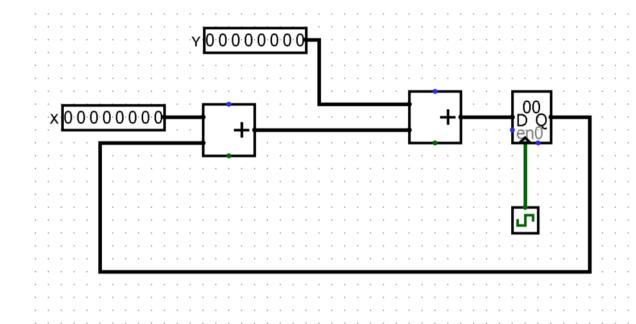
HW5.6. Adder Circuit

Feel free to check out the guide that we have prepared to help you in this problem.

Consider the following circuit:



X and Y update at each rising edge of the clock. You are given the following: the adder propagation delay is 2 ns, the register setup time is 2 ns, the register hold time is 4 ns, the register clk-to-q delay is 3 ns, and the clock frequency is 100 MHz.

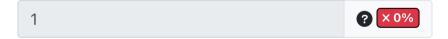
Hint: If an input updates at each rising edge of the clock, you can think of it as an output from a register with $0 \ clk-to-q \ delay$.

As a reminder, a circuit must fulfill the following conditions in order to exhibit consistently correct behavior:

$$t_{
m clk-to-q} + t_{
m shortest-combinational-path} \ge t_{
m hold}$$
 $t_{
m clk-to-q} + t_{
m longest-combinational-path} + t_{
m setup} \le t_{
m clk-period}$

Q1.1: After the rising edge of the clock, how many nanoseconds elapse before the input to the register changes?

Hint: Consider all the paths going into the register, the shortest one will induce the first input change to the register.



Q1.2: Is the hold time requirement of the register met?

Hint: Your answer to the previous question will be relevant for this one.

- (a) Yes(b) No 100%
- Q1.3: Will the circuit work properly?

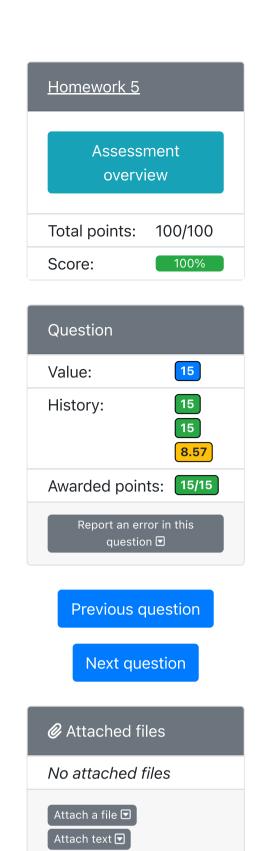
Hint: Recall that both setup and hold time inequalities should be satisfied for the circuit to work properly.

(a) Yes(b) No

Now assume that X and Y update 2 ns after each clock trigger

Hint: Now we can think of the inputs as coming from registers with clk-to-q delay of 2 ns.

Q2.1: What is the the minimum clock period needed to ensure that the system works correctly?



Hint: You would need to identify the longest combinational path delay for this one. Consider all paths that leads to the register input.

1

Q2.2: What is the maximum clock frequency at which the circuit will work properly? Express your answer in MHz.

Hint: Maximum clock frequency = 1/(minimum clock period).

1 ? × 0%

Now we want to rearrange the components of this accumulator.

For each of the following suggestions, state how it will affect the max clock frequency.

Q3.1: Swap X and Y

- (a) Increases max clock frequency
- (b) Doesn't affect max clock frequency
- (c) Decreases max clock frequency

~ 100%

Q3.2: Add X and Y first, then add the result with the output of the register Note that the current setup has input X added to the register output first before being added to Y.

- (a) Increases max clock frequency
- (b) Doesn't affect max clock frequency
- (c) Decreases max clock frequency

~ 100%

Try a new variant

Correct answer

Feel free to check out the guide that we have prepared to help you in this problem.

Q1.1: After the rising edge of the clock, how many nanoseconds elapse before the input to the register changes?

Hint: Consider all the paths going into the register, the shortest one will induce the first input change to the register.

2

Q1.1: Input Y arrives at 0 ns, so the output of that adder changes at 2 ns.

Q1.2: Is the hold time requirement of the register met?

Hint: Your answer to the previous question will be relevant for this one.

(b) No

Q1.3: Will the circuit work properly?

Hint: Recall that both setup and hold time inequalities should be satisfied for the circuit to work properly.

(b) No

Q1.2 and 1.3: We need a hold time of 4 ns but the input changes at 2ns, so the hold time requirement isn't satisfied and the circuit won't be consistent.

Q2.1: What is the the minimum clock period needed to ensure that the system works correctly?

Hint: You would need to identify the longest combinational path delay for this one. Consider all paths that leads to the register input.

Q2.1: 3 ns clk-to-q + 2 ns adder 1 + 2 ns adder 2 + 2 ns setup = 9 ns. Note that the path from the x input takes 8 ns to resolve (2 ns input delay + 2 ns adder 1 + 2 ns adder 2 + 2 ns setup), and the path from the y input takes 6 ns to resolve (2 ns input delay + 2 ns adder 2 + 2 ns setup), so their paths are not critical.

Q2.2: What is the maximum clock frequency at which the circuit will work properly? Express your answer in MHz.

Hint: Maximum clock frequency = 1/(minimum clock period).

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Q2.2: 1/(9 ns) = 1000/9 MHz

Q3.1: Swap X and Y

- (b) Doesn't affect max clock frequency
- Q3.1: The inputs are basically the same, so this doesn't change anything.
- Q3.2: Add X and Y first, then add the result with the output of the register

 Note that the current setup has input X added to the register output first before being added to Y.
- (a) Increases max clock frequency
- Q3.2: Adding the two inputs first allows that addition to be done in parallel with the clk-to-q delay, so we reduce the length of the critical path.

