Doctrine and Covenants 88: 118

And as all have not faith, seek ye diligently and teach one another words of wisdom; yea, seek ye out of the best books words of wisdom; seek learning, even by study and also by faith.

#### Ether 12:26

27 And if men come unto me I will show unto them their weakness. I give unto men weakness that they may be humble; and my grace is sufficient for all men that humble themselves before me; for if they humble themselves before me, and have faith in me, then will I make weak things become strong unto them.

#### Some things

- Homework:
  - Due before class on the day indicated
  - Turn in pdf or jpeg make sure it is legible and easy to read
- Labs
  - Due at midnight
  - Turn in the .ipynb
- Look at a lab

#### **Doing Your Labs**

- Will use scikit-learn in individual labs
  - Whatever you want in group project
- Program in Python in Jupyter notebooks
  - NumPy library Great with arrays, etc.
- Recommended tools and libraries
  - Colab Google IDE for Python and Jupyter notebooks
  - Pandas Data Frames and tools are very convenient
  - MatplotLib
  - Scikit-Learn

#### scikit-learn

- One of the most used and powerful machine learning toolkits out there
- Lots of implemented models and tools to use for machine learning applications
  - Sometimes missing some things we would like, but it is continually evolving
  - Source is available, and you can always override methods with your own, etc.
- Basically a Python Library to call from your Python code
- Familiarize yourself with the scikit-learn website as you will be using it for all labs

#### Machine Learning Tools

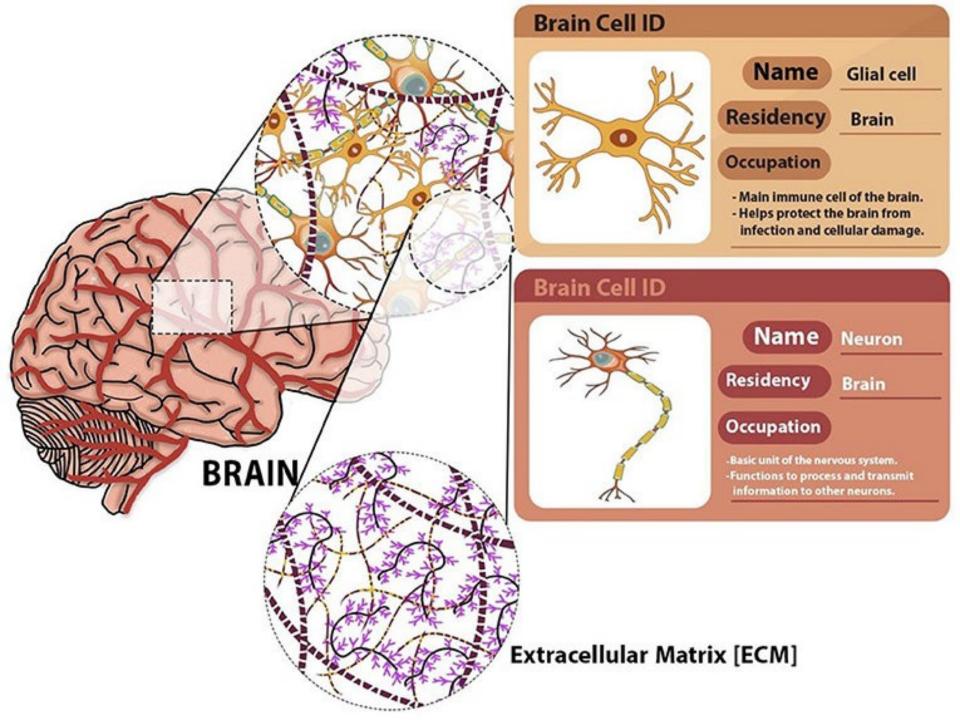
- Lots of new Machine Learning Tools
  - Weka was the first main site with lots of ready to run models
  - Scikit-learn now very popular
  - Languages:
    - Python with NumPy, matplotlib, pandas, other libraries
    - R (good statistical packages), but with growing Python libraries...
  - Deep Learning Neural Network frameworks GPU capabilities
    - Tensorflow Google
    - PyTorch Multiple developers (Facebook, twitter, Nvidia...) Python
    - Others: Caffe2 (Facebook), Keras, Theano, CNTK (Microsoft)
  - Data Mining Business packages Visualization, Expensive
- Great for experimenting and applying to real problems
- But important to "get under the hood" and not just be black box ML users

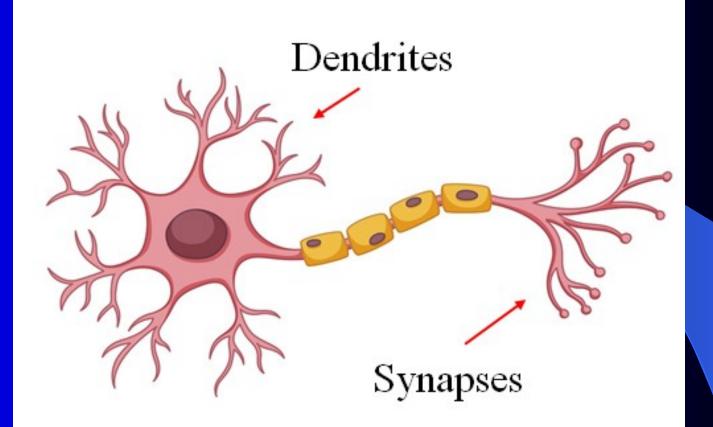
#### Perceptron Project

- Content Section of LS (Learning Suite) for project specifications
  - Review carefully the introductory part regarding all projects
- For each project carefully read the specifications for the lab in the Jupyter notebook on GitHub
- You can just copy the Perceptron notebook from the GitHub site to your computer and then add your work in the code and text boxes

#### Perceptron Learning Algorithm

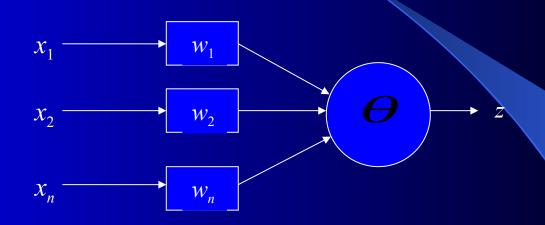
- First neural network learning model in the 1960's
  - Frank Rosenblatt
- Simple and limited (single layer model)
- Basic concepts are similar for multi-layer models so this is a good learning tool
- Still used in some current applications (large business problems, where intelligibility is needed, etc.)





