

# Next Generation Crypto

Light-weight crypto.  
Quantum-robust crypto  
Tokenization.  
Zero-knowledge.  
Homomorphic Encryption.  
zkSnarks, Range-proofs  
IPFS

Prof Bill Buchanan OBE  
<https://asecuritysite.com/>

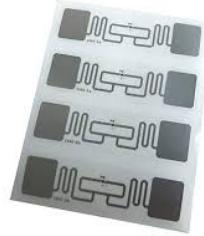


# A Computer?



# Light-weight crypto

- Conventional cryptography. Servers and Desktops. Tablets and smart phones.
- Light-weight cryptography. Embedded Systems. RFID and Sensor Networks.



Thus often light-weight cryptography methods balance performance (throughput) against **power drain and GE (gate equivalents)**. Along with this the method must also have a low requirement for RAM (where the method requires the usage of running memory to perform its operation) and ROM (where the method is stored on the device). In order to assess the strengths of various methods we often **define the area** that the cryptography function will use on the device — and which is defined in  $\mu m^2$ .

[View methods](#)

# Light-weight crypto

Cipher	Key bits	Block bits	Cycles per block	Throughput at 100 kHz (Kbps)	Logic process	Area (GEs)
Block ciphers						
Present	80	64	32	200.00	0.18 $\mu\text{m}$	1,570
AES	128	128	1,032	12.40	0.35 $\mu\text{m}$	3,400
Hight	128	64	34	188.20	0.25 $\mu\text{m}$	3,048
Clefia	128	128	36	355.56	0.09 $\mu\text{m}$	4,993
mCrypton	96	64	13	492.30	0.13 $\mu\text{m}$	2,681
DES	56	64	144	44.40	0.18 $\mu\text{m}$	2,309
DESXL	184	64	144	44.40	0.18 $\mu\text{m}$	2,168
Stream ciphers						
Trivium <sup>5</sup>	80	1	1	100.00	0.13 $\mu\text{m}$	2,599
Grain <sup>5</sup>	80	1	1	100.00	0.13 $\mu\text{m}$	1,294

\*AES: Advanced Encryption Standard; DES: Data Encryption Standard; DESXL: lightweight DES with key whitening.

function will use on the device — and which is defined in  $\mu\text{m}^2$ .

[View methods](#)

# Light-weight crypto

Cipher	Key size (bits)	Block size (bits)	Encryption (cycles/block)	Throughput at 4 MHz (Kbps)	Decryption (cycles/block)	Relative throughput (% of AES)	Code size (bytes)	SRAM size (bytes)	Relative code size (% of AES)
Hardware-oriented block ciphers									
DES	56	64	8,633	29.6	8,154	38.4	4,314	0	152.4
DESSL	184	64	8,531	30.4	7,961	39.4	3,192	0	112.8
Hight	128	64	2,964	80.3	2,964	104.2	5,672	0	200.4
Present	80	64	10,723	23.7	11,239	30.7	936	0	33.1
Software-oriented block ciphers									
AES	128	128	6,637	77.1	7,429	100.0	2,606	224	100.0
IDEA	128	64	2,700	94.8	15,393	123.0	596	0	21.1
TEA	128	64	6,271	40.8	6,299	53.0	1,140	0	40.3
SEA	96	96	9,654	39.7	9,654	51.5	2,132	0	75.3
Software-oriented stream ciphers									
Salsa20	128	512	18,400	111.3	NA	144.4	1,452	280	61.2
LEX	128	320	5,963	214.6	NA	287.3	1,598	304	67.2

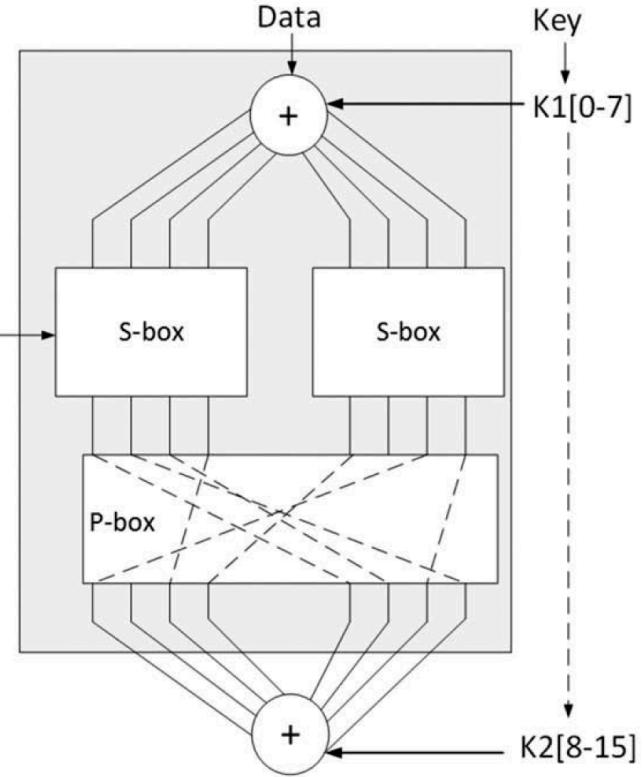
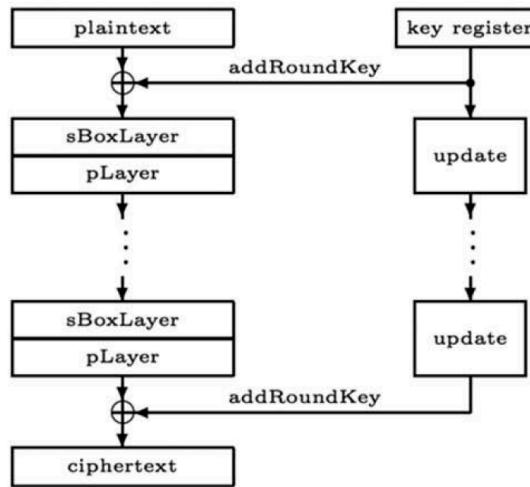
\*IDEA: International Data Encryption Algorithm; TEA: Tiny Encryption Algorithm; SEA: Scalable Encryption Algorithm.

function will use on the device and which is defined in  $\mu\text{m}$ .

View methods

# Light-weight crypto (PRESENT)

```
generateRoundKeys()  
for i = 1 to 31 do  
    addRoundKey(STATE,  $K_i$ )  
    sBoxLayer(STATE)  
    pLayer(STATE)  
end for  
addRoundKey(STATE,  $K_{32}$ )
```



$x$	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
$S[x]$	C	5	6	B	9	0	A	D	3	E	F	8	4	7	1	2

[View methods](#)

# Light-weight crypto (Finalists)

	Area ( $\mu\text{m}^2$ - synthesis over 22nm)	Area (kGE)
TinyJambu	716	3.6
Grain128-AEAD	861	4.3
GIFT-COFB	1,618	8.1
Romulus	1,961	9.8
ASCON	21,93	11
Xoodyak	2,387	11.9
Photon-Beetle	2,523	12.6
ISAP	3,080	15.4
Elephant	3,458	17.3
Sparkle	7,897	739.5

Name	Type	Variant	Underlying Primitive	State (Bits)	Key (Bits)	Mode	Rate/Block (Bits)	Tag (Bits)	Security (Bits)
Ascon	Sponge	Ascon-128 Ascon-128a	Ascon-p Ascon-p	320 320	128 128	Duplex Duplex	64 128	128 128	128
Elephant	Sponge	Jumbo Dumbo Delirium	Spongent Spongent Keccak	176 160 200	128 128 128	Elephant Elephant Elephant	176 160 176	64 64 128	127 112 127
GIFT-COFB	Block	GIFT-COFB	GIFT-128	192	128	COFB	128	128	128
Grain-128AEAD	Stream	Grain-128AEAD	N/A	256	128	N/A	1	64	128
ISAP	Sponge	ISAP-A-128 ISAP-K-128 ISAP-K-128A ISAP-A-128A	Ascon-p Keccak Keccak Ascon-p	320 400 400 320	128 128 128 128	ISAP ISAP ISAP ISAP	64 144 144 64	128 128 128 128	128
PHOTON-Beetle	Sponge	PHOTON-Beetle-AEAD[128] PHOTON-Beetle-AEAD	PHOTON256 PHOTON256	256 256	128 128	Beetle Beetle	128 32	256 256	121 128
Romulus	Block	Romulus-M Romulus-N Romulus-T	Skinny-128-384 Skinny-128-384 Skinny-128-384	384 384 384	128 128 128	COFB COFB COFB	128 128 128	128 128 128	128
SPARKLE	Sponge	SCHWAEMM256-128 SCHWAEMM128-128 SCHWAEMM192-192 SCHWAEMM256-256	SPARKLE SPARKLE SPARKLE SPARKLE	384 256 384 512	128 128 192 256	SPARKLE SPARKLE SPARKLE SPARKLE	256 128 192 256	128 128 192 256	120 120 184 248
TinyJambu	Sponge	TinyJambu	TinyJambu	128	128	TinyJambu	32	64	120
Xoodyak	Sponge	Xoodyak	Xoodoo	384	128	Cyclist	352	128	128

Elsadek, S. Aftabjahani, D. Gardner, E. MacLean, J. R. Wallrabenstein, and E. Y. Tawfik,  
 “Hardware and energy efficiency evaluation of nist lightweight cryptography standardization  
 finalists,” in 2022 IEEE International Symposium on Circuits and Systems (ISCAS). IEEE, 2022,  
 pp. 133–137.  
 H. Madushan, I. Salam, and J. Alawatugoda, “A review of the nist lightweight cryptography  
 finalists and their fault analyses,” Electronics, vol. 11, no. 24, p. 4199, 2022.

