

# Scheme of Evaluation and Sample Solution for FLAT-2017

NOTE: STEP MARKS SHOULD BE AWARDED WHERE EVER APPLICABLE.

Q.1. a) Note that in the body of every production number of a's is twice the number of b's.

b) FALSE.

$$\Sigma = \{a, b\}, \text{ let } L = \{a^n b^n \mid n \geq 0\}$$

$$L = \{a^n b^n \mid n \geq 0\} \subset \Sigma^*$$

where  $\Sigma^*$  is regular but  $L$  is not regular.

c) Let  $L$  be an infinite context-free language. Then there exists some positive integer  $m$  such that any  $w \in L$  with  $|w| \geq m$  can be decomposed as

$$w = uvxy^2 \text{ with}$$

$$|vxy| \leq m$$

$$|vy| \geq 1 \text{ such that } uvx^i y^i z \in L$$

for all  $i = 0, 1, 2, \dots$

d)  ~~$h(a) = 0$~~ ,

$$h(a(a + a^*aa) + aaa)^*$$

$$= \max(\max(h(a), h(a + a^*aa)), h(aaa)) + 1$$

$$= h(a + a^*aa) + 1$$

$$= \max(h(a), h(a^*aa)) + 1$$

$$= 1 + 1 = 2$$

e)  $S \rightarrow aas \mid abs \mid bas \mid bbs \mid \lambda$



f)  $S \rightarrow aSB \mid bSA \mid a \mid b \mid aB$

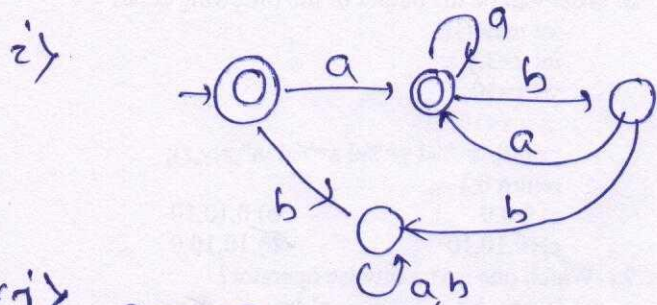
$A \rightarrow a$

$B \rightarrow b$

g) If every grammar that generates  $L$  is ambiguous, then the language is called inherently ambiguous.

Example:  $L = \{a^n b^n c^m\} \cup \{a^n b^m c^m\}$ .

h)  $L = \{a^n b^m \mid n > m\}$



j) FALSE.

Lang.  $L$  is finite therefore  $L$  is recognized by PDA and also by finite Automata.

Q.2

a) (i)  $S \rightarrow OS1 \mid ISO \mid OSO \mid ISI \mid 2$

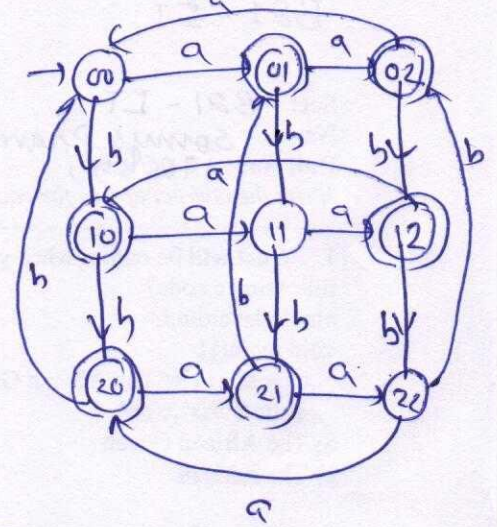
(ii)  $S \rightarrow S_1 \mid S_2, \quad \begin{array}{l} S_1 \rightarrow AS_1 \\ S_1 \rightarrow aS_1b \mid \lambda \\ A \rightarrow aA \mid a \end{array} \quad \left| \quad \begin{array}{l} S_2 \rightarrow S_2B \\ S_2 \rightarrow aS_2b \mid \lambda \\ B \rightarrow bB \mid b \end{array} \right.$

b) considering  $A$  as initial state. a closure of  $\{A\} \rightarrow \{A, B\}$