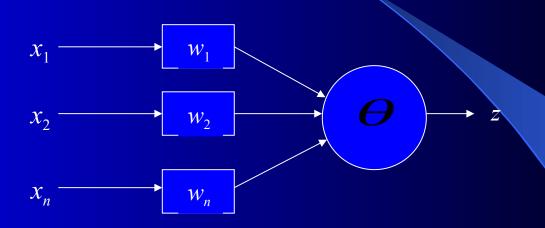
#### **NEURON**

#### Perceptron Node – Threshold Logic Unit



$$z = \begin{cases} 1 & \text{if } \sum_{i=1}^{n} x_i w_i \ge \theta \\ 0 & \text{if } \sum_{i=1}^{n} x_i w_i < \theta \end{cases}$$

#### Perceptron Node – Threshold Logic Unit

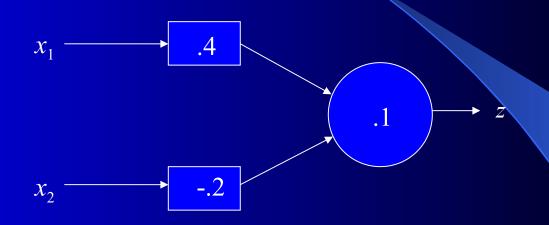


- Learn weights such that an objective function is maximized.
- What objective function should we use?
- What learning algorithm should we use?

$$z = \begin{cases} 1 & \text{if } \sum_{i=1}^{n} x_i w_i \ge \theta \\ 0 & \text{if } \sum_{i=1}^{n} x_i w_i < \theta \end{cases}$$

12

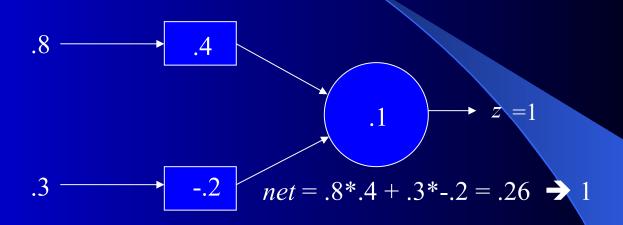
# Perceptron Learning Algorithm



$$\begin{array}{c|cccc} x_1 & x_2 & target \\ \hline .8 & .3 & 1 \\ .4 & .1 & 0 \\ \end{array}$$

$$z = \begin{cases} 1 & \text{if } \sum_{i=1}^{n} x_i w_i \ge \theta \\ 0 & \text{if } \sum_{i=1}^{n} x_i w_i < \theta \end{cases}$$

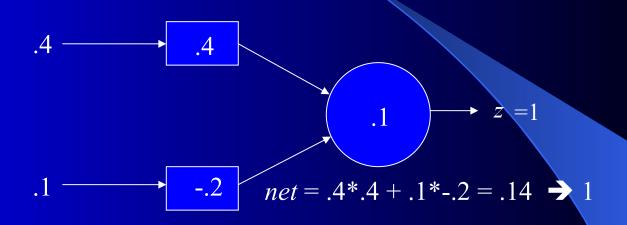
### First Training Instance



$$\begin{array}{c|cccc} x_1 & x_2 & target \\ \hline .8 & .3 & 1 \\ .4 & .1 & 0 \\ \end{array}$$

$$z = \begin{cases} 1 & \text{if } \sum_{i=1}^{n} x_i w_i \ge \theta \\ 0 & \text{if } \sum_{i=1}^{n} x_i w_i < \theta \end{cases}$$

#### Second Training Instance



$$\begin{array}{c|cccc} x_1 & x_2 & target \\ \hline .8 & .3 & 1 \\ .4 & .1 & 0 \\ \end{array}$$

$$z = \begin{cases} 1 & \text{if } \sum_{i=1}^{n} x_i w_i \ge \theta \\ 0 & \text{if } \sum_{i=1}^{n} x_i w_i < \theta \end{cases}$$

Need to make a correction

## Perceptron Rule Learning

$$\Delta w_i = c(t-z) \, x_i$$

- Where  $w_i$  is the weight from input i to the perceptron node,
  - c is the learning rate,
  - t is the target for the current instance,
  - z is the current output, and
  - $-x_i$  is  $i^{th}$  input
- Least perturbation principle
  - Only change weights if there is an error
  - small c rather than changing weights sufficient to make current pattern correct
  - Scale by input value  $x_i$

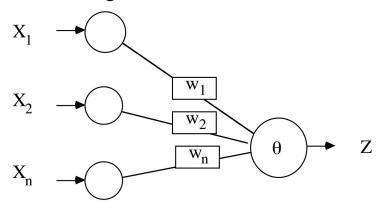
$$w_{ij} \leftarrow w_{ij} - \eta(y_j - t_j) \cdot x_i$$

## Perceptron Rule Learning

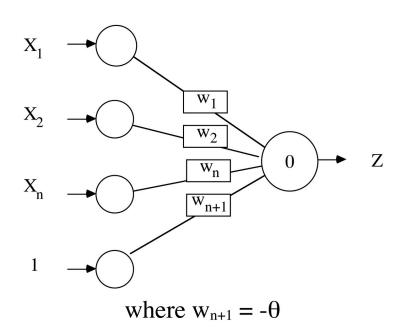
- Create a perceptron node with n inputs
- Iteratively select a pattern from the training set
- Calculate the output value z
- Apply the perceptron rule to adjust weights

- Each iteration through the training set is an epoch
- Continue training until total training set error ceases to improve
- Perceptron Convergence Theorem: Guaranteed to find a solution in finite time if a solution exists