View methods

# Light-weight crypto (Finalists)

Algorithm	Impl.	Primary	Flag	Size	h(8)	h(16)	h(32)	h(64)	h(128)	Benchmark
<b>reference</b>	<i>naclref</i>	yes	O3	18774	768	768	772	1364	1968	1
sparkle	rhys	yes	O1	7912	1036	1036	1468	2272	3884	2
Xoodyak	XKCP-AVR8	yes	O3	2604	1284	1288	1924	3192	5732	2.9
knot	<i>avr8speed</i>	no	Os	1664	2124	2140	8144	8160	2.9	2
ascon	rhys	no	O3	5180	1240	1284	8056	8488	2.8	3.3
GIFT-COFB	rhys	yes	O1	23312	1852	1892	8220	8776	2.7	2.2
saeaes	ref	no	O3	17062	1208	1212	8992	9004	2.6	3.4
hyena	rhys	yes	O3	293860	1912	1964	8960	9396	2.5	2.2
elephant	rhys	no	O3	13106	1924	1948	9260	9796	2.4	2.2
estate	ref	yes	O3	9434	1424	1448	10276	10292	2.3	2.9
romulus	rhys	no	O3	19346	1632	1676	10152	10568	2.2	2.5
spook	rhys	no	O3	12942	2984	2968	10272	10708	2.2	1.4
tinyjambu	rhys	yes	O3	9174	1232	1288	10364	10888	2.2	3.4
subterranean	rhys	yes	Os	6042	3372	3460	10288	10944	2.2	1.2
orange	rhys	yes	O3	12140	2500	2536	11200	11620	2	1.7
gimli	rhys	yes	O3	21272	1920	1956	11944	12360	1.9	2.2
skinny	rhys	no	O1	12452	1604	1644	12960	14372	1.7	2.6
photon-beetle	<i>avr8speed</i>	yes	Os	3536	2444	2472	20076	20092	1.2	1.7
<b>reference</b>	rhys	yes	O2	7874	4152	4156	23812	23764	1	1
grain128aead	rhys	yes	O2	9532	3992	3980	30396	30124	0.8	1
isap	rhys	no	O2	3824	20212	20256	42936	43372	0.5	0.2

Algorithm	Impl.	Primary	Flag	Size	Enc(0:8)	Dec(0:8)	Enc(128:129)	Dec(128:128)	Bench.(128)	Bench.(8)
sparkle	rhys	yes	O3	12290	1276	1316	4648	5072	4.7	3.3
Xoodyak	XKCP-AVR8	yes	O3	4560	2596	2608	7184	7128	3.3	1.6
knot	<i>avr8speed</i>	no	Os	1664	2124	2140	8144	8160	2.9	2
ascon	rhys	no	O3	5180	1240	1284	8056	8488	2.8	3.3
GIFT-COFB	rhys	yes	O1	23312	1852	1892	8220	8776	2.7	2.2
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<b>reference</b>	rhys	yes	O2	7874	4152	4156	23812	23764	1	1
grain128aead	rhys	yes	O2	9532	3992	3980	30396	30124	0.8	1
isap	rhys	no	O2	3824	20212	20256	42936	43372	0.5	0.2

E. Bellini and Y. J. Huang, “Randomness testing of the nist light weight cipher finalist candidates,” in NIST Lightweight Cryptography Workshop, May, 2022.

View methods

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# Quantum-robust crypto

- **Lattice-based cryptography** [[Lattice](#)]—This classification shows great potential and is leading to new cryptography methods, such as for fully homomorphic encryption, and code obfuscation.
- **Code-based cryptography** [[McEliece](#)]—This classification was created in 1978 with the McEliece cryptosystem but has barely been used in real applications. The McEliece method uses linear codes that are used in error correcting codes, and involves matrix-vector multiplication. An example of a linear code is Hamming code.
- **Multivariate polynomial cryptography** [[UOV](#)]—This classification involves the difficulty of solving systems of multivariate polynomials over finite fields. Unfortunately, many of the methods that have been proposed have already been broken.
- **Hash-based signatures** [[GMSS](#)]—This classification involves creating digital signatures using hashing methods. The drawback is that a signer needs to keep a track of all of the messages that have been signed, and that there is a limit to the number of signatures that can be produced. New methods, though, integrate into Merkle Trees, which allows for the signer to use the same keys to sign multiple entities.

# Quantum-robust crypto



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NEWS

## NIST Announces First Four Quantum-Resistant Cryptographic Algorithms

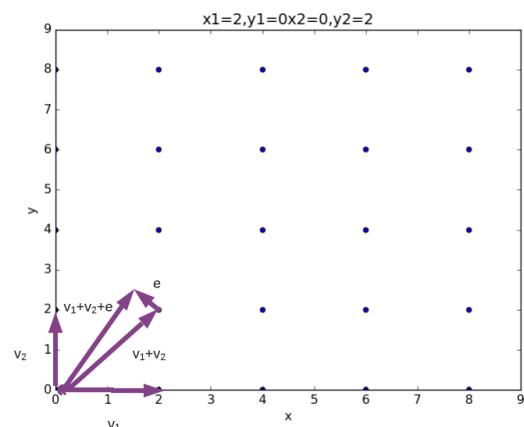
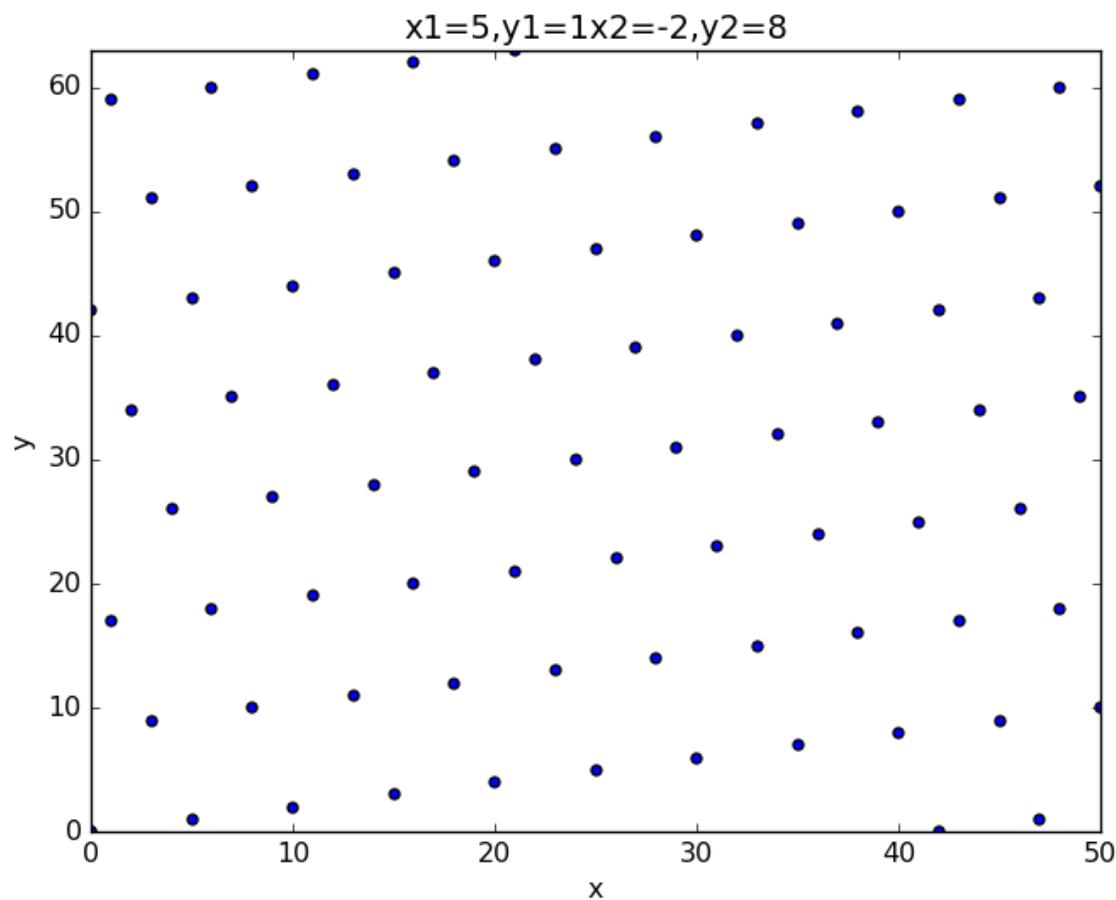
**Federal agency reveals the first group of winners from its six-year competition.**

**For general encryption**, used when we access secure websites, NIST has selected the [CRYSTALS-Kyber](#) algorithm. Among its advantages are comparatively small encryption keys that two parties can exchange easily, as well as its speed of operation.

**For digital signatures**, often used when we need to verify identities during a digital transaction or to sign a document remotely, NIST has selected the three algorithms [CRYSTALS-Dilithium](#) , [FALCON](#) and [SPHINCS+](#) (read as “Sphincs plus”). Reviewers noted the high efficiency of the first two, and NIST recommends CRYSTALS-Dilithium as the primary algorithm, with FALCON for applications that need smaller signatures than Dilithium can provide. The third, SPHINCS+, is somewhat larger and slower than the other two, but it is valuable as a backup for one chief reason: It is based on a different math approach than all three of NIST’s other selections.

# PQC Robust Crypto - Lattice

## Short Vector Problem and Closest Vector Problem



# PQC Robust Crypto – Lattice Methods (LWE)

This is a method defined by Oded Regev in 2005 [[here](#)] and is known as LWE (Learning With Errors). First we select a random series of values for our public key ( $A$ ). For example, let's select 20 random values from 0 to 100:

```
[80, 86, 19, 62, 2, 83, 25, 47, 20, 58, 45, 15, 30, 68, 4, 13, 8, 6, 42, 92]
```

Next we add create a list ( $B$ ) and were the elements are  $B_i = A_i s + e_i \pmod{q}$ , and where  $s$  is a secret value, and  $e$  is a list of small random values (the error values). If we take a prime number ( $q$ ) of 97, and an error array ( $e$ ) of:

```
[3, 3, 4, 1, 3, 3, 4, 4, 1, 4, 3, 3, 2, 2, 3, 2, 4, 4, 1, 3]
```

we generate a list ( $B$ ) of:

```
[15, 45, 2, 20, 13, 30, 32, 45, 4, 3, 34, 78, 55, 51, 23, 67, 44, 34, 17, 75]
```

The  $A$  and  $B$  list will be our public key, and  $s$  will be our secret key. We can now distribute  $A$  and  $B$  to anyone who wants to encrypt a message for us (but keep  $s$  secret). To encrypt we take samples from the  $A$  and  $B$  lists, and take a message bit ( $M$ ), and then calculate two values:

$$u = \sum(A_{samples}) \pmod{q}$$

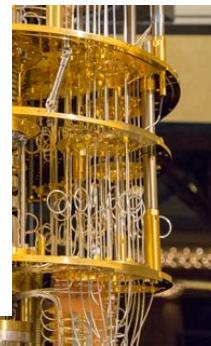
$$v = \sum(B_{samples}) + \frac{q}{2}M \pmod{q}$$

The encrypted message is  $(u, v)$ . To decrypt, we calculate:

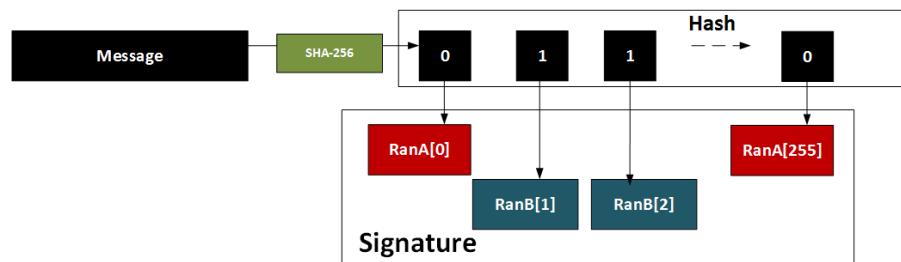
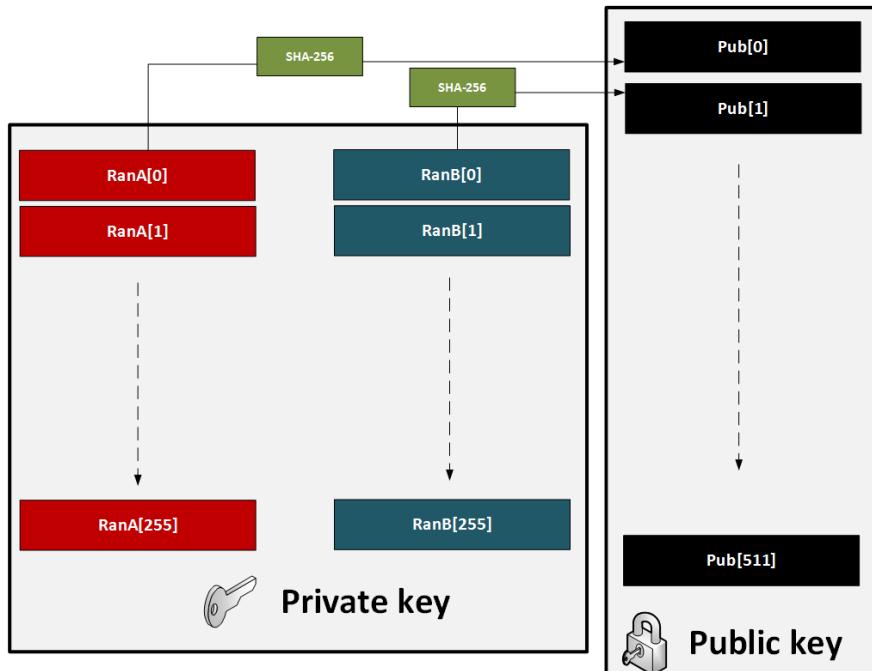
$$Dec = v - su \pmod{q}$$

If  $Dec$  is less than  $\frac{q}{2}$ , the message is a zero, else it is a 1.

