Engine Design Document for the AI Agent of Crossy Road

Yushan Weng Shuwei Zhang Veeraya Sawangsinudomchai yweng@usc.edu shuweiz@usc.edu sawangsi@usc.edu

Wei Sun Junzhe Liu Yilin Zhang wsun9780@usc.edu junzhel@usc.edu yzhang54@usc.edu

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1 Background and Overview

Crossy Road is an arcade video game released on 20 November 2014, developed and published by Hipster Whale. The game has been described as "endless Frogger". The objective of Crossy Road is to cross an endless highway or series of roads and avoid obstacles as far as possible without dying. The game we chose is a simplified browser version of the original Crossy Road, where the obstacles are restricted to two types: the static tree that can block the movement, and the moving cars on the road that potentially can terminate the character.

The intuition of our neural network model is to train an agent that can play a simplified version of *Crossy Road* game like a human being, even outperform than human. Because our model will train an agent to identify the incoming obstacles in the game, and make a decisions based on previous experiences to gain as much reward as it can, the ideal candidates for neural network architectures for our model are convolution network for computing vision, and reinforcement learning for reward functions.

2 Goals

We learned that the current world record for the *Crossy Road* developed by the Hipster Whale is **4,195**. Therefore, our expected our model at least get **1,000** to **2,000** score in the simplified version of *Crossy Road*, and even better to get closer to the world record as possible. The expected result gives a detailed expectation for our model. First, we want the information captured by our convolution neural networks model to be as more accurate as possible. Second, we want the our reinforcement neural network can teach our agent to understand the game as good as a human being.

3 Milestones

Week 2	Proposed Project
Week 3	Compared several approaches to set up the architecture of the project
Week 4	Completed the framework for game agent
Week 5	Set up a CNN for processing game image and collecting data
	Researched about how to combine RL and CNN
Week 6 - Week 8	Built the model and started to tuning parameters

4 Existing Solution

So far, we have built a neural network model that are composed by three parts: computer vision, reinforcement learning, and automating the game playing.

4.1 Game Modification

We notice that the existing version of the web version fo the game could not satisfy some of the needs of our model.

4.1.1 Pause/Resume Feature

Specifically, the existing version does not support resume/pause function. Without the resume/pause it can take considerable amount of time for our model to predict the next action for the agent, and the game state will change and be different from the state fed to the model.

However, the ThreeJS framework does not have the built-in function to pause or resume the animate process. We take a bypass solution. Firstly, we create a global boolean variable to check if the game is pause. Secondly, we add an event listener to check if the user hit the "P" key in the keyboard, which is designed to pause or resume the game.

```
1 // Declare a global boolean variable to record if the game is paused.
2 let paused = false;
  // Event listener
  window.addEventListener("keydown", event => {
    if ((event.keyCode == '38') && (!gameOver) && (!paused)) {
      move('forward');
    if ((event.keyCode == '40') && (!gameOver) && (!paused)) {
      move('backward');
9
    } else if ((event.keyCode == '37') && (!gameOver) && (!paused)) {
      move('left');
11
    } else if ((event.keyCode == '39') && (!gameOver) && (!paused)) {
      move('right');
    } else if ((event.keyCode == '13') && (!gameOver)) {
14
      // Change the state of the game between pause and resume
15
      paused = !paused;
16
    }
17
18 });
```

Next, we need to modify the customized the animate function. There are three parts: animate game scene according to the frame rate per second, execute the action from the agent, and do the hit test. To implement the pause/resume feature, we just let animate function to check the global paused variable, and do not execute the first two animate action.

```
lanes.forEach(lane => {
          if ((lane.type === 'car' || lane.type === 'truck') && (!paused)) {
             const aBitBeforeTheBeginingOfLane = -boardWidth * zoom / 2 - positionWidth * 2 * zoom;
             const aBitAfterTheEndOFLane = boardWidth * zoom / 2 + positionWidth * 2 * zoom;
            lane.vechicles.forEach(vechicle => {
               if (lane.direction) {
6
                 vechicle.position.x = vechicle.position.x < aBitBeforeTheBeginingOfLane ?</pre>
      aBitAfterTheEndOFLane : vechicle.position.x -= lane.speed / 16 * delta;
                vechicle.position.x = vechicle.position.x > aBitAfterTheEndOFLane ?
      aBitBeforeTheBeginingOfLane : vechicle.position.x += lane.speed / 16 * delta;
              }
11
            });
          }
        });
```

