

KALINGA INSTITUTE OF INDUSTRIAL TECHNOLOGY (KIIT)

(Deemed to be University) **DEPARTMENT OF MATHEMATICS SCHOOL OF APPLIED SCIENCES** AUTUMN SEMESTER 2023-24 **COURSE HANDOUT**

Date: 09.08.2023

1. Course Title: PROBABILITY AND STATISTICS

Course Code: MA 21001
 L-T-P Structure: 3-1-0

4. Course Coordinator: Dr. Prasanta Kumar Das5. Associate Course Coordinator: Dr. Arjit Patra

6. COURSE OBJECTIVE

The objective of this course is to familiarize the students with the foundation of probability and statistics and to use it in solving the problems arises in engineering and real life applications.

7. COURSE OUTCOMES

At the end of the course, the students will be expected to: CO1:

understand basic probability and its applications

CO2: study probability distributions and can use it in real life data analysis

CO3: have a knowledge on univariate and bivariate distributions and their properties

CO4: measure the central tendency and dispersion of a data set to draw conclusion from the data and interpret the data with the appropriate pictorial representation.

CO5: have good understanding of the Central Limit Theorem and its applications CO6: analyze the statistical inference

8.COURSE DETAILS Probability and

random variables:

Basic concepts of sample space, events(with example), Axiom of Probability, Conditional Probability, Bayes' Theorem and its applications. Discrete random variable, probability mass function, cumulative distribution function and Moment Generating function for discrete random variable, some special distributions like Uniform distribution, Geometric distribution, Binomial distribution, Negative Binomial distribution, Poisson distribution, Hypergeometric distribution, mean and variance. Continuous random variable, density function, cumulative distribution function and Moment Generating function. Uniform distribution, normal distribution, mean, variance, percentile and critical value of normal distribution, normal approximation of the binomial distribution and exponential distribution.

Joint probability and distributions:

Joint probability mass function and marginal probability mass function, joint probability density function and marginal probability density function, concept of independent random variable(joint probability), conditional probability mass function and conditional probability density function. Expected value, covariance and correlation for jointly distributed random variable(both continuous and discrete). Sum of two independent random variables, and weak law of large number.

Descriptive Statistics:

Frequency distribution, pictorial and tabular representation of data, stem and leaf display, dot plots, histogram, box plots and comparative box plots. Basic concepts on mean, median and mode, Skewness, Kurtosis, Correlation, Coefficient of Correlation, rank correlation, Regression Analysis (Least square method).

Inferential statistics:

Population, sample, random sample, sampling distribution, distribution of sample mean, central limit theorem, point estimator, point estimator, point estimation of parameter using method of maximum likelihood estimation, confidence interval, confidence interval for the mean of a normal population with known and unknown variance, confidence interval for the variance of a normal population, hypothesis testing, one sided and two sided alternatives, Tests for mean of the normal distribution with known variance, tests for variance of the normal distribution.

Text books:

- **T1.** Probability and Statistics for Engineers and Sciences by J. L. Devore, CENGAGE Learning, 9th Edition.
- **T2.** Advanced Engineering Mathematics by Erwin Kreyszig, Wiley, INC, 10th Edition.

Reference Books:

- **R1.** Introduction to Probability and Statistics for Engineers and Scientists by S.M. Ross, Elsevier/AP, 6th Edition.
- **R2.** Introduction to Probability and Statistics by J.S. Milton & J.C. Arnold, McGraw Hill, 4th Edition.
- **R3.** Introduction to Probability Theory and Statistical Inference by H.J. Larson, John Wiley & Sons Inc, 3rd Edition.
- **R4.** Fundamental of Mathematical Statistics by S.C. Gupta & V.K.Kapoor, S. Chand, 12th Edition.

9. LESSON PLAN AND ACTIVITIES

Unit Name	Ame Lect. Learning Topics to be covered No.		Article No./ Text Book	CO Mapping	
		Unit - I (Probability; Discrete random variables and Probability Distributions)			
Basics on Probability	1.	Sample spaces, Events (with examples)	2.1, 2.2 (T1)	CO1	
	2.	Axiom of Probability, Conditional Probability, Bayes' Theorem and its applications.	2.4 (T1)	C01	
	3.	Independent events	2.5 (T1)	CO1	
	4.	Tutorial (Problem Solving)			
Discrete 5. Random variables and Probability Distributions		Discrete random variable, probability mass function, cumulative distribution function	3.1, 3.2 (T1)	CO2	