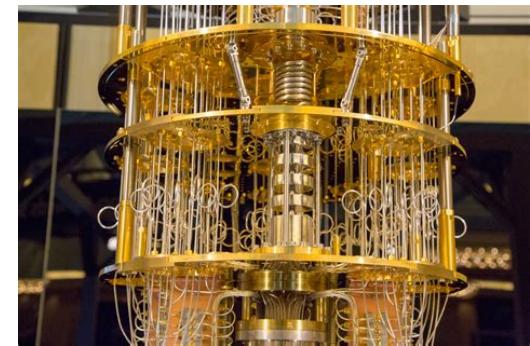
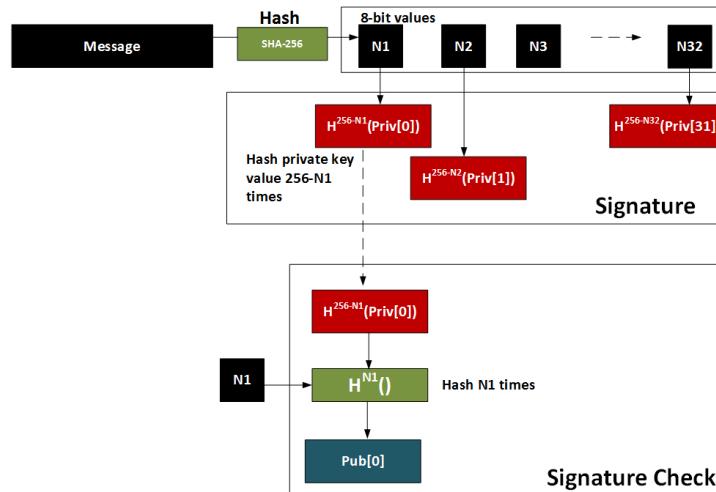
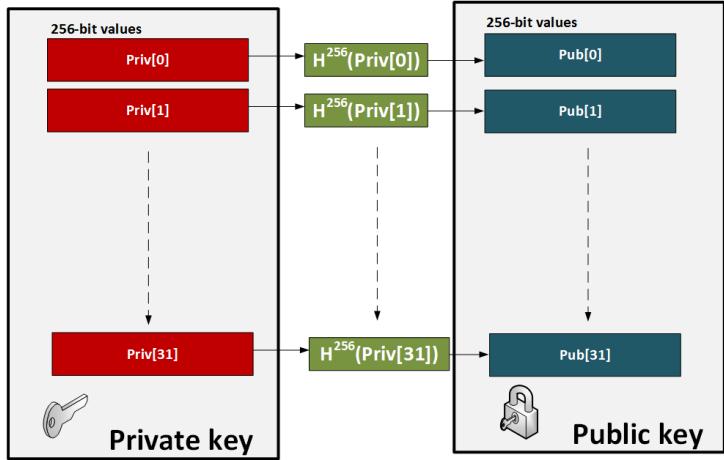
For homomophic encryption, we can perform a single-bit adder function by generating  $(u, v)$  for each of the bits and then performing (for the two values for  $bit_0$  -  $v1_0, u1_0, v2_0$  and  $u2_0$ ):



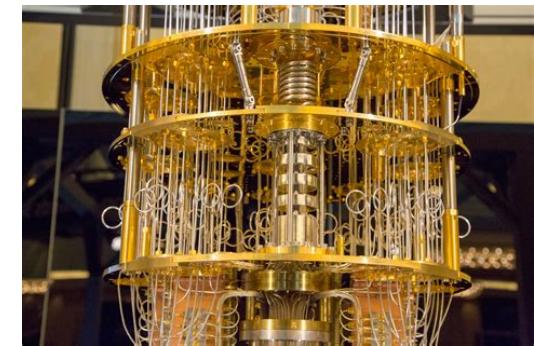
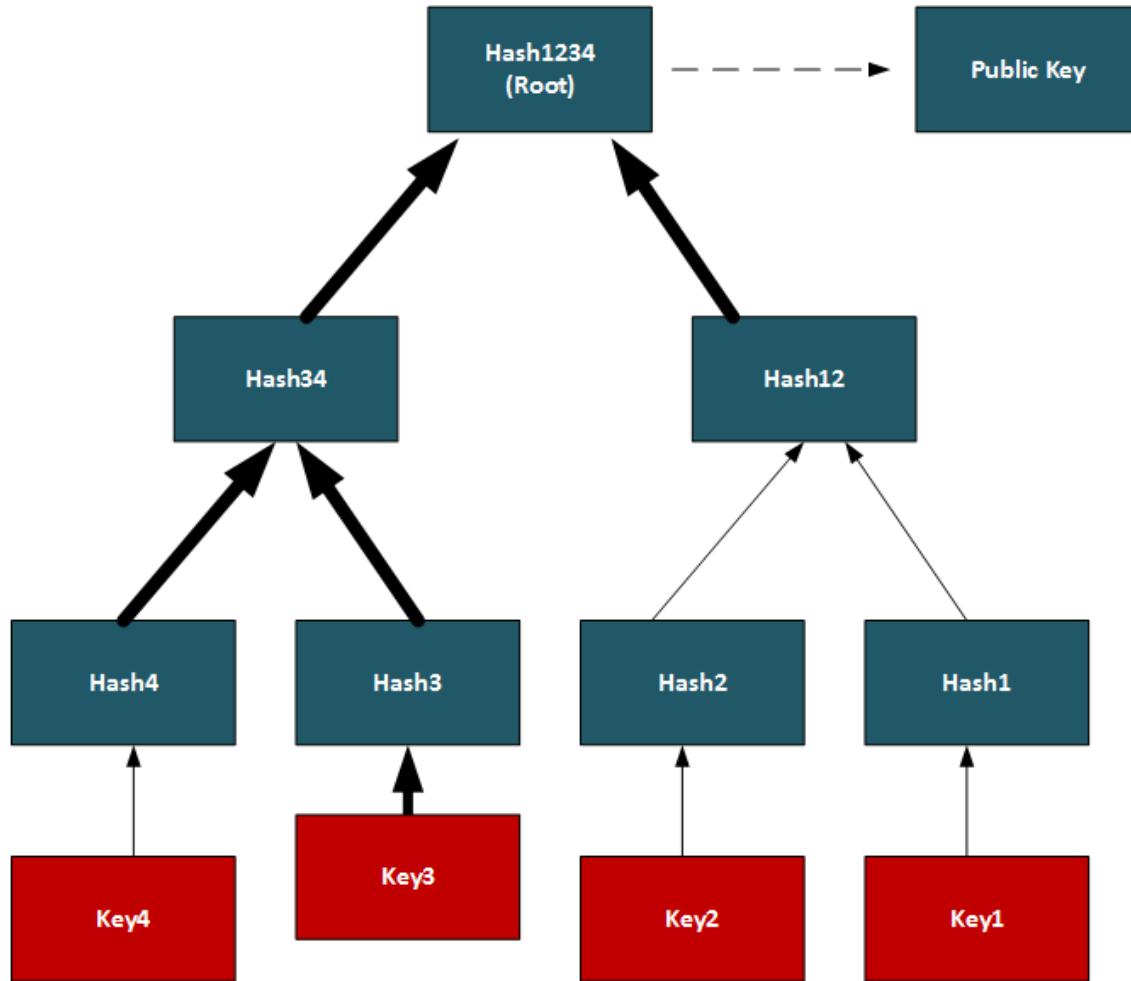
# PQC Robust Crypto – Hash-based (Lamport)



