

## Input Your Article Title Here if it is too Long

### Summary

This is abstract. This section should describe what problem the paper solves, what methods are applied, what results are obtained and summarize them.

This is the second line abstract. And if you look carefully you can see that the spacing within and between paragraphs is different, which facilitates our reading in paragraphs.

This is **the special** special *special special* fonts in abstract.

**Keywords: Fighting Wildfires; Multi-Objective Optimization; Poisson Distribution; Tabu Search Algorithm; Sensitivity Analysis**

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# 1 Ideal Battery

## 1.1 Assumptions

To consider an simplist ideal battery model, the following assumptions are made:

- The battery is kept at a constant environment, so the temperature effects are neglected.
- The battery has no energy loss during charging and discharging.
- The battery has infinite cycle life, so the degradation effects are neglected and all the parameters are constant.
- The Open Circuit Voltage (OCV) is only related to the SoC, so we can express the SoC as a function of  $U_{OC}$ :

$$SoC = f(U_{OC}) \quad (1)$$

in which  $f(\cdot)$  can be obtained through curve fitting based on experimental data.

- The battery behavior is same for charging and discharging. For smartphones, which mostly use LiCoO<sub>2</sub> batteries that has little or no hysteresis, this assumption is reasonable.

## 1.2 Thevenin Model

A Li-ion battery system can be extremely complex, involving electrochemical, thermal and mechanical processes. However, for system-level studies, an equivalent circuit model is often used to represent the battery behavior. The Thevenin model is a widely used equivalent circuit model that captures the dynamic response of the battery voltage during charge and discharge cycles. The model is described as follows:

The relationship between  $U_{OC}$  and other parameters in the Thevenin model can be expressed with Kirchhoff's laws:

$$U_{OC} = U_t + IR_0 + U_1 + U_2 \quad (2)$$

in which  $U_t$  is the terminal voltage.

For  $U_1, U_2$  we have:

$$I = C_1 \frac{dU_1}{dt} + \frac{U_1}{R_1} = C_2 \frac{dU_2}{dt} + \frac{U_2}{R_2} \quad (3)$$

Differentiating the SoC's definition with respect to time, we get:

$$\frac{d(SoC)}{dt} = -\frac{I}{Q_{max}} \quad (4)$$

where  $Q_{max}$  is the maximum capacity of the battery.

Combining the above equations, we can derive the complete Thevenin model in matrix form:

$$\frac{d}{dt} \begin{bmatrix} SoC \\ U_1 \\ U_2 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & -\frac{1}{R_1 C_1} & 0 \\ 0 & 0 & -\frac{1}{R_2 C_2} \end{bmatrix} \begin{bmatrix} SoC \\ U_1 \\ U_2 \end{bmatrix} + \begin{bmatrix} -\frac{1}{Q_{max}} \\ \frac{1}{C_1} \\ \frac{1}{C_2} \end{bmatrix} I \quad (5)$$

where  $R_0, R_1, R_2, C_1, C_2, Q_{max}$  are the model parameters that need to be estimated.

### 1.3 Parameter Estimation

The Hybrid Pulse Power Characterization (HPPC) test is commonly used for this purpose. The test is conducted with steps as follows:

1. The battery is first fully charged to 100% SoC in ways the manufacturer recommends.
2. After resting for a certain period (e.g. 1 hour), the battery is discharged with a constant current pulse (e.g.,  $0.5C$ ) for a short duration (e.g., 10s). The voltage response is recorded.
3. Then discharge the battery to another selected SoC point (e.g., 90%).
4. Repeat steps 2 and 3 until the battery reaches a low SoC point (e.g., 10%) or the maximum discharge limit the manufacturer specifies.
5. If needed, repeat similar steps for charging pulses.

With HPPC data, the model parameters can be estimated through curve fitting techniques. The process are as follows:

- **Estimate  $R_0$ :** The instantaneous voltage drop at the start of each pulse can be used to estimate the internal resistance  $R_0$ , at which point the capacitive effects are negligible.

$$R_0 = \frac{\Delta U_{instant}}{I_{pulse}} \quad (6)$$

- **Estimate  $R_1, C_1$  and  $R_2, C_2$ :** Solve the polarization equation (3), we can get the polarization voltage response:

$$U_{polar} = IR + (U_{init} - IR)e^{-\frac{t}{RC}} \quad (7)$$

where  $U_{init}$  is the voltage at the start of the pulse.

Without loss of generality, let  $R_1 C_1 \leq R_2 C_2$ , so that the faster electrochemical polarization are represented by  $R_1, C_1$  and the slower concentration polarization effects are represented by  $R_2, C_2$ . Then substitute them into (2), we have:

$$U_t = U_{OC} - I(R_0 + R_1 + R_2) - (U_{1,init} - IR_1)e^{-\frac{t}{R_1 C_1}} - (U_{2,init} - IR_2)e^{-\frac{t}{R_2 C_2}} \quad (8)$$

By least squares fitting of (8) to the voltage response data during each pulse, we can estimate the values of  $R_1, C_1$  and  $R_2, C_2$  at different SoC points.

- **Estimate  $Q_{max}$ :** The maximum capacity  $Q_{max}$  can be estimated by integrating the current over the full discharge cycle:

$$Q_{max} = \int_{t_0}^{t_f} I(t)dt \quad (9)$$

where  $t_0$  and  $t_f$  are the start and end times of the discharge cycle. Most of the time this value is provided by the manufacturer.

