**Anomaly Detection** In this exercise, you will implement the anomaly detection algorithm and apply it to detect failing servers on a network. Outline • 1 - Packages 2 - Anomaly detection 2.1 Problem Statement 2.2 Dataset 2.3 Gaussian distribution Exercise 1 Exercise 2 2.4 High dimensional dataset 1 - Packages First, let's run the cell below to import all the packages that you will need during this assignment. • numpy is the fundamental package for working with matrices in Python. • matplotlib is a famous library to plot graphs in Python. • utils.py contains helper functions for this assignment. You do not need to modify code in this file. In [1]: import numpy as np import matplotlib.pyplot as plt from utils import \* %matplotlib inline 2 - Anomaly detection 2.1 Problem Statement In this exercise, you will implement an anomaly detection algorithm to detect anomalous behavior in server computers. The dataset contains two features - throughput (mb/s) and • latency (ms) of response of each server. While your servers were operating, you collected m=307 examples of how they were behaving, and thus have an unlabeled dataset  $\{x^{(1)},\ldots,x^{(m)}\}$ . • You suspect that the vast majority of these examples are "normal" (non-anomalous) examples of the servers operating normally, but there might also be some examples of servers acting anomalously within this dataset. You will use a Gaussian model to detect anomalous examples in your dataset. You will first start on a 2D dataset that will allow you to visualize what the algorithm is doing. • On that dataset you will fit a Gaussian distribution and then find values that have very low probability and hence can be considered anomalies. • After that, you will apply the anomaly detection algorithm to a larger dataset with many dimensions. 2.2 Dataset You will start by loading the dataset for this task. • The load\_data() function shown below loads the data into the variables X\_train, X\_val and y\_val ■ You will use X\_train to fit a Gaussian distribution ■ You will use X\_val and y\_val as a cross validation set to select a threshold and determine anomalous vs normal examples In [2]: # Load the dataset X\_train, X\_val, y\_val = load\_data() View the variables Let's get more familiar with your dataset. • A good place to start is to just print out each variable and see what it contains. The code below prints the first five elements of each of the variables In [3]: # Display the first five elements of X\_train print("The first 5 elements of X\_train are:\n", X\_train[:5]) The first 5 elements of X\_train are: [[13.04681517 14.74115241] [13.40852019 13.7632696 ] [14.19591481 15.85318113] [14.91470077 16.17425987] [13.57669961 14.04284944]] In [4]: # Display the first five elements of X\_val print("The first 5 elements of X\_val are\n", X\_val[:5]) The first 5 elements of X\_val are [[15.79025979 14.9210243 ] [13.63961877 15.32995521] [14.86589943 16.47386514] [13.58467605 13.98930611] [13.46404167 15.63533011]] In [5]: # Display the first five elements of y\_val print("The first 5 elements of y\_val are\n", y\_val[:5]) The first 5 elements of y\_val are [0 0 0 0 0] Check the dimensions of your variables Another useful way to get familiar with your data is to view its dimensions. The code below prints the shape of <code>X\_train</code>, <code>X\_val</code> and <code>y\_val</code>. In [6]: print ('The shape of X\_train is:', X\_train.shape) print ('The shape of X\_val is:', X\_val.shape) print ('The shape of y\_val is: ', y\_val.shape) The shape of X\_train is: (307, 2) The shape of  $X_{val}$  is: (307, 2) The shape of y\_val is: (307,) Visualize your data Before starting on any task, it is often useful to understand the data by visualizing it. • For this dataset, you can use a scatter plot to visualize the data (X\_train), since it has only two properties to plot (throughput and latency) • Your plot should look similar to the one below No description has been provided for this image # Create a scatter plot of the data. To change the markers to blue "x", # we used the 'marker' and 'c' parameters plt.scatter(X\_train[:, 0], X\_train[:, 1], marker='x', c='b') # Set the title plt.title("The first dataset") # Set the y-axis label plt.ylabel('Throughput (mb/s)') # Set the x-axis label plt.xlabel('Latency (ms)') # Set axis range plt.axis([0, 30, 0, 30]) plt.show() The first dataset 30 25 Throughput (mb/s) 15 10 15 20 25 30 10 Latency (ms) 2.3 Gaussian distribution To perform anomaly detection, you will first need to fit a model to the data's distribution. ullet Given a training set  $\{x^{(1)},\dots,x^{(m)}\}$  you want to estimate the Gaussian distribution for each of the features  $x_i$ . • Recall that the Gaussian distribution is given by  $p(x;\mu,\sigma^2) = rac{1}{\sqrt{2\pi\sigma^2}} {
m exp}^{-rac{(x-\mu)^2}{2\sigma^2}}$ where  $\mu$  is the mean and  $\sigma^2$  is the variance. • For each feature  $i=1\dots n$ , you need to find parameters  $\mu_i$  and  $\sigma_i^2$  that fit the data in the i-th dimension  $\{x_i^{(1)},\dots,x_i^{(m)}\}$  (the i-th dimension of each example). 