

N

14.07.09

1. DIAMETER

Single mode \rightarrow 8-10 μm Multimode \rightarrow 50 μm
Multimode \rightarrow 50-200 μm

High \downarrow

2. PATH RATE

Slow

3. RAY PATH

CLADDING

Step index fiber
 $n(r) = \begin{cases} n_1 & r \leq a \\ n_2 & r > a \end{cases}$

core

cladding

core

<p

	May be arrive later than the low angle rays. ∴ single pulses are broadened & distortion takes place. No distortion in single mode step index fiber.	near the center of the core. In effect light rays are continuously refocussed as they travel down the fiber & almost all rays reach the exit end of the fiber at the same path of light propagation time due to helical.	When, $\alpha = 1$ $\alpha = 2$ $\alpha = \infty$ $n(H) =$
10/1/09	Index VARIATION	$\Delta = \frac{n_1 - n_2}{n}$	$A = \frac{n_1^2 - n_2^2}{2n^2}$
MATERIAL USED	Plastic or glass	Chess	
LIGHT SOURCE	LEDs	LED, LASER	
NUMERICAL APERTURE	Remain same.	changes continuously with distance from the fiber axis.	NA(H)
BANDWIDTH	Multimode - 50 MHz.Km - 200 MHz.Km - 600 MHz.Km Single mode > 1 GHz		where, NA(D)
PULSE SPREADING	Mode	Zero.	
APPLICATION	subscriber local n/w LAN & WAN communication.		No. of

GRADED INDEX FIBER STRUCTURE:

$$n(H) = \begin{cases} n_1 [1 - 2\Delta (\frac{H}{a})^\alpha]^{1/2} & 0 \leq H \leq a \quad (\text{core}) \\ n_1 [1 - 2\Delta]^{1/2} \leq n_1 [1 - \Delta] & H \geq a \quad (\text{cladding}) \\ \leq n_2 \end{cases}$$

H → radial distance

a → core radius

$n_1, n_2 \rightarrow$ refractive index of core, cladding.

358 169 165 →

9 88 4 43 8 262