We use a Samsung INR21700 30T 3Ah Li-ion Battery Dataset to demonstrate the parameter estimation process. The fitting result are shown as follows:

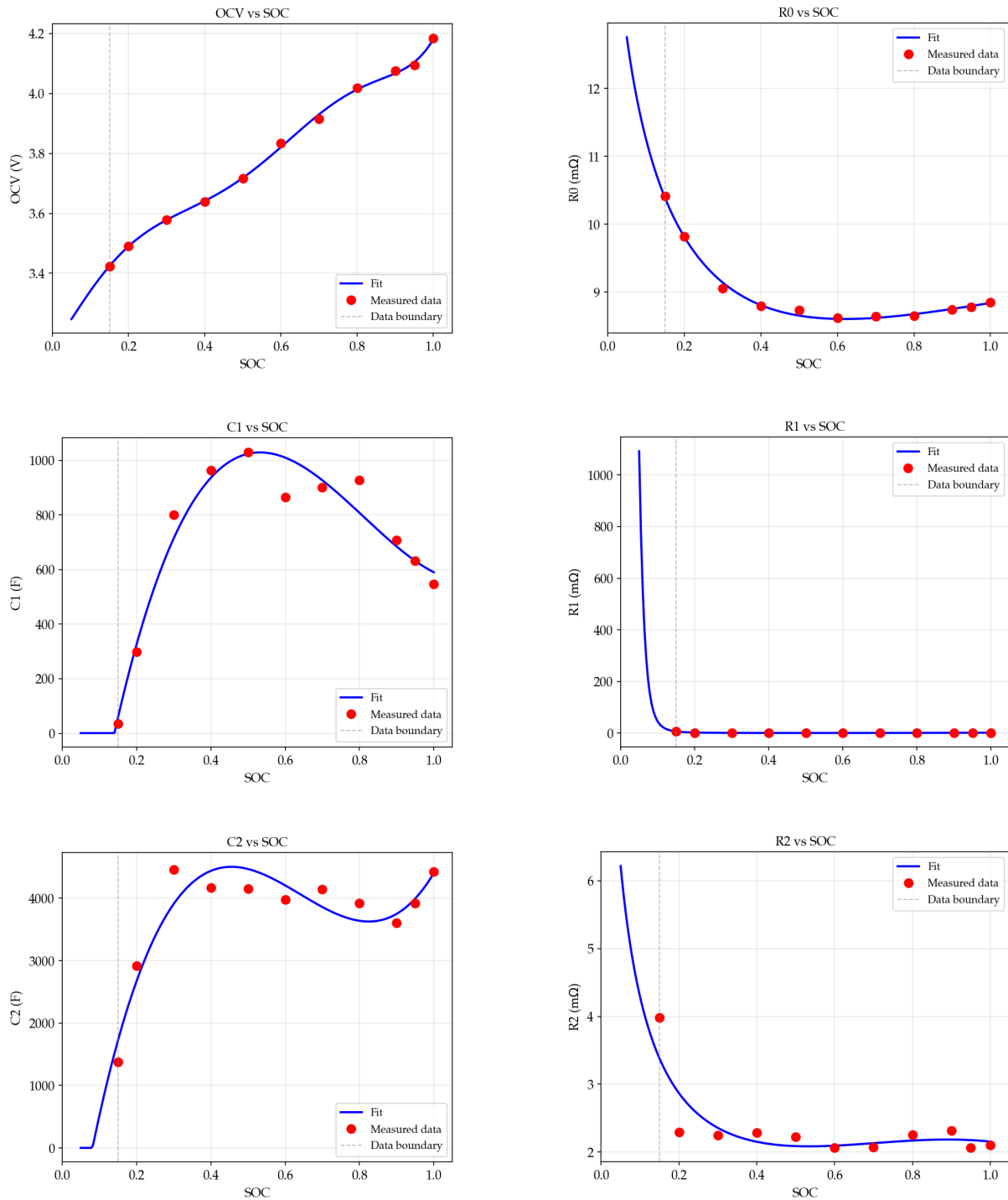


Figure 1: Fitting results of the parameter estimation process.

6-degree polynomial is used to fit the OCV-SOC curve, cubic functions are used to fit the  $C_1$ ,  $C_2$ , and double exponential functions  $y = A_1 e^{B_1 x} + A_2 e^{B_2 x} + C$  are used to fit the  $R_0$ ,  $R_1$ ,  $R_2$  curves.

As the fitting result shows, the Ohm resistance  $R_0$  increases significantly when SoC is low, which may be the main reason for voltage drop and device shutdown. Later we will verify this conclusion. Polarization resistances  $R_1$ ,  $R_2$  also increase when SoC

is low, indicating the battery's internal electrochemical processes are hindered. And Polarization capacitances  $C_1, C_2$  decrease when SoC is low, meaning that the battery's ability to respond to load changes is weakened.

Noticed that  $C_1, C_2$  drop to zero when SoC is low, which means the Thevenin model is not valid in that region. However, the smartphone will actually shutdown before the battery reaches such low SoC, because the output voltage will be too low to power the device.

## 1.4 Simulations

With proper model parameters, we can do numerical simulations of the battery behavior under different load profiles. 2 simplified load profiles are considered here:

- Constant current;
- Constant power.

### 1.4.1 Constant current

Since the current is constant, equation (4) can be directly integrated to get the SoC at time  $t$ :

$$SoC(t) = SoC(0) - \frac{It}{Q_{max}} \quad (10)$$

Then perform Rk45 algorithm to the polarization voltages  $U_1, U_2$  with initial conditions  $U_1(0) = U_2(0) = 0$ , we can get the final result as follows.

