Rozwiązania do zadań z dnia 30 września ASD

1. Zadanie

- a. f_2, f_3, f_1
- b. f_2, f_1, f_3
- c. $f_4 f_3, f_2, f_1$
- d. f_3, f_4, f_2, f_1
- 2. Zadanie (Na zielono poprawne, na czerwono błędne)

$$\begin{aligned} & \text{If } (n) = \Theta \left(\sqrt{n} \right), \ f \left(n \right) = O \left(n^{\frac{3}{2}} \lg n \right), \ f \left(n \right) = \Omega \left(\left| \frac{1}{n} - 1 \right| \right), \\ & \text{gdzie } f \left(n \right) = n \sin^2 \left(n \right), \\ & 2f \left(n \right) = \Theta \left(n \lg n \right), \ f \left(n \right) = O \left(n^{\lg 3} \right), \ f \left(n \right) = \Omega \left(n \sqrt{n} \right), \\ & \text{gdzie } f \left(n \right) = \lg n^{\sqrt{n}}, \\ & 3f \left(n \right) = \Theta \left(\frac{\sqrt{n}}{n!} \right), \ f \left(n \right) = O \left(n \lg n^{2^{\lg n}} \right), \ f \left(n \right) = \Omega \left(n \right), \\ & \text{gdzie } f \left(n \right) = n^2 \left| \sin \left(n \right) \right|, \\ & 4f \left(n \right) = \Theta \left(\left(\lg \frac{3n}{2} \right)^2 \right), \ f \left(n \right) = O \left(\sqrt{n} \right), \ f \left(n \right) = \Omega \left(1 - n^{-1} \right), \\ & \text{gdzie } f \left(n \right) = \lg n \sqrt{n}. \end{aligned}$$

3. Zadanie

a.
$$\sum_{i=1}^{n} \log_2 i = \log_2 1 + \log_2 2 + \log_2 3 + \dots + \log_2 n = \log_2 (1 * 2 * 3 * \dots * n) = \log_2 n! = n * \log_2 n$$
 czyli $n * \log_2 n = \Omega(n)$ PRAWDA

b.
$$\log_2 \sum_{i=1}^n i = \log_2 (1+2+3+\cdots+n) = \log_2 \frac{n*(n+1)}{2} = \log_2 \left((1+n)*n\right) - \log_2 2 = \log_2 \left((1+n)*n\right) - 1$$
 czyli $\log_2 \left((1+n)*n\right) - 1 = \Omega \sqrt{n}$ FAŁUSZ

4. Zadanie

- a. $f_6, f_1, f_5, f_3, f_2, f_4$
- b. $f_6, f_5, f_2, f_4, f_1, f_3$
- c. $f_5, f_2, f_6, f_3, f_4, f_1$
- d. $f_4, f_5, f_3, f_2, f_6, f_1$