4.1.2 Passing Image through RAM

Unfortunately, the Selenium API is not capable to directly access the image rendered on the canvas component. The conventional method to solve this issue is to let the Selenium to pass a javascript script that will encode the image to a string based on encode 64 to the browser, then the Selenium API will receive the encoded string and convert it back to image. However, ThreeJS rendered the scene on a nested canvas, and the conventional does not work with it. Therefore, we added a div in the website, and let animate function encodes the finalized rendered canvas to a string, and update the created div based on the string.

```
imgU.innerText = renderer.domElement.toDataURL().substring(22);
```

The drawback of this approach is obvious. The work load of the front end is aggravated, which will take a significant computational power and lower the efficiency of our model.

4.2 Game Automation: Selenium API

As we known, all the neural networks have to work on given input and will give output in number format. Therefore, we need to build a bridge between the game and neural networks that can pass the game as an input to game and operate game based on the output from neural networks. Because the game we work on is based on browser, we can take a advantage of Selenium API in python to implement this bridge.

4.2.1 Setup Selenium API

We work with Chrome browser because it has a complete console for debugging. Another thing we need to connect python and Chrome is a chromedriver. Then the setup process is as simple as below codes, where the driver is everything we need to operate Chrome through python.

```
driver = webdriver.Chrome()
```

We mainly use the *driver* object to implement following operations:

• Because we have created a div element in the web page to receive the encoded canvas image, we can simply access the content of that element by the selenium, and convert it back to an image by the base64 and PIL.Image packages. Finally, we converted to a np array, which is the format that can be understand by the CNN.

```
img_64 = self.game.driver.find_element_by_id('imgURL').text
screen = np.array(Image.open(BytesIO(base64.b64decode(img_64))))
3
```

• Move the character in the game based on the output from model

```
driver.find_element_by_id("[next movement direction]").send_keys(Keys.[Direction])
```

• Get the score achieved by the model

```
return driver.find_element_by_id('counter').text
```

• Get if the game is over

```
return driver.find_element_by_id('retry').is_displayed()
```

• Restart the game for timeless training

```
WebDriverWait(self._driver, 5).until(EC.element_to_be_clickable((By.ID, "retry"))).click()
# If the game is over, wait 5 seconds until the "retry" button shown up and available to be clicked
```

• Shut down the game and the connection between Chrome and Python

```
1 driver.close()
2
```

4.3 Computer Vision: CNN

In order to let the agent understand the game, we need to give our agent a pair of "eyes" to see the game, which is the computer vision part. This part is built on the convolution neural network architecture. In our implementation, we mainly used *OpenCV* for image processing, and *Sequential* models from *keras* for building the CNN.

4.3.1 Image Preprocessing

With the captured image from the game, which represent the current state of the game, we need to process it to a number form that be understand by our model. There are two requirements: 1. the image contains all necessary environmental information that influences the agent's next-step action decision, 2. the state should be as simple as possible to reduce computational complexity.

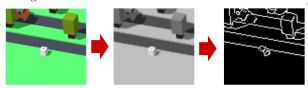
Previously, we set the size of the image to 1200×600 pixels, which is so large that contains too much unnecessary information. After several approaches, we finally decided to chop the image to 80×80 pixels, which contains enough information representing the surrounding environment. This part is done by following code.

```
image = image[200:400, 650:850]
image = cv.resize(image, (80, 80))
```

Next, we observed that the color of the captured image is form (\mathbf{R} , \mathbf{G} , \mathbf{B} , \mathbf{a}). Since the color does not help too much for edge detection, we transformed the image into grey mode. Moreover, we took the advantage of the edge detection in the OpenCV to reduce the state space. The experimental result indicated that, compared to grayscale images, images with edge detection can reduce training time by 40%. The picture below visualizes this process.