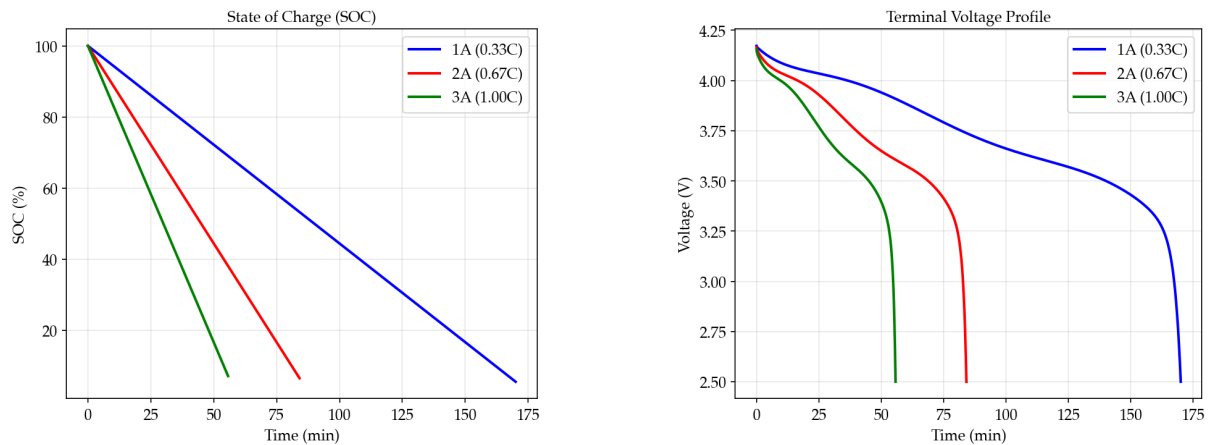


Figure 2: Simulation results under constant current load profile

It can be seen that although the SoC decreases linearly under constant current load, the terminal voltage decreases steadily at first, then suddenly drops to a "dead" value, which makes the device shutdown. The phenomenon is consistent with our daily experience.

### 1.4.2 Constant power

The output power

$$P = U_t I \quad (11)$$

is constant. In this case, analytic solutions are impossible, so we just use the Rk45 algorithm:

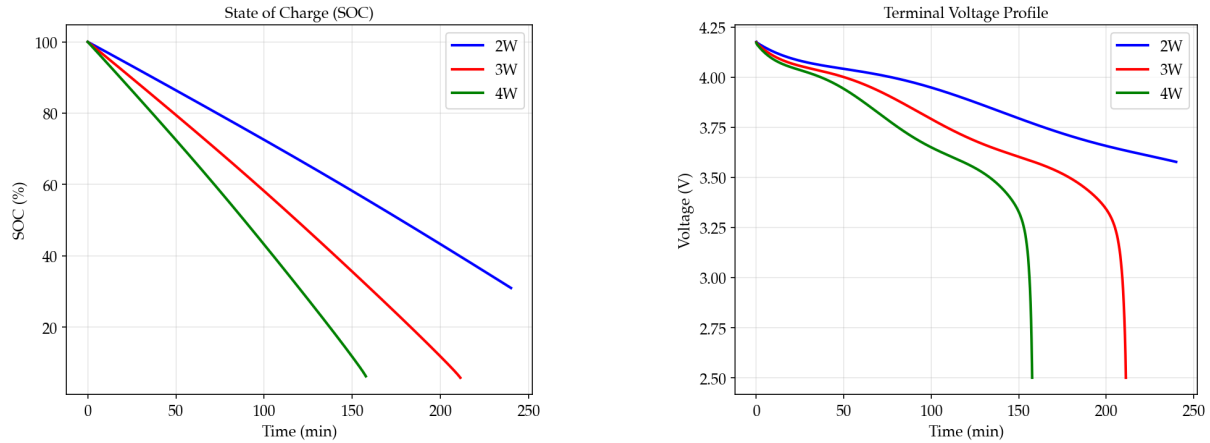


Figure 3: Simulation results under constant power load profile

Similar phenomena can be observed under constant power load profile. However, the terminal voltage drops more rapidly compared to the constant current case, indicating that constant power loads are more stressful to the battery.

## 2 Actual Battery

### 2.1 Assumptions

An actual battery is much more complex than the idealized model presented in the previous section. In this section, we will consider more factors that affect the performance and behavior of real batteries:

- **Temperature:** The performance of a battery can vary significantly with temperature. At low temperatures, the internal resistance increases, leading to reduced capacity and power output. Conversely, high temperatures can enhance performance but may also accelerate degradation.
- **Complex Power Profile:** Real batteries often experience varying power demands, which can affect their efficiency and lifespan. High performance demands can lead to increased heat generation, which in turn affects battery temperature.
- **Shutdown Voltage:** Electronics need a minimum voltage to operate correctly. If the battery voltage drops (steadily or suddenly) below this threshold, the device will shutdown even if SoC is not zero. In this section, we'll assume that if the battery voltage drops below 3.2V, the device will shutdown immediately.

## 2.2 Temperature Behavior of Battery

Actual battery behavior is significantly influenced by temperature variations. The most common parameter affected by temperature is the internal resistance. Using the Arrhenius' equation, we can model the temperature dependence of internal resistance as follows:

$$R = R_0 \cdot e^{\frac{E_a}{R_u T}} \quad (12)$$

where  $R_0$  is a reference resistance,  $E_a$  is the activation energy,  $R_u$  is the universal gas constant and  $T_0$  is a reference temperature.

To conduct the regression, rewrite the equation in linear form by taking the natural logarithm:

$$\ln R = \frac{E_a}{R_u} \cdot \frac{1}{T} + \ln R_0 \quad (13)$$

The Samsung INR21700 30T 3Ah Li-ion Battery Dataset contains experimental data at various temperatures. Using this dataset again, we perform a linear regression, yielding the following results:

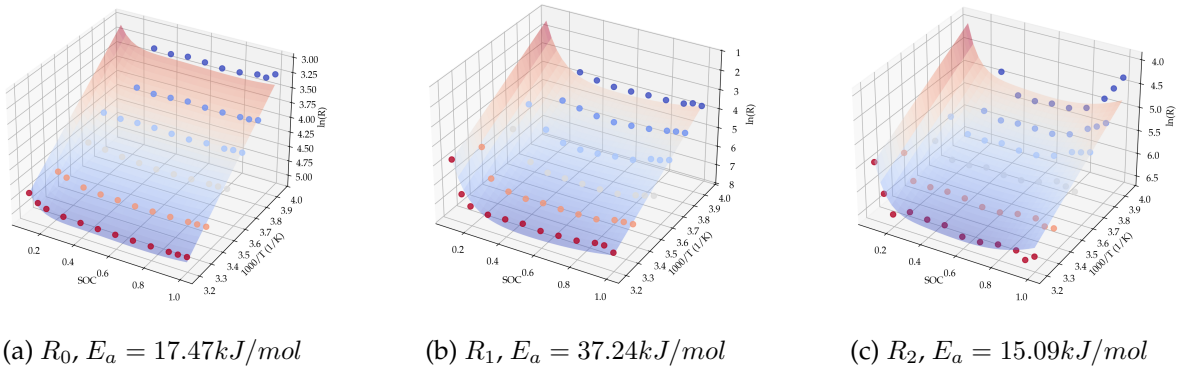


Figure 4: 3D Surface Fitting of Resistance with Temperature and SoC

If we consider the temperature effect, the simulation heatmap of discharge time from 100% SoC under different power load and temperature will be as follows:



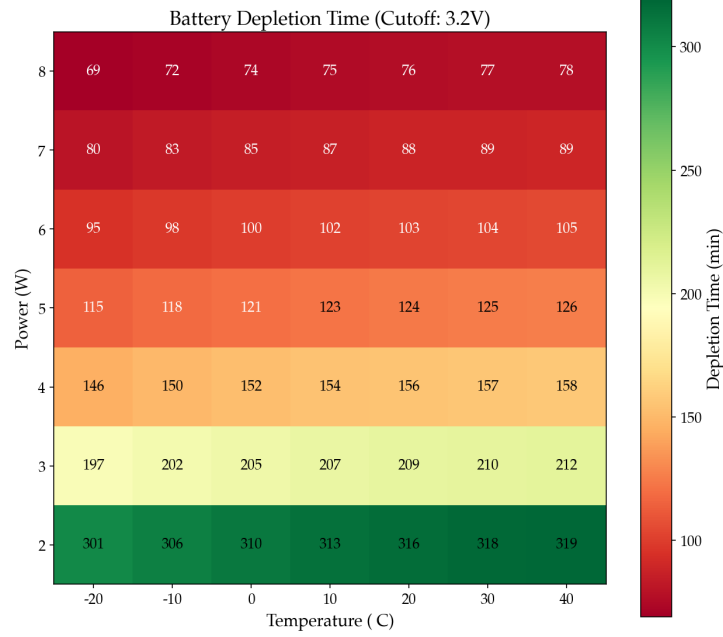


Figure 5: Heatmap of Discharge Time with Power Load and Temperature

It can be observed that battery behaves badly at low temperatures, and the discharge time decreases significantly as temperature drops. However, although high temperature improves battery short-term performance, it also accelerates battery degradation over time. Therefore, in practical applications, maintaining an optimal temperature range is crucial for battery longevity and performance.

### 2.3 Battery in Different Work Loads

A smartphone is a complex embedded system whose total power consumption can be decomposed into the sum of contributions from its independent subsystems. According to the **Principle of Power Superposition**, when individual modules share a power supply but operate relatively independently, the total power draw can be expressed as a linear superposition of the power consumption of each module.

Based on a functional module breakdown, we decompose the smartphone's power consumption into the following six primary sources:

- **Display Screen:** Backlight/OLED driver
- **CPU Computation:** Processor dynamic power
- **Network Communication:** WiFi/Cellular radio frequency (RF)
- **Location Service:** GPS reception and computation
- **Audio Playback:** Codec and speaker driver
- **System Mode:** Adjustment effects from power-saving/flight modes

Overall, the model can be written as:

$$P_{total} = P_{screen} + P_{CPU} + P_{network} + P_{GPS} + P_{audio} + P_{mode} \quad (14)$$

By utilizing acquired smartphone state data, we estimate the parameters within these models, thereby obtaining a comprehensive power consumption model for complex usage scenarios.

### 2.3.1 Screen Power $P_{screen}$

When the screen is on, it exhibits a base power draw plus a near-linear OLED power component (the modeling here assumes an OLED display):

$$P_{screen} = \alpha_S \cdot S + \alpha_B \cdot S \cdot \frac{B}{255} \quad (15)$$

where  $S$  is a screen state indicator and  $B$  is the brightness level (0–255).

### 2.3.2 CPU Power $P_{CPU}$

CPU power is the largest variable power source in a smartphone. According to the dynamic power formula for CMOS circuits:

$$P_{dynamic} = C \cdot V^2 \cdot f \quad (16)$$

where  $C$  is the load capacitance,  $V$  the operating voltage, and  $f$  the clock frequency.

Modern processors employ **Dynamic Voltage and Frequency Scaling (DVFS)**, introducing a coupling between voltage and frequency. Empirical studies suggest:

$$V \propto f^{0.5} \Rightarrow P \propto f^{2.5} \quad (17)$$

Furthermore, modern ARM processors commonly adopt a **big.LITTLE heterogeneous architecture**, featuring separate big and small cores with distinct performance and power characteristics. Additionally, actual CPU power depends on its utilization; idle and fully loaded states at the same frequency exhibit significantly different power draws. Thus, we derive the following CPU power model:

$$P_{CPU} = \alpha_U \cdot U + \alpha_{big} \cdot \left( \frac{f_{big}}{f_{max,big}} \right)^{2.5} + \alpha_{small} \cdot \left( \frac{f_{small}}{f_{max,small}} \right)^{2.5} \quad (18)$$

where  $U$  represents CPU utilization, and  $f_{big}$ ,  $f_{small}$  are the operating frequencies of the big and small cores, normalized to their respective maximum frequencies.

### 2.3.3 Network Power $P_{network}$

Power consumption in wireless communication stems primarily from the Radio Frequency (RF) front-end, especially the Power Amplifier (PA). According to the Friis transmission equation, received power is inversely proportional to the square of the distance:

$$P_r = P_t \cdot G_t \cdot G_r \cdot \left( \frac{\lambda}{4\pi d} \right)^2 \quad (19)$$

Consequently, to maintain communication quality over distances up to several kilometers for cellular networks, relatively high transmit power is required (typically 200 ~ 500mW). In contrast, WiFi communication with a router within tens of meters uses lower transmit power (typically 50 ~ 100mW). Moreover, PA efficiency is typically only 30 ~ 40%, with substantial energy converted to heat, making network power a significant contributor to total consumption.

