

HERCULES 2018

Simulating beamline optics by ray-tracing using ShadowOui

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Outline

- Software
- Sources (BM, wigglers and undulators)
- Optics
 - Reflective (aberrations, slope errors)
 - Diffractive (dispersion)
 - Refractive (chromatic aberrations)
 - Coherence

Each wavefront is a solution of the Helmholtz equation, and it is fully coherent.

Partial coherence require working with many wavefronts. Each individual wavefront is coherent, but incoherent with respect to others

SRW

$$\nabla \cdot \vec{D} = \rho_{\text{free}}$$

$$\nabla \cdot \vec{B} = 0$$

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\nabla \times \vec{H} = \vec{J}_{\text{free}} + \frac{\partial \vec{D}}{\partial t}$$

Maxwell Equations

Wave Equations

$$\frac{\partial^2 \vec{E}}{\partial t^2} - c_0^2 \cdot \nabla^2 \vec{E} = 0$$

$$\frac{\partial^2 \vec{B}}{\partial t^2} - c_0^2 \cdot \nabla^2 \vec{B} = 0$$

Helmholtz Equation

$$(\nabla^2 + k^2)\vec{E} = 0, \vec{B} = -\frac{i}{k} \nabla \times \vec{E},$$

Wave Optics

Fresnel Kirchhoff diffraction formula

Fresnel

Fraunhofer

Geometrical Optics

$$\vec{E} = \vec{e} e^{ik_0 S(r)}$$

$$\vec{H} = \vec{h} e^{ik_0 S(r)}$$

$$(\nabla S)^2 = n^2$$

$$\nabla S = n \vec{s}$$

$$\frac{d}{ds} \left(n \frac{d\vec{r}}{ds} \right) = \nabla n$$

$$\nabla n = 0 \Rightarrow \frac{d\vec{r}}{ds} = 0 \Rightarrow \vec{r} = s\vec{a} + \vec{b}$$

Each ray is a solution of the Helmholtz equation.

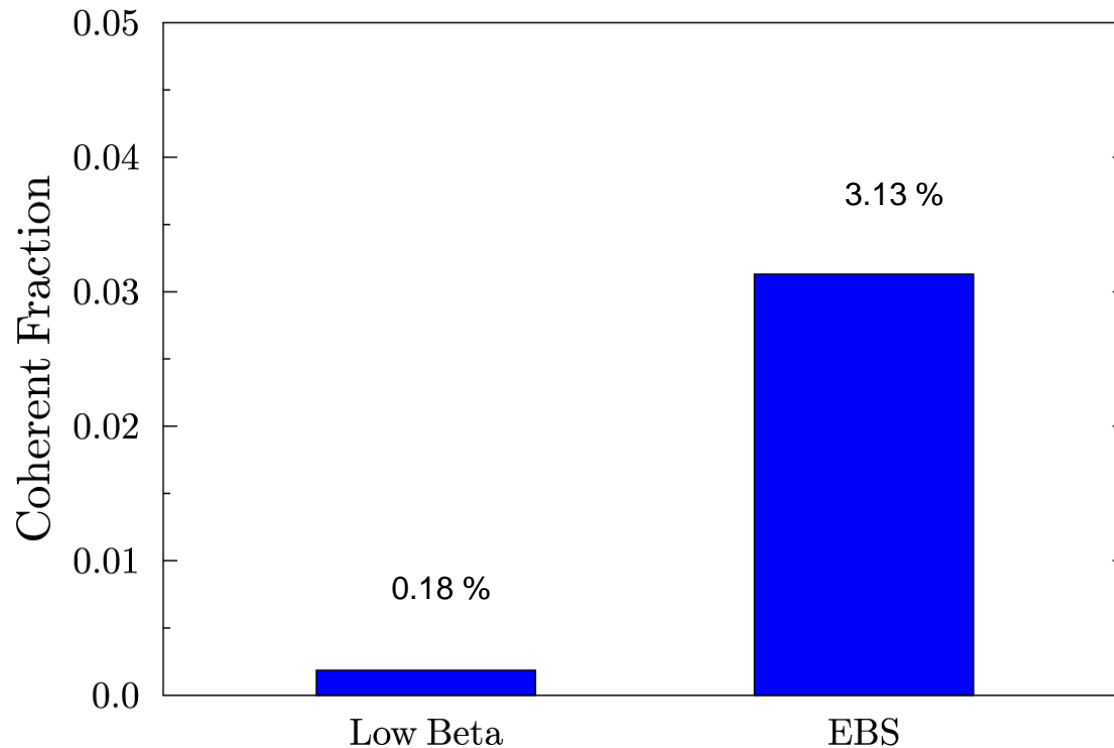
Many rays represent an incoherent beam. Each individual ray is coherent, but incoherent with respect to others

SHADOW

AT HIGH ENERGIES, WE ARE FAR FROM DIFFRACTION-LIMIT (=FULLY COHERENCE)

U17 2m @ 17 keV ($K=0.4842$) $L=2\text{m}$ Coherent Fraction

**THEREFORE, ANY BEAMLINE SIMULATION MUST START WITH RAY TRACING
(INCOHERENT BEAMS)**



CONTEXT: OASYS TOOLBOX TO SIMULATE VIRTUAL EXPERIMENTS

Beamline Experiment Chain

Storage Ring
(e^- optics)



Radiation devices
($e^- \rightarrow \gamma$)



Beamline
(γ optics)



Sample
(γ –matter
interactions)

