

# Chapter 2

## Quadratic Equations

- If the roots of the equation  $bx^2 + cx + a = 0$  be imaginary, then for all real values of  $x$ , the expression  $3b^2x^2 + 6bcx + 2c^2$  is **[AIEEE-2009]**  
(1) Less than  $4ab$  (2) Greater than  $-4ab$   
(3) Less than  $-4ab$  (4) Greater than  $4ab$
- If  $\alpha$  and  $\beta$  are the roots of the equation  $x^2 - x + 1 = 0$ , then  $\alpha^{2009} + \beta^{2009} =$  **[AIEEE-2010]**  
(1)  $-2$  (2)  $-1$   
(3)  $1$  (4)  $2$
- Let for  $a \neq a_1 \neq 0$ ,  
 $f(x) = ax^2 + bx + c$ ,  $g(x) = a_1x^2 + b_1x + c_1$  and  $p(x) = f(x) - g(x)$ .  
If  $p(x) = 0$  only for  $x = -1$  and  $p(-2) = 2$ , then the value of  $p(2)$  is **[AIEEE-2011]**  
(1)  $6$  (2)  $18$   
(3)  $3$  (4)  $9$
- Sachin and Rahul attempted to solve a quadratic equation. Sachin made a mistake in writing down the constant term and ended up in roots  $(4, 3)$ . Rahul made a mistake in writing down coefficient of  $x$  to get roots  $(3, 2)$ . The correct roots of equation are: **[AIEEE-2011]**  
(1)  $-6, -1$  (2)  $-4, -3$   
(3)  $6, 1$  (4)  $4, 3$
- The real number  $k$  for which the equation  $2x^3 + 3x + k = 0$  has two distinct real roots in  $[0, 1]$  **[JEE (Main)-2013]**  
(1) Lies between  $1$  and  $2$   
(2) Lies between  $2$  and  $3$   
(3) Lies between  $-1$  and  $0$   
(4) Does not exist
- If the equations  $x^2 + 2x + 3 = 0$  and  $ax^2 + bx + c = 0$ ,  $a, b, c \in R$ , have a common root, then  $a : b : c$  is **[JEE (Main)-2013]**  
(1)  $1 : 2 : 3$  (2)  $3 : 2 : 1$   
(3)  $1 : 3 : 2$  (4)  $3 : 1 : 2$
- Let  $\alpha$  and  $\beta$  be the roots of equation  $x^2 - 6x - 2 = 0$ .  
If  $a_n = \alpha^n - \beta^n$ , for  $n \geq 1$ , then the value of  $\frac{a_{10} - 2a_8}{2a_9}$  is equal to **[JEE (Main)-2015]**  
(1)  $6$  (2)  $-6$   
(3)  $3$  (4)  $-3$
- The sum of all real values of  $x$  satisfying the equation  $(x^2 - 5x + 5)^{x^2 + 4x - 60} = 1$  is **[JEE (Main)-2016]**  
(1)  $-4$  (2)  $6$   
(3)  $5$  (4)  $3$
- If, for a positive integer  $n$ , the quadratic equation,  $x(x+1) + (x+1)(x+2) + \dots + (x+n-1)(x+n) = 10n$  has two consecutive integral solutions, then  $n$  is equal to **[JEE (Main)-2017]**  
(1)  $9$  (2)  $10$   
(3)  $11$  (4)  $12$
- Let  $S = \{x \in R : x \geq 0 \text{ and } 2|\sqrt{x} - 3| + \sqrt{x}(\sqrt{x} - 6) + 6 = 0\}$ . Then  $S$  **[JEE (Main)-2018]**  
(1) Is an empty set  
(2) Contains exactly one element  
(3) Contains exactly two elements  
(4) Contains exactly four elements
- If both the roots of the quadratic equation  $x^2 - mx + 4 = 0$  are real and distinct and they lie in the interval  $[1, 5]$  then  $m$  lies in the interval **[JEE (Main)-2019]**  
(1)  $(-5, -4)$  (2)  $(3, 4)$   
(3)  $(4, 5)$  (4)  $(5, 6)$
- The number of all possible positive integral values of  $\alpha$  for which the roots of the quadratic equation,  $6x^2 - 11x + \alpha = 0$  are rational numbers is **[JEE (Main)-2019]**  
(1)  $4$  (2)  $5$   
(3)  $2$  (4)  $3$