Since WiFi and cellular networks are typically used exclusively in practice, our model uses a single indicator variable for network type:

$$P_{network} = \alpha_M \cdot M \quad (20)$$

where  $M$  indicates active network type.

#### 2.3.4 GPS Power $P_{GPS}$

The GPS module continuously receives weak signals from multiple satellites and performs complex signal demodulation and position calculation. Its power draw is relatively stable and depends mainly on whether it is active. We adopt a discrete model:

$$P_{GPS} = \alpha_G \cdot G \quad (21)$$

where  $G$  is a binary indicator for GPS activity.

#### 2.3.5 Audio Power $P_{audio}$

The audio module primarily involves compression/decompression processing via an audio DSP, digital-to-analog conversion (DAC), and driving speakers or headphones. We simplify the modeling to a binary indicator for audio playback activity:

$$P_{audio} = \alpha_A \cdot A \quad (22)$$

#### 2.3.6 System Mode Power Adjustment $P_{mode}$

Modern smartphones offer various system modes for power management, such as Power Saving Mode and Flight Mode. However, most of their energy-saving effects are achieved by altering other parameters (e.g., reducing CPU frequency, limiting network activity), which are already captured by other terms in the model. Therefore,  $P_{mode}$  represents additional energy-saving mechanisms. Power Saving Mode may disable unnecessary sensors, reduce refresh rates, and optimize memory management, while Flight Mode directly powers down RF modules. The model is:

$$P_{mode} = \alpha_E \cdot E + \alpha_F \cdot F \quad (23)$$

where  $E$  and  $F$  are indicators for Power Saving Mode and Flight Mode, respectively. Expectedly,  $\alpha_E \leq 0$  and  $\alpha_F \leq 0$ .

#### 2.3.7 Parameter Estimation and Validation

We performed physically constrained regression using the L-BFGS-B optimizer on normalized and binarized data, enforcing non-negative coefficients for power components and non-positive coefficients for power-saving modes. Substituting the estimated parameters yields the final empirical model:

$$P_{total} = 0.250S + 0.615S \frac{B}{255} + 0.860U + 1.125f_{big}^{2.5} + 0.650f_{small}^{2.5} + 0.696M + 0.040G + 0.397A - 0.068E - 0.028F \quad (24)$$

Subsequently, we can analyze the contribution rate of each parameter and evaluate the model's performance. The following figure illustrates the fitting results and validation:

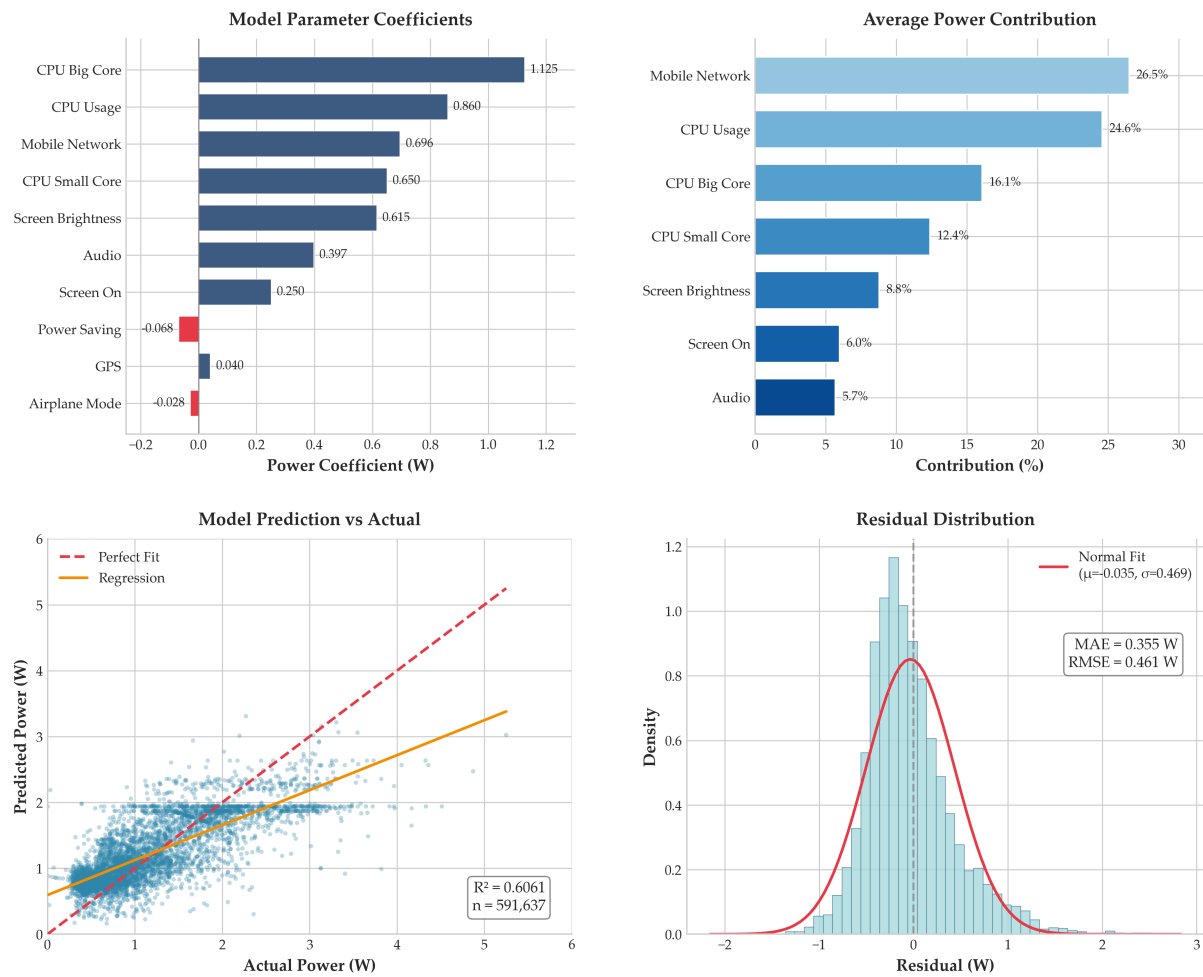


Figure 6: Power consumption model fitting results and validation

Results demonstrate that the white-box power model constructed based on the real-world smartphone dataset achieves satisfactory prediction performance, with an  $R^2$  of 0.606, an MAE of 0.355 W, and an RMSE of 0.461 W. Among the factors analyzed, CPU usage and data network activity exhibit the most significant impact on power draw, whereas GPS consumption and the energy-saving effects of the two included modes show relatively minor influence. As mentioned above, the energy-saving effects of these two modes in practice primarily stem from their influence on the aforementioned features; the small coefficients here reflect that their impact on factors beyond those already captured is relatively minor.

