

## PANJANG BUSUR / KURVA

$$S = \int_{x_1}^{x_2} \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx \quad \text{atau} \quad S = \int_{y_1}^{y_2} \sqrt{1 + \left(\frac{dx}{dy}\right)^2} dy$$

## LUAS PERMUKAAN KULIT BENDA PUTAR

→ Diutar thdp sb.  $x$

$$K = 2\pi \int_{x_1}^{x_2} y \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx$$

→ Diutar thdp sb.  $y$

$$K = 2\pi \int_{y_1}^{y_2} x \sqrt{1 + \left(\frac{dx}{dy}\right)^2} dy$$

## VOLUME BENDA PUTAR

$$V = \int_{x_1}^{x_2} L(x) dx \quad \text{atau} \quad V = \int_{y_1}^{y_2} L(y) dy$$

\* Metode Cakram

$$V = \int_{x_1}^{x_2} \pi y^2 dx \quad \text{atau} \quad V = \int_{y_1}^{y_2} \pi x^2 dy$$

\* Metode Cincin Cakram

$$V = \int_{x_1}^{x_2} 2\pi x y(x) dx \quad \text{atau} \quad V = \int_{y_1}^{y_2} 2\pi y x(y) dy$$

## TB. Luas (Bidang Datar)

$$\bar{x} = \frac{\int_{x_1}^{x_2} x (y_1 - y_2) dx}{\int_{x_1}^{x_2} (y_1 - y_2) dx}$$

$$\bar{y} = \frac{1}{2} \frac{\int_{x_1}^{x_2} (y_1^2 - y_2^2) dx}{\int_{x_1}^{x_2} (y_1 - y_2) dx}$$

## TB. Volum Benda Putar

⇒ diputar thdp sb-x  $(\bar{x}, 0)$

$$\bar{x} = \frac{\int_{x_1}^{x_2} x y^2 dx}{\int_{x_1}^{x_2} y^2 dx}$$

⇒ diputar thdp sb-y  $(0, \bar{y})$

$$\bar{y} = \frac{\int_{y_1}^{y_2} y x^2 dy}{\int_{y_1}^{y_2} x^2 dy}$$

## TB. Kulit Benda Putar

$$\bar{x} = \frac{\int_{x_1}^{x_2} x y \sqrt{1 + f(x)^2} dx}{\int_{x_1}^{x_2} y \sqrt{1 + f(x)^2} dx}$$

TB. Busur

$$\bar{x} = \frac{\int_{x_1}^{x_2} x \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx}{\int_{x_1}^{x_2} \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx}$$

$$\bar{y} = \frac{\int_{x_1}^{x_2} y \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx}{\int_{x_1}^{x_2} \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx}$$