This process is done by following code.

Figure 1: Visualization of color transformation



```
image = cv.cvtColor(input_shot, cv.COLOR_BGR2GRAY)
image = cv.Canny(image, threshold1=100, threshold2=200)
```

In conclusion, the whole preprocessing codes looks like below:

```
def processing_image(self):
    input_shot = cv.imread(screen_shot_output)
    image = cv.cvtColor(input_shot, cv.COLOR_RGBA2GRAY)
    image = image[200:400, 650:850]
    image = cv.resize(image, (80, 80))
```

4.3.2 Structure of Our CNN

With the prepared input, now it's time to feed it into our CNN. Also, we have reduce the space of the image, we do not want miss any detail on the image, so we take 4 inputs to feed into CNN. Our CNN includes three convolutional layers and one flatten layer. In the last dense layer, we flatten into four neurons since we are considering only four operations of the game (move forward, move backward, move left, and move right). The output layer gives us the prediction of Q-value for each operation based on the input state. The picture below visualize the structure of our CNN model.

Conv Conv Conv Conv Dense Dense Flatten Conv Conv 2x2x64

Figure 2: The Structure of CNN

The CNN is built by following code:

```
def buildmodel():
    model = Sequential()
    # First layer
    model.add(Conv2D(32, (8, 8), padding='same', strides=(4, 4), input_shape=(img_cols, img_rows, img_channels)))
    model.add(MaxPooling2D(pool_size=(2, 2)))
    model.add(Activation('relu'))
```

```
# Second layer
      model.add(Conv2D(64, (4, 4), strides=(2, 2), padding='same'))
      model.add(MaxPooling2D(pool_size=(2, 2)))
9
10
      model.add(Activation('relu'))
      # Third layer
11
      model.add(Conv2D(64, (3, 3), strides=(1, 1), padding='same'))
12
      model.add(MaxPooling2D(pool_size=(2, 2)))
13
      model.add(Activation('relu'))
14
      # Flatten layer
      model.add(Flatten())
16
17
      # Fully connect
      model.add(Dense(512))
18
      model.add(Activation('relu'))
19
      model.add(Dense(ACTIONS))
20
      adam = Adam(lr=LEARNING_RATE)
21
      model.compile(loss='mse', optimizer=adam)
22
23
      # Save the model file
24
25
      if not os.path.isfile(loss_file_path):
          model.save_weights(model_file_path)
26
      return model
```

4.4 Reinforcement Learning: Reward Functions

Learning about how to play the game is a learning process based on previous experience. Therefore, we decided to implement this process over reinforcement neural networks architecture. Specifically, we set a reward function. In the game, the agent will first observe the surrounding environment, and make a movement based on its observation. Then, the reward function will give a positive feedback if the decision update the score and a punishment if the decision caused gave over.

4.4.1 Combination of CNN and Bellman Equation

Since our project looks at the long sequence of actions that can get the highest score, we need Bellman's equation to determine the long-term rewards. Therefore, to optimize, the Bellman equation can help us to find the optimal policy and value that can give us the better result.

$$V(S) = \max_{\alpha}(R(s, a) + \gamma \sum_{s'} P(s, a, s')V(s'))$$

As we mentioned before, the goal of the DQN is to choose a certain action(a) at state(s) in order to maximize the reward. Here, in our project, we combine the Convolution Neural Network with reinforcement learning techniques. We use CNN and Bellman's Equation to estimate Q-value function required by Q-learning: the Neural Network serves as a non-linear approximator, which is optimized to minimize the difference between output and the target. In the next step, our agent will take the action with maximum Q-value.

The target, also named as Q-value iterative update function, is defined as follow:

$$target_i = \begin{cases} r_i & \textit{if game is terminated} \\ r_i + \gamma max_{a'} Q(s_{i+1}, a', \theta) & \textit{if game is continued} \end{cases}$$
 (1)

where $\max_{a'} Q(s_{i+1}, a', \theta)$ is the maximum Q-value achievable by any algorithm given the current condition(state s and action a), which is the application of generalized Bellman's Equation. γ , the discounted factor, is used to describe the influence of future reward. θ stands for the current policy, which is the current weights of the neural network.