### 2.3.8 Usage Scenario Simulation

The model allows us to estimate the smartphone's power consumption under various typical usage scenarios. Here are some typical scenarios and their estimated power consumption:

Scenario	Screen (S)	Brightness (B/255)	CPU Usage	Big Core Freq	Small Core Freq	Mobile Network	GPS	Audio	Total Power (W)
Standby	Off	0%	10%	10%	10%	No	Off	Off	0.09
Web Browsing	On	50%	50%	30%	30%	No	Off	Off	1.08
Video Streaming	On	71%	40%	40%	30%	No	Off	On	1.57
Navigation	On	100%	50%	50%	40%	Yes	On	On	2.69
Gaming	On	100%	90%	100%	100%	Yes	Off	On	4.51

Table 1: Power Consumption Under Different Usage Scenarios

## 2.4 Heat Transfer Model in High-Performance Scenarios

In this chapter, we discuss how the heat that battery generates affects the temperature of battery itself, and in turn impacts its own performance.

Let  $Q$  be the internal heat power,  $h$  be the convective heat transfer coefficient,  $A$  be the surface area of the battery (assumed to be the area of the smartphone),  $C$  be the heat capacity of the battery,  $T$  be the battery temperature and  $T_{env}$  be the environmental temperature (assumed constant). With Newton's law of cooling, we have:

$$Q = 2Ah(T - T_{env}) + C \frac{dT}{dt} \quad (25)$$

$Q$  can be divided to:

$$Q = Q_{battery} + Q_{processor} + Q_{other} \quad (26)$$

$Q_{battery}$  can be further expressed with the Joule's law:

$$Q_{battery} = I^2 R_{inter} = I^2 (R_0 + R_1 + R_2) \quad (27)$$

$Q_{processor}$  often is the major part of heat generation, because processors are often energy-intensive and almost all consumed energy is converted to heat. Here we model  $Q_{processor}$  as a part of total power consumption of the device:

$$Q_{processor} = \eta P_{total} \quad (28)$$

in which  $\eta$  is some coefficient.

And the other components' heat generation  $Q_{other}$  can be assumed to be a constant for simplicity.

Considering that  $I$  and  $R$  is time-dependent, equation (25) is a first-order linear ODE. The solution is:

$$T = T_{env} + \frac{1}{C} \int_0^t e^{-\frac{2Ah(t-s)}{C}} Q(s) ds \quad (29)$$

Substitute equation (29) into the Arrhenius' equation, we can get the relation between internal resistance and time, and thus analyze how temperature affects battery performance over time in high-performance scenarios.

The simulation here shows the heatmap of discharge time and max temperature under different power load and environmental temperature. It assumes if the battery

temperature exceeds  $50^{\circ}\text{C}$ , the device will shutdown to protect the battery. In reality, smartphones often decrease processor frequency to reduce heat generation when temperature is too high, but for simplicity we assume an immediate shutdown here.

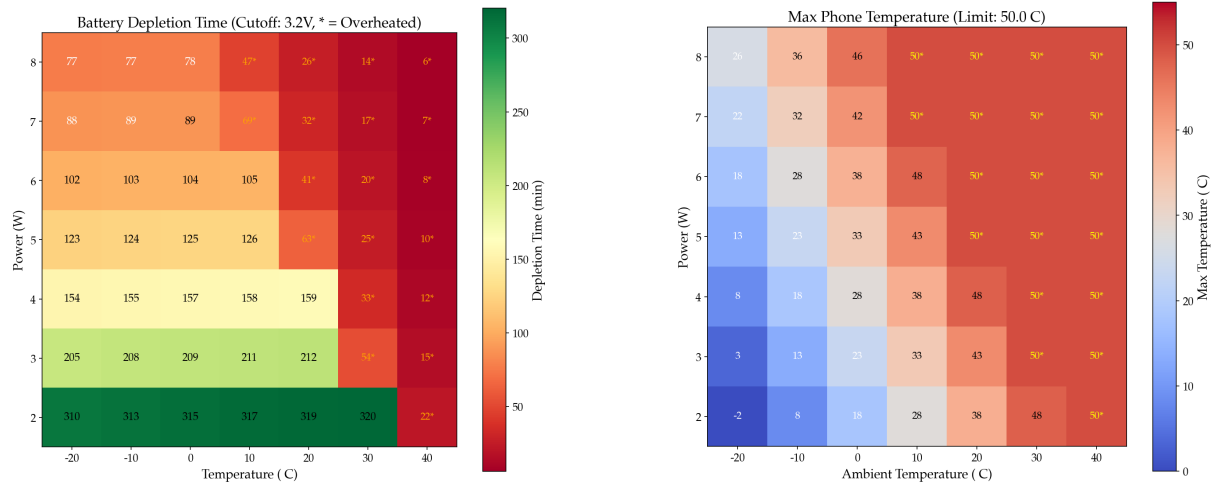


Figure 7: Heatmap of Discharge Time and Max Temperature

In the simulation we set  $C = 160\text{J/K}$ ,  $A = 200\text{cm}^2$ ,  $h = 5\text{W}/(\text{m}^2 \cdot \text{K})$ ,  $\eta = 0.5$  and  $Q_{\text{other}} = 0.8\text{W}$ .

It can be observed that high temperature scenarios are quite dangerous for battery operation. Heavy work loads in  $30^{\circ}\text{C}$  or higher can easily lead to battery overheating.

