

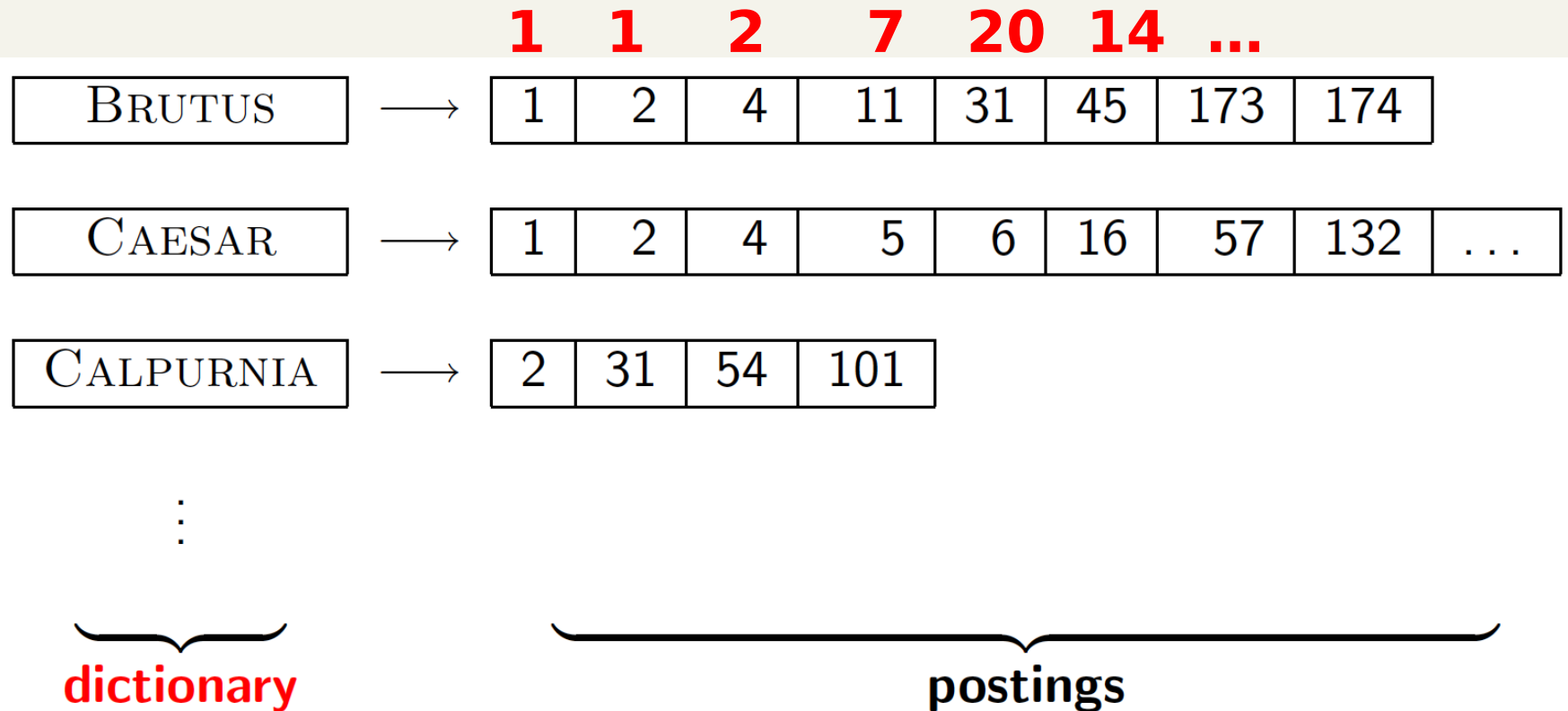
Index construction: Compression of postings

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Gap encoding



Then you compress the resulting integers with variable-length prefix-free codes, as follows...

Variable-byte codes

- Wish to get **very fast** (de)compress → **byte-align**
- Given a binary representation of an integer
 - Append 0s to front, to get a multiple-of-7 number of bits
 - Form groups of 7-bits each
 - Append to the **last** group the bit 0, and to the other groups the bit 1 (**tagging**)

e.g., $v = 2^{14} + 1 \rightarrow \text{binary}(v) = 1000000000000001$
1000000**1** **1**00000000 **0**0000001