#### Weight Versus Threshold

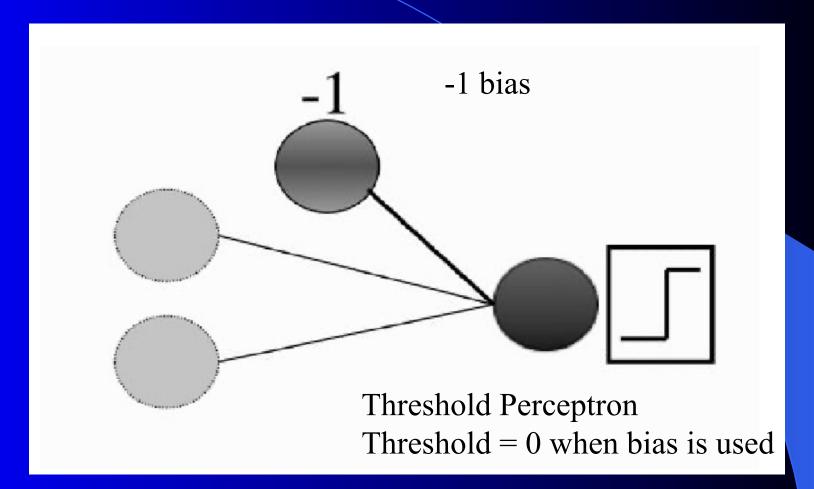


Do you need to adjust Theta? Yes, in most cases



We can learn the threshold by adding another node with an input of 1 (bias)

#### From the textbook



#### Augmented Pattern Vectors

```
1 0 1 -> 0
1 0 0 -> 1
Augmented Version
1 0 1 1 -> 0
1 0 0 1 -> 1
```

- Treat threshold like any other weight. No special case. Call it a *bias* since it biases the output up or down.
- Since we start with random weights anyways, can ignore the  $-\theta$  notion, and just think of the bias as an extra available weight. (note the author uses a -1 input)
- Always use a bias weight

## Perceptron Rule Example

- Assume a 3 input perceptron plus bias (it outputs 1 if net > 0, else 0)
- Assume a learning rate c of 1 and initial weights all 0:  $\Delta w_i = c(t-z) x_i$

```
Training set 0 0 1 -> 0
1 1 1 -> 1
1 0 1 -> 1
0 1 1 -> 0
```

<u>Pattern</u>	<u>Target</u>	(t) Weight Vector $(w_i)$ Net	Output (z)	$\Delta W$
0011	0	0 0 0 0		

- Assume a 3 input perceptron plus bias (it outputs 1 if net > 0, else 0)
- Assume a learning rate *c* of 1 and initial weights all 0:  $\Delta w_i = c(t-z) x_i$

<u>Pattern</u>	<u>Target</u>	(t) Weight Vector	$(w_i)$ Net	<u>Outpı</u>	$\Delta W$
0 0 1 1	0	0000	0	0	0 0 0 0
1111	1	0000			

- Assume a 3 input perceptron plus bias (it outputs 1 if net > 0, else 0)
- Assume a learning rate *c* of 1 and initial weights all 0:  $\Delta w_i = c(t-z) x_i$

<u>Pattern</u>	<u>Targe</u>	et (t) Weight Vector	$r(w_i)$ Net	<u>Outp</u> ı	$\underline{\Delta W}$
0011	0	0 0 0 0	0	0	0 0 0 0
1111	1	0 0 0 0	0	0	1 1 1 1
1011	1	1111			

#### \*\*Challenge Question\*\* - Perceptron

- Assume a 3 input perceptron plus bias (it outputs 1 if net > 0, else 0)
- Assume a learning rate c of 1 and initial weights all 0:  $\Delta w_i = c(t-z) x_i$

```
Training set 0 0 1 -> 0
1 1 1 -> 1
1 0 1 -> 1
0 1 1 -> 0
```

<u>Pattern</u>	Target (t)	Weight Vector $(w_i)$	<u>Net</u>	Output (2	$\Delta W$
0 0 1 1	0	0 0 0 0	0	0	0 0 0 0
1111	1	0 0 0 0	0	0	1 1 1 1
1011	1	1111			

- Once it converges the final weight vector will be
  - A. 1111
  - B. -1010
  - C. 0000
  - D. 1000
  - E. None of the above

slido



# Once it converges, the final weight vector will be

(i) Start presenting to display the poll results on this slide.

- Assume a 3 input perceptron plus bias (it outputs 1 if net > 0, else 0)
- Assume a learning rate *c* of 1 and initial weights all 0:  $\Delta w_i = c(t-z) x_i$

<u>Pattern</u>	<u>Targe</u>	et (t) Weight Vector	$r(w_i)$ Net	<u>Outp</u> ı	$\Delta W$
0011	0	0 0 0 0	0	0	0 0 0 0
1111	1	0 0 0 0	0	0	1 1 1 1
1011	1	1111	3	1	0 0 0 0
0111	0	1111			

- Assume a 3 input perceptron plus bias (it outputs 1 if net > 0, else 0)
- Assume a learning rate c of 1 and initial weights all 0:  $\Delta w_i = c(t-z) x_i$

<u>Pattern</u>	Target (t)	Weight Vector (w <sub>i</sub> )	<u>Net</u>	Output (2	<u>z)</u>	$\Delta W$
0 0 1 1	0	0 0 0 0	0	0	0 0 0 0	
1111	1	0 0 0 0	0	0	1 1 1 1	
1011	1	1111	3	1	0 0 0 0	
<u>0 1 1 1</u>	0	1111	<u>3</u>	1	<u>0 -1 -1 -1</u>	
0.0.1.1	0	1 0 0 0				

- Assume a 3 input perceptron plus bias (it outputs 1 if net > 0, else 0)
- Assume a learning rate c of 1 and initial weights all 0:  $\Delta w_i = c(t-z) x_i$

```
Training set 0 0 1 -> 0
1 1 1 -> 1
1 0 1 -> 1
0 1 1 -> 0
```

<u>Pattern</u>	Target (t	) Weight Ve	ector (w <sub>i</sub> )	<u>Net</u>	<u>Outpu</u>	$\Delta W$	
0 0 1 1	0	0000		0	0	0 0 0 0	
1111	1	0000		0	0	1 1 1 1	
1011	1	1111		3	1	0 0 0 0	
<u>0 1 1 1</u>	0	<u>1111</u>		<u>3</u>	1	<u>0 -1 -1 -1</u>	
0 0 1 1	0	1000		0	0	0 0 0 0	
1111	1	1000		1	1	0 0 0 0	
1011	1	1000		1	1	0 0 0 0	
0 1 1 1	0	1000	CS 270 D	0	0	0 0 0 0	