4.4.2 Certain Length Memory

When the agent interacts with the environment, the sequence of experience can be highly correlated. In order to prevent the risk of getting swayed, we applied experience replay in our project. We sampled a minibatch of size of 32 from the replay memory we set up when initialization. Also, we set a fixed length for the memory to refresh the replay space and ensure timeliness.

4.4.3 Observe, Explore, and Train

To have enough data for training, our Deep Q-learning algorithm was designed by two phases: Observation and Train. In the Observation phase, we need to choose an action (a) randomly. Considering the balance between exploitation and exploration, we deployed the Epsilon-greedy strategy to random choose an action a. The agent will take action (a) and observe reward (r) and next state (s). With several experiments, we find that 10,000 is a reasonable steps, in which the agent can gain enough experience without over training. The tuple for the transaction (s, a, r, s', is_dead) was stored in the experience replay memory.

In the training phase, we sample a random minibatch of 32 transitions from the experience replay memory. We enumerate the batch and update the expected state-action values using the Bellman's Equation. The whole Q-network was updated by minimizing the loss with Adaptive Moment Estimation optimizer.

In conclusion, here is a pseudo code demonstrating how the DQN agent is built.

5 Alternative Solution

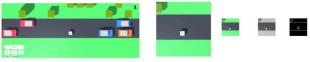
According to the results from the initial implementation, we noticed that there are two potential variables that affect the accuracy of our model: obstacles detection and the design of the reinforcement learning feature. Therefore, we proposed several alternative solutions.

```
\mathbf{1} \text{ train\_round} = 0;
\mathbf{2} memory = Deque();
  while True do Timeless training
      state = game screen capture;
      if train_round \leq 10,000 then
5
         action = random(forward, backward, left, right);
6
7
       action = model.predict(state);
8
      nextMove(action);
9
      new state = game screen capture;
10
      is\_dead = if game is over;
11
      game score = game score;
12
      reward = rewardFunction(action, new state, is dead, game score);
13
      memory.pushRight((state, new state, reward, is dead));
14
      if train round > 10,000 then
15
          mini batch = sample(memory, 32);
16
         Optimize the model by train on mini batch;
17
      train round++;
18
```

5.1 Accuracy of Object Detection of CNN

We realized that the top priority of our model is to detect the obstacles in the game. We observed that the current view of the game is from the top left corner, which has negative impact to our model. Therefore, we decide to lower the difficulty our model and transfer the original view to the top view.

Figure 3: Top view Image Processing



Even if the agent seems to perform better with the lower difficulty, there are several issues occurring in the training process. The first problem is the high variance of Q value, and it makes the bellman equation too weak since the reward is too small from the biggest Q value. It does not make any changes in the reward function. The second challenge is the complexity of the image input. It is not only a 3D game, but also the shadow as well.

To solve the high Q value, we normalize the image input by the code in below.

```
def processing_image():
    img_64 = self.game.driver.find_element_by_id('imgURL').text
    screen = np.array(Image.open(BytesIO(base64.b64decode(img_64))))
    img = cv.cvtColor(screen, cv.COLOR_RGBA2GRAY)
    img = img[100:800, 850:1550]
    img = cv.resize(img, (80, 80))
    img = cv.Canny(img, threshold1=100, threshold2=200)
# Normalize the image input
    img = (img - img.mean()) / (img.std() + 1e-8)
    return img
```

Next, we added the following code in the training process to normalize the Q value.

```
temp_next_state = model.predict(state_t1)
# Normalize q value in list to range between 0 and 1
normal_target_next_state = np.linalg.norm(temp_next_state)
normal_next_array = temp_next_state / normal_target_next_state
Q_sa = normal_next_array
```

According to the result, we restricted the Q value between 0 and 1.

Moreover, although we introduced the edge detection from OpenCV, we noticed that shadow of objects increased the complexity of the input state, like in the figure 4.

Figure 4: Example of the edges of shadow





Since the only thing that we consider is the obstacles in game, which are cars, trucks, and trees, we can reduce the complexity of the game by changing the background color to black, like in figure 5. This solution also solves the shadow problem from the game as well.