NEW OASYS-BASED TOOLBOX

ShadowOUI

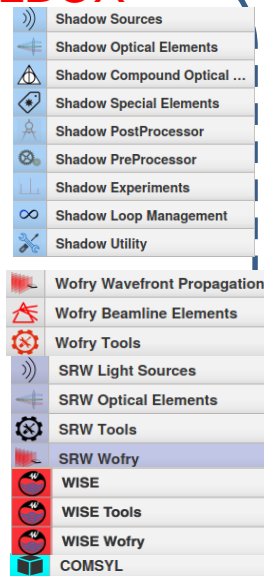
XOPPY

SRW

WOFRY

X-rayserver

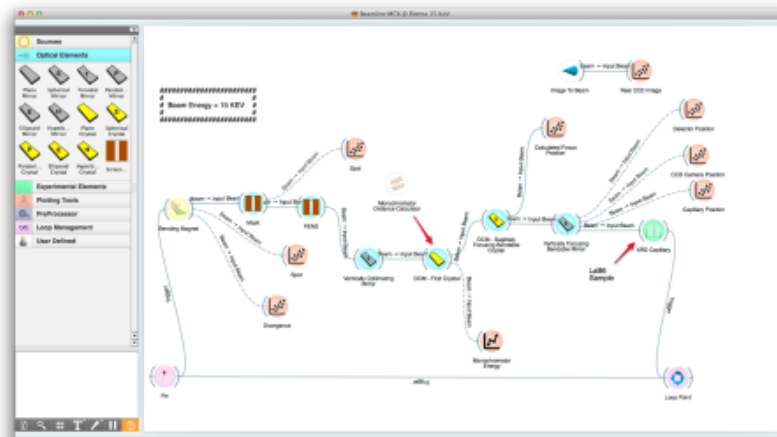
wise



<http://www.elettra.eu/oasys.html>

OASYS: A NEW PLATFORM FOR BEAMLINE SIMULATIONS

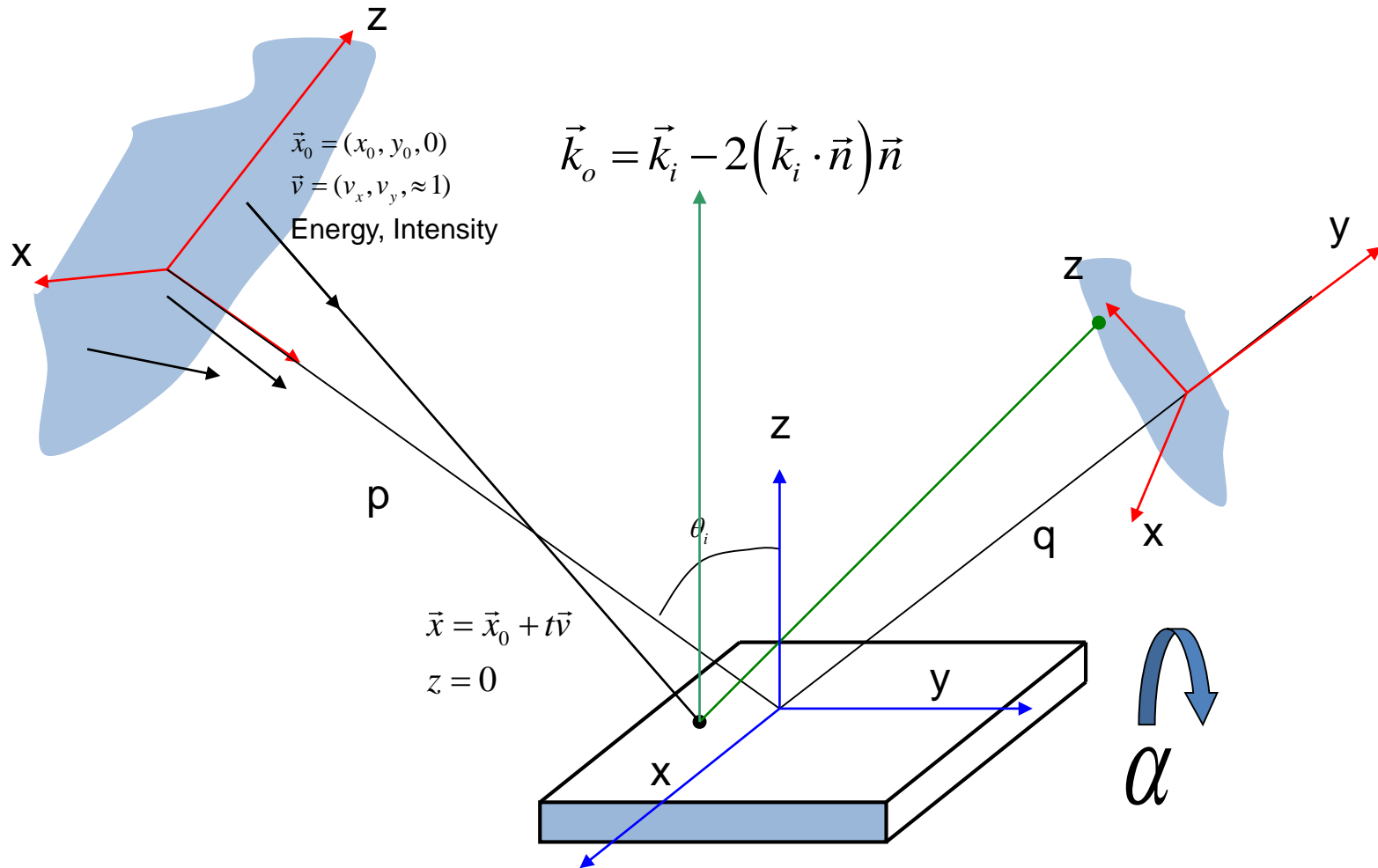
- Oasys is a new software platform for simulating virtual experiments in the synchrotron radiation world
- Oasys is the result of a collaboration among ESRF, Elettra and University of Ljubljana.
- It integrates different state-of-the-art simulation packages for beamline simulation and X-ray optics.



