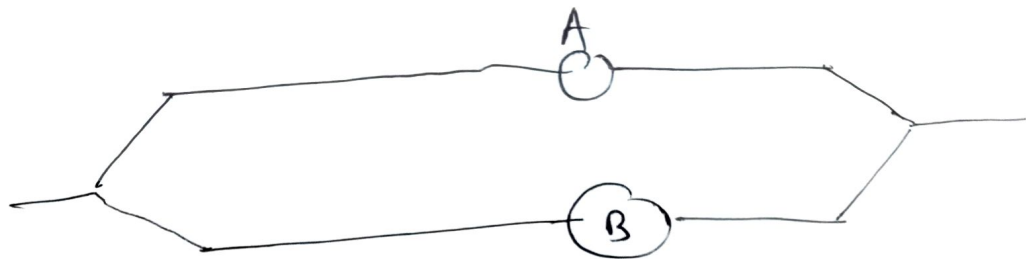


Ex

A system consists of two components A & B connected parallelly in the following way:



The event  $E_1$  denotes that <sup>the</sup> component A works with probability 0.9 and the event  $E_2$  denotes that the component B works with probability 0.8. Find the prob. that the system works

Sol<sup>n</sup> Given  $P(E_1) = P(\{A \text{ works}\}) = 0.9$   
 $P(E_2) = P(\{B \text{ works}\}) = 0.8$

Since  $E_1$  &  $E_2$  are independent, we have

$$P(E_1 \cap E_2) = P(E_1) \cdot P(E_2) = 0.9 \times 0.8 = 0.72$$

The prob. that system works is

$$P(E_1 \cup E_2) = P(E_1) + P(E_2) - P(E_1 \cap E_2) = 0.9 + 0.8 - 0.72 = 0.98$$

Alternative

$$P(\text{System does not work}) = P(E_1' \cap E_2')$$

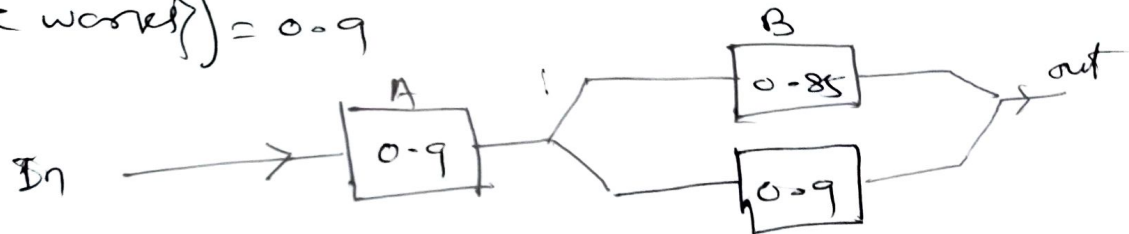
$$= P(E_1') P(E_2') = 0.1 \times 0.2 = 0.02$$

$$\therefore P(\text{System works}) = 1 - 0.02 = 0.98$$

✓

Ex

Q In the following system A, B & C are the components works with probabilities  
 $P(\{A \text{ works}\}) = 0.9$ ,  $P(\{B \text{ works}\}) = 0.85$   
 $P(\{C \text{ works}\}) = 0.9$



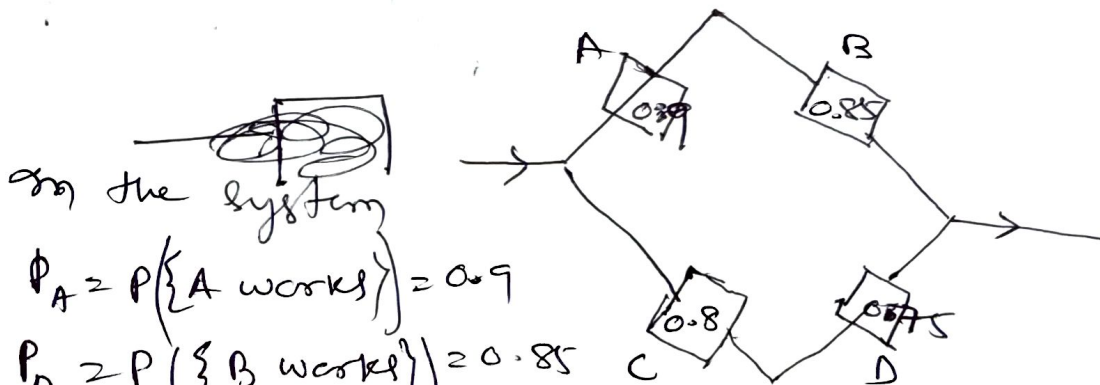
Find the prob. that the system works

Soln

Probability of system works is

$$\begin{aligned}
 &= P(A \cap (B \cup C)) = P((A \cap B) \cup (A \cap C)) \\
 &= P(A \cap B) + P(A \cap C) - P(A \cap B \cap C) \\
 &= P(A)P(B) + P(A)P(C) - P(A)P(B)P(C) \\
 &= 0.9 \times 0.85 + 0.9 \times 0.9 - 0.9 \times 0.85 \times 0.9 \\
 &= 0.8895
 \end{aligned}$$

Ex



In the system

$$P_A = P(\{A \text{ works}\}) = 0.9$$

$$P_B = P(\{B \text{ works}\}) = 0.85$$

$$P_C = P(\{C \text{ works}\}) = 0.8$$

$$P_D = P(\{D \text{ works}\}) = 0.75$$

Find the prob. that system works

Soln

$$\begin{aligned}
 P(\{\text{system works}\}) &= P((A \cap B) \cup (C \cap D)) \\
 &= P(A \cap B) + P(C \cap D) - P(A \cap B \cap C \cap D) \\
 &= 0.9 \times 0.85 + 0.8 \times 0.75 - 0.9 \times 0.85 \times 0.8 \times 0.75 \\
 &= 0.906
 \end{aligned}$$