Figure 5: Example of game view in black background



As a result after training our agent more than 5000 episodes with the new environment of the game, as in figure 6, the agent seems to not be making any improvement. We notice that the agent cannot avoid the vehicles at all.

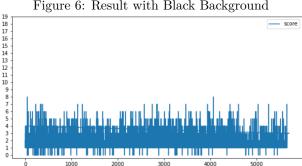


Figure 6: Result with Black Background

New Action 5.2

We noticed that people will hesitate to consider for next movement while they are playing the game. The next attempt is rather than considering only four actions, which are move forward, move left, move right, and move backward, we will consider five actions by adding stay still for our agent. We notice that "STAY" is more important in the game since the agent needs to wait until the vehicle is passed, and the best action based on this scenario is to choose the stay action and wait. Therefore, "STAY" action has been implemented for the next attempt. Below is the mapping value that we use to map the action with the number.

Action	Key
Stay	0
Forward	1
Backward	2
Left	3
Right	4

5.3 New Design of the Model

5.3.1 Prepartion

To construct every new model, this process takes some amount of time to build a new code, so the idea of implementing Stable Baselines comes in. Stable Baselines library is introduced by the openAI team, which consists of the set of improvement implementations on Reinforcement learning in openAI such as DQN, A2C, PPO, etc.

Since Stable baselines is the RL tool on openAI, and openAI will work on the environment that follows the structure on openAI Gym. Therefore, a custom environment has been built by constructing the openAI Gym structure with following code.

```
class ChromeCrossyRoadEnv(gy.Env):
   def __int__(self):
        self.game = CrossyRoadGame()
```

```
n_action = 5

self.action_space = spaces.Discrete(n_actions)

self.observation_space = spaces.Box(low=0, high=255, shape=(80, 80), dtype=np.uint8)

self.gametime_reward = 0.1

self.gameOver_penalty = -1

self.current_frame = self.observation_space.low

self._action_set = [0, 1, 2, 3, 4]

self.game_score = self.game.get_score()
```

5.3.2 New Approaction 1: Deep Q-Network (DQN) with Prioritized Experience Replay (PER)

The biggest problem of the vanilla Deep Q-network is uniformly sampling the experience from a replay memory or buffer, but some experiences are more important than others. To feed the important experience into the neural network, we try to bring the idea of Prioritized Experience Replay in our model. With PER, it will weigh the samples so that the important experience will be drawn more often on the training process. The main goal of DQN is to find a policy that maps a given state to an action that can maximize the expected reward of the agent. To be prioritized the experience, the absolute TD error is used.

$$\delta_i = r_t + \gamma \cdot \max_{a \in A} (Q_{\theta^-}(s_{t+1}, a)) - Q_{\theta}(s_t, a_t)$$

TD error is used as the absolute error $|\delta_i|$ as the absolute, so the negative error and the positive error will be the same in this method. In order to work with the DQN, we assign $|\delta_i|$ into the samples, which is $(s_t, a_t, r_t, s_{t+1}, |\delta_i|)$. In order to update the absolute TD errors, we do not need to update all values. We do need to update $|\delta_i|$ term for the item that is actually sampled during the mini batch gradient updates. For a minibatch size of 32, each gradient update will change the priorities of only 32 samples in the replay buffer, and leave most of the item alone with touching.

There are two ways to calculate the priorities score, denoted as p_i :

A Rank Based Method:

$$p_i = \frac{1}{\operatorname{rank}(i)}$$

Where rank(i) is the rank of transition from sorting the replay memory based on $|\delta_i|$.

A Proportional Variant:

$$p_i = |\delta_i| + \epsilon$$

Where ϵ is a small constant that prevent the transition from zero probability of being drawn.

Either two method above, we will be able to get a probabilistic distribution for sampling by calculating the

equation below:

$$P(i) = \frac{p_i^{\alpha}}{\sum_k p_k^{\alpha}}$$

Where α determines the prioritized level in the memory. If α is close to 0, then there is no prioritization. If α is close to 1, then there is prioritization in the sampling.

