

Course Title: Linear Algebra

Credit: 3

Course CSIT.123

Nature of the Course: Theory

Total hours: 45

Year: First, Semester: Second

Level: B.Sc. CSIT .

1. Course description

The course intends to enable the students to understand the basics of linear algebra. In this course students will be able to study linear equation and matrices, linear transformation, vector space. At the same time students get much idea about matrix algebra, Eigen values and Eigen vectors.

2. Course objectives

The general objectives of the course are as follows:

- To acquaint the students with basics of linear algebra.
- To enable the students, to understand the concept of linear equation, and its solution.
- To know the basic concept of Eigen values and Eigen vectors and its further application.

Specific objectives and contents

Specific Objectives

Unit 1: Linear equation & Matrices

- 8 hou

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| • Define system of linear equations | 1.1 | System of linear equations |
| • Give the concept of row reduction and Echelon form and example. | 1.2 | Row reduction and Echelon form |
| • Define the vector equation. | 1.3 | vector equation |
| • Discuss the matrix equation of the form $Ax = b$ and its solution. | 1.4 | The matrix equations $Ax = b$ |
| • Explain the meaning of solution set of linear equation. | 1.5 | Solution set of linear system |
| | 1.6 | Linear independence |

Unit 2: Matrix Algebra

- 6 hou

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| • Define linear independence and Examples. | 2.1 | Matrix operation |
| • Discuss the inverse of a matrix. | 2.2 | The inverse of a matrix |
| • Discuss the characterization of invertible matrix. | 2.3 | Characterization of invertible matrices |
| • Explain partitioned matrices. | 2.4 | Partitioned matrices |
| • Discuss Leontief input output model and its application to computer graphics. | 2.5 | The Leontief input output model |
| | 2.6 | Application to computer graphics |

Unit 3: Vector Spaces

- 8 hou

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| • Define the meaning of vector spaces and its various examples. | 3.1 | Definition and examples |
| • Define vector subspace and examples. | 3.2 | Vector subspaces |
| • Explain the term linear combination, linear dependence and independence. | 3.3 | Linear combination, linear dependence independence |
| • Define Basis and dimension of vector space. | 3.4 | Basis and dimension of a vector space. |
| • Compute the row rank and column rank of a matrix. | 3.5 | Row and Column space of a matrix. |
| | 3.6 | Row rank and column rank. |

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| <ul style="list-style-type: none">• Define linear transformation and how this concept used in matrix?• Discuss the term Kernel and Image of linear transformation.• Compute Kernel and Image of any function.• State and prove Rank Nullity theorem and some examples related to this.• Define linear isomorphism.• State the meaning of $L(V, N)$ how it is vector space?• Discuss the matrix of linear transformation.• Give the concept of Euclidian space and define dot product.• Discuss the general inner product space.• Define the term orthogonality, orthogonal projection and orthogonal basis.• Discuss Gram-Schmidt orthogonalization process.• Define orthogonal transformation.• Define Eigen values and Eigen vectors.• Define characteristics equation.• Discuss the term diagonalization.• Obtain the relation between linear transformation and Eigen vectors.• Define Complex Eigen values.• State Caley Hamilton theorem | <table><tr><td colspan="2">Unit 4: Linear Transformation</td><td>- 8 hours</td></tr><tr><td>4.1</td><td>Linear transformation, representation by a matrix.</td><td></td></tr><tr><td>4.2</td><td>Kernel and image of linear transformation.</td><td></td></tr><tr><td>4.3</td><td>Rank nullity theorem</td><td></td></tr><tr><td>4.4</td><td>Linear isomorphism</td><td></td></tr><tr><td>4.5</td><td>$L(V, W)$ is a vector space dimension of $L(V, W)$ (statement only)</td><td></td></tr><tr><td>4.6</td><td>The matrix of liner transformation.</td><td></td></tr><tr><td colspan="2">Unit 5: Inner Product Space</td><td>- 7 hours</td></tr><tr><td>5.1</td><td>The Euclidian space & dot product.</td><td></td></tr><tr><td>5.2</td><td>General Inner product spaces</td><td></td></tr><tr><td>5.3</td><td>Orthogonality, orthogonal projection onto a line, orthogonal basis.</td><td></td></tr><tr><td>5.4</td><td>Gram-schmidt orthogonalization.</td><td></td></tr><tr><td>5.5</td><td>Orthogonal transformation.</td><td></td></tr><tr><td colspan="2">Unit 6: Eigen Values and Eigen Vectors</td><td>- 8 hours</td></tr><tr><td>6.1</td><td>Eigen values and Eigen vectors</td><td></td></tr><tr><td>6.2</td><td>The characteristic equation,</td><td></td></tr><tr><td>6.3</td><td>Diagonalization</td><td></td></tr><tr><td>6.4</td><td>Eigen vectors and linear transformation.</td><td></td></tr><tr><td>6.5</td><td>Complex Eigen values</td><td></td></tr><tr><td>6.6</td><td>Caley Hammiton theorem (statement only)</td><td></td></tr></table> | Unit 4: Linear Transformation | | - 8 hours | 4.1 | Linear transformation, representation by a matrix. | | 4.2 | Kernel and image of linear transformation. | | 4.3 | Rank nullity theorem | | 4.4 | Linear isomorphism | | 4.5 | $L(V, W)$ is a vector space dimension of $L(V, W)$ (statement only) | | 4.6 | The matrix of liner transformation. | | Unit 5: Inner Product Space | | - 7 hours | 5.1 | The Euclidian space & dot product. | | 5.2 | General Inner product spaces | | 5.3 | Orthogonality, orthogonal projection onto a line, orthogonal basis. | | 5.4 | Gram-schmidt orthogonalization. | | 5.5 | Orthogonal transformation. | | Unit 6: Eigen Values and Eigen Vectors | | - 8 hours | 6.1 | Eigen values and Eigen vectors | | 6.2 | The characteristic equation, | | 6.3 | Diagonalization | | 6.4 | Eigen vectors and linear transformation. | | 6.5 | Complex Eigen values | | 6.6 | Caley Hammiton theorem (statement only) | |
| Unit 4: Linear Transformation | | - 8 hours | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4.1 | Linear transformation, representation by a matrix. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4.2 | Kernel and image of linear transformation. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4.3 | Rank nullity theorem | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4.4 | Linear isomorphism | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4.5 | $L(V, W)$ is a vector space dimension of $L(V, W)$ (statement only) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4.6 | The matrix of liner transformation. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Unit 5: Inner Product Space | | - 7 hours | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 5.1 | The Euclidian space & dot product. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 5.2 | General Inner product spaces | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 5.3 | Orthogonality, orthogonal projection onto a line, orthogonal basis. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 5.4 | Gram-schmidt orthogonalization. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 5.5 | Orthogonal transformation. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Unit 6: Eigen Values and Eigen Vectors | | - 8 hours | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6.1 | Eigen values and Eigen vectors | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6.2 | The characteristic equation, | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6.3 | Diagonalization | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6.4 | Eigen vectors and linear transformation. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6.5 | Complex Eigen values | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6.6 | Caley Hammiton theorem (statement only) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

Text Books and References

Text Books

- David C. Lay: Linear Algebra and its applications. 3rd Edition, Pearson Edition
- S. Lang: Introduction to Linear Algebra, second Edition. Springer verlag, New York (1986)

Reference Books

- I. Kolman, Bernard: Introductory Linear Algebra, with application, 7th Edition. Pearson Ed.
- G. Strang: Linear Algebra and its application 3rd Ed. Harcourt Brace Jovanovich Orlando (1986)