# PQC Robust Crypto – Hash-based (W-OTS)



# PQC Robust Crypto – Merkle signature scheme (MSS)



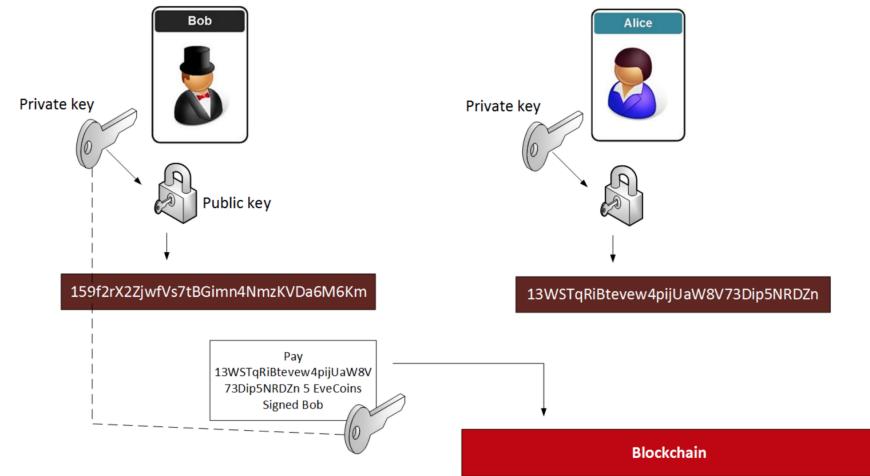
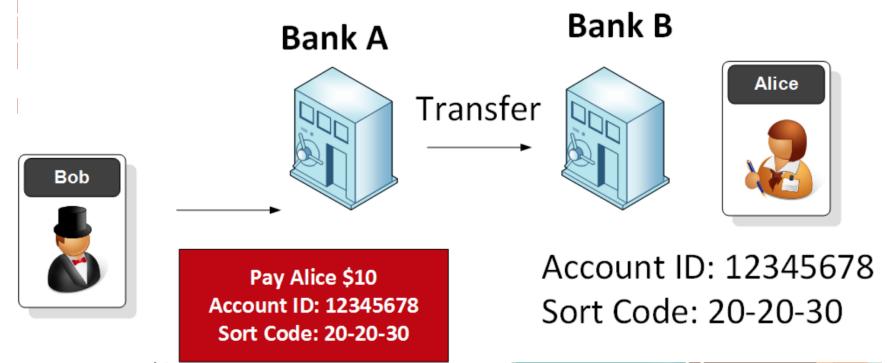
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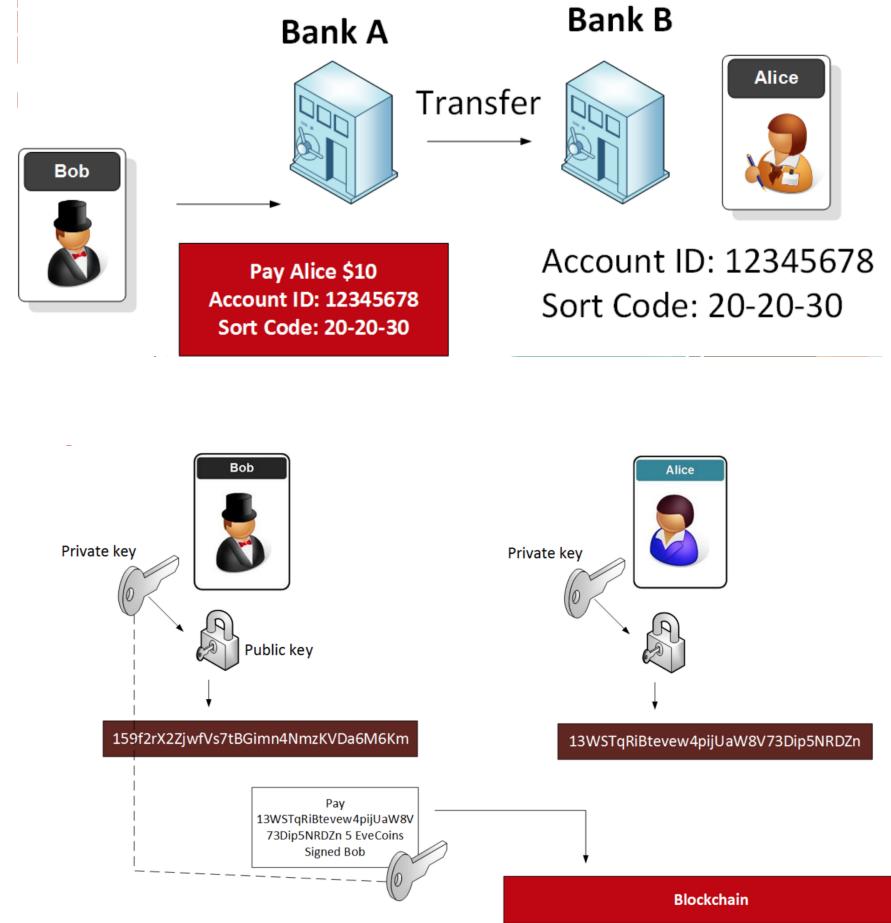
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<https://asecuritysite.com/tokens>



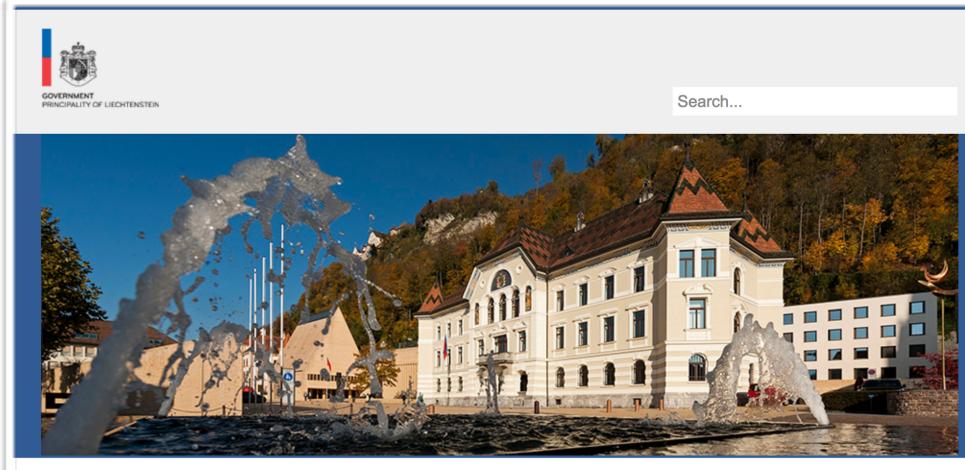
# Blockchain Act



# Blockchain Act



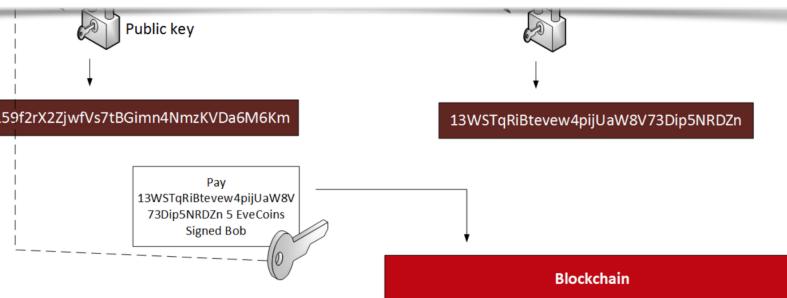
# Blockchain Act



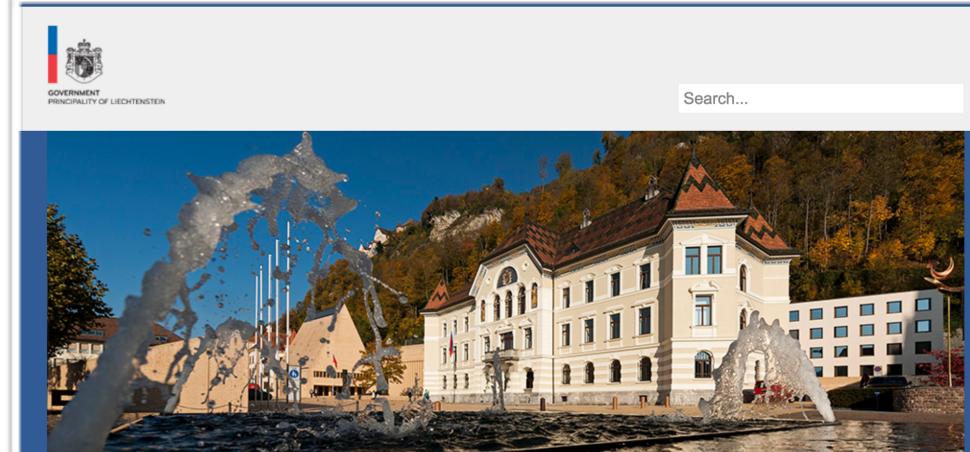
29.08.2018

## Consultation launched on Blockchain Act

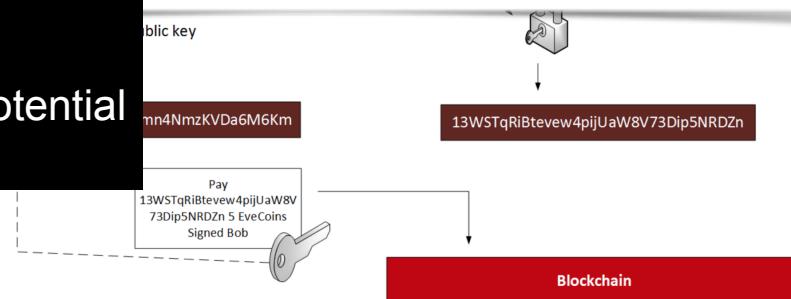
In its meeting of 28 August 2018, the Government adopted the consultation report on the Law on Transaction Systems Based on Trustworthy Technologies (TT) (Blockchain Act; TT Act; VTG) and the amendment of further laws.



# Blockchain Act



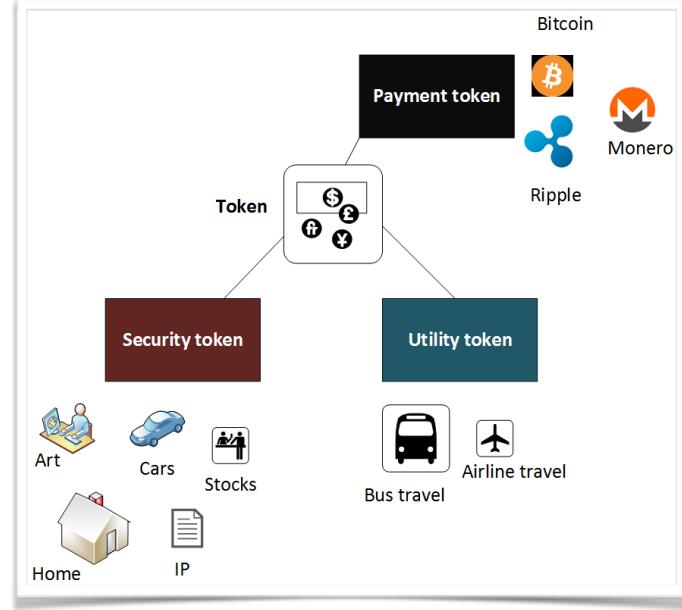
enable the transformation of the ‘real’ world to blockchain systems while ensuring legal certainty, thereby opening up the full application potential of the token economy.



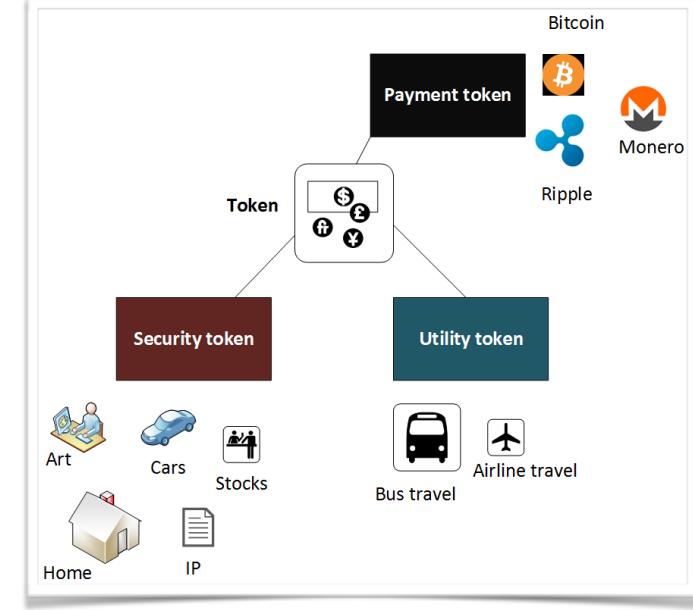
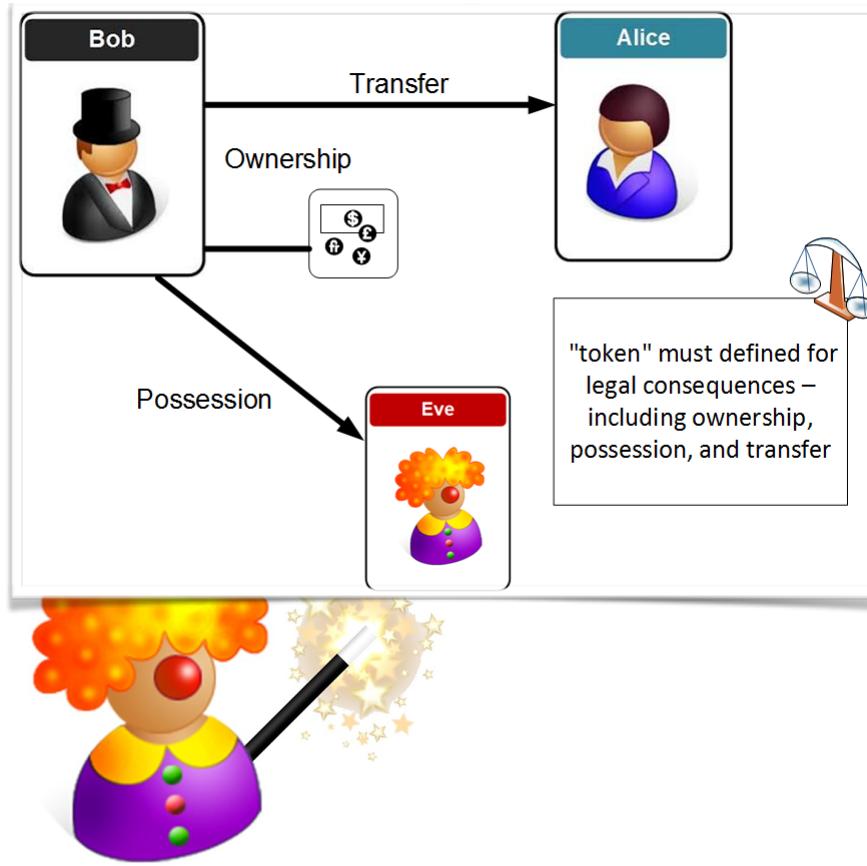
# Blockchain Act