28

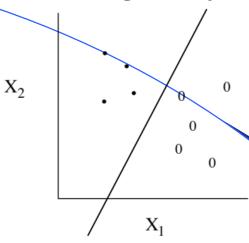
#### Perceptron Homework

- Assume a 3 input perceptron plus bias (it outputs 1 if net > 0, else 0)
- Assume a learning rate c of 1 and initial weights all 1:  $\Delta w_i = c(t-z) x_i$
- Show weights after each pattern for just one epoch
- Training set 1 0 1 -> 0
  1 .5 0 -> 0
  1 -.4 1 -> 1
  0 1 .5 -> 1

Pattern Target (t) Weight Vector 
$$(w_i)$$
 Net Output  $(z)$   $\Delta W$ 

# Code

#### Linear Separability



2-d case (two inputs)

$$W_1X_1 + W_2X_2 > \theta \ (Z=1)$$

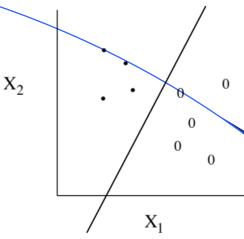
$$W_1X_1 + W_2X_2 < \theta \ (Z=0)$$

So, what is decision boundary?

$$W_1X_1 + W_2X_2 = \theta$$
  
 $X_2 + W_1X_1/W_2 = \theta/W_2$   
 $X_2 = (-W_1/W_2)X_1 + \theta/W_2$ 

$$Y = MX + B$$





2-d case (two inputs)

If no bias weight, the hyperplane must go through the origin.

Note that since 
$$\Theta$$
 = bi

Note that since  $\Theta =$  -bias, the equation with bias is:

$$X_2 = (-W_1/W_2)X_1 - bias/W_2$$

$$\mathbf{M} = -\mathbf{W}_1/\mathbf{W}_2$$

$$B = -bias/W_2$$

$$W_1X_1 + W_2X_2 > \theta \ (Z=1)$$

$$W_1X_1 + W_2X_2 < \theta \ (Z=0)$$

So, what is decision boundary?

$$W_1X_1 + W_2X_2 = \theta$$

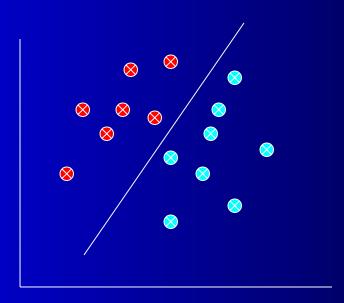
$$X_2 + W_1 X_1 / W_2 = \theta / W_2$$

$$X_2 = (-W_1/W_2)X_1 + \theta/W_2$$

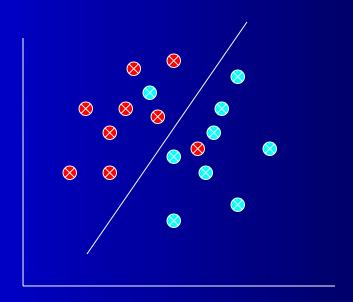
$$Y = MX + B$$

Note: bias is the weight for bias input

# Linear Separability

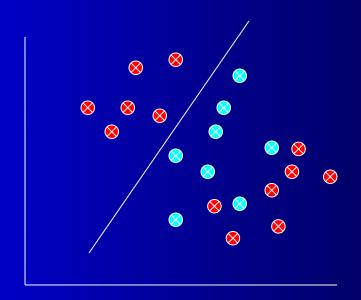


# Linear Separability and Generalization

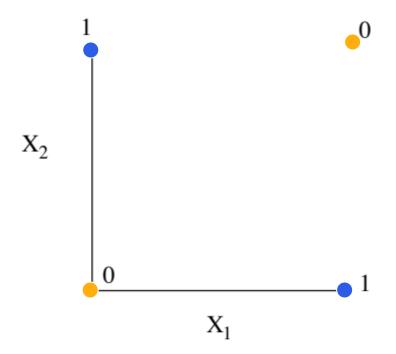


When is data noise vs. a legitimate exception

# Limited Functionality of Hyperplane



#### Exclusive Or



Is there a dividing hyperplane?

### Linear Models which are Non-Linear in the Input Space

So far we have used

$$f(\mathbf{x}, \mathbf{w}) = sign(\sum_{i=1}^{n} w_i x_i)$$

• We could preprocess the inputs in a non-linear way and do

$$f(\mathbf{x}, \mathbf{w}) = sign(\sum_{i=1}^{m} w_i \phi_i(\mathbf{x}))$$

- To the perceptron algorithm it is the same but with more/different inputs. It still uses the same learning algorithm.
- For example, for a problem with two inputs x and y (plus the bias), we could also add the inputs  $x^2$ ,  $y^2$ , and  $x \cdot y$
- The perceptron would just think it is a 5-dimensional task, and it is linear (5-d hyperplane) in those 5 dimensions
  - But what kind of decision surfaces would it allow for the original 2-d input space?

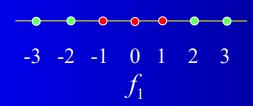
### Quadric Machine

- All quadratic surfaces (2<sup>nd</sup> order)
  - ellipsoid
  - parabola
  - etc.
- That significantly increases the number of problems that can be solved
- Can we solve XOR with this setup?

### Quadric Machine

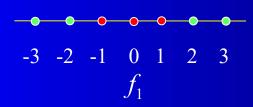
- All quadratic surfaces (2<sup>nd</sup> order)
  - ellipsoid
  - parabola
  - etc.
- That significantly increases the number of problems that can be solved
- But still many problems which are not quadrically separable
- Could go to 3<sup>rd</sup> and higher order features, but number of possible features grows exponentially
- Multi-layer neural networks will allow us to discover highorder features automatically from the input space

### Simple Quadric Example



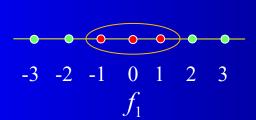
- What is the decision surface for a 1-d (1 input) problem?
- Perceptron with just feature  $f_1$  cannot separate the data
- Could we add a transformed feature to our perceptron?

