

# USEFUL FORMULAS

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Arithmetic mean  $\bar{X} = \frac{\Sigma X}{n}$  (Formula 4.1)

Standard deviation  
(defining formula)  $S = \sqrt{\frac{\Sigma (X - \bar{X})^2}{n}} = \sqrt{\frac{SS}{n}}$  (Formula 5.2)

SS (calculating formula)  $SS = \Sigma X^2 - \frac{(\Sigma X)^2}{n}$  (Formula 5.3)

z score  $z = \frac{X - \bar{X}}{S}$  (Formula 6.1)

Covariance  $Cov = \frac{\Sigma (X - \bar{X})(Y - \bar{Y})}{n}$  (Formula 7.1)

Pearson  $r$   
(calculating formula)  $r = \frac{\Sigma XY - \frac{(\Sigma X)(\Sigma Y)}{n}}{\sqrt{\left(\Sigma X^2 - \frac{(\Sigma X)^2}{n}\right)\left(\Sigma Y^2 - \frac{(\Sigma Y)^2}{n}\right)}}$  (Formula 7.3)

Y-on-X regression  
equation: Raw score  
formula  $Y' = \overbrace{\bar{Y} - r\left(\frac{S_Y}{S_X}\right)\bar{X}}^{\text{intercept}} + \overbrace{r\left(\frac{S_Y}{S_X}\right)X}^{\text{slope}}$  (Formula 8.4)

Regression equation:  
z-Score formula  $z_{Y'} = rz_X$  (Formula 8.5)

Standard error of estimate  $S_{Y \cdot X} = S_Y \sqrt{1 - r^2}$  (Formula 8.8)

Standard error of the mean  $\sigma_{\bar{X}} = \frac{\sigma}{\sqrt{n}}$  (Formula 10.2)



The test statistic  $z$   
( $\sigma$  known)

$$z = \frac{\bar{X} - \mu_0}{\sigma_{\bar{X}}} \quad (\text{Formula 11.1})$$

General rule for a confidence  
interval for  $\mu$  ( $\sigma$  known)

$$\bar{X} \pm z_{\alpha} \sigma_{\bar{X}} \quad (\text{Formula 12.3})$$

Estimate of the population  
standard deviation

$$s = \sqrt{\frac{SS}{n-1}} \quad (\text{Formula 13.1})$$

Estimated standard error  
of the mean

$$s_{\bar{X}} = \frac{s}{\sqrt{n}} \quad (\text{Formula 13.2})$$

The test statistic  $t$

$$t = \frac{\bar{X} - \mu_0}{s_{\bar{X}}} \quad (\text{Formula 13.3})$$

General rule for a confidence  
interval for  $\mu$  ( $\sigma$  not known)

$$\bar{X} \pm t_{\alpha} s_{\bar{X}} \quad (\text{Formula 13.4})$$

Estimate of  $\sigma_{\bar{X}_1 - \bar{X}_2}$   
(independent samples)

$$s_{\bar{X}_1 - \bar{X}_2} = \sqrt{\frac{SS_1 + SS_2}{n_1 + n_2 - 2} \left( \frac{1}{n_1} + \frac{1}{n_2} \right)} \quad (\text{Formula 14.5})$$

$t$  test for two  
independent samples

$$t = \frac{\bar{X}_1 - \bar{X}_2}{s_{\bar{X}_1 - \bar{X}_2}} \quad (\text{Formula 14.6})$$

Rule for a confidence  
interval for  $\mu_1 - \mu_2$

$$(\bar{X}_1 - \bar{X}_2) \pm t_{\alpha} s_{\bar{X}_1 - \bar{X}_2} \quad (\text{Formula 14.7})$$

Effect size  
(sample estimate)

$$d = \frac{\bar{X}_1 - \bar{X}_2}{s_{\text{pooled}}} = \frac{\bar{X}_1 - \bar{X}_2}{\sqrt{\frac{SS_1 + SS_2}{n_1 + n_2 - 2}}} \quad (\text{Formula 14.8})$$

$t$  test for two dependent samples:  
Direct-difference method

$$t = \frac{\bar{D}}{\sqrt{\frac{SS_D}{n(n-1)}}} = \frac{\bar{D}}{\sqrt{\frac{\sum D^2 - (\sum D)^2/n}{n(n-1)}}} \quad (\text{Formula 15.5})$$

(continued on back endpapers)



# USEFUL FORMULAS

Rule for a confidence interval for  $\mu_D$

$$\bar{D} \pm t_{\alpha} s_{\bar{D}}$$

(Formula 15.6)

Standard error of  $r$   
( $\rho = 0$ )

$$s_r = \sqrt{\frac{1 - r^2}{n - 2}}$$

(Formula 16.2)