Oasys+ShadowOui

- Install Oasys+ShadowOui:
 - <https://github.com/oasys-kit/oasys-installation-scripts/wiki>
- Today: Use rnice.
- Download Tutorials:
 - `export all_proxy=http://proxy.esrf.fr:3128/`
 - `git clone https://github.com/srio/ShadowOui-Tutorial`
- Start OASYS:
 - `oarsub -I -l nodes=1/cpu=1/core=8,walltime=10:00:00`
 - `/scisoft/XRayOptics/OASYS1_RNICE8/start_oasys.sh`

Trace (the beamline)



X-ray sources

- X-ray tubes
- Radioactive sources / Excitation by radioactive decay
- Synchrotron Bending Magnets
- Synchrotron insertion devices (wigglers and undulators)
- X-ray lasers
- Others: Inverse Compton, Channeling
- Pulsars/Quasars/Black holes etc.

ShadowOui has tools to simulate synchrotron sources. In addition a “Geometrical Source” can be used to approximate any source.

Compute e⁻ beam sizes

$$\Sigma = \begin{pmatrix} \langle x^2 \rangle & \langle xx' \rangle \\ \langle xx' \rangle & \langle x'^2 \rangle \end{pmatrix} = \begin{pmatrix} \beta_x \varepsilon_x & -\alpha_x \varepsilon_x \\ -\alpha_x \varepsilon_x & \gamma_x \varepsilon_x \end{pmatrix} + \eta^2 \sigma_\delta^2 I_{2 \times 2}$$

With ε the emittance (constant), and Twiss parameters:

$$\alpha = -\frac{1}{2} \frac{d\beta}{ds}; \quad \gamma = \frac{1 + \alpha^2}{\beta}$$

At **s** (any point of the trajectory):

$$\sigma_x = \sqrt{\langle x^2 \rangle} = \sqrt{\beta_x \varepsilon_x}; \quad \sigma_{x'} = \sqrt{\langle x'^2 \rangle} = \sqrt{\gamma_x \varepsilon_x}; \quad \sigma_x \sigma_{x'} = \varepsilon_x \sqrt{1 + \alpha_x^2}$$

At **waist** (zero correlation, $\rho = \alpha = 0$, β is minimum):

$$\sigma_x = \sqrt{\langle x^2 \rangle} = \sqrt{\beta_x \varepsilon_x}; \quad \sigma_{x'} = \sqrt{\langle x'^2 \rangle} \Big|_w = \sqrt{\frac{\varepsilon_x}{\beta_x}}; \quad \boxed{\sigma_x \sigma_{x'} = \varepsilon_x}$$



ShadowOui asks for σ and ε at waist (plus distance from waist to center of device)

Onuki & Elleaume Undulators, Wigglers and their applications, CRC press, 2002

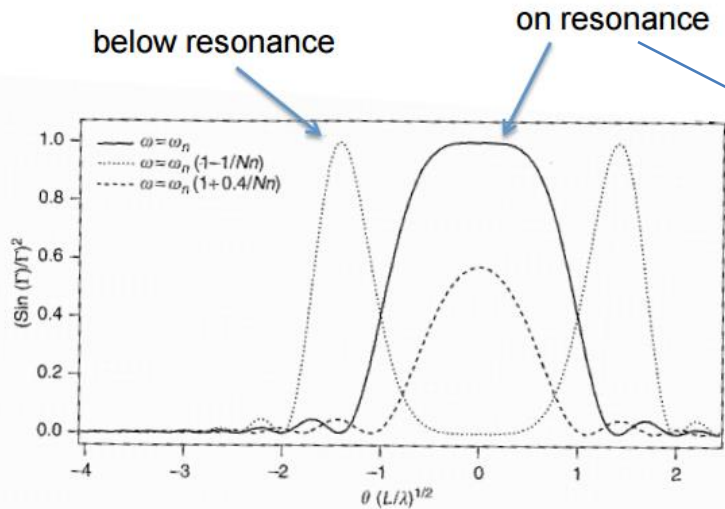


Figure 3.3 Graph of $(\sin(\Gamma)/\Gamma)^2$ as a function of the angle $\theta = \sqrt{\theta_x^2 + \theta_z^2}$ for three different frequencies. ω_n is an abbreviation for $n\omega_1(0, 0)$.

78 P. Elleaume

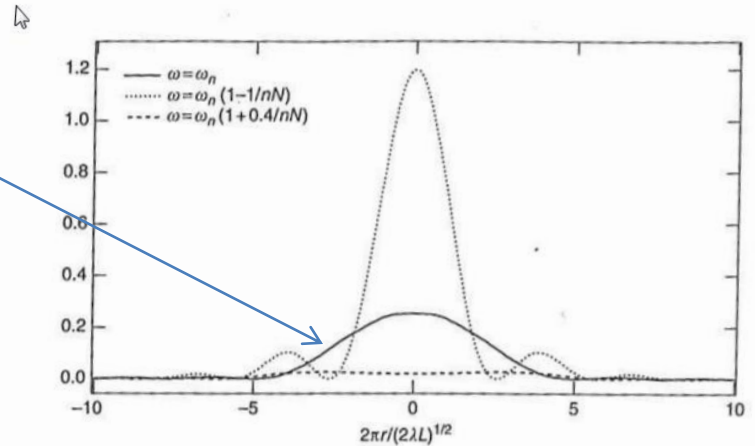


Figure 3.4 Spectral flux per unit surface in the middle of the undulator for three frequencies close to the on-axis resonant frequency $\omega_n = n\omega_1(0, 0)$.