13. Consider the quadratic equation  $(c - 5)x^2 - 2cx + (c - 4) = 0$ ,  $c \neq 5$ . Let  $S$  be the set of all integral values of  $c$  for which one root of the equation lies in the interval  $(0, 2)$  and its other root lies in the interval  $(2, 3)$ . Then the number of elements in  $S$  is [JEE (Main)-2019]
- (1) 11 (2) 18  
(3) 12 (4) 10
14. The value of  $\lambda$  such that sum of the squares of the roots of the quadratic equation,  $x^2 + (3 - \lambda)x + 2 = \lambda$  has the least value is [JEE (Main)-2019]
- (1) 2 (2) 1  
(3)  $\frac{15}{8}$  (4)  $\frac{4}{9}$
15. If one real root of the quadratic equation  $81x^2 + kx + 256 = 0$  is cube of the other root, then a value of  $k$  is [JEE (Main)-2019]
- (1) -300 (2) 144  
(3) -81 (4) 100
16. Let  $\alpha$  and  $\beta$  the roots of the quadratic equation  $x^2 \sin \theta - x(\sin \theta \cos \theta + 1) + \cos \theta = 0$  ( $0 < \theta < 45^\circ$ ), and  $\alpha < \beta$ . Then  $\sum_{n=0}^{\infty} \left( \alpha^n + \frac{(-1)^n}{\beta^n} \right)$  is equal to [JEE (Main)-2019]
- (1)  $\frac{1}{1 + \cos \theta} - \frac{1}{1 - \sin \theta}$  (2)  $\frac{1}{1 - \cos \theta} + \frac{1}{1 + \sin \theta}$   
(3)  $\frac{1}{1 - \cos \theta} - \frac{1}{1 + \sin \theta}$  (4)  $\frac{1}{1 + \cos \theta} + \frac{1}{1 - \sin \theta}$
17. If  $\lambda$  be the ratio of the roots of the quadratic equation in  $x$ ,  $3m^2x^2 + m(m - 4)x + 2 = 0$ , then the least value of  $m$  for which  $\lambda + \frac{1}{\lambda} = 1$ , is [JEE (Main)-2019]
- (1)  $4 - 2\sqrt{3}$  (2)  $4 - 3\sqrt{2}$   
(3)  $2 - \sqrt{3}$  (4)  $-2 + \sqrt{2}$
18. The number of integral values of  $m$  for which the quadratic expression,  $(1 + 2m)x^2 - 2(1 + 3m)x + 4(1 + m)$ ,  $x \in \mathbb{R}$ , is always positive, is [JEE (Main)-2019]
- (1) 8 (2) 3  
(3) 6 (4) 7
19. If  $\alpha$  and  $\beta$  be the roots of the equation  $x^2 - 2x + 2 = 0$ , then the least value of  $n$  for which  $\left(\frac{\alpha}{\beta}\right)^n = 1$  is [JEE (Main)-2019]
- (1) 4 (2) 5  
(3) 3 (4) 2
20. The sum of the solutions of the equation  $|\sqrt{x} - 2| + \sqrt{x}(\sqrt{x} - 4) + 2 = 0$ , ( $x > 0$ ) is equal to [JEE (Main)-2019]
- (1) 4 (2) 10  
(3) 9 (4) 12
21. If three distinct numbers  $a, b, c$  are in G.P. and the equations  $ax^2 + 2bx + c = 0$  and  $dx^2 + 2ex + f = 0$  have a common root, then which one of the following statements is correct? [JEE (Main)-2019]
- (1)  $d, e, f$  are in A.P.  
(2)  $\frac{d}{a}, \frac{e}{b}, \frac{f}{c}$  are in G.P.  
(3)  $\frac{d}{a}, \frac{e}{b}, \frac{f}{c}$  are in A.P.  
(4)  $d, e, f$  are in G.P.
22. The number of integral values of  $m$  for which the equation  $(1 + m^2)x^2 - 2(1 + 3m)x + (1 + 8m) = 0$  has no real root is : [JEE (Main)-2019]
- (1) Infinitely many (2) 3  
(3) 2 (4) 1
23. Let  $p, q \in \mathbb{R}$ . If  $2 - \sqrt{3}$  is a root of the quadratic equation,  $x^2 + px + q = 0$ , then [JEE (Main)-2019]
- (1)  $q^2 - 4p - 16 = 0$  (2)  $p^2 - 4q + 12 = 0$   
(3)  $p^2 - 4q - 12 = 0$  (4)  $q^2 + 4p + 14 = 0$
24. If  $m$  is chosen in the quadratic equation  $(m^2 + 1)x^2 - 3x + (m^2 + 1)^2 = 0$  such that the sum of its roots is greatest, then the absolute difference of the cubes of its roots is [JEE (Main)-2019]
- (1)  $8\sqrt{3}$  (2)  $10\sqrt{5}$   
(3)  $4\sqrt{3}$  (4)  $8\sqrt{5}$