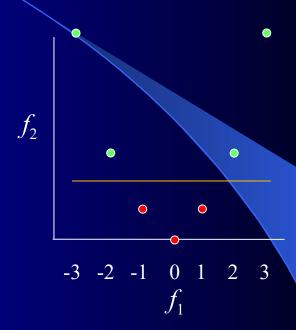
### Simple Quadric Example



- Perceptron with just feature  $f_1$  cannot separate the data
- Could we add a transformed feature to our perceptron?
- $f_2 = f_1^2$

### Simple Quadric Example





- Perceptron with just feature  $f_1$  cannot separate the data
- Could we add another feature to our perceptron  $f_2 = f_1^2$
- Note could also think of this as just using feature  $f_1$  but now allowing a quadric surface to divide the data
  - Note that  $f_1$  not actually needed in this case

### Quadric Machine Homework

- Assume a 2-input perceptron expanded to be a quadric (2<sup>nd</sup> order) perceptron, with 5 input weights  $(x, y, x \cdot y, x^2, y^2)$  and the bias weight
  - Assume it outputs 1 if net > 0, else 0
- Assume a learning rate c of .5 and initial weights all 0
  - $\Delta w_i = c(t-z) x_i$
- Show all weights after each pattern for one epoch with the following training set

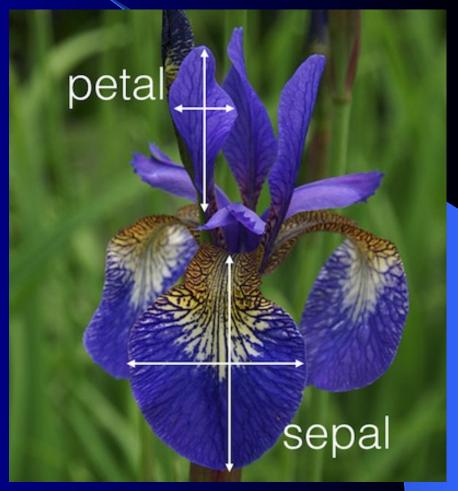
X	у	Target
0	.4	0
1	1.2	1
.5	.8	0

### How to Handle Multi-Class Output

- This is an issue with learning models which only support binary classification (perceptron, SVM, etc.)
- Create 1 perceptron for each output class, where the training set considers all other classes to be negative examples (one vs the rest)
  - Run all perceptrons on novel data and set the output to the class of the perceptron which outputs high
  - If there is a tie, choose the perceptron with the highest net value
- Another approach: Create 1 perceptron for each pair of output classes, where the training set only contains examples from the 2 classes (one vs one)
  - Run all perceptrons on novel data and set the output to be the class with the most wins (votes) from the perceptrons
  - In case of a tie, use the net values to decide
  - Number of models grows by the square of the output classes

# UC Irvine Machine Learning Data Base Iris Data Set

4.8,3.0,1.4,0.3,	Iris-setosa
5.1,3.8,1.6,0.2,	Iris-setosa
4.6,3.2,1.4,0.2,	Iris-setosa
5.3,3.7,1.5,0.2,	Iris-setosa
5.0,3.3,1.4,0.2,	Iris-setosa
7.0,3.2,4.7,1.4,	Iris-versicolor
6.4,3.2,4.5,1.5,	Iris-versicolor
6.9,3.1,4.9,1.5,	Iris-versicolor
5.5,2.3,4.0,1.3,	Iris-versicolor
6.5,2.8,4.6,1.5,	Iris-versicolor
6.0,2.2,5.0,1.5,	Iris-viginica
6.9,3.2,5.7,2.3,	Iris-viginica
5.6,2.8,4.9,2.0,	Iris-viginica
7.7,2.8,6.7,2.0,	Iris-viginica
6.3,2.7,4.9,1.8,	Iris-viginica



## Quiz

Password is - perceptron

### **Determining Model Performance**

### Objective Functions: Accuracy

- How do we judge the quality of a particular model (e.g. Perceptron with a particular setting of weights)
- Consider how accurate the model is on the data set
  - Classification accuracy = # Correct/Total instances
  - Classification error = # Misclassified/Total instances (= 1 acc)

### Objective Functions: Error

- Usually minimize a Loss function (aka cost, error)
- For real valued outputs and/or targets
  - Pattern error = Target output: Errors could cancel each other
    - $\Sigma |t_j z_j|$  (L1 loss), where j indexes all outputs in the pattern
    - $\sum (t_i z_i)^2$  (L2 loss), sum squared error (SSE)
  - L2 loss is generally preferred except in cases of large outliers
- For nominal data, pattern error is typically 1 for a mismatch and 0 for a match
  - For nominal (including binary) output and targets, L1, L2, and classification error are equivalent

### Mean Squared Error

- Mean Squared Error (MSE) = SSE/n where n is the number of instances in the data set
  - This can be nice because it normalizes the error for data sets of different sizes
  - MSE is the average squared error per pattern
- Root Mean Squared Error (RMSE) is the square root of the MSE
  - This puts the error value back into the same units as the features and can thus be more intuitive
    - Since we squared the error on the SSE
  - RMSE is the average distance (error) of targets from the outputs in the same scale as the features
  - Note RMSE is the root of the total data set MSE, and NOT the sum of the root of each individual pattern MSE

### \*\*Challenge Question\*\* - Error

Given the following data set, what is the L1  $(\Sigma | t_i - z_i|)$ , SSE  $(L2) (\Sigma (t_i - z_i)^2)$ , MSE, and RMSE error for the entire data set?

X	У	Output	Target	Data Set
2	-3	1	1	
0	1	0	1	
.5	.6	.8	.2	
L1				?
SSE				?
MSE				?
RMSE				?

- A. .4 1 1 1
- B. 1.6 2.36 1 1
- C. .4 .64 .21 0.453
- D. 1.6 1.36 .67 .82
- E. None of the above

slido



### What are the errors for the data?

① Start presenting to display the poll results on this slide.

### \*\*Challenge Question\*\* - Error

Given the following data set, what is the L1  $(\Sigma | t_i - z_i|)$ , SSE  $(L2) (\Sigma (t_i - z_i)^2)$ , MSE, and RMSE error for the entire data set?

X	У	Output	Target	Data Set
2	-3	1	1	
0	1	0	1	
.5	.6	.8	.2	
L1				1.6
SSE				1.36
MSE				1.36/3 = .453
RMSE				.45^.5 = .67

- A. .4 1 1 1
- B. 1.6 2.36 1 1
- C. .4 .64 .21 0.453
- D. 1.6 1.36 .67 .82
- E. None of the above

### Error Values Homework

- Given the following data set, what is the L1, SSE (L2), MSE, and RMSE error of Output1, Output2, and the entire data set? Fill in cells that have a ?.
  - Notes: For instance 1 the L1 pattern error is 1 + .4 = 1.4 and the SSE pattern error is 1 + .16 = 1.16. The Data Set L1 and SSE errors will just be the sum of each of the pattern errors.

