Sec II Q1

restart;

r1 := rl; r2 := rk # Labor and Capital

$$r1 := rl$$

$$r2 := rk$$
(1)

$$ProfitStar := \frac{p^4}{5 \cdot rl \cdot rk^2};$$

$$ProfitStar := \frac{p^4}{5 r l r k^2}$$
 (2)

1. b:

 $Hottlings_Lemma_SupplyFunction := simplify(diff(ProfitStar, p)); #Hottlings_Lemma_gives_supply_function.$

$$Hottlings_Lemma_SupplyFunction := \frac{4 p^3}{5 r l r k^2}$$
(3)

1.a:

Ordinary_Input_Demand_Function_x1 := simplify(-diff(ProfitStar, r1));#This is same as X1Star (Labor) from profit maximization.

$$Ordinary_Input_Demand_Function_x1 := \frac{p^4}{5 rl^2 rk^2}$$
 (4)

Ordinary_Input_Demand_Function_x2 := simplify(-diff(ProfitStar, r2));#This is same as X2Star (Capital) from profit maximization.

$$Ordinary_Input_Demand_Function_x2 := \frac{2 p^4}{5 r l r k^3}$$
(5)

1. c:

 $Own_Price_Effect_Labor \coloneqq diff(Ordinary_Input_Demand_Function_x1\ , r1);$

$$Own_Price_Effect_Labor := -\frac{2 p^4}{5 r l^3 r k^2}$$
 (6)

 $Own_Price_Effect_Capital := diff(Ordinary_Input_Demand_Function_x2, r2);$

$$Own_Price_Effect_Capital := -\frac{6 p^4}{5 r l r k^4}$$
(7)