	6.	Expected values, Moments, Central moments	3.3 (T1)	CO2
	7.	Moment Generating function	24.5 (T2)	CO2
	8.	Tutorial (Problem Solving)	24.3 (12)	CO2
	9.	some special distributions like Uniform distribution, Binomial distribution	3.3, 3.4 (T1)	CO2
	10.	Hypergeometric distribution	3.5 (T1)	CO2
	11.	Geometric distribution, Negative Binomial distribution	3.5 (T1)	CO2
	12.	Poisson distribution	3.6 (T1)	CO2
	13.	Tutorial (Problem solving)		
		Doubt Clearing		
		Quiz Test-1		
		Assignment-I		
Continuous random variables and Probability distributions	14.	Continuous random variable, density function, cumulative distribution function, density function of the function of random variable	4.1(T1)	CO2
	15.	Uniform distribution, Mean, variance and median	4.2(T1)	CO2
	16.	normal distribution, mean, variance, percentile and critical value of normal distribution,	4.3(T1)	CO2
	17.	normal approximation of the binomial distribution, Applications	4.3(T1)	CO2
	18.	exponential distribution, Mean, variance and median	4.4(T1)	CO2
	19.	Tutorial (Problem solving)		
Joint probability and distributions	20.	Joint probability mass function and marginal probability mass functions	5.1(T1)	C03
	21.	Mean and variance of Joint probability mass function and marginal probability mass functions	5.1(T1)	CO3
	22.	Joint probability density function and marginal probability density function	5.1(T1)	C03
	23.	Mean and variance of Joint probability density function and marginal probability density functions	5.2(T1)	CO3
	24.	Tutorial (Problem solving)		CO3
	25.	Independent random variables (joint probability), conditional	5.2(T1)	CO3

		probability mass function and conditional probability density function.		
	26.	Expected value, covariance and Correlation coefficient for jointly distributed joint discrete random variable	5.3(T1)	CO3
	27.	Expected value, covariance and Correlation coefficient for jointly distributed joint continuous random variable	5.3(T1)	CO3
	28.	Linear Combination of random variables, Mean Random variable, mean and variance of mean random variable of the identically independent random variables	5.4(T1)	CO3
	29.	Tutorial (Problem solving)		
	30.	Doubt Clearing		
		Quiz Test-II		
		Assignment-II		
Descriptive Statistics	31.	Frequency distribution, pictorial and tabular representation of data	1.2(T1)	CO4
	32.	stem and leaf display, dot plots,	1.2(T1)	CO4
	33.	histogram, box plots and comparative box plots.	1.2, 1.4(T1)	C04
	34.	Tutorial (Problem solving)		
	35.	Basic concepts on mean, median and mode	1.3(T1)	CO4
	36.	Skewness, Kurtosis Correlation	24.6 (T2)	CO4
	37.	Coefficient of Correlation, rank correlation	25.9 (T2)	CO4
	38.	Tutorial (Problem solving)		
	39.	Regression Analysis: Least square method	20.5 (T2)	CO4
	40.	Linear regression	20.5 (T2)	CO4
	41.	Problems solving on Linear regression	20.5 (T2)	CO4
	42.	Regression: Fitting straight line using correlation coefficient of the data	25.9 (T2)	CO4
	43.	Tutorial (Problem solving)		
Inferential statistics	44.	Population, sample, random sample,	25.1(T2)	CO5
	45.	sampling distribution, distribution of sample mean	25.1(T2)	CO5
	46.	Central limit theorem	25.1(T1)	CO5
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48.	Point estimator, point estimation of parameter using method of maximum likelihood estimation	25.2(T2)	CO5
49.	estimation of parameter of binomial, geometric, poison, exponential, normal distribution		CO5
50.	confidence interval, confidence interval for the mean of a normal population with known variance,	25.3 (T2)	CO6
51.	t-distribution, confidence interval for the mean of a normal population with unknown variance,	25.3(T2)	CO6
52.	Tutorial (Problem solving)		
53.	chi squared distribution, confidence interval for the variance of a normal population,	25.3(T2)	CO6
54.	hypothesis testing, one sided and two sided alternatives,	25.4(T2)	CO6
55.	Tests for mean of the normal distribution with known variance,	25.4(T2)	CO6
56.	Tests for mean of the normal distribution with unknown variance	25.4(T2)	CO6
57.	tests for variance of the normal distribution		CO6
58.	Tutorial (Problem solving)		
59.	Doubt Clearing		
	Quiz Test-III		
	Assignment-III (Critical Q. Sets)		
60 -	Previous Year's question & answer		
62	discussion		

Sl. No.	Assessment Component	Duration	Weightage / Marks	Nature of the Component
1	Mid Semester Examination	90 min	20	Closed Book
2	End Semester Examination	3 Hours	50	Closed Book
3	Problem Solving (Assignment)	1 week	10	Open Book
4	Quiz Test	20 min	15	Closed Book
5	Critical Thinking	15 days	05	Open Book

11. ACTIVITIES CALENDAR

Sl. No.	Type of Activity/ Nature of the Component	Marks	Schedule for Activities	Duration For Submission	Publication of result	Mapping with COs
1	Assignment-I (Open Book)	5	3 rd week of August	1 week	1st week of September	CO1 & CO2
2	Quiz -I (Closed Book)	5	3 rd week of August	30min	3 rd week of August	CO1 & CO2
3	Assignment-II (Open Book)	5	2 nd week of September	1 week	4 th week of September	CO3 & CO4
4	Quiz -II (Closed Book)	5	2 nd week of September	30min	2 nd week of September	CO3 & CO4
5	Critical Thinking (Open Book)	5	2 nd week of November	15 days	4 th week of November	CO1, CO2, CO3, CO4, CO5 & CO6
6	Quiz -III (Closed Book)	5	4 th week of November	30min	4 th week of November	CO5 & CO6