

Definition 0.0.4 (Reduction) The *reduction relation* \longrightarrow is the smallest contextual relation that satisfies the following rules:

$$\begin{array}{ll}
c!\langle \bar{V} \rangle \mid c?(\bar{X}).R & \longrightarrow R[\bar{V}/\bar{X}] & \text{(R-COMM)} \\
\text{rec } p.R & \longrightarrow R[\text{rec } p.R/p] & \text{(R-REP)} \\
\text{if } v = v \text{ then } P \text{ else } Q & \longrightarrow P & \text{(R-EQ)} \\
\text{if } v_1 = v_2 \text{ then } P \text{ else } Q & \longrightarrow Q \quad (\text{where } v_1 \neq v_2) & \text{(R-NEQ)} \\
\frac{P \equiv P', P \longrightarrow Q, Q \equiv Q'}{P' \longrightarrow Q'} & & \text{(R-STRUC)}
\end{array}$$

We use the notation $P \dots \longrightarrow Q$ when an arbitrary number of these rules have been applied in reducing P to Q .