25. If  $\alpha$  and  $\beta$  are the roots of the equation

$$375x^2 - 25x - 2 = 0, \text{ then } \lim_{n \rightarrow \infty} \sum_{r=1}^n \alpha^r + \lim_{n \rightarrow \infty} \sum_{r=1}^n \beta^r$$

is equal to [JEE (Main)-2019]

- (1)  $\frac{21}{346}$  (2)  $\frac{7}{116}$   
 (3)  $\frac{29}{358}$  (4)  $\frac{1}{12}$

26. If  $\alpha$ ,  $\beta$  and  $\gamma$  are three consecutive terms of a non-constant G.P. such that the equations  $\alpha x^2 + 2\beta x + \gamma = 0$  and  $x^2 + x - 1 = 0$  have a common root, then  $\alpha(\beta + \gamma)$  is equal to

[JEE (Main)-2019]

- (1) 0 (2)  $\alpha\gamma$   
 (3)  $\beta\gamma$  (4)  $\alpha\beta$

27. Let  $\alpha$  and  $\beta$  be two real roots of the equation  $(k+1)\tan^2 x - \sqrt{2} \cdot \lambda \tan x = (1-k)$ , where  $k(\neq -1)$  and  $\lambda$  are real numbers. If  $\tan^2(\alpha + \beta) = 50$ , then a value of  $\lambda$  is [JEE (Main)-2020]

- (1) 10 (2)  $10\sqrt{2}$   
 (3) 5 (4)  $5\sqrt{2}$

28. Let  $\alpha$  and  $\beta$  be the roots of the equation  $x^2 - x - 1 = 0$ . If  $p_k = (\alpha)^k + (\beta)^k$ ,  $k \geq 1$ , then which one of the following statements is not true?

[JEE (Main)-2020]

- (1)  $p_3 = p_5 - p_4$   
 (2)  $(p_1 + p_2 + p_3 + p_4 + p_5) = 26$   
 (3)  $p_5 = 11$   
 (4)  $p_5 = p_2 \cdot p_3$

29. Let S be the set of all real roots of the equation,  $3^x(3^x - 1) + 2 = |3^x - 1| + |3^x - 2|$ . Then S

[JEE (Main)-2020]

- (1) Contains at least four elements  
 (2) Is a singleton  
 (3) Contains exactly two elements  
 (4) Is an empty set

30. The number of real roots of the equation,  $e^{4x} + e^{3x} - 4e^{2x} + e^x + 1 = 0$  is [JEE (Main)-2020]

- (1) 4 (2) 2  
 (3) 3 (4) 1

31. Let  $a, b \in R$ ,  $a \neq 0$  be such that the equation,  $ax^2 - 2bx + 5 = 0$  has a repeated root  $\alpha$ , which is also a root of the equation,  $x^2 - 2bx - 10 = 0$ . If  $\beta$  is the other root of this equation, then  $\alpha^2 + \beta^2$  is equal to [JEE (Main)-2020]

- (1) 25 (2) 24  
 (3) 26 (4) 28

32. Let  $\alpha$  and  $\beta$  be the roots of the equation,  $5x^2 + 6x - 2 = 0$ . If  $S_n = \alpha^n + \beta^n$ ,  $n = 1, 2, 3, \dots$ , then [JEE (Main)-2020]

- (1)  $5S_6 + 6S_5 = 2S_4$  (2)  $6S_6 + 5S_5 + 2S_4 = 0$   
 (3)  $6S_6 + 5S_5 = 2S_4$  (4)  $5S_6 + 6S_5 + 2S_4 = 0$

33. Let  $f(x)$  be a quadratic polynomial such that  $f(-1) + f(2) = 0$ . If one of the roots of  $f(x) = 0$  is 3, then its other root lies in [JEE (Main)-2020]