Even on resonance, beam is not fully Gaussian
But for resonance, can be reasonably approximated as Gaussian

$$\sigma_{r'} = 0.69 \sqrt{\frac{\lambda}{L}} \approx \sqrt{\frac{\lambda}{2L}}$$

$$\sigma_r = \frac{2.704}{4\pi} \sqrt{\lambda L} \approx \sqrt{\frac{\lambda L}{2\pi^2}}$$

$$\sigma_r \sigma_{r'} = \frac{1.89\lambda}{4\pi} \approx \frac{\lambda}{2\pi}$$

- Undulator beams have not Gaussian profiles (even at resonances)
- BY NOW, WE APPROXIMATE UNDULATORS BY GEOMETRIC SOURCES WITH GAUSSIAN SIZES AND DIVERGENCES

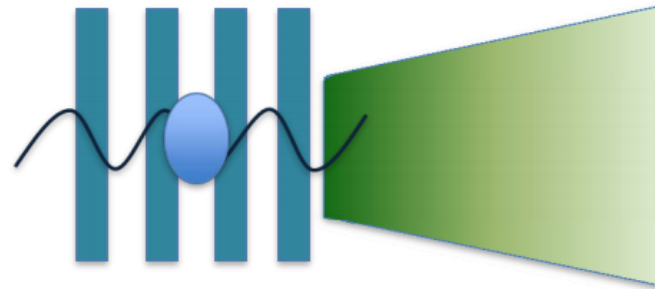
Photon beam size and divergence
is determined by a combination of electron
beam and single electron emission

$$\Sigma_x^2 = \sigma_{x,elec}^2 + \sigma_{x,photon}^2$$

$$\Sigma_{x'}^2 = \sigma_{x',elec}^2 + \sigma_{x',photon}^2$$

$$\Sigma_z^2 = \sigma_{z,elec}^2 + \sigma_{z,photon}^2$$

$$\Sigma_{z'}^2 = \sigma_{z',elec}^2 + \sigma_{z',photon}^2$$



Courtesy: Boaz Nash

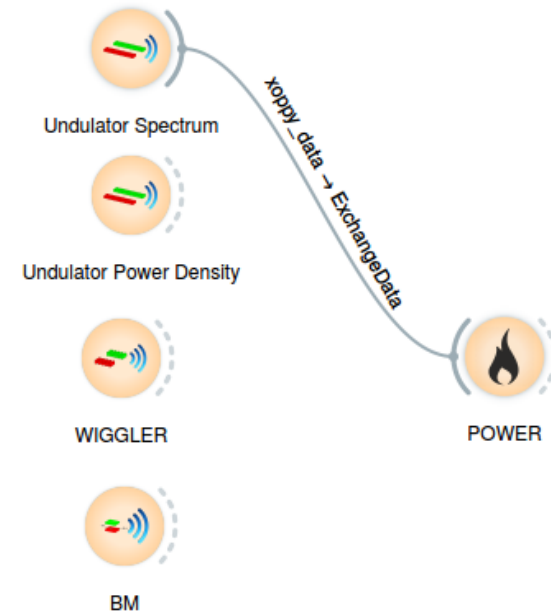
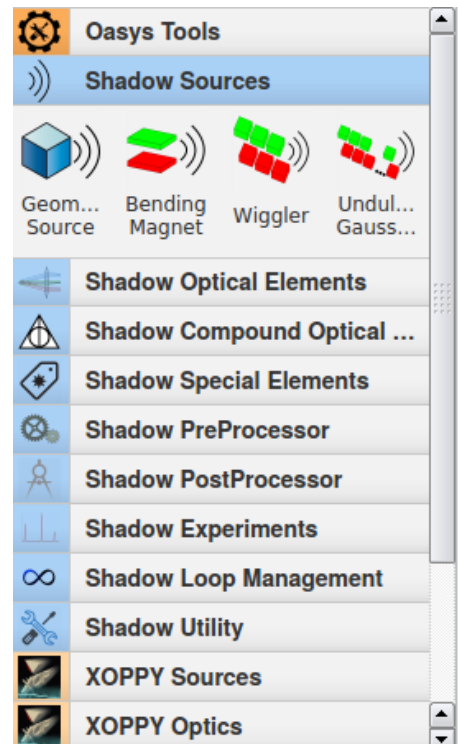
These are at source. A distance D away, beam size become: $\Sigma_{x,0}^2 + \Sigma_{x',0}^2 D^2$

(FOR UNDULATORS, THESE FORMULAS ARE VALID AT THE WAIST, AT THE UNDULATOR RESONANCE, AND SUPOSSING GAUSSIAN EMISSION OF PHOTONS)

ShadowOui performs “numeric convolution” by Monte Carlo sampling of the electron beam [Gaussian] and photon emission [non Gaussian]

Source characteristics (XOPPY)

