

Semantyka i weryfikacja - praca domowa nr 2
Mateusz Bieganski mb385162

1 Expressions

1.1 e

$$\llbracket e \rrbracket_{\varrho_V, \varrho_P, s} = q \in \mathbb{Q}$$

1.2 x

$$\llbracket x \rrbracket_{\varrho_V, s} = s(\varrho_V x)$$

1.3 $e + e$

$$\llbracket e_1 + e_2 \rrbracket_{\varrho_V, s} = \llbracket e_1 \rrbracket_{\varrho_V, s} + \llbracket e_2 \rrbracket_{\varrho_V, s}$$

1.4 $e * e, e - e$ - analogicznie

2 Bool Expressions

2.1 $true$

$$\llbracket true \rrbracket_{\varrho_V, s} = tt$$

2.2 $false$

$$\llbracket false \rrbracket_{\varrho_V, s} = ff$$

2.3 $e < e$

$$\llbracket e_1 < e_2 \rrbracket \varrho_V, s = ifte(\llbracket e_1 \rrbracket \varrho_V, s < \llbracket e_2 \rrbracket \varrho_V, s, tt, ff)$$

2.4 $e = e, b \wedge b, \neg b$ - analogicznie

3 Declarations

3.1 $\text{var } x = e$

$$\begin{aligned} \llbracket \text{var } x = e \rrbracket \varrho_V, \varrho_P, s &= \varrho_V[x \mapsto l], \varrho_P, s[l \mapsto n] \\ \text{where } l &= \text{newloc}(s), n = \llbracket e \rrbracket \varrho_V, s \end{aligned}$$

3.2 ϵ

$$\llbracket \epsilon \rrbracket \varrho_V = id_P$$

3.3 $\text{proc } p(x) \text{ I}$

$$\begin{aligned} \llbracket \text{proc } p(x) \text{ I} \rrbracket \varrho_V \varrho_P &= \varrho_P[p \mapsto P] \\ \text{where } P &= \lambda.s : \text{State}. \llbracket I \rrbracket \varrho_V \varrho_P[p \mapsto P] s[l \mapsto \llbracket s(\varrho_V x) \rrbracket \varrho_V, s], \\ & l = \text{newloc}(s) \end{aligned}$$

3.4 $D_1; D_2$

$$\begin{aligned} \llbracket D_1; D_2 \rrbracket \varrho_V \varrho_P &= \llbracket D_2 \rrbracket \varrho'_P \varrho'_D \\ \text{where } \varrho'_P \varrho'_D &= \llbracket D_1 \rrbracket \varrho_V \varrho_P \end{aligned}$$