- (1)  $(-1, 0)$  (2)  $(-3, -1)$   
 (3)  $(0, 1)$  (4)  $(1, 3)$

34. If  $\alpha$  and  $\beta$  are the roots of the equation  $x^2 + px + 2 = 0$  and  $\frac{1}{\alpha}$  and  $\frac{1}{\beta}$  are the roots of the equation  $2x^2 + 2qx + 1 = 0$ , then

$$\left(\alpha - \frac{1}{\alpha}\right)\left(\beta - \frac{1}{\beta}\right)\left(\alpha + \frac{1}{\beta}\right)\left(\beta + \frac{1}{\alpha}\right) \text{ is equal to}$$

[JEE (Main)-2020]

- (1)  $\frac{9}{4}(9 - q^2)$  (2)  $\frac{9}{4}(9 + p^2)$   
 (3)  $\frac{9}{4}(9 + q^2)$  (4)  $\frac{9}{4}(9 - p^2)$

35. The set of all real values of  $\lambda$  for which the quadratic equations,  $(\lambda^2 + 1)x^2 - 4\lambda x + 2 = 0$  always have exactly one root in the interval  $(0, 1)$  is [JEE (Main)-2020]

- (1)  $(-3, -1)$  (2)  $(2, 4)$   
 (3)  $(0, 2)$  (4)  $(1, 3)$

36. Let  $\lambda \neq 0$  be in  $R$ . If  $\alpha$  and  $\beta$  are the roots of the equation,  $x^2 - x + 2\lambda = 0$  and  $\alpha$  and  $\gamma$  are the roots of the equation,  $3x^2 - 10x + 27\lambda = 0$ , then

$$\frac{\beta\gamma}{\lambda} \text{ is equal to} \quad \text{[JEE (Main)-2020]}$$

- (1) 18 (2) 9  
 (3) 27 (4) 36

37. The product of the roots of the equation  $9x^2 - 18|x| + 5 = 0$ , is [JEE (Main)-2020]

- (1)  $\frac{25}{9}$  (2)  $\frac{25}{81}$   
(3)  $\frac{5}{9}$  (4)  $\frac{5}{27}$

38. If  $\alpha$  and  $\beta$  are the roots of the equation,  $7x^2 - 3x - 2 = 0$ , then the value of  $\frac{\alpha}{1-\alpha^2} + \frac{\beta}{1-\beta^2}$  is equal to [JEE (Main)-2020]

- (1)  $\frac{1}{24}$  (2)  $\frac{27}{32}$   
(3)  $\frac{3}{8}$  (4)  $\frac{27}{16}$

39. If  $\alpha$  and  $\beta$  be two roots of the equation  $x^2 - 64x + 256 = 0$ . Then the value of  $\left(\frac{\alpha^3}{\beta^5}\right)^{\frac{1}{8}} + \left(\frac{\beta^3}{\alpha^5}\right)^{\frac{1}{8}}$  is [JEE (Main)-2020]

- (1) 3 (2) 2  
(3) 4 (4) 1

40. If  $\alpha$  and  $\beta$  are the roots of the equation  $2x(2x + 1) = 1$ , then  $\beta$  is equal to [JEE (Main)-2020]

- (1)  $2\alpha^2$   
(2)  $-2\alpha(\alpha + 1)$   
(3)  $2\alpha(\alpha - 1)$   
(4)  $2\alpha(\alpha + 1)$

41. The least positive value of 'a' for which the equation,  $2x^2 + (a - 10)x + \frac{33}{2} = 2a$  has real roots is [JEE (Main)-2020]

42. The integer 'k', for which the inequality  $x^2 - 2(3k - 1)x + 8k^2 - 7 > 0$  is valid for every x in R, is : [JEE (Main)-2021]

- (1) 2 (2) 3  
(3) 4 (4) 0

43. Let  $\alpha$  and  $\beta$  be the roots of  $x^2 - 6x - 2 = 0$ . If  $a_n = \alpha^n - \beta^n$  for  $n \geq 1$ , then the value of  $\frac{a_{10} - 2a_8}{3a_9}$  is : [JEE (Main)-2021]

- (1) 2 (2) 4  
(3) 3 (4) 1

44. Let  $\alpha$  and  $\beta$  be two real numbers such that  $\alpha + \beta = 1$  and  $\alpha\beta = -1$ . Let  $p_n = (\alpha)^n + (\beta)^n$ ,  $p_{n-1} = 11$  and  $p_{n+1} = 29$  for some integer  $n \geq 1$ . Then, the value of  $p_n^2$  is [JEE (Main)-2021]

