

ECE 358: Computer Networks

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- (a) Consider two nodes (computers or routers), A and B, that have been connected by means of a single optical fibre link of length 2500 kilometers. Assume that optical signal propagates over the link at the speed of 2.5×10^8 m/s (meter/sec), and the link speed is 2 Mbps. If computer A is sending a frame of length 1,000 bytes to B, how long does it take the frame to be completely copied from A to B?

Solution:

Time to completely copy a frame, $T = T_{\text{prop}}$ (time to propagate) + T_{trans} (time to transmit) T_{prop}
= Distance/ speed of signal = $2500 \text{ Km} / (2.5 \times 10^8 \text{ m/s}) = (2500 \times 10^3 \text{ m}) / (2.5 \times 10^8 \text{ m/s})$
= 10 ms.

$T_{\text{trans}} = \text{Length of a frame} / \text{Link speed} = 1000 \text{ bytes} / 2 \text{ Mbps} = (1000 \times 8 \text{ bits}) / (2 \times 10^6 \text{ bps})$
= 4 ms.

Therefore,

$$T = 10 \text{ ms} + 4 \text{ ms} = 14 \text{ ms.}$$

It takes **14 ms** to completely copy a frame of 1000 bytes from A to B.

- (b) Assume that a computer, A, is transmitting a frame to another computer, B, at a link speed (i.e., transmission rate) of 100 Mbps; the length of the CAT6 cable between A and B is 100 meters, and signal travels at the speed of 2×10^8 meters/sec in the cable. Compute the maximum number of bits of the frame that can simultaneously appear on the cable.

Solution:

T_{prop} (time to propagate) = Cable Length / speed of signal = $100 \text{ m} / (2 \times 10^8 \text{ m/s})$
= $0.5 \times 10^{-6} \text{ Sec}$

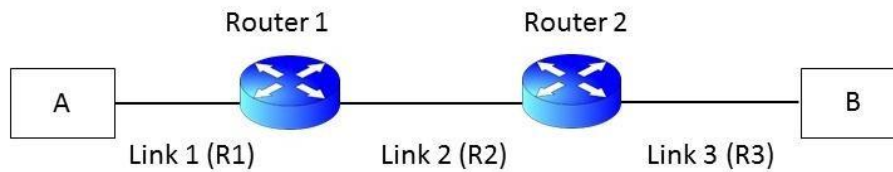
The maximum number of bits that can simultaneously appear on the cable

= The Bandwidth-delay product = $(R \times T_{\text{prop}})$

= $100 \text{ Mps} * (0.5 \times 10^{-6} \text{ Sec}) = 50 \text{ Bits}$

(c) Suppose that host A wants to send a 1 Gigabit file to host B . The network between A and B has three links (See Fig. 1.) of rates $R_1 = 4 \text{ Mbps}$, $R_2 = 2 \text{ Mbps}$, and $R_3 = 1 \text{ Mbps}$. “Giga” means 10^9 , “Mega” means 10^6 , and “Kilo” means 10^3 . Assume that the propagation delays on the three links are zero seconds. Make other assumptions as necessary and appropriate.

- I. If A sends the file as 1000-byte packets, how long does it take to move the file from A to B ? Show the details of your calculation.
- II. Also, give an approximate answer to part (I) by using the concept of bottleneck bandwidth.



Solution:

(I)

File size: 1 Gigabits

Pkt size = 1000 bytes

Given: Propagation time = 0

- Assumption: - We ignore the various headers.
- Routers have infinite buffers.
 - Processing delay is 0

