

**CS 353 Fall 2024**

**Homework 5**

**Due:** November 27, Wednesday till midnight

**You will use the Moodle course page for submission of this assignment**

**Q.1 [10 pts, 5 pts each]** Given the relation schema  $R(A, B, C, D, E)$  with the set of functional dependencies  $F = \{A \rightarrow B, B \rightarrow D\}$ . Determine if the decomposition of  $R$  into  $R_1$  and  $R_2$  is lossless for each of the following cases.

(a)  $R_1(A, B, C, D), R_2(B, E)$

(b)  $R_1(A, B, D), R_2(A, C, E)$

**Q.2 [15 pts, 3 pts each]** Given the relation schema  $R(A, B, C, D, E, F, G)$ , determine if the following functional dependencies hold by the set of functional dependencies  $F = \{BD \rightarrow A, BC \rightarrow E, A \rightarrow F, B \rightarrow G, C \rightarrow D, A \rightarrow B\}$ .

(a)  $B \rightarrow A$

(b)  $A \rightarrow D$

(c)  $AD \rightarrow FG$

(d)  $AC \rightarrow D$

(e)  $BC \rightarrow F$

**Q.3 [15 pts]** Given the relation schema  $R(A, B, C, D, E)$  with the set of functional dependencies  $F = \{A \rightarrow C, B \rightarrow D, CD \rightarrow E, E \rightarrow A\}$ .

Using **only Armstrong's axioms** show that  $BE \rightarrow CD$  also holds on  $R$ .

**Q.4 [15 pts]** Given the relation schema  $R(A, B, C)$ , determine if the following two functional dependency sets on  $R$  are equivalent:

$F_1 = \{A \rightarrow C, B \rightarrow A\}, \quad F_2 = \{A \rightarrow B, B \rightarrow A, B \rightarrow C\}$

**Q.5 [20 pts]** Given the relation schema  $R(A, B, C, D, E, G)$  and a set of functional dependencies  $F = \{A \rightarrow B, AC \rightarrow D, C \rightarrow E, E \rightarrow G\}$  that hold on  $R$ .

Determine if  $R$  is in BCNF. If not, give a lossless decomposition of  $R$  into BCNF.

**Q.6 [25 pts]** Given the relation schema  $R(A, B, C, D)$  with the functional dependency set  $F = \{A \rightarrow C, BCD \rightarrow A, C \rightarrow D, B \rightarrow C, B \rightarrow D\}$ .

(a) **[10 pts]** Find a canonical cover  $F_c$  of  $F$ . Show all your work.

(b) **[15 pts]** Check if  $R$  is in 3NF. If not, decompose it into 3NF relations using the lossless and dependency preserving decomposition algorithm.