45. The value of  $4 + \frac{1}{5 + \frac{1}{4 + \frac{1}{5 + \frac{1}{4 + \dots \infty}}}}$  is : [JEE (Main)-2021]

- (1)  $2 + \frac{4}{\sqrt{5}}\sqrt{30}$  (2)  $4 + \frac{4}{\sqrt{5}}\sqrt{30}$   
(3)  $2 + \frac{2}{5}\sqrt{30}$  (4)  $5 + \frac{2}{5}\sqrt{30}$

46. The value of  $3 + \frac{1}{4 + \frac{1}{3 + \frac{1}{4 + \dots \infty}}}$  is equal to [JEE (Main)-2021]

- (1)  $2 + \sqrt{3}$   
(2)  $3 + 2\sqrt{3}$   
(3)  $4 + \sqrt{3}$   
(4)  $1.5 + \sqrt{3}$

47. The number of real roots of the equation  $e^{6x} - e^{4x} - 2e^{3x} - 12e^{2x} + e^x + 1 = 0$  is [JEE (Main)-2021]

- (1) 1 (2) 2  
(3) 6 (4) 4

48. If  $\alpha, \beta$  are roots of the equation  $x^2 + 5(\sqrt{2})x + 10 = 0$ ,  $\alpha > \beta$  and  $P_n = \alpha^n - \beta^n$  for each positive integer n, then the value of  $\left(\frac{P_{17}P_{20} + 5\sqrt{2}P_{17}P_{19}}{P_{18}P_{19} + 5\sqrt{2}P_{18}^2}\right)$  is equal to [JEE (Main)-2021]

49. The number of real solutions of the equation,  $x^2 - |x| - 12 = 0$  is [JEE (Main)-2021]

- (1) 4 (2) 2  
(3) 1 (4) 3

50. If  $a + b + c = 1$ ,  $ab + bc + ca = 2$  and  $abc = 3$ , then the value of  $a^4 + b^4 + c^4$  is equal to \_\_\_\_.

[JEE (Main)-2021]

51. Let  $\alpha, \beta$  be two roots of the equation  $x^2 + (20)^{\frac{1}{4}}x + (5)^{\frac{1}{2}} = 0$ . Then  $\alpha^8 + \beta^8$  is equal to

[JEE (Main)-2021]

- (1) 160 (2) 10  
(3) 50 (4) 100

52. Let  $\alpha = \max_{x \in \mathbb{R}} \{8^{2\sin 3x} \cdot 4^{4\cos 3x}\}$  and

$$\beta = \min_{x \in \mathbb{R}} \{8^{2\sin 3x} \cdot 4^{4\cos 3x}\}$$

If  $8x^2 + bx + c = 0$  is a quadratic equation whose roots are  $\alpha^{\frac{1}{5}}$  and  $\beta^{\frac{1}{5}}$ , then the value of  $c - b$  is equal to:

[JEE (Main)-2021]

- (1) 43 (2) 42  
(3) 50 (4) 47

53. The number of real roots of the equation  $e^{4x} - e^{3x} - 4e^{2x} - e^x + 1 = 0$  is equal to \_\_\_\_.

[JEE (Main)-2021]

54. The sum of all integral values of  $k (k \neq 0)$  for which the equation  $\frac{2}{x-1} - \frac{1}{x-2} = \frac{2}{k}$  in  $x$  has no real roots, is \_\_\_\_.

[JEE (Main)-2021]

55. Let  $\lambda \neq 0$  be in  $\mathbb{R}$ . If  $\alpha$  and  $\beta$  are the roots of the equation  $x^2 - x + 2\lambda = 0$ , and  $\alpha$  and  $\gamma$  are the roots of the equation  $3x^2 - 10x + 27\lambda = 0$ , then  $\frac{\beta\gamma}{\lambda}$  is equal to \_\_\_\_.