2.3.1 Estimating parameters for a Gaussian distribution Implementation: Your task is to complete the code in estimate\_gaussian below. Exercise 1 Complete the estimate\_gaussian function below to calculate mu (mean for each feature in X) and var (variance for each feature in X). You can estimate the parameters,  $(\mu_i, \sigma_i^2)$ , of the *i*-th feature by using the following equations. To estimate the mean, you will use:  $\mu_i = rac{1}{m} \sum_{j=1}^m x_i^{(j)}$   $\sigma_i^2 = rac{1}{m} \sum_{j=1}^m (x_i^{(j)} - \mu_i)^2$ and for the variance you will use: In [8]: # GRADED FUNCTION: estimate\_gaussian def estimate\_gaussian(X): Calculates mean and variance of all features in the dataset Args: X (ndarray): (m, n) Data matrix mu (ndarray): (n,) Mean of all features var (ndarray): (n,) Variance of all features m, n = X.shape### START CODE HERE ### mu = np.mean(X, axis=0)var = np.var(X, axis=0)### END CODE HERE ### return mu, var You can check if your implementation is correct by running the following test code: In [9]: # Estimate mean and variance of each feature mu, var = estimate\_gaussian(X\_train) print("Mean of each feature:", mu) print("Variance of each feature:", var) # UNIT TEST from public\_tests import \* estimate\_gaussian\_test(estimate\_gaussian) Mean of each feature: [14.11222578 14.99771051] Variance of each feature: [1.83263141 1.70974533] All tests passed! **Expected Output:** Mean of each feature: [14.11222578 14.99771051] Variance of each feature: [1.83263141 1.70974533] Now that you have completed the code in estimate\_gaussian, we will visualize the contours of the fitted Gaussian distribution. You should get a plot similar to the figure below. No description has been provided for this image From your plot you can see that most of the examples are in the region with the highest probability, while the anomalous examples are in the regions with lower probabilities. In [10]: # Returns the density of the multivariate normal # at each data point (row) of X\_train p = multivariate\_gaussian(X\_train, mu, var) #Plotting code visualize\_fit(X\_train, mu, var) The Gaussian contours of the distribution fit to the dataset 30 25 Throughput (mb/s) 12 05 10 10 15 20 25 30 35 Latency (ms) 2.3.2 Selecting the threshold  $\epsilon$ Now that you have estimated the Gaussian parameters, you can investigate which examples have a very high probability given this distribution and which examples have a very low probability. • The low probability examples are more likely to be the anomalies in our dataset. • One way to determine which examples are anomalies is to select a threshold based on a cross validation set. In this section, you will complete the code in select\_threshold to select the threshold  $\varepsilon$  using the  $F_1$  score on a cross validation set. • For this, we will use a cross validation set  $\{(x_{\text{cv}}^{(1)}, y_{\text{cv}}^{(1)}), \dots, (x_{\text{cv}}^{(m_{\text{cv}})}, y_{\text{cv}}^{(m_{\text{cv}})})\}$ , where the label y=1 corresponds to an anomalous example, and y=0 corresponds to a normal example. • For each cross validation example, we will compute  $p(x_{\text{cv}}^{(i)})$ . The vector of all of these probabilities  $p(x_{\text{cv}}^{(1)}), \dots, p(x_{\text{cv}}^{(m_{\text{cv}})})$  is passed to <code>select\_threshold</code> in the vector <code>p\_val</code>. ullet The corresponding labels  $y_{ ext{cv}}^{(1)},\dots,y_{ ext{cv}}^{(m_{ ext{cv}})}$  are passed to the same function in the vector <code>y\_val</code> . Exercise 2 Complete the select\_threshold function below to find the best threshold to use for selecting outliers based on the results from the validation set (p\_val) and the ground truth (y\_val). • In the provided code select\_threshold, there is already a loop that will try many different values of  $\varepsilon$  and select the best  $\varepsilon$  based on the  $F_1$  score. • You need to implement code to calculate the F1 score from choosing epsilon as the threshold and place the value in F1. lacktriangledown Recall that if an example x has a low probability p(x)<arepsilon, then it is classified as an anomaly. ■ Then, you can compute precision and recall by: where  $\circ$  tp is the number of true positives: the ground truth label says it's an anomaly and our algorithm correctly classified it as an anomaly.  $\circ$  fp is the number of false positives: the ground truth label says it's not an anomaly, but our algorithm incorrectly classified it as an anomaly.  $\circ$  fn is the number of false negatives: the ground truth label says it's an anomaly, but our algorithm incorrectly classified it as not being anomalous. ■ The  $F_1$  score is computed using precision (prec) and recall (rec) as follows: **Implementation Note**: In order to compute tp, fp and fn, you may be able to use a vectorized implementation rather than loop over all the examples. In [13]: # GRADED FUNCTION: select\_threshold def select\_threshold(y\_val, p\_val): Finds the best threshold to use for selecting outliers based on the results from a validation set (p\_val) and the ground truth (y\_val) Args: y\_val (ndarray): Ground truth on validation set p\_val (ndarray): Results on validation set epsilon (float): Threshold chosen F1 (float): F1 score by choosing epsilon as threshold  $best_epsilon = 0$  $best_F1 = 0$ F1 = 0 $step\_size = (max(p\_val) - min(p\_val)) / 1000$ for epsilon in np.arange(min(p\_val), max(p\_val), step\_size): ### START CODE HERE ### predictions = p\_val < epsilon</pre> tp = np.sum((predictions == 1) & (y\_val == 1))  $fp = np.sum((predictions == 1) & (y_val == 0))$  $fn = np.sum((predictions == 0) & (y_val == 1))$ precision = tp / (tp + fp) if (tp + fp) > 0 else 0 recall = tp / (tp + fn) if (tp + fn) > 0 else 0 F1 = (2 \* precision \* recall) / (precision + recall) if (precision + recall) > 0 else 0### END CODE HERE ### if F1 > best\_F1:  $best_F1 = F1$ best\_epsilon = epsilon return best\_epsilon, best\_F1 You can check your implementation using the code below In [14]: p\_val = multivariate\_gaussian(X\_val, mu, var) epsilon, F1 = select\_threshold(y\_val, p\_val) print('Best epsilon found using cross-validation: %e' % epsilon) print('Best F1 on Cross Validation Set: %f' % F1) # UNIT TEST select\_threshold\_test(select\_threshold) Best epsilon found using cross-validation: 8.990853e-05 Best F1 on Cross Validation Set: 0.875000 All tests passed! **Expected Output:** Best epsilon found using cross-validation: 8.99e-05 Best F1 on Cross Validation Set: Now we will run your anomaly detection code and circle the anomalies in the plot (Figure 3 below). No description has been provided for this image In [15]: # Find the outliers in the training set outliers = p < epsilon # Visualize the fit visualize\_fit(X\_train, mu, var) # Draw a red circle around those outliers plt.plot(X\_train[outliers, 0], X\_train[outliers, 1], 'ro', markersize= 10, markerfacecolor='none', markeredgewidth=2) Out[15]: [<matplotlib.lines.Line2D at 0x25d67935a90>] The Gaussian contours of the distribution fit to the dataset 35 30 25 10 5 · 0 -10 25 30 35 15 20 Latency (ms) 2.4 High dimensional dataset Now, we will run the anomaly detection algorithm that you implemented on a more realistic and much harder dataset. In this dataset, each example is described by 11 features, capturing many more properties of your compute servers. Let's start by loading the dataset. • The load\_data() function shown below loads the data into variables X\_train\_high, X\_val\_high and y\_val\_high \_high is meant to distinguish these variables from the ones used in the previous part ■ We will use X\_train\_high to fit Gaussian distribution ■ We will use X\_val\_high and y\_val\_high as a cross validation set to select a threshold and determine anomalous vs normal examples In [16]: # load the dataset X\_train\_high, X\_val\_high, y\_val\_high = load\_data\_multi() Check the dimensions of your variables Let's check the dimensions of these new variables to become familiar with the data In [17]: print ('The shape of X\_train\_high is:', X\_train\_high.shape) print ('The shape of X\_val\_high is:', X\_val\_high.shape) print ('The shape of y\_val\_high is: ', y\_val\_high.shape) The shape of X\_train\_high is: (1000, 11) The shape of X\_val\_high is: (100, 11) The shape of y\_val\_high is: (100,) Anomaly detection Now, let's run the anomaly detection algorithm on this new dataset. The code below will use your code to • Estimate the Gaussian parameters ( $\mu_i$  and  $\sigma_i^2$ ) • Evaluate the probabilities for both the training data X\_train\_high from which you estimated the Gaussian parameters, as well as for the the cross-validation set X\_val\_high. • Finally, it will use select\_threshold to find the best threshold  $\varepsilon$ . In [18]: # Apply the same steps to the larger dataset # Estimate the Gaussian parameters mu\_high, var\_high = estimate\_gaussian(X\_train\_high) # Evaluate the probabilites for the training set p\_high = multivariate\_gaussian(X\_train\_high, mu\_high, var\_high) # Evaluate the probabilites for the cross validation set p\_val\_high = multivariate\_gaussian(X\_val\_high, mu\_high, var\_high) # Find the best threshold epsilon\_high, F1\_high = select\_threshold(y\_val\_high, p\_val\_high) print('Best epsilon found using cross-validation: %e'% epsilon\_high) print('Best F1 on Cross Validation Set: %f'% F1\_high) print('# Anomalies found: %d'% sum(p\_high < epsilon\_high))</pre> Best epsilon found using cross-validation: 1.377229e-18 Best F1 on Cross Validation Set: 0.615385 # Anomalies found: 117 **Expected Output:** Best epsilon found using cross-validation: 1.38e-18 Best F1 on Cross Validation Set: 0.615385 # anomalies found: 117