Implementation Below is the pseduo-code of the DQN with PER.

```
Algorithm 1: DQN with experience replay
```

```
1 Initialize replay memory D to capacity N;
 2 Initialize action-value function Q with random weights \theta;
 3 Initialize target action-value function \hat{Q} with weights \theta^- = \theta;
 4 for episode = 1 \text{ do}
       Initialize sequence s_1 = x_1 and preprocessed sequence \phi_1 = \phi(s_1);
       for t = 1 do
 6
           if Observation Stage then
             With probability \varepsilon select a random action a_t;
 8
 9
             a_t = \operatorname{argmax}_a(Q(\phi(s_t), a; \theta));
10
            Execute action a_t in the game and observe reward r_t and game state s_{t+1};
11
            Store transition (\phi_t, a_t, r_t, \phi_{t+1}) in D;
12
            Sample random minibatch of transition (\phi_j, a_j, r_j, \phi_{j+1}) from D;
13
            if Episode terminates at step j + 1 then
14
15
             r_j;
16
             r_j + \gamma \max_{a'}(\hat{Q}(\phi_{j+1}, a'; \theta^-))
17
           Perform a gradient descent step on (y_j - Q(\phi_i, a_j; \theta))^2 with respect to the network parameter
18
             \theta;
            \hat{Q} = Q;
```

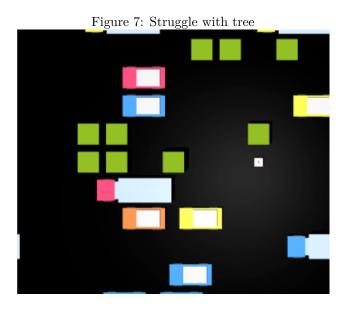
With the openAI package and previously set baselines environment, the actually implementation is as simple as the code in below

5.3.3 New Approaction 2: Advantage Actor Critic (A2C)

To recall, we use the value based methods to train our agent where we learn a value function by mapping the state and action pair to a value. We will select the best action by selecting the action that can give the biggest Q value. But there are several methods of reinforcement learning that exist in this world, which are Policy based methods or Reinforcement with Policy Gradients. Rather using the value function, we can directly optimize the policy. This method is trying to find a good score function to compute how good a policy is.

However, these two methods on reinforcement learning have the biggest drawback; therefore, instead of selecting either value base methods or policy based methods, we do use two methods to train our agent. This is how A2C comes in.

The biggest problem of the Policy Gradients is that we need to wait until the end of the episode in order to calculate the score, which is known as Monte Carlo. Especially in the Crossy Road game, the chicken can be alive for a long time, but it does mean that we can earn a high score from the game. It may end with the very high reward. But in fact, our agent got stuck with the obstacle, like in figure 7; therefore, we decided to implement A2C to solve that problem.



A2C is the hybrid method that uses both value based method and policy based method. It use two neural network as below:

- A Critic will measure how good the taken action is(value-based)
- An Action will measure how well our agent performs(policy-based)

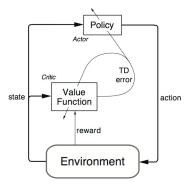
Instead of waiting until the end of the episode to calculate the reward, we do update them after each time step. Since we update the

Policy Update:
$$\Delta\theta = \alpha \cdot \nabla_{\theta}(\log(\pi(S_t, A_t, \theta))) \cdot R(t)$$
 \Downarrow New update: $\Delta\theta = \alpha \cdot \nabla_{\theta}(\log(\pi(S_t, A_t, \theta))) \cdot Q(S_t, A_t)$

Since we update the weight in each time step, the total reward (R(t)) from each episode cannot be used in this model. The total reward R(t) is replaced by the function value, which is the idea of value based method. This is how the value based method comes in the A2C.

As we mention, A2C needs two neural networks to implement and need to run parallel. The first one is the Actor Neural Network. It starts randomly performing the action, and then the Critic Neural Network will observe and provide the feedback from the action that is taken inside the game in terms of loss. Based on the feedback from the Critic neural network, the Actor neural network will be able to update the policy and get better results. Not only the Actor, but also the Critic as well, will update the feedback policy in order to give useful feedback to the Actor.