- Undulator spectrum – power
- Undulator power density
- Wiggler spectrum
- BM



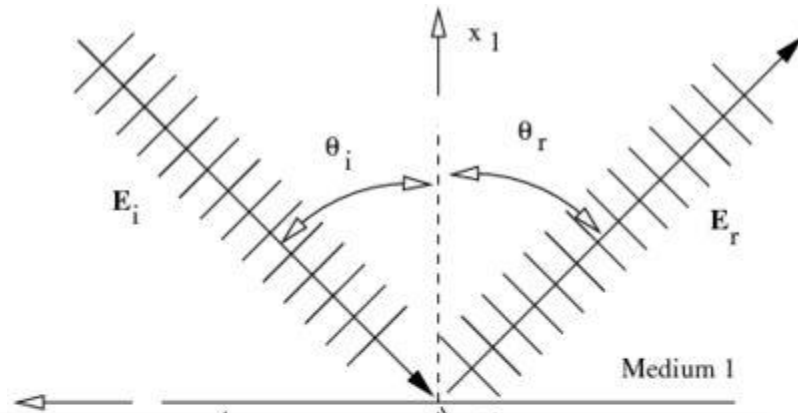
Optical elements

For each optics element SHADOW includes:

- Geometrical model: how the direction of the rays are changed (reflected, refracted or diffracted)
- Physical model: how the ray intensity (in fact electric fields) decreases because of the interaction
 - Structures along the surface => playing with the direction
 - Structures in depth => playing with the reflectivity

Mirrors

Geometrical model

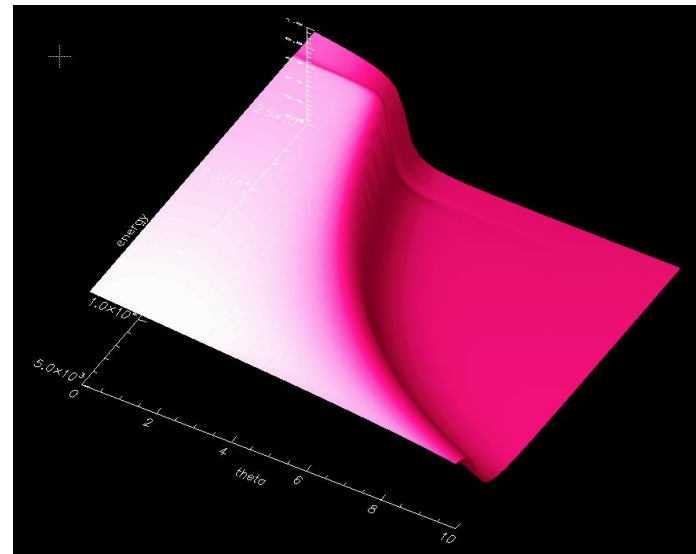


$$\hat{\mathbf{d}}_s = 2 (\hat{\mathbf{d}}_n \cdot \hat{\mathbf{d}}_i) \hat{\mathbf{d}}_n - \hat{\mathbf{d}}_i,$$

Physical model

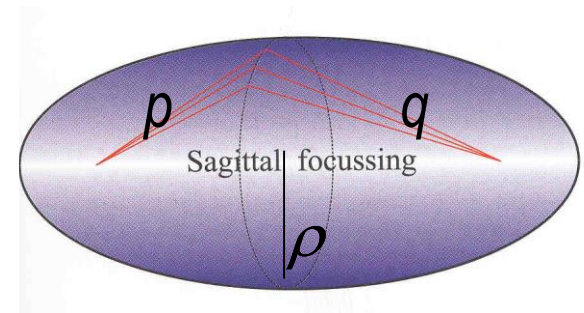
Fresnel equations give the reflectivity as a function of angle and photon energy. As a consequence, one gets the critical angle:

$$1 = \left(\frac{n_1}{n_2} \right)^2 \cos^2 \theta_c \Leftrightarrow \sin \theta_c = \sqrt{2\delta - \delta^2} \approx \sqrt{2\delta}$$



Mirror shape

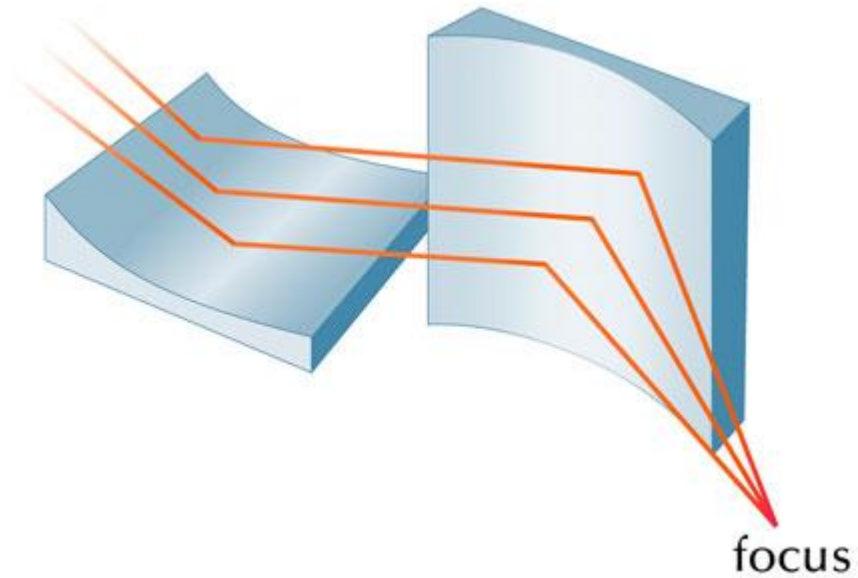
- Point to point focusing (ellipsoid)
- Collimating (paraboloid)
- Focalization in two planes
 - Tangential or Meridional (ellipse or parabola)
 - Sagittal (circle)
- Demagnification: $M=p/q$
- Easier manufacturing:
 - 2D: Ellipsoid => Toroid
 - Only one plane: cylinder Ellipsoid (ellipse)=> cylinder (circle)
 - Sagittal radius: non-linear (ellipsoid) => constant (cylinder) or linear (cone),
- Aberrations