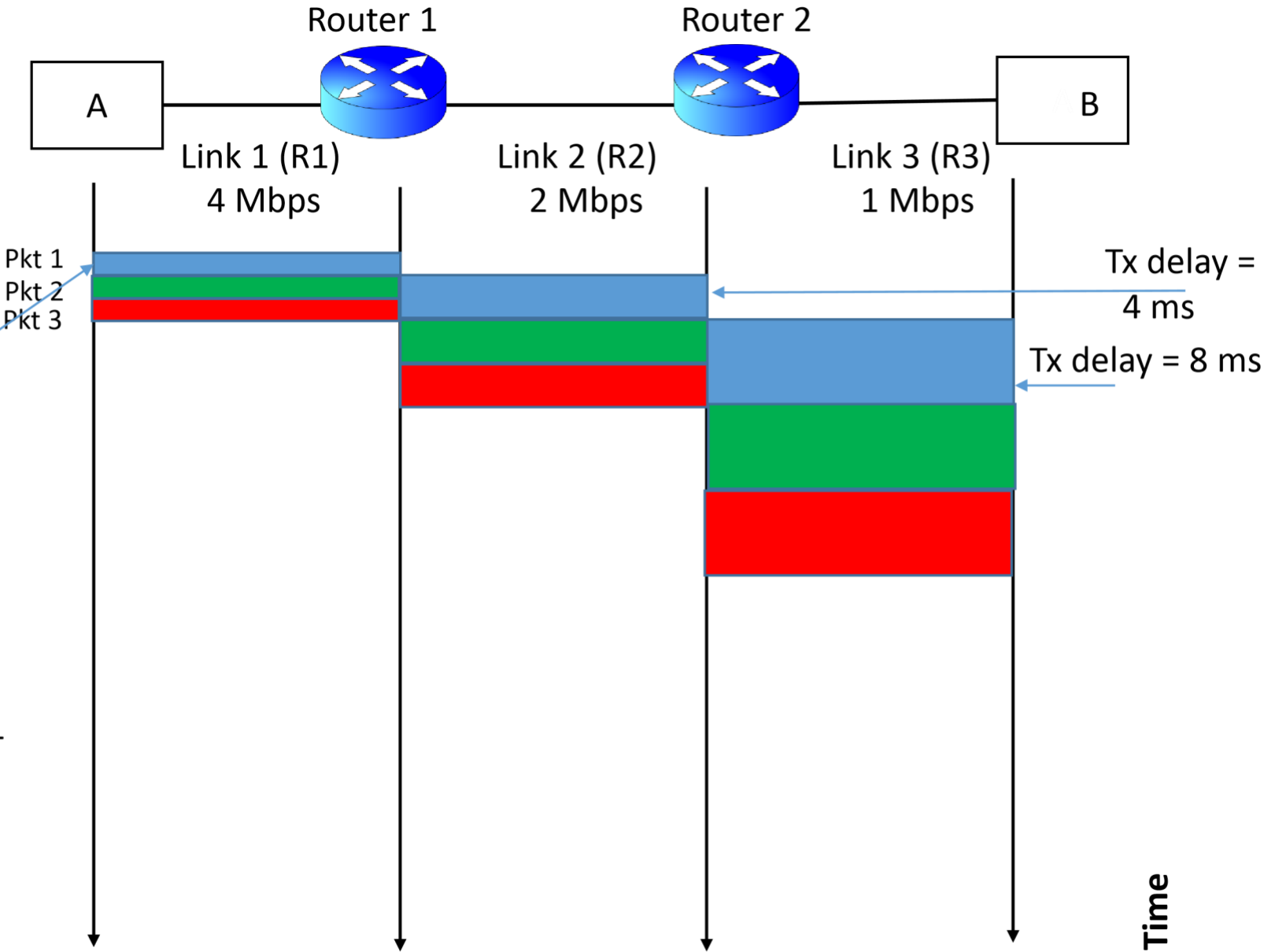
$$\begin{aligned} \text{Tx delay} &= \text{Pkt size} / \text{Tx rate} \\ &= (1000 \times 8) \text{ bits} / 4 \text{ Mbps} \\ &= 8000 \text{ bits} / (4 \times 10^6) \text{ bps} \\ &= 2 \times 10^{-3} \text{ s} \\ &= 2 \text{ ms} \end{aligned}$$

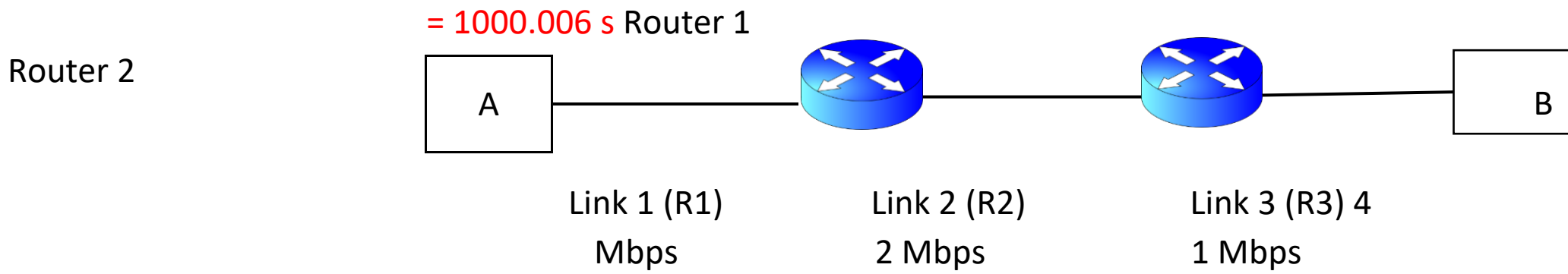
Total # of pkts is N.

File transfer time, $T_f = (N \times \text{link \#3 Tx delay}) + 2 \text{ ms} + 4 \text{ ms}$

$$\begin{aligned} N &= 1 \text{ Gigabits} / 8000 \text{ bits} = 10^9 / 8000 = 10^6 / 8 \\ &= 125,000 \end{aligned}$$

$$T_f = (125,000 \times 8 \text{ ms}) + 6 \text{ ms} = 1000 \text{ s} + 6 \text{ ms}$$





Part (ii) Also, give an approximate answer to

part (i) by using the concept of **Bottleneck link** bottleneck

bandwidth.

$$\begin{aligned}
 \text{File transfer time} &\approx \text{Total amount of data} / \text{rate of the bottleneck link} \\
 &= 1 \text{ Gigabits} / 1 \text{ Mbps} \\
 &= 10^9 \text{ bits} / 10^6 \text{ bits} \\
 &= 1000 \text{ s}
 \end{aligned}$$