Consider a matrix  $A \in M_{86}(F)$  in RREF and has 4 pivot columns. Determine the nullity of A

**Problem Solving** - What are the terms/strategies I may need? What do I know?

## Theorems:

- 1) Rank of A is the number of pivots in the RREF matrix.
- 2) Nullity of A is the number of non-pivots in A.

## Definition of $M_{86}(F)$

A matrix with 8 rows 6 columns with entries over the field of F.

Consider a matrix  $A \in M_{86}$  in RREF and has 4 pivot columns. Determine the nullity of A

**Steps & Process** – Try to answer the question writing in many steps to avoid small errors.

Since there are 4 pivot columns in the matrix and 6 columns in R, there are 2 non-pivot columns.

Therefore Nullity(A) = 2

Consider a matrix  $A \in M_{86}$  in RREF and has 4 pivot columns. Determine the nullity of A

**Solidify Understanding** – Explain why the steps makes sense by connecting to math you know.

- Why do we select the columns of A for col space but the rows of B for the row space?
- Why does Rank + Nullity = m when a matrix is an  $A_{nm}$ ?
- Would the columns of A span  $R^6$ ? Would they span  $R^8$ ? Why or why not?
- What would be the maximum and minimum Rank values for this matrix?
- What would be the maximum and minimum Nullity values for this matrix?

For Video Please click the link below:

<u>Video</u>