The test statistic  $t$   
(for testing  $\rho = 0$ )

$$t = \frac{r}{s_r}$$

(Formula 16.3)

Within-groups  
sum of squares:  
One-way  
ANOVA

$$\begin{aligned} SS_{\text{within}} &= \sum_{\text{all scores}} (X - \bar{X})^2 \\ &= \sum_{\text{all scores}} X^2 - \left[ \frac{(\sum X_1)^2}{n_1} + \frac{(\sum X_2)^2}{n_2} + \dots + \frac{(\sum X_k)^2}{n_k} \right] \end{aligned}$$

(Formulas 18.1  
and 18.11)

Between-groups  
sum of squares:  
One-way  
ANOVA

$$\begin{aligned} SS_{\text{between}} &= \sum_{\text{all scores}} (\bar{X} - \bar{X})^2 \\ &= \left[ \frac{(\sum X_1)^2}{n_1} + \frac{(\sum X_2)^2}{n_2} + \dots + \frac{(\sum X_k)^2}{n_k} \right] - \frac{\left( \sum_{\text{all scores}} X \right)^2}{n_{\text{total}}} \end{aligned}$$

(Formulas 18.3  
and 18.12)

Total sum of squares:  
One-way ANOVA

$$\begin{aligned} SS_{\text{total}} &= \sum_{\text{all scores}} (X - \bar{X})^2 \\ &= \sum_{\text{all scores}} X^2 - \frac{\left( \sum_{\text{all scores}} X \right)^2}{n_{\text{total}}} \end{aligned}$$

(Formulas 18.5  
and 18.13)

Within-groups  
variance estimate

$$s_{\text{within}}^2 = \frac{SS_{\text{within}}}{n_{\text{total}} - k}$$

(Formula 18.8)

Between-groups  
variance estimate

$$s_{\text{between}}^2 = \frac{SS_{\text{between}}}{k - 1}$$

(Formula 18.9)

$F$  ratio for one-way  
ANOVA

$$F = \frac{s_{\text{between}}^2}{s_{\text{within}}^2}$$

(Formula 18.10)





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Critical HSD  
for Tukey's test

$$HSD = q \sqrt{\frac{s_{\text{within}}^2}{n_{\text{group}}}}$$

(Formula 18.14)

Rule for confidence  
interval for  $\mu_i - \mu_j$

$$\bar{X}_i - \bar{X}_j \pm HSD$$

(Formula 18.16)

Within-groups sum of squares:  
Two-way ANOVA

$$SS_{\text{within}} = \sum_{\text{all scores}} X^2 - \frac{\sum_{\text{all cells}} \left( \sum_{\text{cell}} X \right)^2}{n_{\text{cell}}}$$

(Formula 19.3)

Sum of squares:  
Factor A

$$SS_A = \frac{(\sum X_{A_1})^2 + (\sum X_{A_2})^2 + \dots}{n_A} - \frac{\left( \sum_{\text{all scores}} X \right)^2}{n_{\text{total}}}$$

(Formula 19.5)

Sum of squares:  
Factor B

$$SS_B = \frac{(\sum X_{B_1})^2 + (\sum X_{B_2})^2 + \dots}{n_B} - \frac{\left( \sum_{\text{all scores}} X \right)^2}{n_{\text{total}}}$$

(Formula 19.7)

Sum of squares:  
The A  $\times$  B interaction

$$SS_{A \times B} = SS_{\text{total}} - (SS_{\text{within}} + SS_A + SS_B)$$

(Formula 19.9)

Chi-square

$$\chi^2 = \sum \left[ \frac{(f_o - f_e)^2}{f_e} \right]$$

(Formula 20.1)

Chi-square for a  
2  $\times$  2 table

$$\chi^2 = \frac{n(AD - BC)^2}{(A + B)(C + D)(A + C)(B + D)}$$

(Formula 20.7)

Mann-Whitney test statistic  
for larger samples

$$z = \frac{\sum R_1 - .5[n_1(n_1 + n_2 + 1)]}{\sqrt{\frac{n_1 n_2 (n_1 + n_2 + 1)}{12}}}$$

(Formula 21.1)

Kruskal-  
Wallis test  
statistic: H

$$H = \frac{12}{n_{\text{total}}(n_{\text{total}} + 1)} \left[ \frac{(\sum R_1)^2}{n_1} + \frac{(\sum R_2)^2}{n_2} + \dots + \frac{(\sum R_k)^2}{n_k} \right] - 3(n_{\text{total}} + 1)$$

(Formula 21.2)

Spearman rank correlation

$$r_{\text{ranks}} = 1 - \frac{6 \sum D^2}{n(n^2 - 1)}$$

(Formula 21.3)