Instance	X	У	Output1	Target1	Output2	Target 2	Data Set
1	-1	-1	0	1	.6	1.0	
2	-1	1	1	1	3	0	
3	1	-1	1	0	1.2	.5	
4	1	1	0	0	0	2	
L1			?		?		?
SSE			?		?		?
MSE			?		?		?
RMSE			?		?		?

### **Error Surface**

Error is a function of the weights

$$- E = \sum (t_i - z_i)^2 = \sum (t_i - \sum x_j w_{ij})^2$$

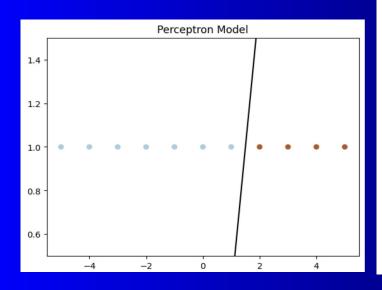
• If we could search this space, we could find the minimum

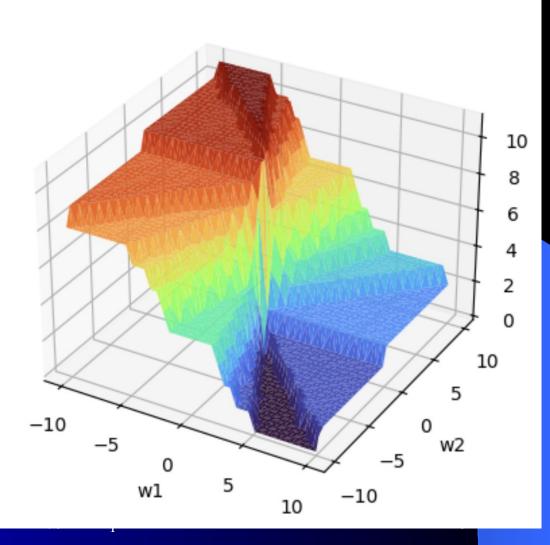
Total SSE: Sum Squared Error  $\sum (t-z)^2$ 



### Error Surface

Single perceptron –1d input with bias





# Gradient Descent Learning: Minimize (Maximize) the Objective Function

- Gradient descent algorithm
  - Find a starting location set of weights
  - Loop
    - Calculate output values
    - Use the gradient to adjust your weight values
- Adjusting the weights
  - Derivative of the error function w.r.t the weights slope or gradient

$$w_i\!\leftarrow\!w_i\!+\!\Delta w_i \ \Delta w_i\!=\!-\eta rac{\partial E}{\partial w_i}$$

# GRADIENT DESCENT VISUALIZATION

# Deriving a Gradient Descent Learning Algorithm

- Goal is to decrease overall error (or other loss function) each time a weight is changed
- Sum Squared error one possible loss function  $E = \sum (t-z)^2$ 
  - Actually use  $E = \sum (t z)^2$
- Other reasons to use SSE
  - All errors are positive
  - Amplifies the effect of larger errors
  - Transforms the error surface smooth and differentiable
- Partial derivative of the error function w.r.t the weights gives us a weight update function

$$\begin{split} \frac{\partial E}{\partial w_i} &= \frac{\partial}{\partial w_i} \frac{1}{2} \sum_{d \in D} (t_d - o_d)^2 \\ &= \frac{1}{2} \sum_{d \in D} \frac{\partial}{\partial w_i} (t_d - o_d)^2 \\ &= \frac{1}{2} \sum_{d \in D} 2(t_d - o_d) \frac{\partial}{\partial w_i} (t_d - o_d) \\ &= \frac{1}{2} \sum_{d \in D} 2(t_d - o_d) \frac{\partial}{\partial w_i} (t_d - \vec{w}.\vec{x}) \end{split}$$
 Chain rule

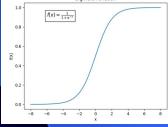
$$\Delta w_i = \eta \sum\nolimits_{d \in D} (t_d - o_d) x_{id}$$

### Delta rule algorithm

- Simple perceptron rule has a problem for gradient descent
  - Threshold output makes the error function non-differentiable
- Delta rule uses (target net) before the net value goes through the threshold in the learning rule to decide weight update

$$\Delta w_i = c(t - net)x_i$$

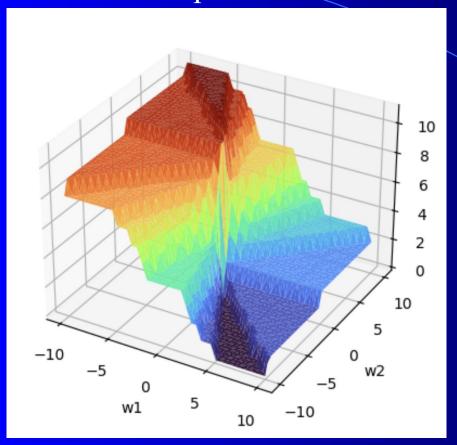
Use sigmoid(net) if you want 0/1 output

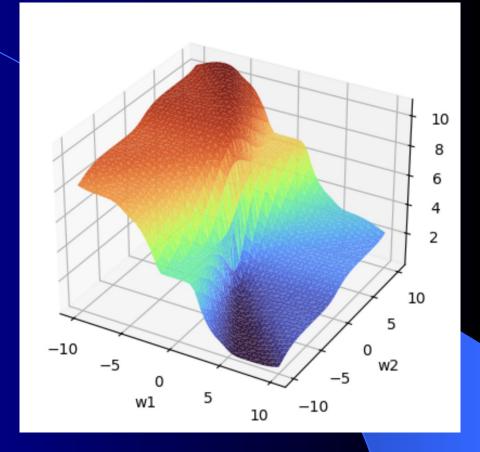


- Weights are updated even when the output would be correct
- Because this model is single layer and because of the SSE objective function, the error surface is guaranteed to be parabolic with only one minima
- Learning rate
  - If learning rate is too large can jump around global minimum
  - If too small, will get to minimum, but will take a longer time
  - Can decrease learning rate over time to give higher speed and still attain the global minimum (although exact minimum is still just for training set and thus...)

