

MontyHall(n doors, k revealed)

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1 n doors, k are revealed

We have n doors, with a car behind 1 of them. The probability of choosing the door with the car behind it on first pick is $\frac{1}{n}$.

Monty reveals k doors, all revealed doors are goats so $0 \leq k \leq n - 2$ The probability of picking the car if you choose a different door, is the probability of not having picked the car in initial choice times the probability of picking it now .

$$P(\text{not picking in initial choice}) = \frac{n-1}{n}$$

$$P(\text{picking the cardoor after switching}) = \frac{1}{n-k-1} (k \text{ revealed}, 1 \text{ is players initial choice})$$

$$\text{Total probability} = \frac{n-1}{n} \cdot \frac{1}{n-k-1}$$

When no doors are revealed ($k=0$) its value is $\frac{1}{n}$.

When $n-2$ doors are revealed its values if $\frac{n-1}{n}$, which is maximum.