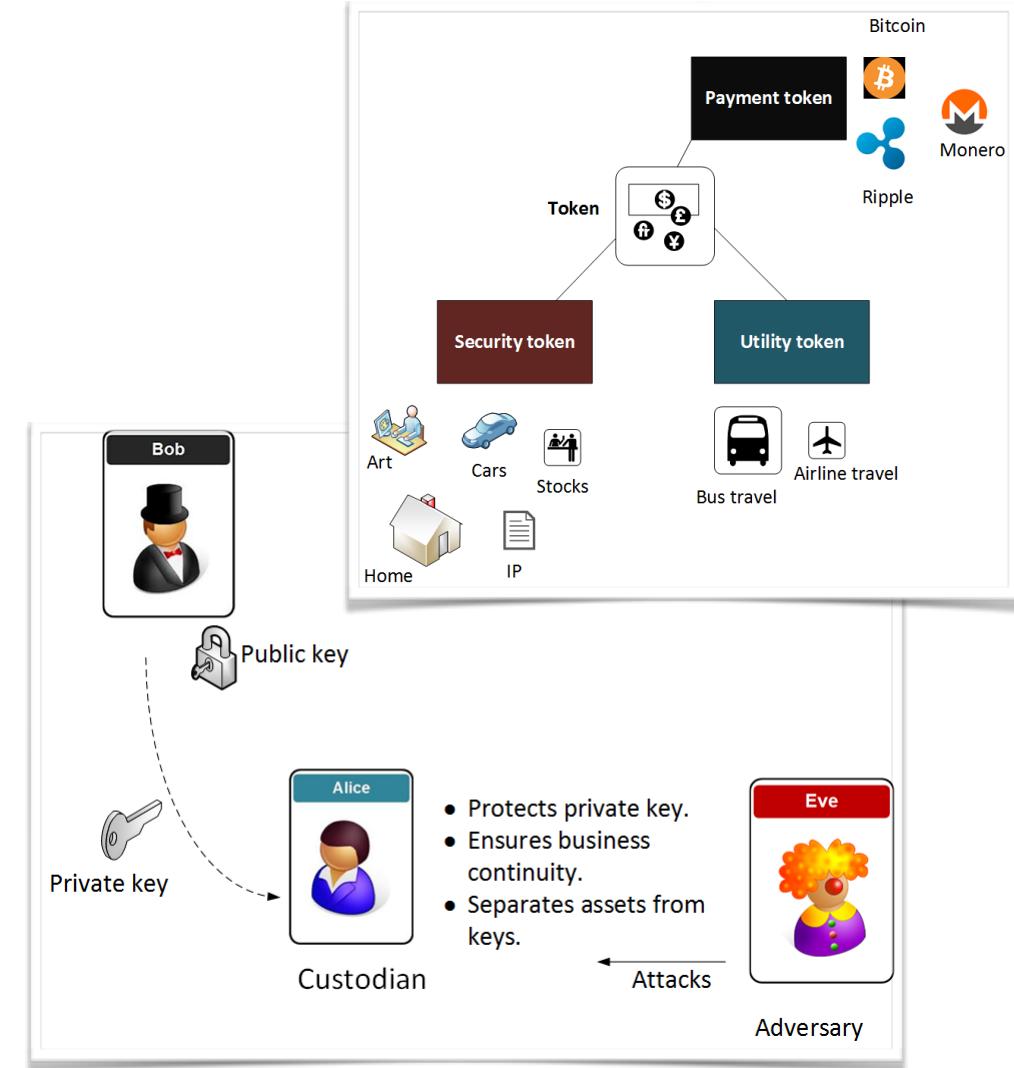
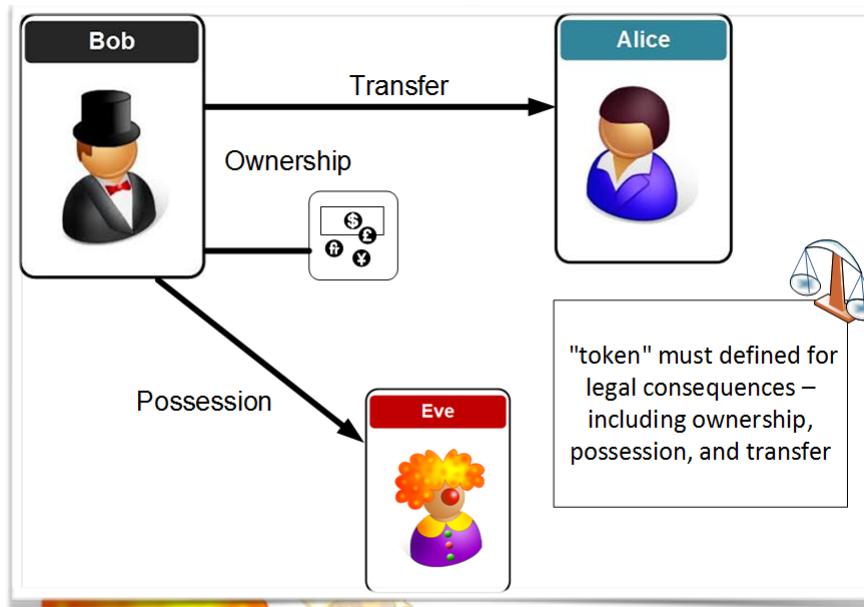
# Blockchain Act



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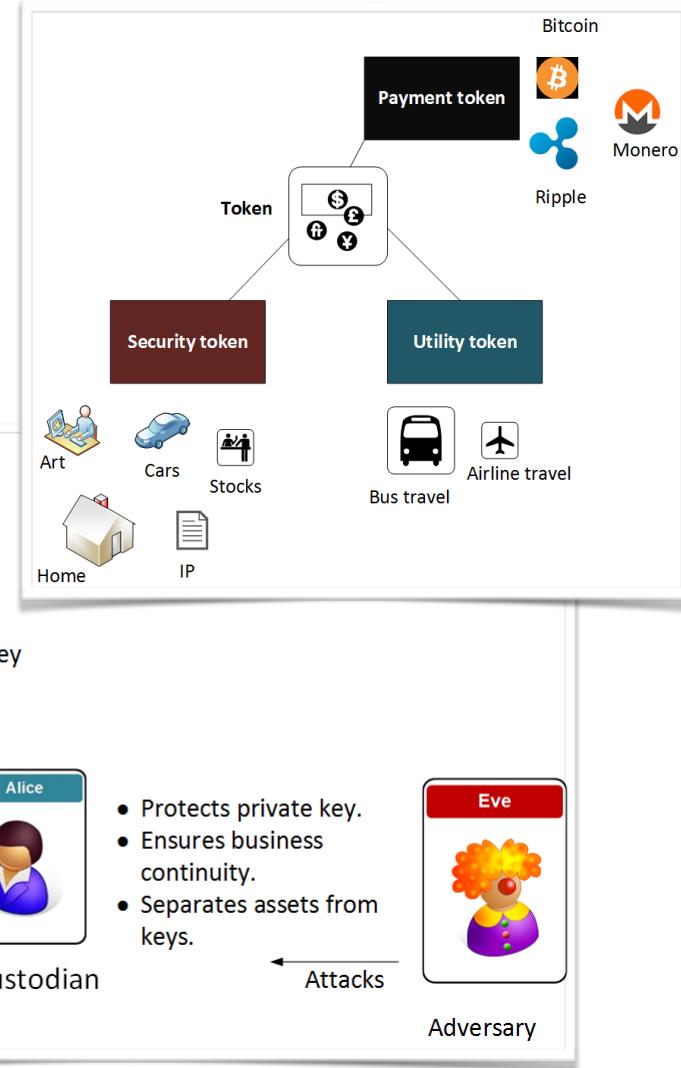
**Definitions (Art. 3 VE-VTG):** This defines a token as something that defines claims of a person to the rights to goods.

**Rights of disposal (Art. 6 ff. VE-VTG):** This defines the rights to transfer tokens, and is normally defined by the owner of a private key signing the transaction. A disposition is defined as the transfer of the disposition authorization on the token. Within the Act, it is defined that a buyer has the rights to dispose of a token, even if the seller was not authorized to dispose of the same token.