#### Perceptron Rule

#### Delta Rule + Sigmoid(net)





Changing to the Delta Rule and using Sigmoid(net) for output changes the decision surface to smooth and differentiable

67

### Batch vs Stochastic Update

- To get the true gradient, we need to sum errors over the entire training set and only update weights at the end of each epoch
- Batch (gradient) vs stochastic (on-line, incremental)
  - SGD (Stochastic Gradient Descent)
  - With the stochastic gradient descent algorithm, you update after every pattern, just like with the perceptron algorithm (even though that means each change may not be along the true gradient)
  - Stochastic is more efficient and best to use in almost all cases, though not all have figured it out yet
  - We'll talk about this in more detail when we get to Backpropagation

### Perceptron rule vs Delta rule

- Perceptron rule (target thresholded output) guaranteed to converge to a separating hyperplane if the problem is linearly separable. Otherwise may not converge could get in a cycle
- Single layer Delta rule guaranteed to have only one global minimum. Thus, it will converge to the best SSE solution whether the problem is linearly separable or not.
  - Could have a higher misclassification rate than with the perceptron rule and a less intuitive decision surface – we will discuss this later with regression where Delta rules is more appropriate
- Stopping Criteria For these models we stop when no longer making progress
  - When you have gone a few epochs with no significant improvement/change between epochs (including oscillations)

# Training/Testing

### Training/Testing

- Gradient descent algorithm gives a training algorithm
  - Doesn't define testing
- How do we know how good it is?
  - Are we in a local minima?
- Four methods that we commonly use:
  - Training set method
  - Static split test set
  - Random split test set CV
  - N-fold cross-validation
  - The last two are the more accurate approaches

### Training Set Method

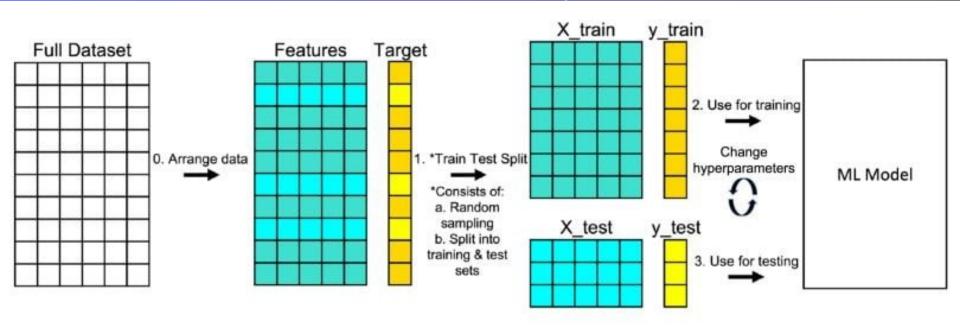
- Procedure
  - Build model from the training set
  - Compute accuracy on the same training set
- Simple but least reliable estimate of future performance on unseen data (a rote learner could score 100%!)
- Not used as a performance metric but it is often important information in understanding how a machine learning model learns
- This is information which you will often report in your labs and then compare it with how the learner does on a better method

### Static Training/Test Set

- Static Split Approach
  - The data owner makes available to the machine learner two distinct datasets:
    - One is used for learning/training (i.e., inducing a model), and
    - One is used exclusively for testing
- Note that this gives you a way to do repeatable tests
- Can be used for challenges (e.g. to see how everyone does on one particular unseen set, method we use for helping grade your labs.)
- Be careful not to overfit the Test Set ("Gold Standard")

### Random Training/Test Set Approach

- Random Split CV Approach (aka holdout method)
  - The data owner makes available to the machine learner a single dataset
  - The machine learner splits the dataset into a training and a test set, such that:
    - Instances are randomly assigned to either set
    - The distribution of instances (with respect to the target class) is hopefully similar in both sets due to randomizing the data before the split
      - Stratification is an option to ensure proper distribution
    - Typically 60% to 90% of instances is used for training and the remainder for testing the more data there is the more that can be used for training and still get statistically significant test predictions
  - Useful quick estimate for computationally intensive learners
  - Not statistically optimal (high variance, <u>unless</u> lots of data)
    - Could get a lucky or unlucky test set
  - Best to do multiple training runs with different random splits. Train and test m different splits and then average the accuracy over the m runs to get a more statistically accurate prediction of generalization accuracy.



```
In [3]:
            url = 'https://raw.githubusercontent.com/mGalarnyk/Tutorial_Data/master/King_County/kingCountyHouseData.csv'
            df = pd.read csv(url)
            # Selecting columns I am interested in
            columns = ['bedrooms','bathrooms','sqft_living','sqft_lot','floors','price']
            df = df.loc[:, columns]
            df.head(10)
Out[3]:
              bedrooms bathrooms sqft_living sqft_lot floors
                                                                               price
           0
                        3
                                   1.00
                                                1180
                                                          5650
                                                                     1.0
                                                                           221900.0
           1
                        3
                                   2.25
                                                2570
                                                          7242
                                                                     2.0
                                                                          538000.0
           2
                        2
                                   1.00
                                                 770
                                                         10000
                                                                           180000.0
                                                                     1.0
           3
                                   3.00
                                                1960
                                                          5000
                                                                     1.0
                                                                          604000.0
                        3
           4
                                                1680
                                                          8080
                                   2.00
                                                                     1.0
                                                                           510000.0
                                                5420
                                                        101930
                                                                     1.0 1225000.0
           5
                                   4.50
           6
                        3
                                   2.25
                                                1715
                                                          6819
                                                                     2.0 257500.0
In [4]:
           features = ['bedrooms','bathrooms','sqft living','sqft lot','floors']
           X = df.loc[:, features]
           y = df.loc[:, ['price']]
              bedrooms bathrooms sqft_living sqft_lot
                                                   floors
                                                                 price
                                                                                          bedrooms bathrooms sqft_living
                                                                                                                     sqft_lot
                                                                                                                               floors
            0
                        1.000000
                                     1180
                                            5650
                                                 1.000000
                                                          221900.000000
                                                                                                                             1.000000
                                                                                                                                               221900.000000
                                                                                                     1.000000
                                                                                                                 1180
                                                                                                                        5650
                         2.250000
                                     2570
                                            7242
                                                 2.000000
                                                          538000.000000
                                                                                                                                               538000.000000
                                                                                                 3
                                                                                                     2.250000
                                                                                                                 2570
                                                                                                                       7242
                                                                                                                             2.000000
                        1.000000
                                     770
                                           10000
                                                 1.000000
                                                          180000.000000
                                                                                                2
                                                                                                     1.000000
                                                                                                                       10000
                                                                                                                             1.000000
                                                                                                                                               180000.000000
                                                                                                                 770
                                                                       X = df.loc[:, features]] 3
                        3.000000
                                            5000
                                                 1.000000
                                                          604000.000000
                                                                                                                                               604000.000000
                                     1960
                                                                                                 4
                                                                                                    3.000000
                                                                                                                 1960
                                                                                                                        5000
                                                                                                                             1.000000
                                                                         y = df.loc[:, 'price']
                                                 1.000000
                                                          510000.000000
                                                                                                                                               510000.000000
                         2.000000
                                     1680
                                                                                                3
                                                                                                    2.000000
                                                                                                                 1680
                                                                                                                             1.000000
                                                                                                                                              1225000.000000
                         4.500000
                                     5420
                                          101930
                                                 1.000000
                                                         1225000.000000
                                                                                                     4.500000
                                                                                                                 5420
                                                                                                                      101930
                                                                                                                             1.000000
                     3
                        2.250000
                                     1715
                                            6819
                                                 2.000000
                                                          257500.000000
                                                                                                3
                                                                                                                                               257500.000000
                                                                                                    2.250000
                                                                                                                 1715
                                                                                                                        6819
                                                                                                                             2.000000
                         1.500000
                                     1060
                                            9711
                                                 1.000000
                                                          291850.000000
                                                                                                3
                                                                                                     1.500000
                                                                                                                 1060
                                                                                                                       9711
                                                                                                                             1.000000
                                                                                                                                               291850.000000
```

