

Project 1

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Abstract—

We develop a classification model that allows to determine whether the decay observed corresponds to a Higgs Boson particle or to another one. We propose a boosted linear regression model and a logistic one. For the former, we estimate the vector of weights using least squares method which aims to minimize the MSE (Here describe the boosted model!!). For the latter, we use the maximum likelihood method modified by adding a random vector. This modifications avoids convergence to local minima. Additionally, we only update the weights if we have an improvement of the loss function.

I. INTRODUCTION

The aim of this project is to develop a classification model for the decay processes observed. Such that we are able to predict if they correspond either to a Higgs Boson particle or to another one. For this purpose, we propose to use a boosted linear regression model and a logistic one. For the former, we estimate the vector of weights using least squares method which aims to minimize the MSE (Here describe the boosted model!!). For the latter, we use the maximum likelihood method. For the maximization of the likelihood we use Gradient Descent that we modify by adding a standard gaussian d-dimensional vector which allows to avoid to be converge to local minima. Additionally, we only update the weights if we have an improvement of the loss function. Results ..., Conclusions...

II. THE MODEL

In order to estimate the likelihood that an event signature is the result of a High boson process, we model the data using a boolean variable called $y_i, \forall i \in \{1, 2, \dots, 2500\}$ as:

$$y_i = \begin{cases} 1, & \text{if } prediction_i = b \\ 0, & \text{otherwise} \end{cases},$$

Since the expectation of a boolean variable is equal to the probability that the variable is equal to 1, we can model the probability that the event is the result of a High Boson process with a linear model:

$$p_w(y_i = 1 | \mathbf{x}_i) = E(y_i | \mathbf{x}_i) = \mathbf{x}_i' w$$

Where \mathbf{x}_i is a vector of D attributes considered in the regression and $w \in \mathbb{R}^D$ are the weights. However, as it is well known the biggest pitfall of this model is the fact that the estimated probability is out of the boundaries of the closed interval (0, 1). In order to address the problem mentioned, we use the

logistic regression. This model lies within the framework of a Generalized Linear Model. In this case, the probability of having a HB process is modeled as following:

$$p_w(y_i = 1 | \mathbf{x}_i) = \frac{\exp(\mathbf{x}_i' w)}{1 + \exp(\mathbf{x}_i' w)}$$

For purposes of simplicity and because it is well known, we don't present the expression of the likelihood of the model.

III. METHODS

In the previous section, we have presented the models that we used. Now, we will describe the methods employed for the estimation of the vector of weights w . Since we have two different models, the estimation technique will be different. For the linear regression model, we use Ordinary Least Squares method aiming to minimize the MSE. For this, we used the normal equations and the closed form solution for the weights. For the logistic regression model, we aim to maximize the likelihood. For this we used Gradient Descent. We modified the gradient descent method by adding a d-dimensional gaussian random vector such that we avoid convergence to local minima.

$$w^{m+1} = w^m - \lambda \nabla l(w^m) + v^{m+1}$$

with $v^{m+1} \sim d - \text{Gaussian}(0, I)$. Where I is a DxD identity matrix and 0 a vector of zeros in \mathbb{R}^D . Moreover, we add the condition that we will update the weight in each iteration only if the loss function is lower than in the previous step. While it is true that adding this condition increases the computational burden, the benefit is that we improve our prediction results since we reach better convergence.

IV. THE DATA

In this section, we will discuss the data used to test and compare the models that mentioned above. Our training dataset consists of 250.000 instances for 30 features and 1 output variable. The latter indicates if the decay corresponds to a Higgs boson particle collision event or from other event. The dataset is generated from simulation which mimics the actual particle collision events in which Higgs bosons (with fixed mass 125GeV) were produced and 3 other background processes.

The set of features consist of both raw data which were measured by actual sensors and derived quantities computed from raw features. We can see the statistical description of first 5 features in table IV. We can conclude that the standard deviation is extremely high. This is why we also standardized the features. Moreover, in figure 1 we study the separability of

signal from background on a sample of 2 features. Here, it is clear that there is an overlapping thus the selection of features is important.