	0	1
$\{A, B\}$	$\{A, B, C\}$	$\{B, C\}$
$\{B, C\}$	$\{A, B\}$	$\{B, C\}$
$\{A, B, C\}$	$\{A, B, C\}$	$\{B, C\}$



Q.3 a) The language is regular as the following DFA accepts it.



$$b) S \rightarrow bS \mid aA$$

$$A \rightarrow aA \mid bB$$

$$B \rightarrow aB \mid bB \mid \lambda$$

$$L = \rightarrow S \xrightarrow{b} A \xrightarrow{a} B \xrightarrow{a,b}$$

$$L^R = \leftarrow S \xleftarrow{b} A \xleftarrow{a} B \xleftarrow{a,b}$$

$$B \rightarrow aB \mid bB \mid bA$$

$$A \rightarrow aA \mid aS$$

$$S \rightarrow bS \mid \lambda$$

$$B \rightarrow Ba \mid Bb \mid Ab$$

$$A \rightarrow Aa \mid Sa$$

$$S \rightarrow Sb \mid \lambda$$

where B is stand variable.

Q.4

① Mark should be given based on removal of removal of  $\lambda$  - production removal of Unit - production etc.

② If possible, let  $L = \{x^n y^m \mid n \neq m\}$  be regular.

that implies  $\bar{L}$  is also regular

So, Now  $\bar{L}$  is regular and  $L(x^* y^*)$  is regular.

$$\Rightarrow \bar{L} \cap L(x^* y^*)$$

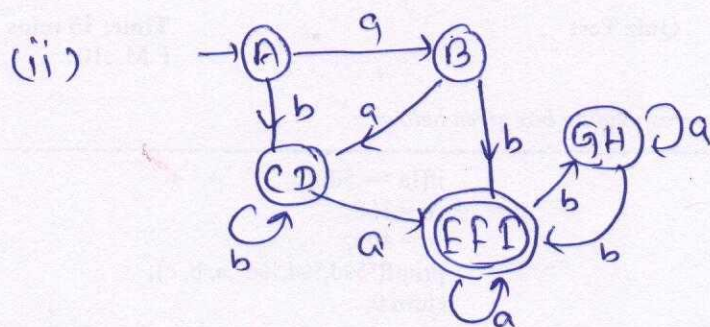
$$\Rightarrow \{x^n y^n \mid n \geq 0\} \text{ is regular.}$$

which is contradiction.

$\{x^n y^n \mid n \geq 0\}$  is not regular can easily be proved using pumping lemma.



Q.5 a) (i) indistinguishable pairs:  $(C, D), (G, H), (E, F, I)$ .

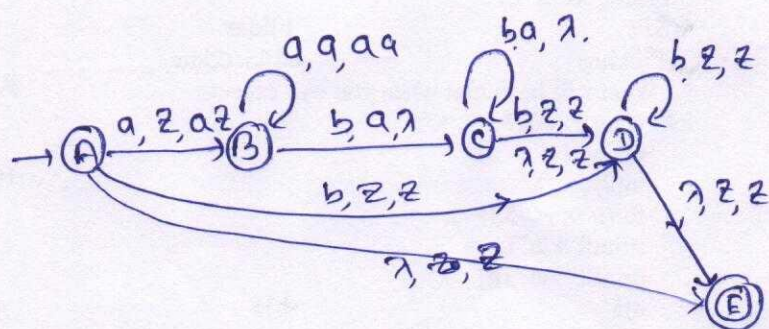


b) The family of regular language is closed under complementation and union.

$$\text{Now } L \cap M = \overline{\overline{L} \cup \overline{M}}$$

Therefore intersection of two regular language is also regular.

Q.6 a)  $L = \{a^n b^m \mid m \geq n\}$ .



b)  $S \rightarrow SS$

①  $S \rightarrow aS \mid Sb \mid ab$

for a string  $aababbb$  there exist two left-most derivations.