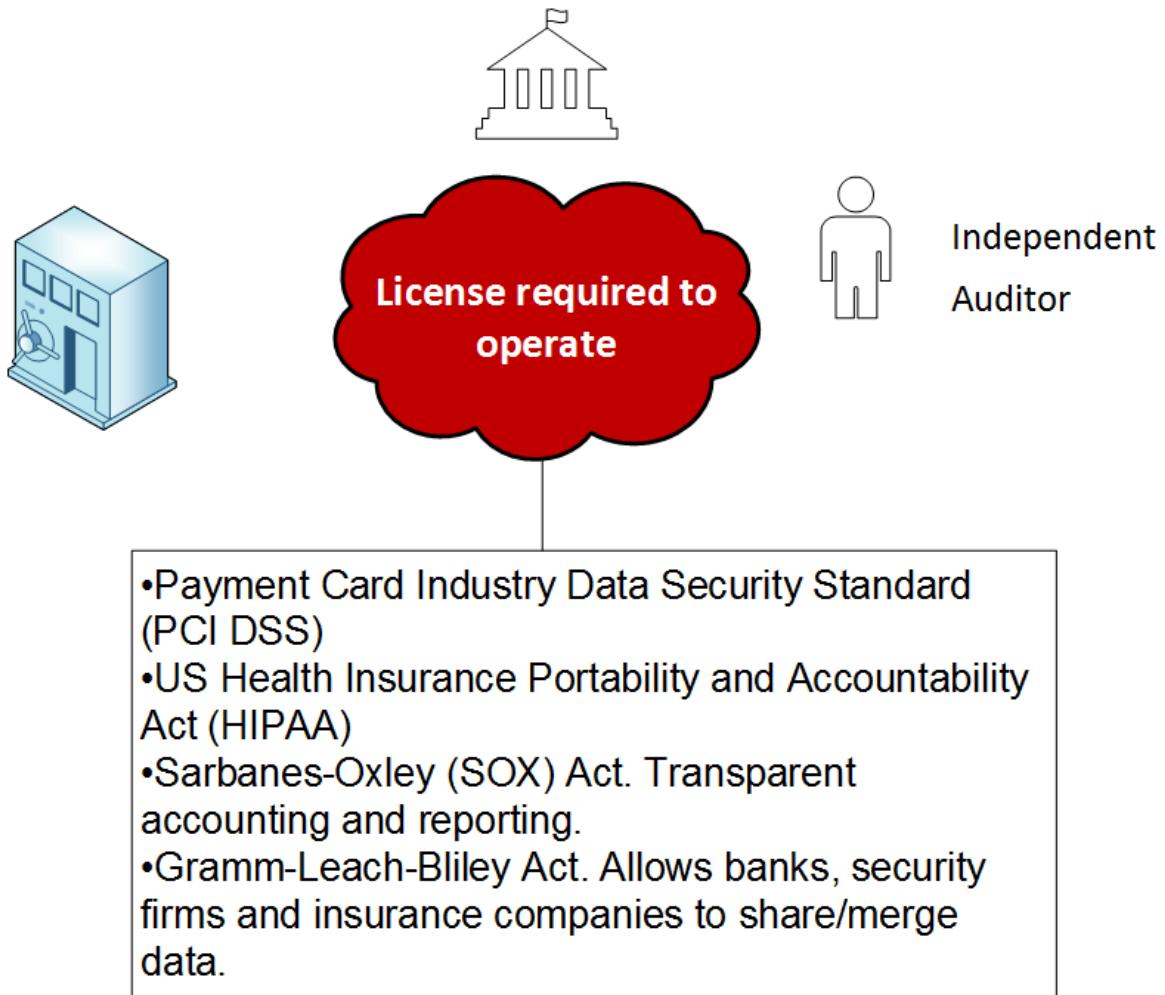
**Requirements for VT service providers (Art. 13 ff. VE-VTG):** This defines the entities who will perform services within the VT. These entities must provide an organisational structure, control mechanisms and a minimum amount of capital.

**Basic information on the issuance of tokens (Art. 28 ff. VE-VTG):** This defines the assurance in the issuing of tokens and their legal requirements. They must provide a minimum amount of information, such as the technology used, the purpose of the token, and any risks. There should be at least 10 years of issuance, and to also prevent token cloning, along with prevention of a token not being released with the same rights.

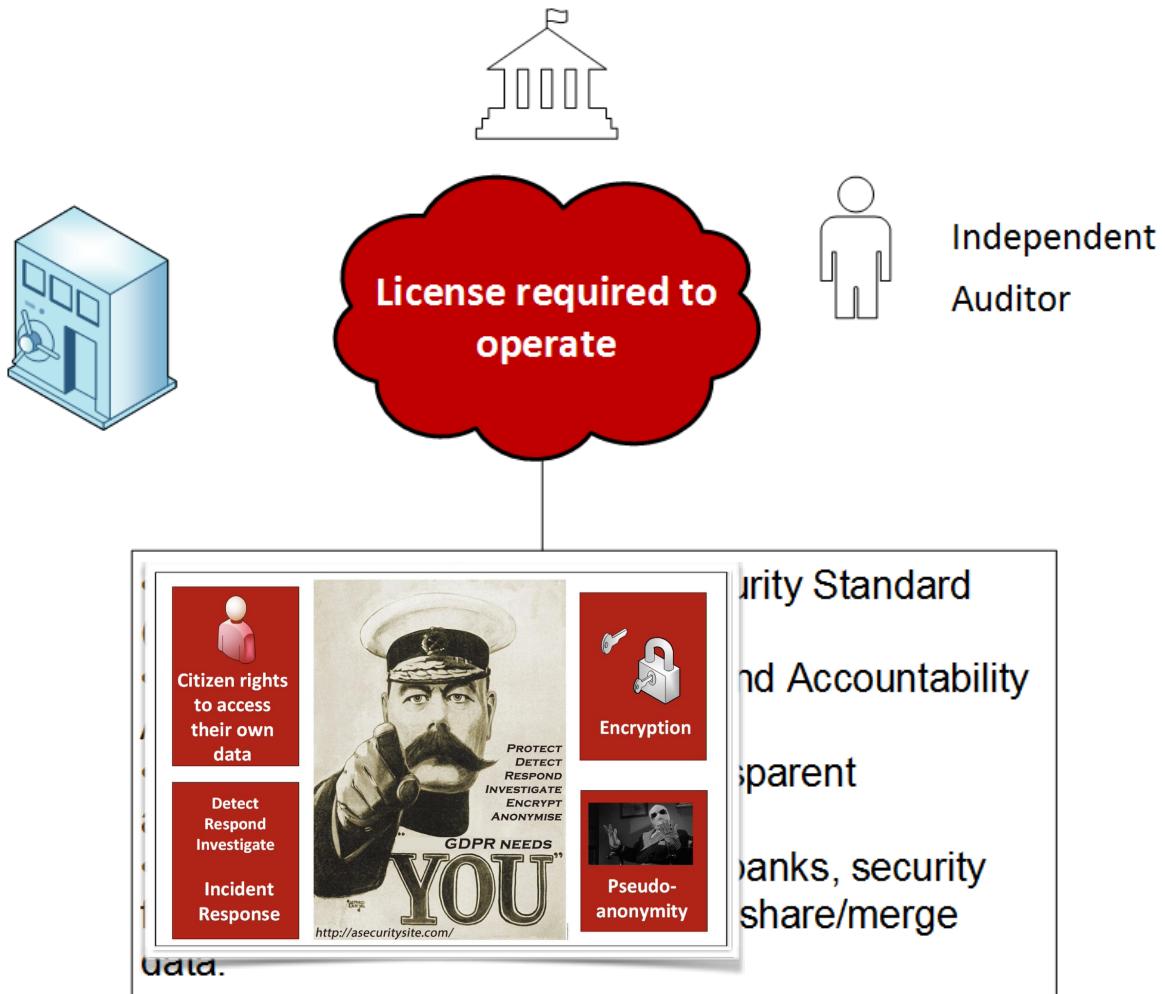
**Obligation to register (Art. 36 ff. VE-VTG):** This defines that service providers



# Audit Compliance



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# Surrogate identifiers

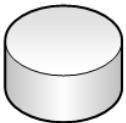
## Personally Identifiable Information (PII)



PAN – Primary  
Account Number

ID=543 611 041

Name: Bobby Smith  
Address: 10 Eve Row  
Date of Birth: 5/5/55



Surrogate mapping  
table

Real

Surrogate

ID=543 611 041

ID=741 534 011

ID=533 841 943

ID= 666 001 845

## Transactions



Surrogate  
Identifier

ID=741 534 011

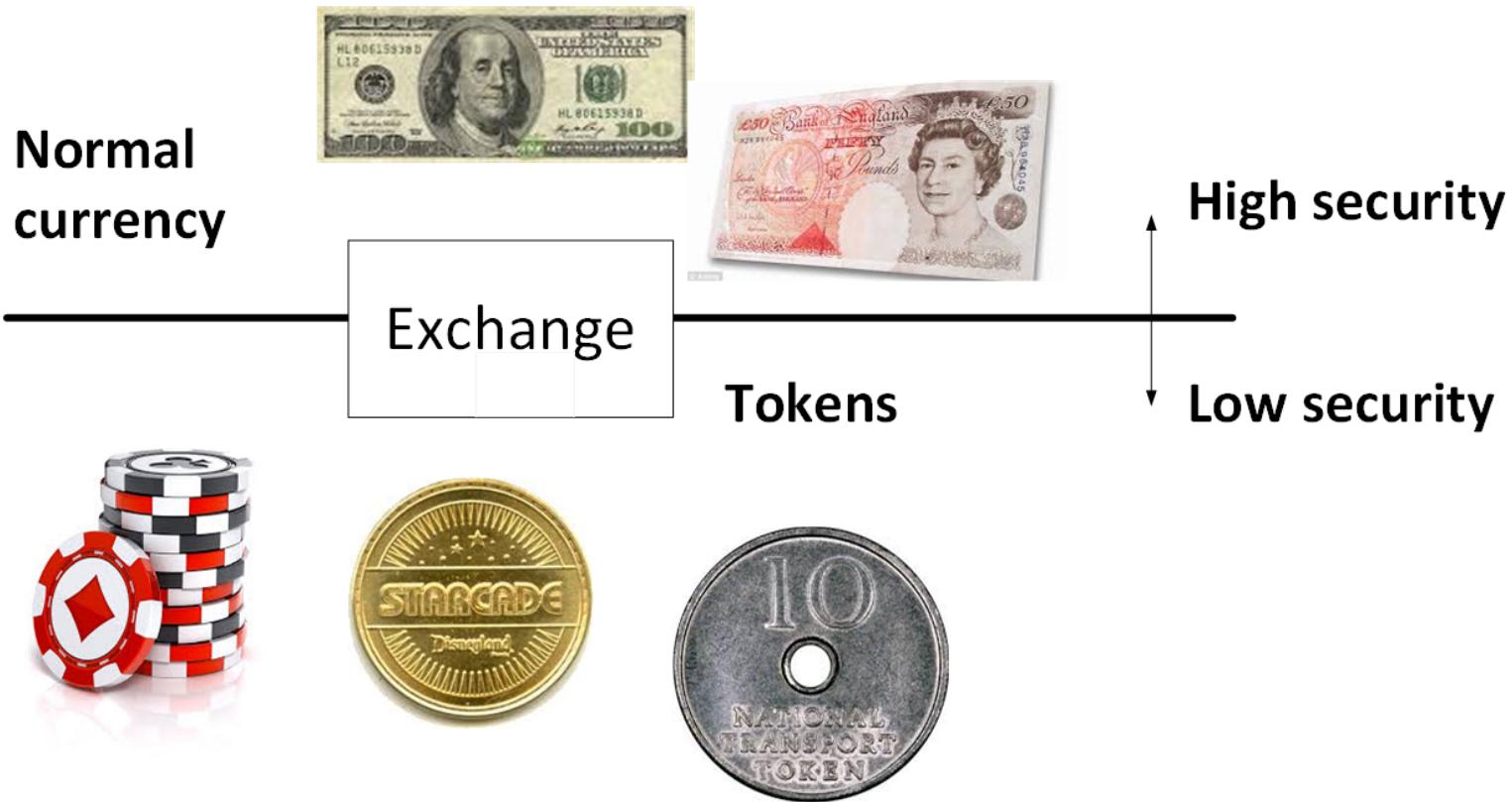
ID

ID	Transaction
741 534 001	Pay 666 001 845 \$10
532 550 423	Pay 741 534 011 \$190