## A Notation

### A.1 Battery Parameters

Parameter	Symbol	Physical Meaning	Unit
Internal Resistance	$R$	Total internal resistance of battery	$\Omega$
Ohmic Resistance	$R_0$	Ionic and electronic resistance	$\Omega$
Polarization Resistance 1	$R_1$	Charge transfer resistance	$\Omega$
Polarization Resistance 2	$R_2$	Concentration polarization	$\Omega$
Activation Energy	$E_a$	Energy barrier for charge transfer	kJ/mol
Universal Gas Constant	$R_u$	Physical constant in Arrhenius equation	8.314 J/(mol·K)
Battery Temperature	$T$	Real-time battery temperature	K
Environmental Temperature	$T_{env}$	Ambient temperature (constant)	K
State of Charge	SoC	Battery capacity percentage	0–100%
Discharge Current	$I$	Current flowing out during discharge	A
Battery Voltage	$V$	Voltage output by battery	V
Battery Capacity	$C_{cap}$	Total energy capacity	Ah

### A.2 Power Consumption Parameters

#### A.2.1 Total Power Model

Parameter	Symbol	Physical Meaning	Unit
Total Power	$P_{total}$	Sum of all power components	W

### A.2.2 Screen Power

Parameter	Symbol	Physical Meaning	Range/Unit
Screen Power	$P_{screen}$	Power consumption of display system	W
Screen State	$S$	On/off indicator (0: off, 1: on)	0, 1
Brightness Level	$B$	Display brightness value	0–255
Base Coeff.	$\alpha_S$	Base power when screen on	W
Brightness Coeff.	$\alpha_B$	Additional power per brightness unit	W

### A.2.3 CPU Power

Parameter	Symbol	Physical Meaning	Range/Unit
CPU Power	$P_{CPU}$	Power consumption of CPU	W
CPU Utilization	$U$	Fraction of time CPU is active	0–1
Big Core Frequency	$f_{big}$	Frequency of high-performance cores	GHz
Small Core Frequency	$f_{small}$	Frequency of efficiency cores	GHz
Max Big Core Freq.	$f_{max,big}$	Maximum frequency of big cores	GHz
Max Small Core Freq.	$f_{max,small}$	Maximum frequency of small cores	GHz
Utilization Coeff.	$\alpha_U$	Power per unit utilization	W
Big Core Coeff.	$\alpha_{big}$	Power consumption at max frequency	W
Small Core Coeff.	$\alpha_{small}$	Power consumption at max frequency	W

### A.2.4 Network Power

Parameter	Symbol	Physical Meaning	Range/Unit
Network Power	$P_{network}$	Wireless communication power	W
Network Type	$M$	Type (0: WiFi, 1: Cellular)	0, 1
Mobile Network Coeff.	$\alpha_M$	Cellular power vs WiFi	W



### A.2.5 GPS Power

Parameter	Symbol	Physical Meaning	Range/Unit
GPS Power	$P_{GPS}$	GPS receiver power	W
GPS Activity	$G$	On/off indicator (0: off, 1: on)	0, 1
GPS Power Co-eff.	$\alpha_G$	GPS active power	W

### A.2.6 Audio Power

Parameter	Symbol	Physical Meaning	Range/Unit
Audio Power	$P_{audio}$	Audio playback power	W
Audio Playback	$A$	Active indicator (0: no, 1: yes)	0, 1
Audio Power Coeff.	$\alpha_A$	Audio playback power	W

### A.2.7 System Mode Power Adjustment

Parameter	Symbol	Physical Meaning	Range/Unit
Mode Adjustment	$P_{mode}$	Power adjustment from system modes	W
Power Saving Mode	$E$	On/off indicator (0: off, 1: on)	0, 1
Flight Mode	$F$	On/off indicator (0: off, 1: on)	0, 1
Power Saving Coeff.	$\alpha_E$	Power reduction from power saving	W
Flight Mode Co-eff.	$\alpha_F$	Power reduction from flight mode	W

Note: The coefficients  $\alpha_S, \alpha_B, \alpha_U, \alpha_{big}, \alpha_{small}, \alpha_M, \alpha_G, \alpha_A$  are positive (power increase), while  $\alpha_E, \alpha_F$  are negative (power reduction).

### A.3 Thermal Parameters

Parameter	Symbol	Physical Meaning	Unit
Internal Heat Power	$Q$	Total heat generation rate	W
Battery Heat	$Q_{battery}$	Joule heat from internal resistance	W
Processor Heat	$Q_{processor}$	Heat from CPU and circuits	W
Other Heat	$Q_{other}$	Heat from other modules	W
Heat Transfer Coeff.	$h$	Convective heat transfer coefficient	W/(m <sup>2</sup> ·K)
Surface Area	$A$	Heat dissipation area	m <sup>2</sup>
Heat Capacity	$C$	Thermal mass of battery	J/K
Heat Efficiency	$\eta$	Fraction of power to heat	Dimensionless

### A.4 Time and Derived Quantities

Parameter	Symbol	Physical Meaning	Unit
Time	$t$	Elapsed time from start	s
Discharge Time	$t_{discharge}$	Time to shutdown voltage	h
Maximum Temperature	$T_{max}$	Peak temperature during discharge	K

Typical Values (Samsung INR21700 30T 3Ah Li-ion Battery):

- Heat capacity:  $C = 160$  J/K
- Convective heat transfer coefficient:  $h = 5$  W/(m<sup>2</sup>·K)
- Smartphone surface area:  $A = 200$  cm<sup>2</sup>
- Processor heat fraction:  $\eta = 0.5$
- Other heat generation:  $Q_{other} = 0.8$  W
- Shutdown voltage:  $V_{min} = 3.2$  V (device stops regardless of SoC)
- Thermal shutdown temperature:  $T_{max} = 50$  C (protection limit)

## B Use of AI

This section documents authentic interactions between the team and AI assistant (GitHub Copilot) during the development of this paper. These examples demonstrate responsible AI usage focused on **data analysis**, **result interpretation**, and **document formatting**, while all core modeling work was completed independently by the team.

