

Persamaan Parametrik

- Lingkaran $\rightarrow x = a \cos \theta$ & $y = a \sin \theta$; $0 \leq \theta \leq 2\pi$

Garis Singgung Scr. 1-Parametrik

$$\frac{dy}{dx} = \frac{dy}{dt} \frac{dt}{dx} = \frac{dy/dt}{dx/dt} = \frac{y'(t)}{x'(t)}$$

Panjang Busur Parametrik

$$S = \int_{t_1}^{t_2} \sqrt{\left(\frac{dx}{dt}\right)^2 + \left(\frac{dy}{dt}\right)^2} dt$$

Koordinat Kutub (r, θ) :

Hubungan koordinat kutub dengan siku " (kartesian)

$$x = r \cos \theta \quad y = r \sin \theta$$

$$r^2 = x^2 + y^2 \quad \tan \theta = \frac{y}{x}$$

Grafik Dalam Koordinat Kutub

$$r \cos \theta = a \quad r \sin \theta = b$$

*Lingkaran Dalam Koordinat Kutub

$$r = a \rightarrow P(a, \theta)$$

Jika Lingkaran berpusat sb-x

$$r = 2a \cos \theta \quad \text{atau} \quad r = -2a \cos \theta$$

Jika Lingkaran berpusat di sb-y

$$r = 2a \sin \theta \quad \text{atau} \quad r = -2a \sin \theta$$

* Kardioida & Limacon

$$r = a + b \cos \theta \quad \dots (1)$$

$$r = a - b \cos \theta \quad \dots (2)$$

$$r = a + b \sin \theta \quad \dots (3)$$

$$r = a - b \sin \theta \quad \dots (4)$$

Limacons



$$\frac{a}{b} < 1$$



$$\frac{a}{b} = 1$$



$$\frac{1 < a}{b < 2}$$



$$\frac{a}{b} \geq 2$$

(Kardioida) (limacon cekung) (limacon cembung)

* Lemniscate

$$r^2 = a^2 \cos 2\theta$$

$$r^2 = -a^2 \cos 2\theta$$

$$r^2 = a^2 \sin 2\theta$$

$$r^2 = -a^2 \sin 2\theta$$



* Spiral

$$r = a\theta \quad (\theta \geq 0)$$

$$r = -a\theta \quad (\theta \leq 0)$$

* Kurva Rose



$$r = a \sin n\theta$$

Jika n ganjil, maka daun = n

$$r = a \cos n\theta$$

Jika n genap, maka daun = $2n$

* Luas Dalam Koordinat Kutub

$$A = \int_{\theta_1}^{\theta_2} \frac{1}{2} r^2 d\theta$$

$$V = \int_{\theta_1}^{\theta_2} \frac{2}{3} \pi r^3 \sin \theta d\theta \quad (\text{diputar thdp sb-x})$$

$$V = \int_{\theta_1}^{\theta_2} \frac{2}{3} \pi r^3 \cos \theta d\theta \quad (\text{diputar thdp sb-y})$$

* Garis Singgung Koordinat Kutub

$$\frac{dy}{dx} = \frac{dy/d\theta}{dx/d\theta} = \frac{r \cos \theta + \sin \theta \frac{dr}{d\theta}}{-r \sin \theta + \cos \theta \frac{dr}{d\theta}}$$

* Panjang Busur Kurva Kutub

$$s = \int_{\theta_1}^{\theta_2} \sqrt{r^2 + \left(\frac{dr}{d\theta}\right)^2} d\theta$$