[JEE (Main)-2021]

56. The set of all values of  $k > -1$ , for which the equation  $(3x^2 + 4x + 3)^2 - (k + 1)(3x^2 + 4x + 3)(3x^2 + 4x + 2) + k(3x^2 + 4x + 2)^2 = 0$  has real roots, is

[JEE (Main)-2021]

- (1)  $\left[\frac{1}{2}, \frac{3}{1}\right] - \{1\}$  (2)  $\left[-\frac{1}{2}, 1\right]$   
(3)  $[2, 3]$  (4)  $\left(1, \frac{5}{2}\right]$

57.  $\operatorname{cosec} 18^\circ$  is a root of the equation

[JEE (Main)-2021]

- (1)  $x^2 - 2x + 4 = 0$  (2)  $x^2 + 2x - 4 = 0$   
(3)  $x^2 - 2x - 4 = 0$  (4)  $4x^2 + 2x - 1 = 0$

58. The number of pairs  $(a, b)$  of real numbers, such that whenever  $\alpha$  is a root of the equation  $x^2 + ax + b = 0$ ,  $\alpha^2 - 2$  is also a root of this equation, is :

[JEE (Main)-2021]

- (1) 8 (2) 4  
(3) 6 (4) 2

59. Let  $f(x)$  be a polynomial of degree 3 such that  $f(k) = -\frac{2}{k}$  for  $k = 2, 3, 4, 5$ . Then the value of  $52 - 10 f(10)$  is equal to \_\_\_\_.

[JEE (Main)-2021]

60. If  $\alpha$  and  $\beta$  are the roots of the quadratic equation,  $x^2 + x \sin \theta - 2 \sin \theta = 0$ ,  $\theta \in \left(0, \frac{\pi}{2}\right)$ , then  $\frac{\alpha^{12} + \beta^{12}}{(\alpha^{-12} + \beta^{-12}) \cdot (\alpha - \beta)^{24}}$  is equal to

[JEE (Main)-2021]

- (1)  $\frac{2^{12}}{(\sin \theta - 8)^6}$  (2)  $\frac{2^{12}}{(\sin \theta - 4)^{12}}$   
(3)  $\frac{2^6}{(\sin \theta + 8)^{12}}$  (4)  $\frac{2^{12}}{(\sin \theta + 8)^{12}}$

61. If for some  $p, q, r \in \mathbb{R}$ , not all have same sign, one of the roots of the equation  $(p^2 + q^2)x^2 - 2q(p + r)x + q^2 + r^2 = 0$  is also a root of the equation  $x^2 + 2x - 8 = 0$ , then  $\frac{q^2 + r^2}{p^2}$  is equal to \_\_\_\_.

[JEE (Main)-2022]

62. If  $\alpha, \beta$  are the roots of the equation

$$x^2 - \left(5 + 3^{\sqrt{\log_3 5}} - 5^{\sqrt{\log_5 3}}\right) + 3 \left(3^{(\log_3 5)^{\frac{1}{2}}} - 5^{(\log_5 3)^{\frac{2}{3}}} - 1\right) = 0,$$

then the equation, whose roots are  $\alpha + \frac{1}{\beta}$  and

$\beta + \frac{1}{\alpha}$ , is [JEE (Main)-2022]

- (1)  $3x^2 - 20x - 12 = 0$  (2)  $3x^2 - 10x - 4 = 0$   
(3)  $3x^2 - 10x + 2 = 0$  (4)  $3x^2 - 20x + 16 = 0$

63. Let  $a, b$  be the roots of the equation

$$x^2 - \sqrt{2}x + \sqrt{6} = 0 \text{ and } \frac{1}{\alpha^2} + 1, \frac{1}{\beta^2} + 1, \frac{1}{\beta^2} + 1 \text{ be}$$

the roots of the equation  $x^2 + ax + b = 0$ . Then the roots of the equation  $x^2 - (a + b - 2)x + (a + b + 2) = 0$  are

[JEE (Main)-2022]

- (1) non-real complex number  
(2) real and both negative  
(3) real and both positive  
(4) real and exactly one of them is positive

64. Let  $f(x) = ax^2 + bx + c$  be such that  $f(1) = 3$ ,  $f(-2) = \lambda$  and  $f(3) = 4$ . If  $f(0) + f(1) + f(-2) + f(3) = 14$ , then  $\lambda$  is equal to **[JEE (Main)-2022]**

- (1)  $-4$  (2)  $\frac{13}{2}$   
(3)  $\frac{23}{2}$  (4)  $4$

65. Let  $a, b (a > b)$  be the roots of the quadratic equation  $x^2 - x - 4 = 0$ . If  $P_n = \alpha^n - \beta^n$ ,  $n \in \mathbb{N}$ ,

then  $\frac{P_{15}P_{16} - P_{14}P_{16} - P_{15}^2 + P_{14}P_{15}}{P_{13}P_{14}}$  is equal to

