Online Machine Learning Algorithms

1 Binary-classifiers

1.1 Algorithm

Generic implementation of online binary-classifier algorithm is shown below. Input and output arguments of the following implementation can be augmented, if necessary.

```
Algorithm 1: Online Binary-Classifier Algorithm
```

```
Input : \mathcal{D}: Training example data set, \mathcal{N}: Maximum number of training iterations
Output: w: final weight vector

1 initialize weight vector, w = 0
2 for i \leftarrow 1 to \mathcal{N} do
3 for j \leftarrow 1 to each\ (x_t, y_t) \in \mathcal{D} do
4 \hat{y}_t = sign(w \cdot x_t)
5 if \hat{y}_t \neq y_t then
6 w = w + \tau \cdot x_t \cdot y_t
7 end
8 end
9 end
10 return final weight vector, w
```

In standard Perceptron algorithm, learning rate, τ , is assumed as constant (say, $\tau=1$) and for Passive-Aggressive (PA) algorithm, learning rate, τ , needs to be computed using following equation for each mistake in prediction:

$$\frac{1 - y_t \cdot (w \cdot x_t)}{||x_t||^2}$$

For Averaged Perceptron, above algorithm can be modified by keeping track of a mistake counter variable, C, and cumulative weight vector, w_{sum} , and returning the final weight vector as w_{sum}/C .

1.2 binaryclasstest.m

Learn a binary classifier to classify even labels (0, 2, 4, 6, 8) and odd labels (1, 3, 5, 7, 9).

- a. Compute the online learning curve for both Perceptron and PA algorithm by plotting the number of training iterations (1 to 50) on the x-axis and the number of mistakes on the y-axis.
- b. Compute the accuracy of Perceptron, PA, and Averaged Perceptron algorithm on testing data for 20 training iterations by plotting the number of training iterations (1 to 20) on the x-axis and accuracy on the y-axis.

2 Multiple-classifiers

2.1 Algorithm

Generic implementation of online multi-classifier algorithm is shown below. Input and output arguments of the following implementation can be augmented, if necessary.

```
Algorithm 2: Online Multiple-Classifier Algorithm
```

```
Input : \mathcal{D}: Training example data set, \mathcal{N}: Maximum number of training iterations
    Output: w: final weight vector
 1 initialize weight vector, w=0
2 for i \leftarrow 1 to \mathcal{N} do
        for j \leftarrow 1 to each (x_t, y_t) \in \mathcal{D} do
             \hat{y}_t = \arg \max_{y \in 1, 2, \dots k} (w \cdot F(x_t, y_t))
 4
             if \hat{y}_t \neq y_t then
 5
                 w = w + \tau \cdot (F(x_t, y_t) - F(x_t, \hat{y}_t))
 6
             end
 7
        end
 9 end
10 return final weight vector, w
```

Each training example is of the form (x_t, y_t) , where $x_t \in \mathbb{R}^d$ is the input and $y_t \in 1, 2, ..., k$ is the class (output) label. In this representation, you will have a single weight-vector $w \in \mathbb{R}^{k \times d}$ and the augmented feature function $F(x_t, y) \in \mathbb{R}^{k \times d}$ will have k blocks of size d and it will have zeroes everywhere except for the y^{th} block, which will have x_t in it.

Similar to binary-classifier implementation, learning rate, τ , will be considered constant in standard multi-classifier Perceptron and for standard multi-classifier Passive Aggressive algorithm, learning rate, τ , needs to be computed using following formula for each mistake in prediction:

$$\frac{1 - (w \cdot F(x_t, y_t) - w \cdot F(x_t, \hat{y}_t))}{||(F(x_t, y_t) - F(x_t, \hat{y}_t))||^2}$$

For multi-classifier Averaged Perceptron, above algorithm can be modified to return the final weight vector as w_{sum}/C , similar to binary-classifier Averaged Perceptron.

2.2 multiclasstest.m

Learn a multi-class classifier to map images to the corresponding fashion label. Repeat the same experiments using multi-class classifier algorithms as described in section 1.2 (binaryclasstest.m).