### B.1 Battery Dataset Selection

#### Question: Using 18650 Data for Smartphone Modeling

We found some 18650 cylindrical cell datasets with complete HPPC test data. Can we use 18650 data directly for smartphone battery modeling?

#### AI Response

Using 18650 data directly for smartphone modeling is not ideal due to several differences:

- **Form Factor:** 18650 is cylindrical with rigid metal casing, while smartphone batteries are flat pouch cells
- **Internal Resistance:** 18650 cells typically have higher resistance due to smaller electrode surface area
- **Thermal Characteristics:** Metal-cased 18650 cells have better heat dissipation; pouch cells are more thermally sensitive
- **Chemistry:** 18650 often uses NCA/NMC, while smartphones typically use  $\text{LiCoO}_2$

These differences would introduce systematic errors. I recommend searching for smartphone-specific battery test data if available.

**Team's Contribution:** Following this advice, we searched for smartphone-specific datasets and found the Samsung INR21700 30T battery dataset, which includes complete HPPC characterization at multiple temperatures (0°C, 23°C, 45°C). We selected this dataset for our parameter identification.

### B.2 Dataset Overview and Statistics

#### Question: Analyzing Dataset Structure

I have a large smartphone usage dataset. Can you help me analyze the overall data distribution and summarize what features are available?

#### AI Response

Based on your dataset structure, here's an overview:

- **Total records:** 3.24 million discharge data points
- **Target device:** Device ID ab47b5f5ecdcd6b8 (largest data volume)
- **After filtering:** 2.96 million valid points (excluding battery > 95%)

- **Sampling result:** 591,637 observations for regression

Key features available: screen state and brightness, CPU utilization and core frequencies, network connection status, GPS/Bluetooth/audio states, and power-saving mode indicators.

**Team's Contribution:** We designed the complete data processing pipeline, defined filtering criteria based on domain knowledge (excluding high battery levels to avoid trickle charging artifacts), and implemented the feature engineering logic.

### B.3 Coefficient Reasonableness Analysis

#### Question: Validating Model Coefficients

My regression model produced these coefficients: Screen On (0.250W), Big Core (1.125W), Small Core (0.650W), Mobile Network (0.696W), GPS (0.040W), Power Saving (-0.068W). Can you help analyze whether they are physically reasonable?

#### AI Response

These coefficients appear physically reasonable:

1. **Big Core > Small Core:** Consistent with big.LITTLE architecture where performance cores consume more power than efficiency cores.
2. **Mobile Network is significant:** Cellular RF transmission requires higher power than WiFi due to longer communication distances.
3. **GPS is small:** GPS is primarily a receiver with low power consumption.
4. **Power-saving modes are negative:** The small magnitudes suggest most savings come from reducing other parameters already captured in the model.

**Team's Contribution:** We derived the model structure from first principles (power superposition, CMOS dynamic power formula, DVFS scaling law). AI assisted in reviewing whether the estimated coefficients align with expected physical behavior.

### B.4 Data Sampling Strategy

#### Question: Efficient Sampling for Large Datasets

I have 3 million data points but need to reduce computational cost. What sampling approach would preserve data quality?

#### AI Response

For time-series data, use systematic sampling (jump sampling) rather than random sampling:

```
df_sorted = df.sort_values('timestamp')
sample = df_sorted.iloc[::5] # Every 5th point
```

This preserves temporal distribution and maintains representation of different usage patterns.

**Team's Contribution:** We determined the 1:5 sampling ratio based on computational constraints and validated that model coefficients remain stable across different sampling ratios.

## B.5 LaTeX Equation Formatting

### Question: Breaking Long Equations

My power model equation is too long and overflows the page margin. How do I split it across lines?

### AI Response

Use the aligned environment inside equation:

```
\boxed{\begin{aligned}
P_{\text{total}} &= 0.250S + 0.615S\frac{B}{255} + \dots \\
&\quad + 0.696M + 0.040G + \dots
\end{aligned}}
```

**Team's Contribution:** The model equation and all physical terms were derived by the team. AI assisted only with LaTeX syntax.

## B.6 LaTeX Table Column Width Adjustment

### Question: Uniform Table Column Widths

My notation table has inconsistent column widths, and the table is too narrow compared to the page width. How can I make all columns have uniform width and expand the table to fill the text width?

### AI Response

Use the tabularx package with equal-width columns:

```
\usepackage{tabularx}
\newcolumntype{Y}{>\centering\arraybackslash}

\begin{tabularx}{\textwidth}{|Y|Y|Y|}
\hline
\textbf{Symbol} & \textbf{Description} & \textbf{Unit} \\
\hline
 $R_0$  & Ohmic resistance &  $\Omega$ 
```

```
...
\end{tabularx}
```

The x column type automatically distributes remaining width equally. Using `\textwidth` ensures the table spans the full page width.

**Team’s Contribution:** We created all table content and symbol definitions. AI assisted with LaTeX table formatting syntax.

B.7 Summary of AI Usage

Category	AI Assistance	Team Responsibility
Core Modeling	—	Thevenin model, Arrhenius, DVFS
Data Selection	Advised against 18650	Found Samsung dataset
Data Analysis	Dataset statistics	Filtering, feature engineering
Result Interpretation	Coefficient review	Model fitting, validation
Documentation	LaTeX table/equation formatting	All technical writing

Table 2: Division of work between AI assistance and team contribution

B.8 Declaration

All theoretical frameworks in this paper—including the second-order RC equivalent circuit model, Arrhenius temperature dependence, CMOS dynamic power formula ( $P \propto f^{2.5}$ ), Friis transmission equation for RF power, and Newton’s law of cooling for thermal modeling—were **independently researched, derived, and implemented by the team members**. AI tools were used for comparing battery types, understanding dataset structure, reviewing coefficient reasonableness, and LaTeX formatting—reflecting responsible AI assistance for productivity enhancement without replacing human judgment in scientific analysis.