maximize:f(A)

subject to:

$$f(A) = \min_{A_{i1,j1} = A_{i2,j2}} \{ \sqrt{(i2 - i1)^2 + (j2 - j1)^2} \},$$

 $A \in \mathbb{R}^{m \times n} , A_{i,j} \in \{0, 1, 2, 3...47\}$

$$f(A) = \begin{cases} +\infty, & S(A) = \emptyset \\ \min_{(P_1, P_2) \in S(A)} D(P_1, P_2), & S(A) \neq \emptyset \end{cases}$$

$$S(A) = \{(P_1, P_2) \mid M(P_1) = M(P_2), P_1 \in A, P_2 \in A\}$$

$$f(A) = \begin{cases} +\infty, & S(A) = \emptyset \\ \min_{(P_1, P_2) \in S(A)} D(P_1, P_2), & S(A) \neq \emptyset \end{cases}$$

$$S(A) = \{(P_1, P_2) \mid A(P_1) = A(P_2) \neq -1\}$$