$$\frac{1}{p} + \frac{1}{q} = \frac{2}{R \sin \theta}$$

$$\frac{1}{p} + \frac{1}{q} = \frac{2 \sin \theta}{\rho}$$

Kirkpatrick-Baez

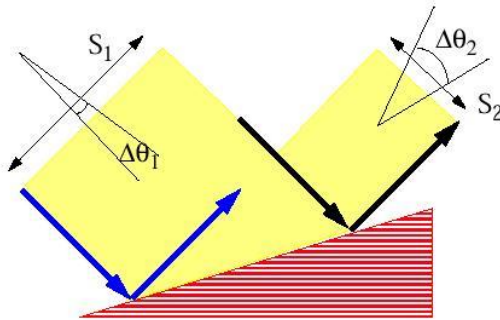


ex16_kb.ows

Crystals

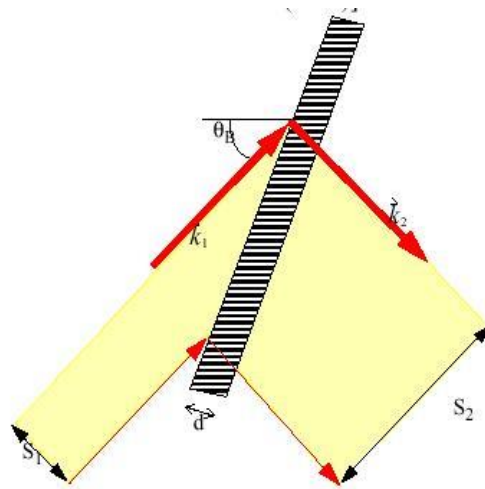
Geometrical model

like a grating originated by the truncation of the Bragg planes with the crystal surface. Crystals are dispersive elements, except for the most used case of Bragg-Symmetric reflection.



BRAGG or reflection

[ex17_sagittalfocusing.ows](#)
[OTHER_EXAMPLES/crystal_analyzer_diced.ows](#)
[OTHER_EXAMPLES/crystal_asymmetric_backscattering.ows](#)

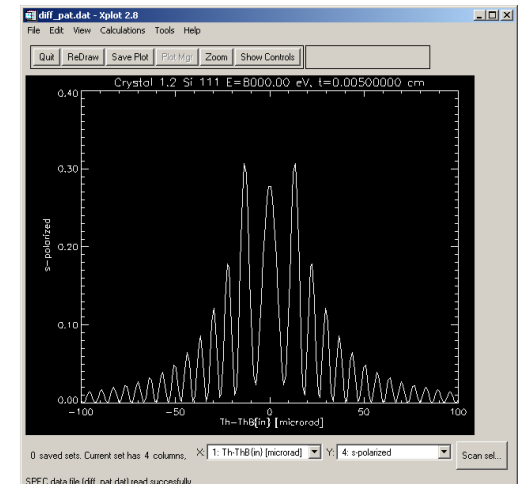
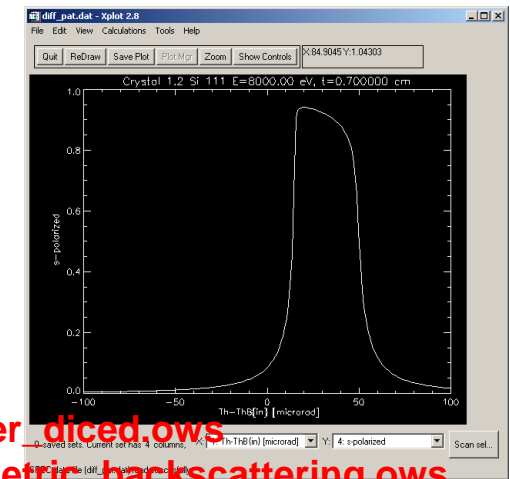


LAUE or transmission

([ex23_crystal_laue.ows](#))