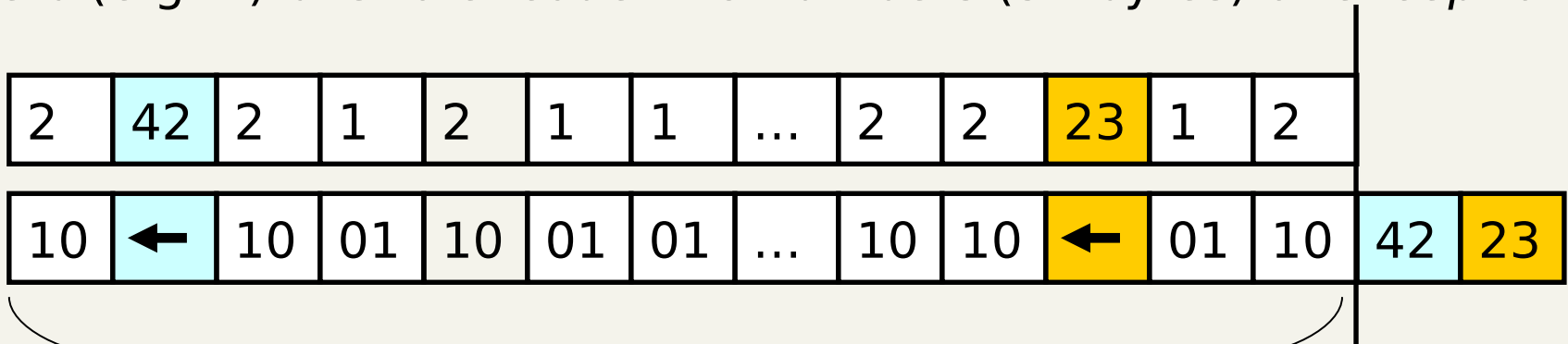
Note: We waste 1 bit per byte, and avg 4 for the first byte.

But it is a prefix code, and encodes also the value 0 !!

T-nibble: We could design this code over t -bits, not just $t=8$

PForDelta coding

Use b (e.g. 2) bits to encode 128 numbers (32 bytes) or *exceptions*



a block of 128 numbers = 256 bits = 32 bytes

Translate data: $[\text{base}, \text{base} + 2^b - 2] \rightarrow [0, 2^b - 2]$

Encode exceptions with value $2^b - 1$

Choose b to encode 90% values, or trade-off:

$b \uparrow$ waste more bits, $b \downarrow$ more exceptions

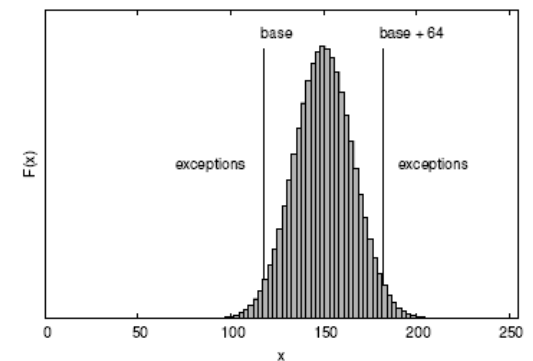
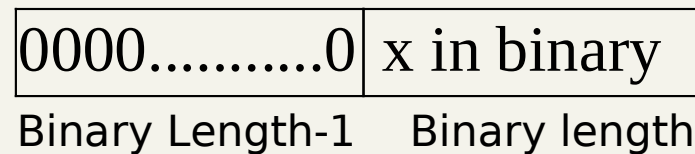


Figure 4.13: PFOR compression for $b = 6$ and $\text{base} = 118$ captures most of the values of this 256 value domain as codes.

γ -code



- $x > 0$ and Binary length = $\lfloor \log_2 x \rfloor + 1$

e.g., 9 represented as 0001001.

- γ -code for x takes $2 \lfloor \log_2 x \rfloor + 1$ bits
(ie. factor of 2 from binary)

It is a prefix-free encoding...

- Given the following sequence of γ -coded integers, reconstruct the original sequence:

000100000011001100000011101100111

8 6 3 59 7

The diagram illustrates the reconstruction of original integers from their gamma-coded binary representations. The sequence of gamma-coded integers is 000100000011001100000011101100111. Red arrows point from the original integers (8, 6, 3, 59, 7) to their corresponding gamma-coded strings. The gamma-coded strings are 00010000 (8), 001100 (6), 0011 (3), 0000001110 (59), and 100111 (7).

Elias-Fano

1 =	000	01
4 =	001	00
7 =	001	11
18 =	100	10
24 =	110	00
26 =	110	10
30 =	111	10
31 =	111	11

$z = 3, w = 2$



$L = 0100111000101011$

$B = 01001001000000000010000010100011$
 $x[0..7] = \{1, 4, 7, 18, 24, 26, 30, 31\}$

Represent numbers in $\text{ceil}[\log m]$ bits, where $m = |B|$

Set $z = \text{ceil}[\log n]$ and where $n = \#1$ then it can be proved

\mathcal{L} takes $\cong n \log(m/n)$ bits

\mathcal{H} takes $= n \text{ 1s} + n \text{ 0s} = 2n$ bits

In unary

$H = \begin{array}{c|c|c|c|c|c|c|c} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \hline 1 & 0 & 1 & 1 & 0 & 0 & 0 & 1 \end{array}$

How to get the i -th number? Take the i -th group of w bits in L and then represent the value $((\text{pos of } i\text{-th } 1) - i)$ in z bits