

En la función final no debe haber términos negativos

Ecuaciones principales

$$V_c(t) = R i_1(t) + L \frac{d[i_1(t) - i_2(t)]}{dt} + R [i_1(t) - i_2(t)]$$

$$L \frac{d[i_1(t) - i_2(t)]}{dt} + R [i_1(t) - i_2(t)] = R i_2(t) + R i_2(t) + \frac{1}{C} \int i_2(t) dt$$

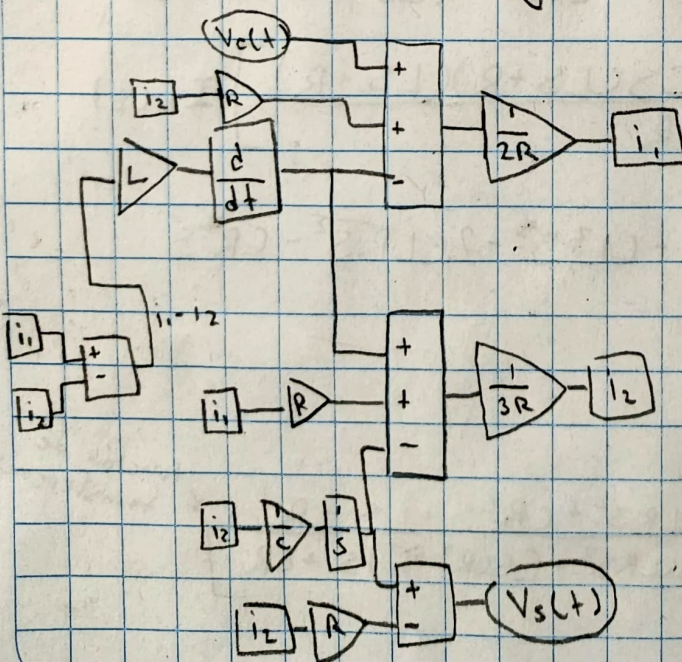
$$V_s(t) = R i_2(t) + \frac{1}{C} \int i_2(t) dt$$

Modelo de ecuaciones integro-diferenciales

$$i_1(t) = \left[V_c(t) - L \frac{d[i_1(t) - i_2(t)]}{dt} + R i_2(t) \right] \frac{1}{2R}$$

$$i_2(t) = \left[L \frac{d[i_1(t) - i_2(t)]}{dt} + R i_1(t) - \frac{1}{C} \int i_2(t) dt \right] \frac{1}{3R}$$

$$V_s(t) = R i_2(t) + \frac{1}{C} \int i_2(t) dt$$



Transformada de Laplace

$$V_c(s) = RI_1(s) + LS[I_1(s) - I_2(s)] + R[I_1(s) - I_2(s)]$$

$$LS[I_1(s) - I_2(s)] + R[I_1(s) - I_2(s)] = RI_2(s) + RI_2(s) + \frac{I_2(s)}{Cs}$$

$$V_c(s) = RI_2(s) + \frac{I_2(s)}{Cs} = \frac{(RS+1)}{Cs} I_2(s) \quad (3)$$

Procedimiento algebraico

$$V_c(s) = (R + LS + R)I_1(s) - (LS + R)I_2(s)$$

$$= (LS + 2R)I_1(s) - (LS + R)I_2(s) \quad (1)$$

$$LSI_1(s) - LSI_2(s) + RI_1(s) - RI_2(s) = 2RI_2(s) + \frac{I_2(s)}{Cs}$$

$$LSI_1(s) + RI_1(s) = 3RI_2(s) + LSI_2(s) + \frac{I_2(s)}{Cs}$$

$$(LS + R)I_1(s) = (3R + LS + \frac{1}{Cs})I_2(s)$$

$$I_1(s) = \frac{3CRS + (LS^2 + 1)}{Cs(LS + R)} I_2(s) = \frac{(LS^2 + 3CRS + 1)}{Cs(LS + R)} I_2(s) \quad (2)$$

$$V_c(s) = \frac{(LS + 2R)(CLS^2 + 3CRS + 1)}{Cs(LS + R)} I_2(s) - (LS + R)I_2(s)$$

$$= \left[\frac{(LS + 2R)(CLS^2 + 3CRS + 1) - Cs(LS + R)(LS + R)}{Cs(LS + R)} \right] I_2(s)$$

Mult:

$$CL^2S^3 + 3CLRS^2 + LS + 2RCLS^2 + 6CR^2S + 2R - CL^2S^3 - 2CLRS^2 - CR^2S$$

$$\therefore V_c(s) = \frac{3CLRS^2 + (5CR^2 + L)S + 2R}{Cs(LS + R)}$$

$$\frac{V_c(s)}{V_c(s)} = \frac{\frac{(RS+1)}{Cs} I_2(s)}{\frac{3CLRS^2 + (5CR^2 + L)S + 2R}{Cs(LS+R)}} = \frac{LS^2 + CR^2S + LS + R}{3CLRS^2 + (5CR^2 + L)S + 2R} \quad \leftarrow \text{función de transferencia}$$

$$(CRS+1)(LS+R) = CLRS^2 + CR^2S + LS + R$$

$$C = 100 \times 10^{-6}$$

$$R = 1K$$

$$L = 68m$$

Estabilidad en lazo abierto

Calcular los polos de la función de transferencia

$$\frac{V_e(s)}{V_o(s)} = \frac{CLR s^2 + (CR^2 + L)s + R}{3CLR s^2 + (5CR^2 + L)s + 2R}$$

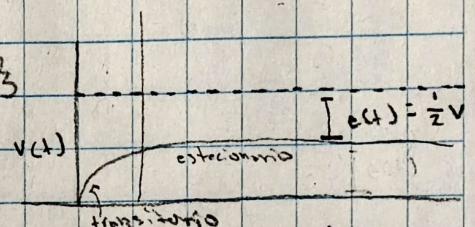
$$\text{den} = [3 * C * L * R, 5 * C * R^2 + L, 2 * R]$$

$L = \text{np.roots}(\text{den})$

→ print : Los raíces son $\{L[0]\}$ y $\{L[1]\}$

$$\lambda_1 = -24509803.25490105$$

$$\lambda_2 = -4.000001088000205$$



El sistema presenta una respuesta estable y sobreamortiguada

Error en estado estacionario

$$e(s) = \lim_{s \rightarrow 0} s V_e(s) \left[1 - \frac{V_s(s)}{V_o(s)} \right]$$

$$= \lim_{s \rightarrow 0} s \cdot \frac{1}{s} \left[1 - \frac{CLR s^2 + (CR^2 + L)s + R}{3CLR s^2 + (5CR^2 + L)s + 2R} \right] = \frac{R}{2R}$$

$$e(t) = \frac{1}{2} V$$