Figure 8: A2C Architecture



Since we have two neural networks for the Actor and the Critic, we need to estimate both networks.

Actor: A policy function, controls how our agent acts: $\pi(s, a, \theta)$

Critic: A value function, measures how good these actions are: $\hat{q}(s, a, w)$

We need to train both networks simultaneously, which means that we need two sets of the weight for each network.

Policy Update:
$$\Delta \theta = \alpha \ \nabla_{\theta}(\log \pi_{\theta}(s,a)) \hat{q}_w(s,a)$$
 qearning function approximation (estimate action value)

Value update: $\Delta w = \beta \ (\underbrace{R(s,a) + \gamma \hat{q}_w(s_{t+1},a_{t+1}) - \hat{q}_w(s_t,a_t)}_{\text{TD error}}) \nabla_w \hat{q}_w(s_t,a_t)$

Gradient of our value function function

For each input, the Critic will observe and compute the Q value after taking the action on the state, and the Actor will update the policy parameter (weight) by using the Q value that the Critic.

$$\Delta \theta = \alpha \cdot \nabla_{\theta} (\log \pi(S_t, A_t, \theta)) \cdot \hat{q}_w(S_t, A_t)$$

After the Actor updates the weight, it will produce the next action to take with the next state, and the Critic then will update its values parameter.

$$\Delta w = \beta (R(s, a) + \gamma \hat{q}_w(s_{t+1}, a_{t+1}) - \hat{q}_w(s_t, a_t)) \nabla_w \hat{q}_w(s_t, a_t)$$

Implementation Below is the pseduo-code of the A2C.

```
Algorithm 2: Advantage Actor Critic (A2C)
```

```
1 Initialize parameters s, \theta, w and learning rates \alpha_{\theta}, \alpha_{w}; sample a \sim \pi_{\theta}(a|s);

2 for t: 1 \to T do

3 Sample reward r_{t} \sim R(s, a) and next state s' \sim P(s'|s, a);

4 Sample the next action a' \sim \pi_{\theta}(a'|s');

5 Update the policy parameters: \theta \leftarrow \theta + \alpha_{\theta}Q_{w}(s, a)\nabla_{\theta}\log\pi_{\theta}(a|s);

6 Compute the correction (TD-error) for action-value at time t: \delta_{t} = r_{t} + \gamma Q_{w}(s', a') - Q_{w}(s, a);

7 Update the parameters of Q function: w = w + \alpha_{w}\delta_{t}\nabla_{w}Q_{w}(s, a) a = a';

8 s = s';
```

With the openAI package and previously set baselines environment, the actually implementation is as simple as the code in below

5.3.4 New Approaction 3: Proximal Policy Optimization (PPO)

In 2017, the openAI team introduced Proximal Policy Optimization or PPO, which is the improvement of Advantage Actor Critic(A2C). The implementation of PPO is the same as A2C, but the big difference is the way to estimate the policy gradient. PPO used the ratio between the new and old policy that is scaled by advantages instead of using the logarithm of the new policy.

$$L^{CPI}(\theta) = \hat{\mathbb{E}}_t \left[\frac{\pi_{\theta}(a_t|s_t)}{\pi_{\theta_{\text{odd}}(a_t|s_t)}} \hat{A}_t \right] = \hat{\mathbb{E}}_t [r_t(\theta) \hat{A}_t]$$