1.000000 1780 7470 1.000000 229500.000000 2.500000 6560 2.000000 323000.000000 1890

3 1.000000 1780 1.000000 7470 2.500000 2.000000 1890 6560

229500.000000 323000.000000

df

X

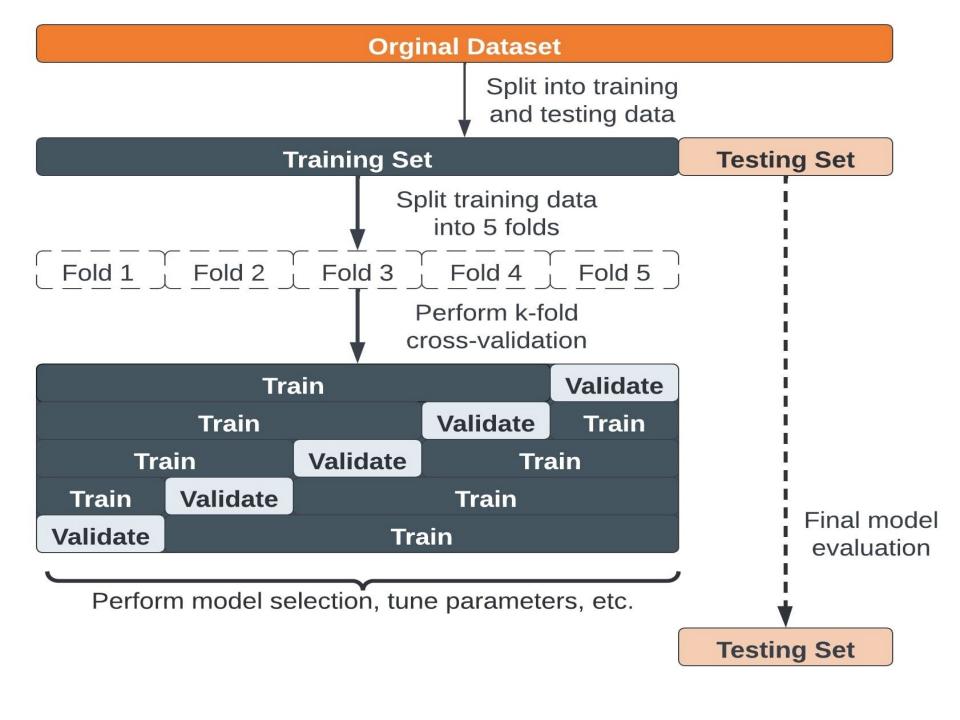
### Cross-Validation (CV)

- Cross-Validation (CV) Cross-validation is a resampling method that uses different portions of the data to test and train a model on different iterations
- We then average the results of these iterations
- With CV we avoid having data just used for either training or test, and give all data a chance to be part of each, thus getting more accurate results

Mainly used for comparing different learning models

#### N-fold Cross-validation

- Use all the data for both training and testing
  - Statistically more reliable
  - All data can be used which is good, especially for small data sets
- Procedure
  - Partition the randomized dataset (call it D) into N equally-sized subsets  $S_1, ..., S_N$
  - For k = 1 to N
    - Let  $M_k$  be the model induced from D  $S_k$
    - Let  $a_k$  be the accuracy of  $M_k$  on the instances of the test fold  $S_k$
  - Return  $(a_1 + a_2 + ... + a_N)/N$



### N-fold Cross-validation (cont.)

- The larger N is, the smaller the variance in the final result
- The limit case where N = |D| is known as *leave-one-out CV* and provides the most reliable estimate. However, it is typically only practical for small instance sets
- Commonly, a value of N=10 is considered a reasonable compromise between time complexity and reliability
- Still must chose an actual model to use during execution how?

### N-fold Cross-validation (cont.)

- The larger N is, the smaller the variance in the final result
- The limit case where N = |D| is known as *leave-one-out CV* and provides the most reliable estimate. However, it is typically only practical for small instance sets
- Commonly, a value of N=10 is considered a reasonable compromise between time complexity and reliability
- Still must chose an actual model to use during execution how?
  - Could select the one model that was best on its fold?
  - All data! With any of the approaches
- Note that N-fold CV is just a better way to estimate how well we will do on novel data, rather than a way to do *model selection*

# Quiz

- Password is:
  - gradient