Physical model

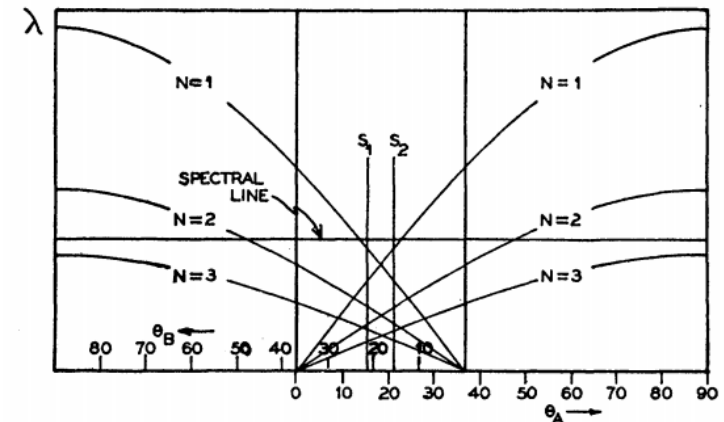
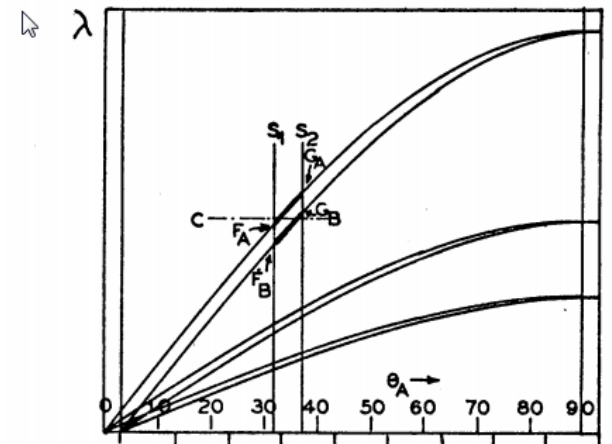
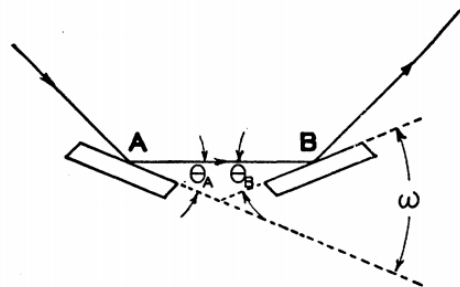
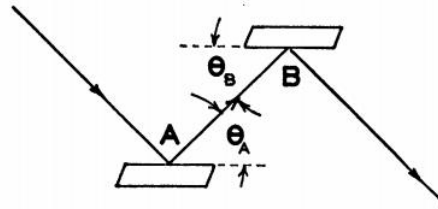
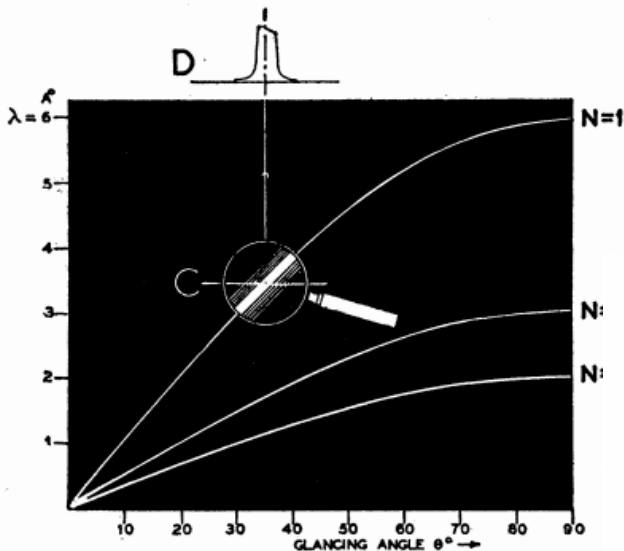
(crystal reflectivity) is given by the Dynamical Theory of Diffraction and gives the “Darwin width”



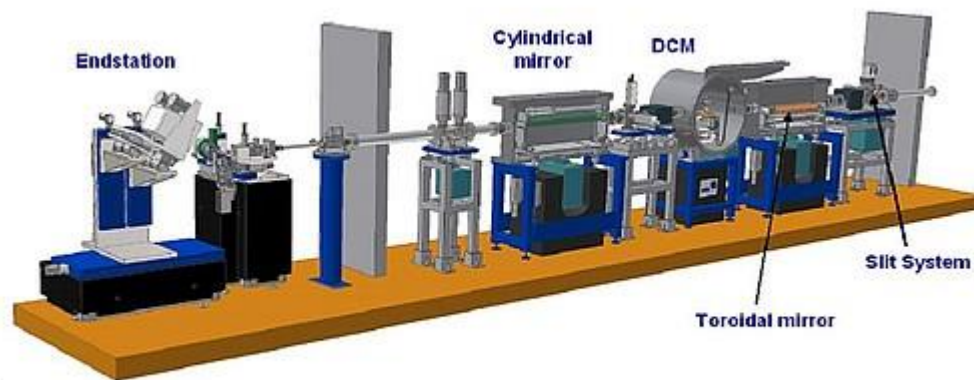
Theory of the Use of More Than Two Successive X-Ray Crystal Reflections to Obtain Increased Resolving Power

J W. M. DuMond Phys. Rev. **52**, 872 – (1937)

<http://dx.doi.org/10.1103/PhysRev.52.872>



Other



ex19_beamline.ows

LENS = TWO INTERFACES

Geometrical model

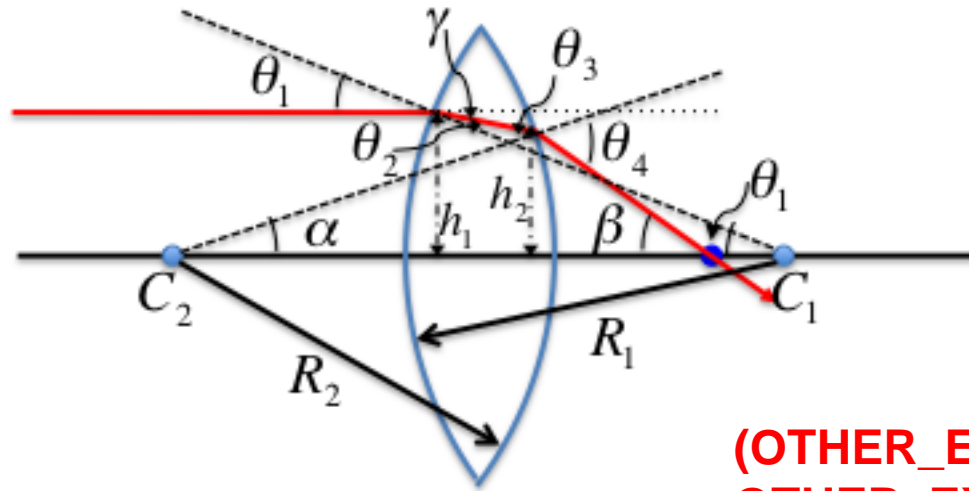
Physical model

Law of Refraction (Snell's Law)