(i)  $S \rightarrow aS \rightarrow aSS \rightarrow aabS \rightarrow aabSb \rightarrow aababbb$

(ii)  $S \rightarrow Sb \rightarrow SSb \rightarrow Sabbb \rightarrow aSabb \rightarrow aababbb$

② The language for the given grammar is

$L = \{ \text{any string that starts with } a \text{ and ends with } b \}$ .

So unambiguous grammar for it is

$$\begin{array}{l} S \rightarrow aAb \\ A \rightarrow aA \mid bA \mid \lambda \end{array}$$



Q.7

a)

$S \rightarrow ABA | aSa | bSb$   
 $A \rightarrow aA | aAb | B$   
 $B \rightarrow bB | \lambda$

Removal of  $\lambda$ -production.

$S \rightarrow ABA | aSa | bSb | AB | BA | B | A | aa | bb$   
 $A \rightarrow aA | aAb | B | ab | a$   
 $B \rightarrow bB | b$

Removal of unit production

$S \rightarrow ABA | aSa | bSb | AB | BA | bB | b | aA | aAb | bB | b | ab | a$   
 $A \rightarrow aA | aAb | bB | b | ab | a$   
 $B \rightarrow ab | b$

b) If  $m$  be the max. no. of symbols in RHS, then for each production we have at most  $(m-1)$  productions in CNF.

As we have  $|P|$  productions, then we have  $(m-1)|P|$  no. of production.

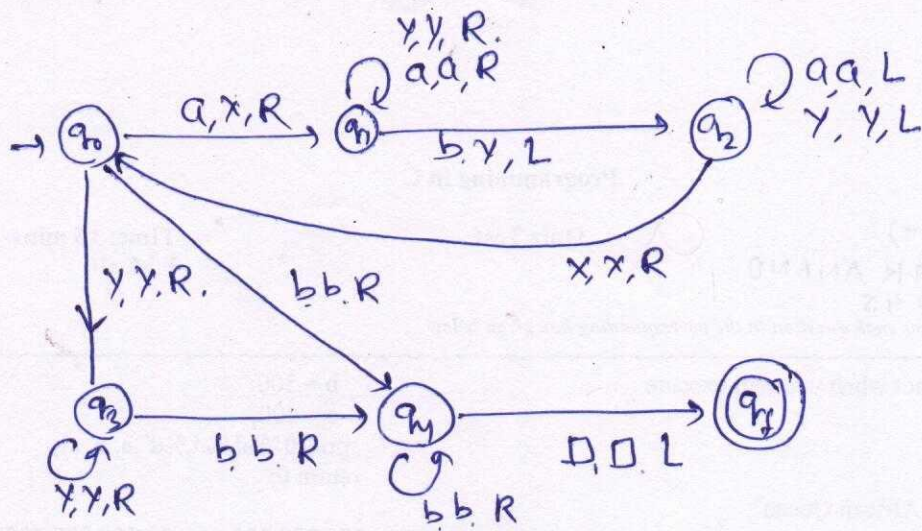
We will have exactly one production of the form  $A \rightarrow a$  for each terminal  $a$ .

Hence our equivalent grammar in CNF will have at most

$(m-1)|P| + |T|$  number of productions.



Q.8  
a)



b)  $S \rightarrow aABB | aAA$  |  $S \rightarrow aAAB | aAA$   
 $A \rightarrow aBB | b$  |  $A \rightarrow aBB | b$   
 $B \rightarrow bBB | A$  |  $B \rightarrow bBB | aBB | b$

$$\delta(q_0, \lambda, z) \rightarrow \{(q_1, Sz)\}$$

$$\delta(q_1, \lambda, z) \rightarrow \{(q_f, z)\} \text{ final state.}$$

$$\delta(q_1, a, S) \rightarrow \{(q_1, ABB), (q_1, AA)\}$$

$$\delta(q_1, a, A) \rightarrow \{(q_1, BB)\}$$

$$\delta(q_1, b, A) \rightarrow \{(q_1, \lambda)\}$$

$$\delta(q_1, b, B) \rightarrow \{(q_1, BB), (q_1, \lambda)\}$$

$$\delta(q_1, a, B) \rightarrow \{(q_1, BB)\}$$

end