TABLE I
DESCRIPTIVE STATISTICS

Variable	3d Quartile	Mean	St. Dev.
mass`MMC	130.61	-49.02	406.35
mass`transverse`met`lep	73.59	49.24	35.34
mass`vis	92.26	81.18	40.83
pt`h	79.17	57.89	63.66
deltaeta`jet`jet	0.49	-708.42	454.48

Even though we have considerably large variation of features almost 70% of all events lack at least one feature. In order to solve this problem, we used an imputation method using the mean values of the respective feature. The goal is to minimize the effects of missing data.

And finally, we have applied 2 discriminative transformations. First we used polynomial terms up to second order. Secondly, we obtained the sinus and cosine of the feature. As a result, we obtained 90 features including the original ones. From this new set, we have selected the best combination of features with a forward selection method. This method consisted on an iterative process, in each iteration we chose the best regressors based on the ones that reduced MSE the most. (See figure 2)

V. RESULTS

To test and compare each 6 regression functions we need to have general testing method. First, we divided our dataset 80% for training and 20% on testing. And then, we used actual prediction error rate on testing dataset, instead of MSE or likelihood to measure model's performance. In figure 3, we can see the relationship between error rate and number of training iteration (note that least regression and ridge regression doesn't require iteration).

From the figure 3 we can see that logistic regression converges into much lower error rate (0.22) while other linear regressions converge into 0.26. However, least squares method

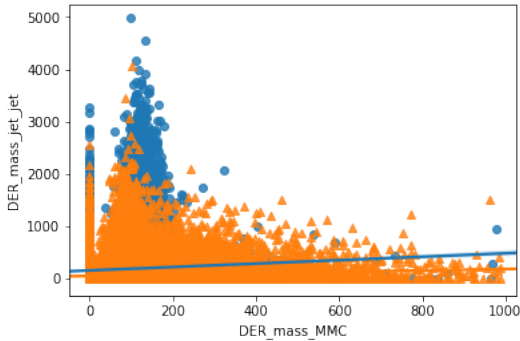


Fig. 1. Separability of the training set

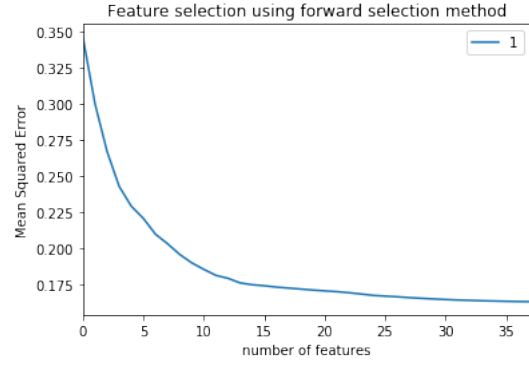


Fig. 2. Result of forward selection method

considerably high performance using much lower computational expense than that of logistics.

VI. DISCUSSION

In our approach we have used solid feature selection method which filtered most effective features from large pool. By removing outliers the best threshold value to quantize the result of regression stabilized at 0.5 in any linear regression. In addition, we compared our result with gradient boosting using least squares method. Apparently, gradient boosting converged into same result of single least squares method. Since we've proved using sigmoid function results better performance, there is possibility of improving our model much further by using different exponential functions.

VII. SUMMARY

Summarize your contributions in light of the new results.

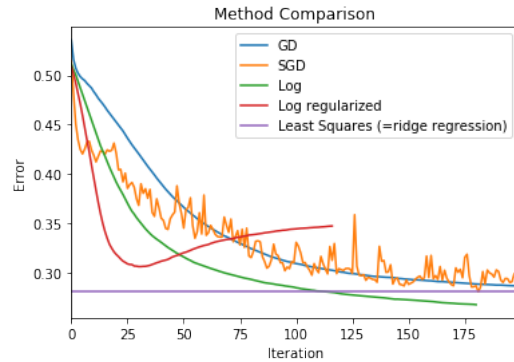


Fig. 3. Separability of the training set