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

absorption in media

$$I/I_0 = \exp(-\mu t)$$



(OTHER_EXAMPLES/lens_elliptical.ows)
OTHER_EXAMPLES/CRL_Snigirev_1996.ows
ex24_transfocator.ows

CRL = n identical Lenses

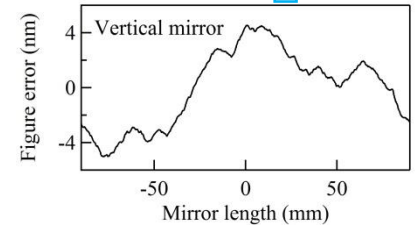
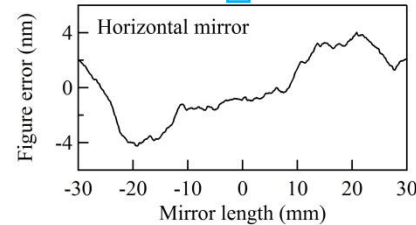
TRANSFOCATOR = m different CRLs

HYBRID METHOD IN SHADOW (X. Shi *et al.*)

Combining ray tracing and wavefront propagation

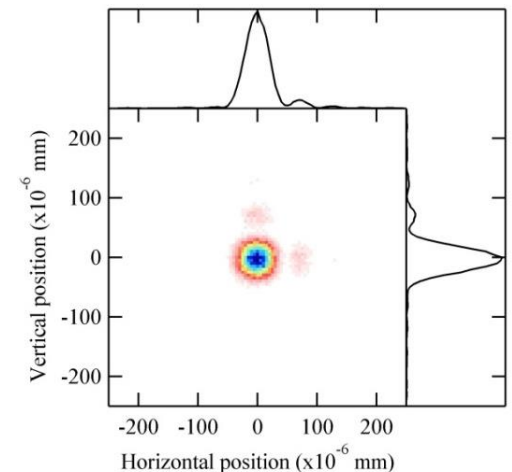
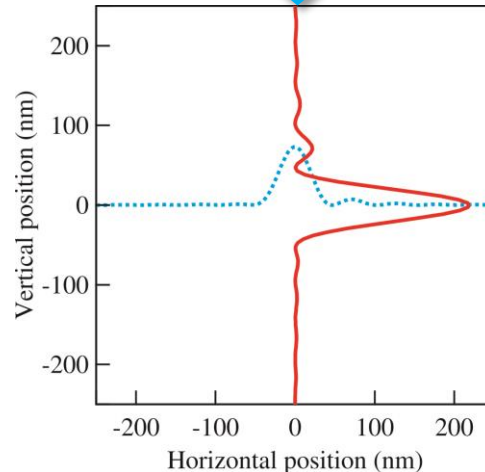
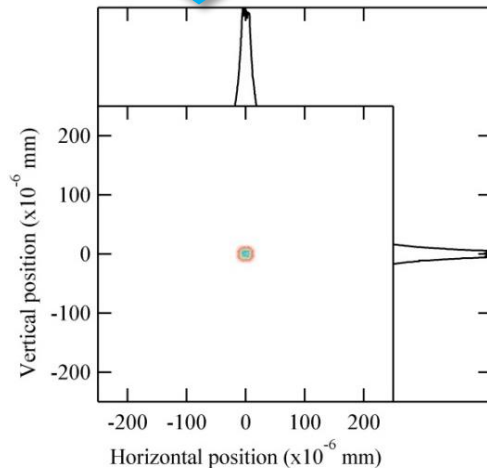
$$\text{Plane wave} \times \exp \left[-ik \left(\frac{x^2}{2f_x} + \frac{z^2}{2f_z} \right) \right] \times \exp[-i2k \sin \theta_x \cdot \text{Height}(x)] \times \exp[-i2k \sin \theta_z \cdot \text{Height}(z)]$$

Ideal lens with focal lengths of f_x and f_z



Ray tracing of the beamline

$$E(x, z) \rightarrow \boxed{\text{FFT}} \xrightarrow{\mathcal{F}(u, v)} \times \exp \left[-\frac{i2\pi^2}{k} (u^2 + v^2) y \right] \xrightarrow{\mathcal{F}'(u, v)} \boxed{\text{Inverse FFT}} \rightarrow E(x', z')$$



X. Shi, R. Reininger, M. Sanchez del Rio, L. Assoufid " J. Synchrotron Rad. (2014) 21, doi:10.1107/S160057751400650X

X. Shi, M. Sanchez del Rio and Ruben Reininger Proc. SPIE 9209, 920911 (2014); doi:10.1117/12.2061984

X. Shi, R. Reininger, M. Sánchez del Río, J. Qian and L. Assoufid Proc. SPIE 9209, 920909 (2014); doi:10.1117/12.2061950

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File Edit View Widget Options Help Shadow Tools

Syned Sources

- Syned Beamline Elements
- Syned Utilities
- Wofry Wavefront Propagation
- Wofry Beamline Elements
- Wofry Tools
- Shadow Sources
- Shadow Optical Elements
- Shadow Compound Optical...

Lens Comp... Refrac... Transf... Kirkpa... Mirror

Doubl... Monoc...

Shadow Special Elements

- Shadow PostProcessor
- Shadow PreProcessor
- Shadow Experiments
- Shadow Loop Management
- Shadow Utility
- SRW Light Sources
- SRW Optical Elements
- SRW Tools
- SRW Wofry
- XOPPY Sources

Python Script

