

Automata and Formal Languages(CS-2010)

Spring Mid-Semester Examination- 2020
School of Computer Engineering
KIIT Deemed to be University,
Bhubaneswar-24

Time: 1 hour 30 mins

Full Marks: 20

(Answer any four questions including question number 1)

1. Answer the following questions briefly. [1×5]

- Show that the language $L = \{a^n : n \geq 0, n \neq 4\}$ is regular.
- Prove or disprove that the following pairs of regular expressions define the same language over the alphabet $\Sigma = \{a, b\}$
 $(ab + a)^*ab$ and $(aa^*b)^*$
- Find an NFA with three states that accepts the language $L = \{a^n : n \geq 1\} \cup \{b^m a^k : m \geq 0, k \geq 0\}$.
- Construct an NFA equivalent to regular expression $r = (01 + 2^*)^* 1$.
- Find the shortest string not in the language over $\Sigma = \{a, b\}$ of the regular expression $a^* b^* (ba)^* a^*$.

2. [2.5×2]

- Design a DFA to accept all the strings w over $\Sigma = \{1, 2, 3\}$ such that the digits in w appear in non-decreasing order. For example, it accepts 1123, but not 1232.
- Design a DFA for the following language on $\Sigma = \{a, b\}$
 $L = \{w : n_a(w) + 2n_b(w) \bmod 3 < 2\}$

3. [2.5×2]

- Design an NFA that accepts strings over $\{0, 1\}$ that ends in 0 but doesn't have 11 as sub-string. Convert your NFA to DFA.
- Find the minimum state DFA equivalent to the following DFA.

$M = (\{q_0, q_1, q_2, q_3, q_4, q_5\}, \Sigma = \{0, 1\}, \delta, q_0, F = \{q_3, q_5\})$

$Q \backslash \Sigma$	0	1
$\rightarrow q_0$	q_1	q_3
q_1	q_0	q_3
q_2	q_1	q_4
$*q_3$	q_5	q_5
q_4	q_3	q_3
$*q_5$	q_5	q_5

[2+3]

4.

- a) Draw the transition diagram for the following transition table. Find a regular expression equivalent to the DFA.

$Q \backslash \Sigma$	0	1
$\rightarrow q_0$	q_0	q_1
q_1	q_2	q_1
$*q_2$	q_0	q_2

- b) Write regular expression for the following language:

- $L = \{b^m ab^n \mid m > 0, n > 0\}$
- Any string of length multiple of 5 over $\{0, 1, 2\}$
- Any string where first symbol is 0 and third symbol from right is 0 over $\{0, 1\}$

[2+3]

5.

- a) If L_1 and L_2 are two regular languages then prove that $L_1 - L_2$ is also regular.
- b) State Pumping Lemma for the regular languages. Show that the language $L = \{a^n b^{2n} \mid n \geq 1\}$ is not regular.

All The Best