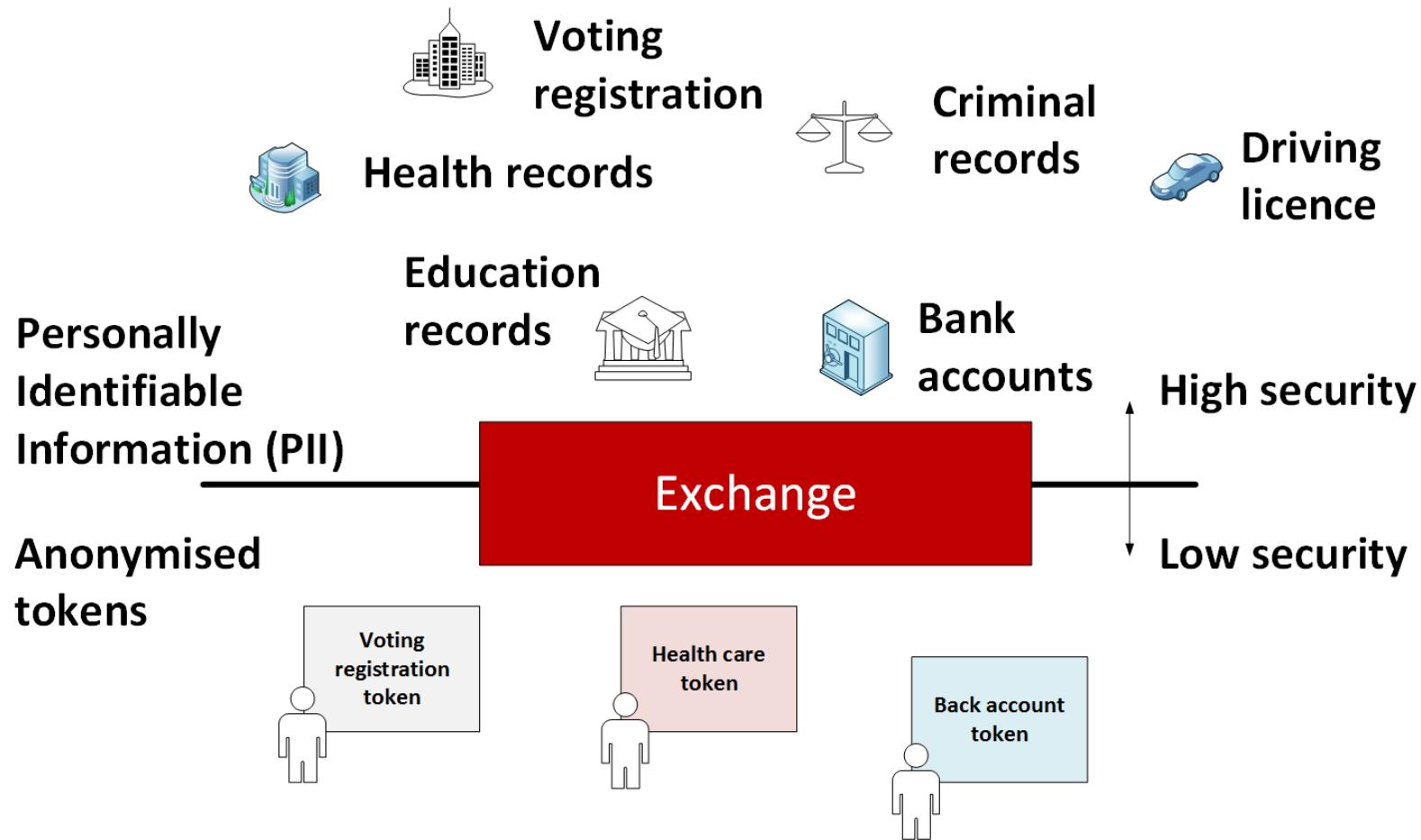
Transaction



# Tokenization with currency

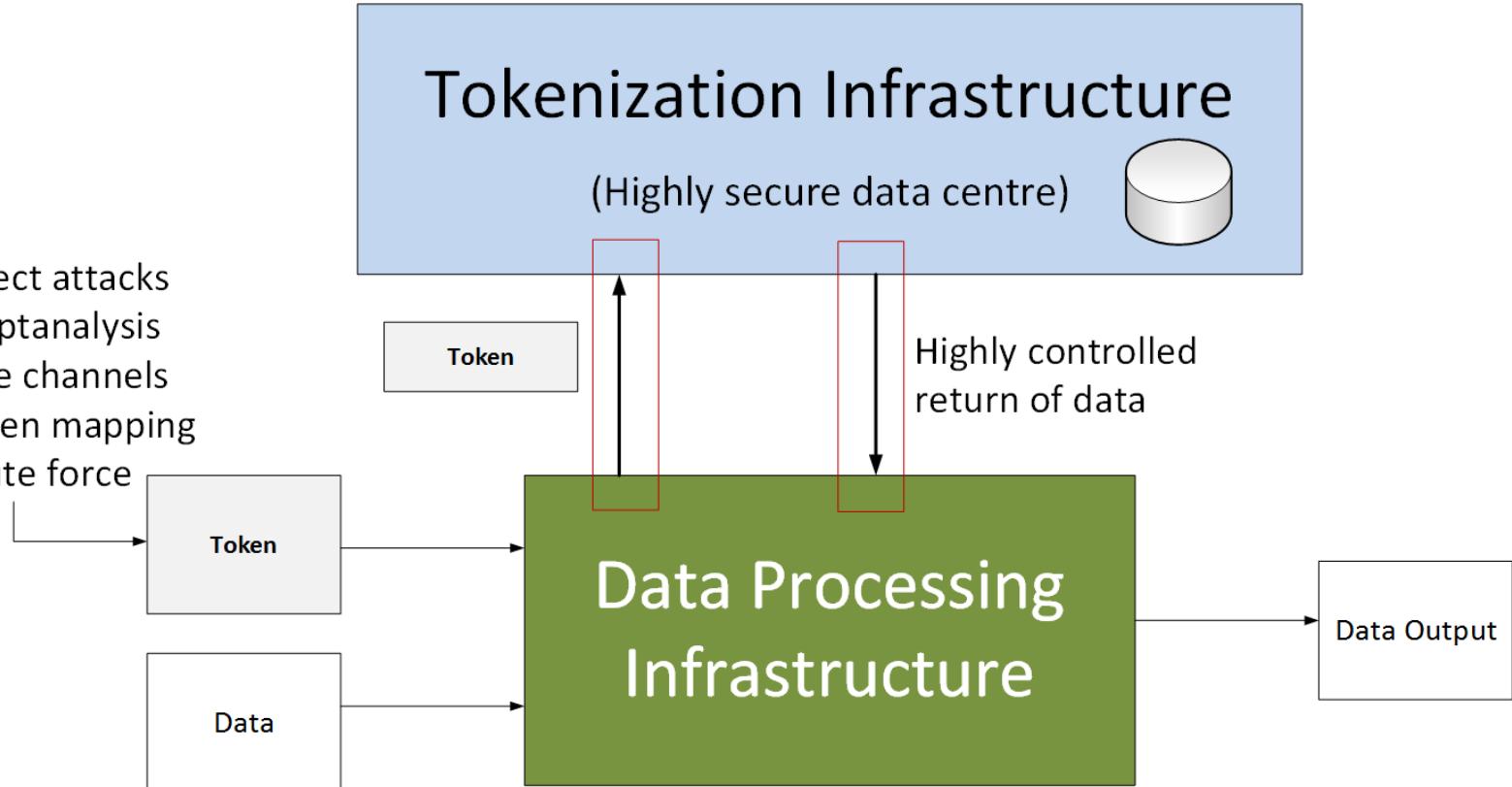


# Tokenization with data

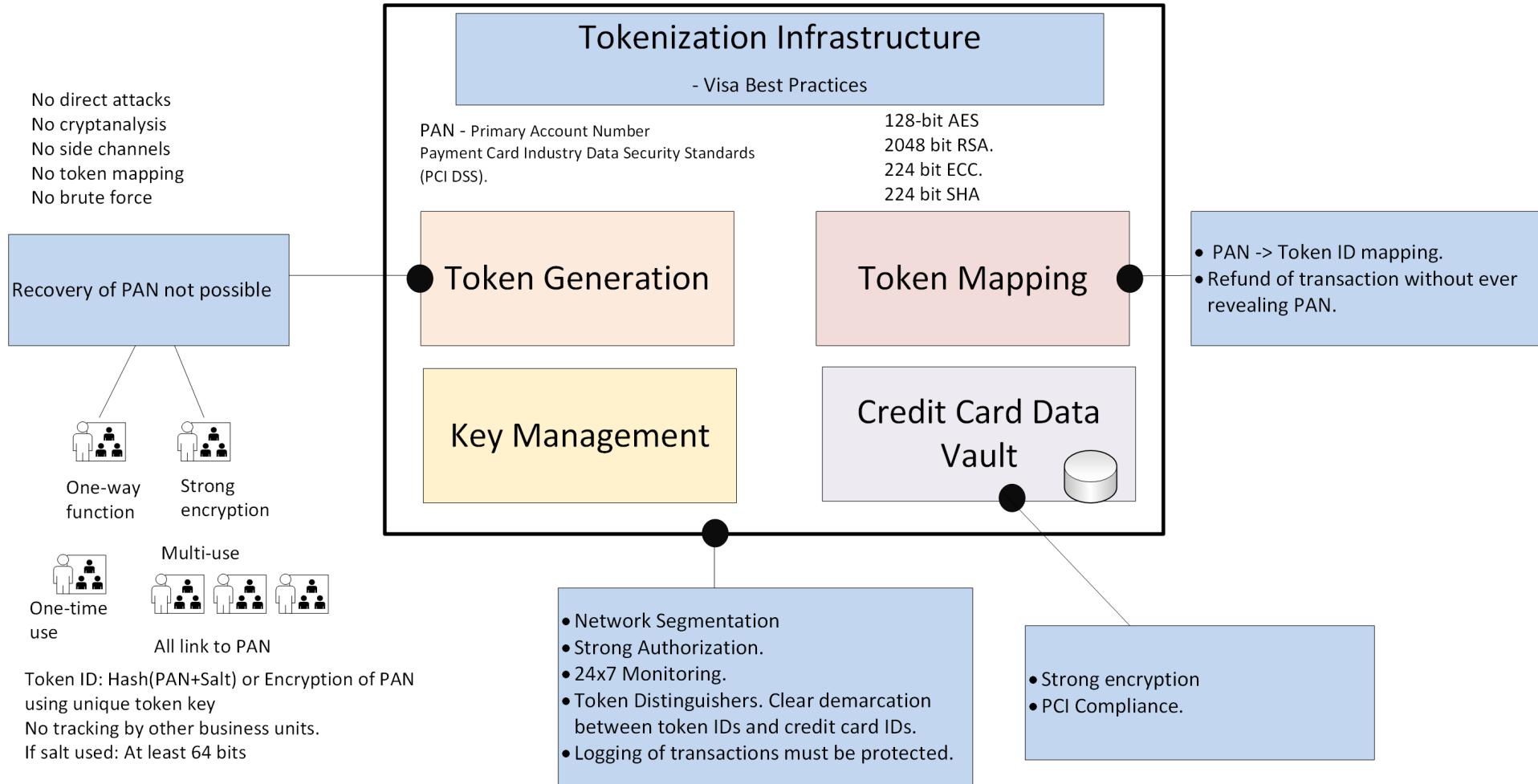


# Tokenization with data

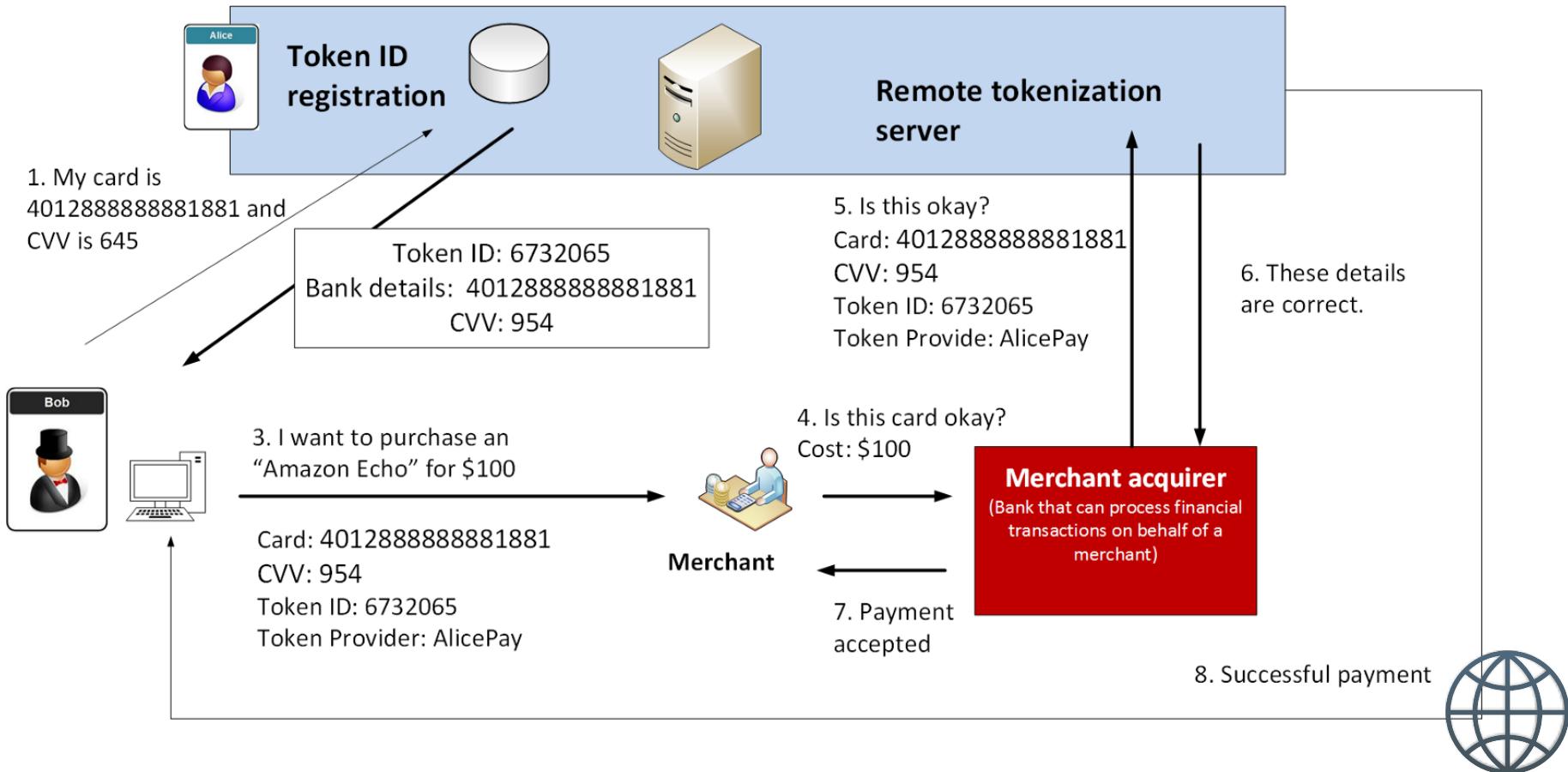
- No direct attacks
- No cryptanalysis
- No side channels
- No token mapping
- No brute force