**[JEE (Main)-2022]**

66. If the sum of the squares of the reciprocals of the roots  $\alpha$  and  $\beta$  of the equation  $3x^2 + \lambda x - 1 = 0$  is 15, then  $6(\alpha^3 + \beta^3)^2$  is equal to :

- (1) 18 (2) 24  
(3) 36 (4) 96

**[JEE (Main)-2022]**

67. The sum of all the real roots of the equation  $(e^{2x} - 4)(6e^{2x} - 5e^x + 1) = 0$  is

- (1)  $\log_e 3$  (2)  $-\log_e 3$   
(3)  $\log_e 6$  (4)  $-\log_e 6$

**[JEE (Main)-2022]**

68. Let  $a, b \in \mathbb{R}$  be such that the equation  $ax^2 - 2bx + 15 = 0$  has a repeated root  $\alpha$ . If  $\alpha$  and  $\beta$  are the roots of the equation  $x^2 - 2bx + 21 = 0$ , then  $\alpha^2 + \beta^2$  is equal to

- (1) 37 (2) 58  
(3) 68 (4) 92

**[JEE (Main)-2022]**

69. The sum of the cubes of all the roots of the equation  $x^4 - 3x^3 - 2x^2 + 3x + 1 = 0$  is \_\_\_\_\_.

**[JEE (Main)-2022]**

70. Let  $p$  and  $q$  be two real numbers such that  $p + q = 3$

and  $p^4 + q^4 = 369$ . Then  $\left(\frac{1}{p} + \frac{1}{q}\right)^{-2}$  is equal to \_\_\_\_\_.

**[JEE (Main)-2022]**

71. If the sum of all the roots of the equation  $e^{2x} - 11e^x - 45e^{-x} + \frac{81}{2} = 0$  is  $\log_e p$ , then  $p$  is equal to \_\_\_\_\_.

**[JEE (Main)-2022]**

72. Let  $\alpha, \beta$  be the roots of the equation  $x^2 - 4\lambda x + 5 = 0$  and  $\alpha, \gamma$  be the roots of the equation

$$x^2 - (3\sqrt{2} + 2\sqrt{3})x + 7 + 3\lambda\sqrt{3} = 0, \quad \lambda > 0. \text{ If}$$

$\beta + \lambda = 3\sqrt{2}$ , then  $(\alpha + 2\beta + \gamma)^2$  is equal to \_\_\_\_\_.

**[JEE (Main)-2022]**

73. The number of real solutions of the equation  $e^{4x} + 4e^{3x} - 58e^{2x} + 4e^x + 1 = 0$  is \_\_\_\_\_.

74. Let  $f(x)$  be a quadratic polynomial such that  $f(-2) + f(3) = 0$ . If one of the roots of  $f(x) = 0$  is  $-1$ , then the sum of the roots of  $f(x) = 0$  is equal to:

- (1)  $\frac{11}{3}$  (2)  $\frac{7}{3}$   
(3)  $\frac{13}{3}$  (4)  $\frac{14}{3}$

**[JEE (Main)-2022]**

75. Let  $f(x)$  and  $g(x)$  be two real polynomials of degree 2 and 1 respectively. If  $f(g(x)) = 8x^2 - 2x$  and  $g(f(x)) = 4x^2 + 6x + 1$ , then the value of  $f(2) + g(2)$  is \_\_\_\_\_.

**[JEE (Main)-2022]**

76. Let  $f(x)$  be a quadratic polynomial with leading coefficient 1 such that  $f(0) = p$ ,  $p \neq 0$ , and

$$f(1) = \frac{1}{3}. \text{ If the equations } f(x) = 0 \text{ and } f(f(x)) = 0 \text{ have a common real root, then } f(-3) \text{ is equal to } \underline{\hspace{2cm}}.$$

**[JEE (Main)-2022]**

77. The sum of all real value of  $x$  for which

$$\frac{3x^2 - 9x + 17}{x^2 + 3x + 10} = \frac{5x^2 - 7x + 19}{3x^2 + 5x + 12} \text{ is equal to } \underline{\hspace{2cm}}.$$

**[JEE (Main)-2022]**

78. The minimum value of the sum of the squares of the roots of  $x^2 + (3 - a)x + 1 = 2a$  is **[JEE (Main)-2022]**

- (1) 4 (2) 5  
(3) 6 (4) 8

