#### 关于自旋系统的一些统计处理(复习):

模拟其M、 $\chi$ 、 $\xi$ 、C等与温度的关系,特别是在 $T_c$ 附近;

$$H = H(\sigma) = -\sum_{\langle i,j \rangle} J\sigma_i \sigma_j - h \sum_{\langle i \rangle} \sigma_i, \quad \sigma = \pm 1$$

$$F = -\frac{1}{\beta} \ln \sum_{i} \exp(-\beta \tilde{H}_{i})$$

$$m_{i} = \frac{1}{2L^{2}} \sum_{j}^{L \times L} s_{j}$$

$$\langle A \rangle = \frac{\sum_{i} A_{i} \exp(-\beta \widetilde{H}_{i})}{\sum_{i} \exp(-\beta \widetilde{H}_{i})}$$

$$m_i = \frac{1}{2L^2} \sum_{j}^{L \times L} s_j$$

$$m = \langle m_i \rangle$$

$$\chi_m = \beta(\langle m_i^2 \rangle - \langle m_i \rangle^2)$$



• 统计物理中有涨落-耗散定理:

$$C_V = \frac{\partial \langle E \rangle}{\partial T} = \frac{\beta}{T} \left[ \langle E^2 \rangle - \langle E \rangle^2 \right]$$

• 看看一些粗糙的模拟结果:













