

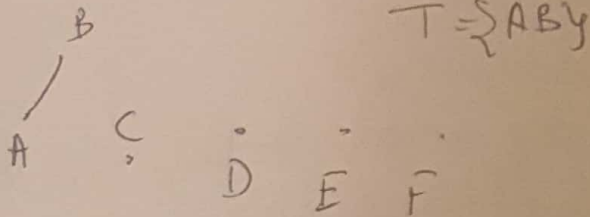
1) step 1: initialisation

A B C D E F

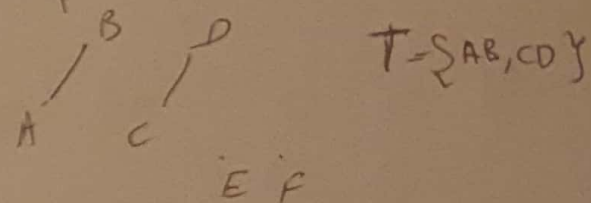
sorted edges: $\{$
 $AB, CD, AE, BD, EF,$
 $AF, DF, BC, AD\}$

$T = \{ \}$

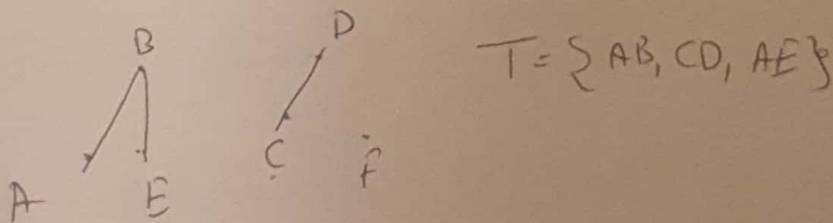
step 2: $C(A) \neq C(B)$



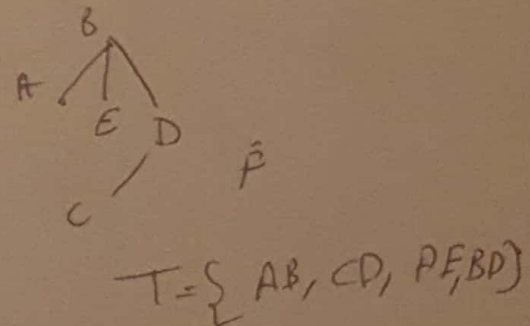
step 3: $C(C) \neq C(D)$



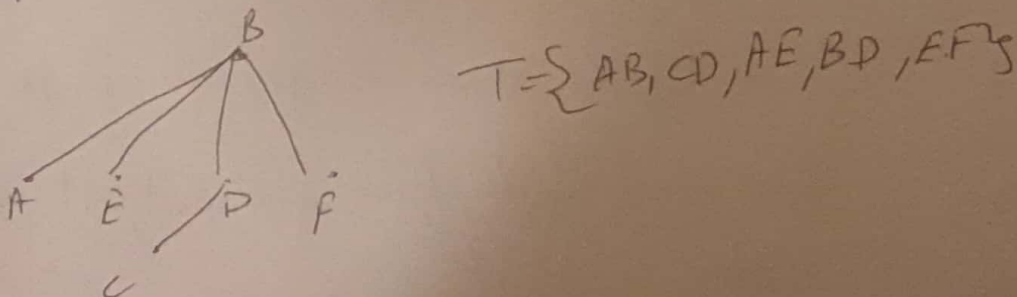
step 4: $C(A) \neq C(E)$



step 5: $C(B) \neq C(D)$



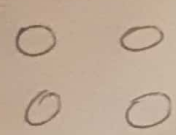
step 6: $C(E) \neq C(F)$

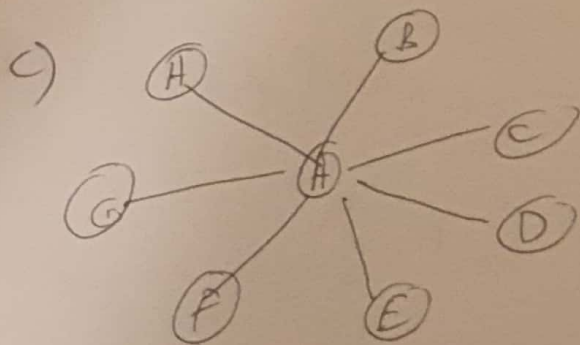


2) suppose $G = (V, E)$ is undirected (unweighted) simple graph. A subset u of V is called a base for G if every edge for G has at least one endpoint in u .

A) given $G = (V, E)$ is it true that V itself is a base for G ?

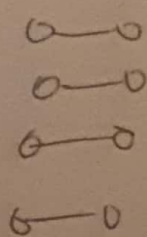
yes, by definition of E , every $e \in E$ has an endpoint in V .

B)  yes any graph with one or more vertices and no edges is an example.



if $u = \{A\}$ and every edge has one endpoint in u .

D) give an example of graph G having n vertices with the property that every base graph G has size at least n .



if n of the given edges are in u then each node has one endpoint in the graph.

e) devise an algorithm to solve smallest Base decision problem

$p \leftarrow$ obtain set of all subsets of V .

CurrentMin $\leftarrow |V|$

Current $\leftarrow V$

for u in p do

for e in E do

$a \leftarrow$ left endpoint of e

$b \leftarrow$ right endpoint of e

if a in u or b in u then

CurrentMin $\leftarrow |u|$

CurrentBase $\leftarrow u$

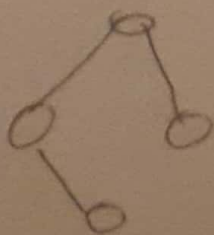
return U

the running time is $O(m^2)$.

3) suppose $G = (V, E)$ is an undirected graph \subset ~~any~~ unweighted

simple graph. A spanning cycle for G is a simple cycle in G that contains every vertex of G .

A)



B) The spanning cycle decision problem is

a graph G itself a simple cycle if G is connected and every vertex in G has degree 2.

algorithm check for spanning ($G(V, E)$)

Input: edges and vertices of G

output: true if spanning and false otherwise

Take all edges of G build adjacency Matrix

1 \rightarrow if edge exists

0 \rightarrow if does not exist

while (there are unvisited edges) {

check if there is connection from root to the first node

check graph is connected

check if each vertex = $\deg(v) = 2$ }