Implementation Below is the pseduo-code of the Proximal Policy Optimization

Algorithm 3: PPO-Clip

```
Input: Initial policy parameters \theta_0, initial value function parameter \phi_0

1 for k: 1 \to \infty do

2 | Collect set of trajectories \mathcal{D}_k = \{\tau_i\} by running policy \pi_k = \pi(\theta_k) in the environment;

3 | Compute rewards-to-go \hat{R}_t;

4 | Compute advantage estimates, \hat{A}_t based on the current value function V_{\phi_k};

5 | Update the policy by maximizing the PPO-Clip objective:

\theta_{k+1} = \arg\max_{\theta} \frac{1}{|\mathcal{D}_k|T} \sum_{\tau \in \mathcal{D}_k} \sum_{t=0}^{T} \min_{\theta} (\frac{\pi_{\theta}(a_t|s_t)}{\pi_{\theta_k}(a_t|s_t)} A^{\pi_{\theta_k}}(s_t, a_t), g(\epsilon, A^{\pi_{\theta_k}}(s_t, a_t)));

6 | Fit value function by regression on mean-squared error:

\phi_{k+1} = \arg\min_{\phi} \frac{1}{|\mathcal{D}_k|T} \sum_{\tau \in \mathcal{D}_k} \sum_{t=0}^{T} (V_{\phi}(s_t) - \hat{R}_t)^2;
```

With the openAI package and previously set baselines environment, the actually implementation is as simple as the code in below

5.3.5 Model Selection

As we mentioned before, we are encountering limitations on the training process since our game environment does not work well with Google colab. It takes some amount of time to train each model and check the result. Therefore, we do some model selection by training only 30,000 timesteps with the same set of parameters and keep monitoring the result for DQN, A2C, and PPO so that we can focus on training only one model and tune hyperparameter. During the training process, PPO seems to perform better than the other two since this agent can avoid the tree, which is the most challenging that we were encountering for a long time, while the other two models still get stuck within the tree. Now we will mainly focus on training our agent on the PPO model.

After tuning multiple times, below is the hyperparameter that we set in order to achieve the high score.

Reward
-10
+7
-200
0
0

6 Experiments and Results

We noticed that there are variables that potentially can affect the performance of our model: the accuracy of the CNN model and the setting of our reward functions. Therefore, we divided into two branches that each branch will check one of the variables.

6.1 Reward Function Setting

We checked three different sets of reward functions

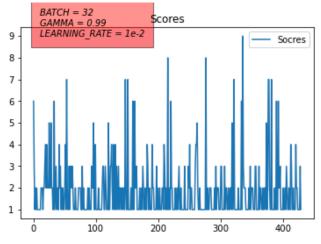
6.1.1 The control group

For the control agent, we set all the rewards for different actions to be the same. And the reward was set to -1 if the game crashed.

Action State	Reward
Forward	0.1
Backward	0.1
Left	0.1
Right	0.1
Game Over	-1

Here is the result of the control group

Figure 9: Visualization of color transformation



6.1.2 First Attempt

Next, we set the reward to be more reasonable. Give more reward if the agent goes forward. At the same time, give a negative reward on moving backward since we don't want it to move backward. The reward for left and right is smaller than forward because we'd like to encourage the agent to move forward instead of doing a left-to-right jump.

Action State	Reward
Forward	1
Backward	-1
Left	0.1
Right	0.1
Game Over	-10

Based on the experiment we did on Agent 1, we found that we need the agent to go backward sometimes. For example, there are some "traps" in the game. We could not get a better result when the agent was trapped.

Figure 10: Trap in the game



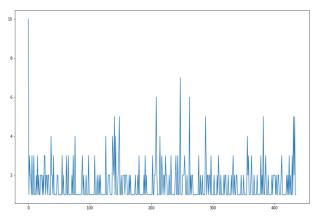
6.1.3 Second Attempt

The previous agent tends to be stuck at the same point in the last experiment. Thus, we set the second agent as below, which we do not punish the agent for backward movement since it can be necessary in some scenarios:

Action State	Reward
Forward	1
Backward	0
Left	0.1
Right	0.1
Game Over	-10

Here is the result of the second group. According to the figure below, it is clear that the result was not improved too much.

Figure 11: The result of the Second Agent



6.1.4 Third Agent

For the third agent, we designed it to build some relationship between score and reward. Thus, we set the reward to be changes of score.

Action State	Reward
Forward	New_Score - Old_Score
Backward	New_Score - Old_Score
Left	New_Score - Old_Score
Right	New_Score - Old_Score
Game Over	-10

We can tell from the result of Agent 3 that the improvement in score is limited. However, the variance of the score is much lower.

Figure 12: The Result of the Third Agent

