

# DMS RELATIONS FOR PROBLEM SOLVING

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## BASIC LAWS:

1. IDENTITY LAW: **REMEMBERING TRICK**: GIVES THE SAME IDENTITY
  - $P \text{ AND TRUE} == P$
  - $P \text{ OR FALSE} == P$
2. DOMINATION LAW: **REMEMBERING TRICK**: TRUE AND FALSE ARE ALWAYS DOMINANT IN BOTH AND/OR OPERATION.
  - $P \text{ AND T} == T$
  - $P \text{ OR F} == F$
3. NEGATION LAW: **REMEMBERING TRICK**:  
OR  $\rightarrow T$  AND  $\rightarrow F$ 
  - $P \text{ OR } \sim P == T$  ( $\sim$  REPRESENTS NEGATION)
  - $P \text{ AND } \sim P == F$
4. DOUBLE-NEGATION LAW:  
**REMEMBERING TRICK**:  
NEGATION OF NEGATION IS ITSELF.
  - $\sim \sim P == P$
5. IDEMPOTENT LAW: **REMEMBERING TRICK**:  
AND/OR OPERATION AMONG SAME OPERAND GIVE THE SAME OUTPUT
  - $P \text{ OR } P == P$
  - $P \text{ AND } P == P$

NOTE::::\*\*\*\*P,Q,R ARE ALL CALLED OPERANDS.

6. COMMUTATIVE LAW: REMEMBERING TRICK:

JUST LIKE  $A+B==B+A$

- $P \text{ AND } Q == Q \text{ AND } P$
- $P \text{ OR } Q == Q \text{ OR } P$

7. DE-MORGAN'S LAW: (IMP)

- $\sim (P \text{ OR } Q) == \sim P \text{ AND } \sim Q$
- $\sim (P \text{ AND } Q) == \sim P \text{ OR } \sim Q$

8. ASSOCIATIVE LAW: REMEMBERING TRICK:  
THREE OPERANDS WITH SAME OPERATION  
(EITHER AND / OR ) WE USE ASSOCIATIVE LAW.

- $P \text{ AND } (Q \text{ AND } R) == (P \text{ AND } Q) \text{ AND } R$
- $P \text{ OR } (Q \text{ OR } R) == (P \text{ OR } Q) \text{ OR } R$

9. DISTRIBUTIVE LAW: REMEMBERING TRICK:  
THREE OPERANDS WITH DIFFERENT  
OPERATIONS (EITHER AND / OR ) WE USE  
DISTRIBUTIVE LAW.

- $P \text{ AND } (Q \text{ OR } R) == (P \text{ AND } Q) \text{ OR } (P \text{ AND } R)$
- $P \text{ OR } (Q \text{ AND } R) == (P \text{ OR } Q) \text{ AND } R$

10. ABSORPTION LAW:

- $P \text{ OR } (P \text{ AND } Q) == P$
- $P \text{ AND } (P \text{ OR } Q) == P$

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## LOGICAL EQUIVALENCE

1.  $P \rightarrow Q \equiv \sim P \vee Q$
2.  $P \rightarrow Q \equiv \sim Q \rightarrow \sim P$
3.  $\sim P \rightarrow Q \equiv P \vee Q$
4.  $\sim(Q \rightarrow \sim P) \equiv P \wedge Q$
5.  $P \rightarrow (Q \wedge R) \equiv (P \rightarrow Q) \wedge (P \rightarrow R)$
6.  $(P \vee Q) \rightarrow R \equiv (P \rightarrow R) \wedge (Q \rightarrow R)$
7.  $P \rightarrow (Q \vee R) \equiv (P \rightarrow Q) \vee (P \rightarrow R)$
8.  $(P \wedge Q) \rightarrow R \equiv (P \rightarrow R) \vee (Q \rightarrow R)$
9.  $P \leftrightarrow Q \equiv (P \rightarrow Q) \wedge (Q \rightarrow P)$
10.  $P \leftrightarrow Q \equiv \sim P \leftrightarrow \sim Q$
11.  $P \leftrightarrow Q \equiv (P \wedge Q) \vee (\sim P \wedge \sim Q)$
12.  $\sim(P \leftrightarrow Q) \equiv P \leftrightarrow \sim Q$

## ORDER OF PRECEDENCE OF OPERATIONS

1. NEGATION ( $\sim$ )
2. AND
3. OR
4. IMPLIES ( $\rightarrow$ )
5. DOUBLE IMPLIES ( $\leftrightarrow$ )

HERE:  $5 > 4 > 3 > 2 > 1$  i.e top to bottom  
precedence increases.

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