# Visa Best Practice for Tokenization

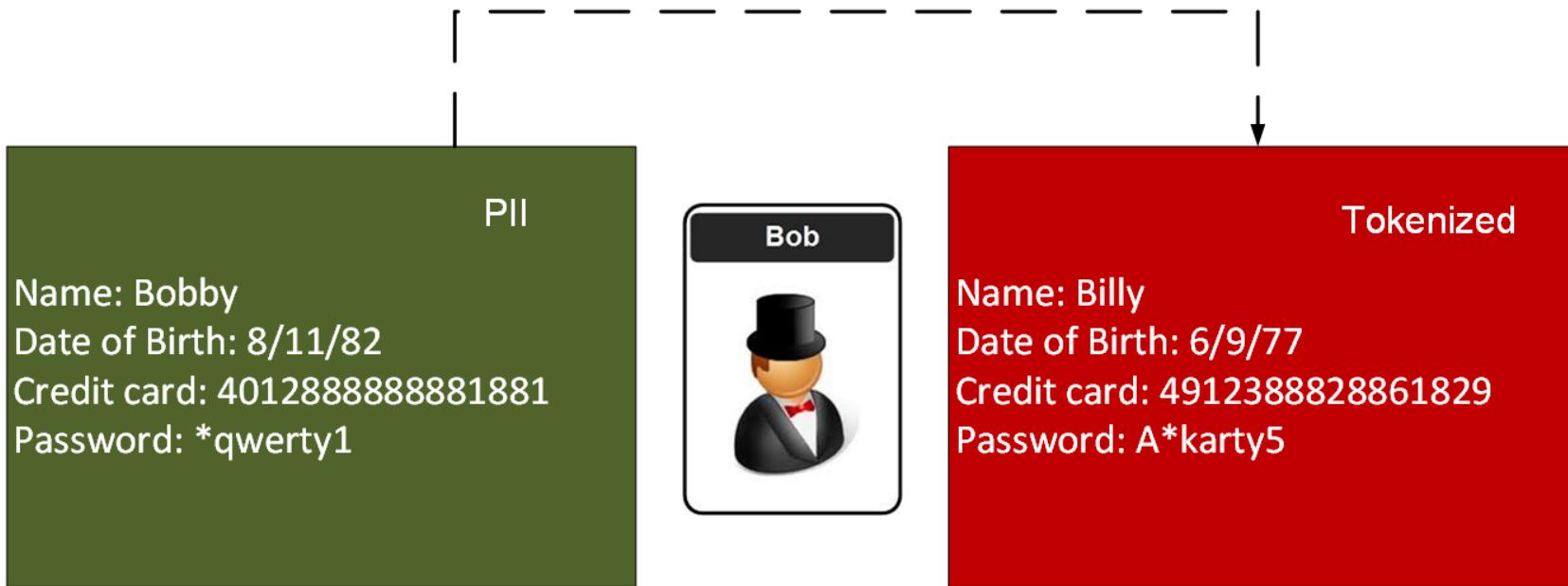


# Token Mapping



# Token Mapping

A random value (nonce) creates token values



# Next Generation Crypto

Light-weight crypto.  
Quantum-robust crypto  
Tokenization.  
Zero-knowledge.  
Homomorphic Encryption.  
zkSnarks, Range-proofs

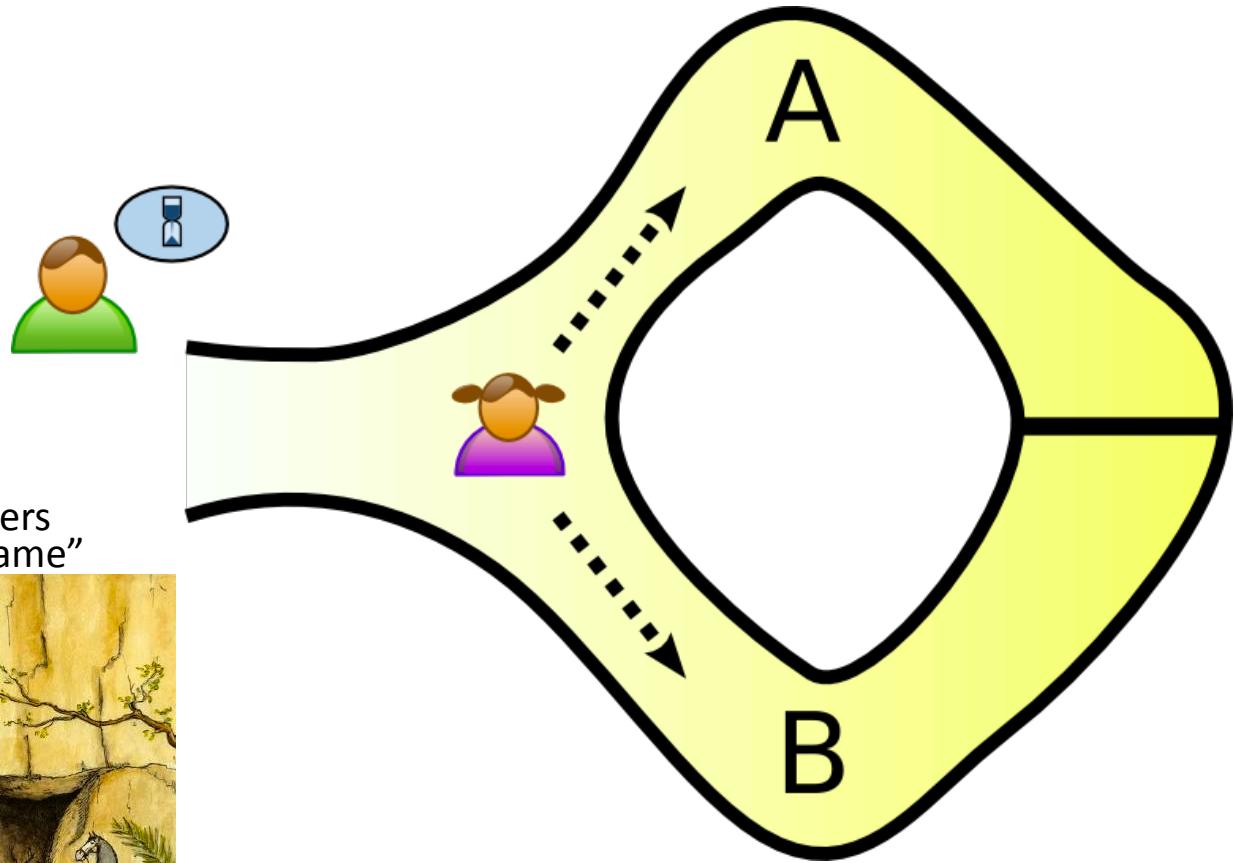
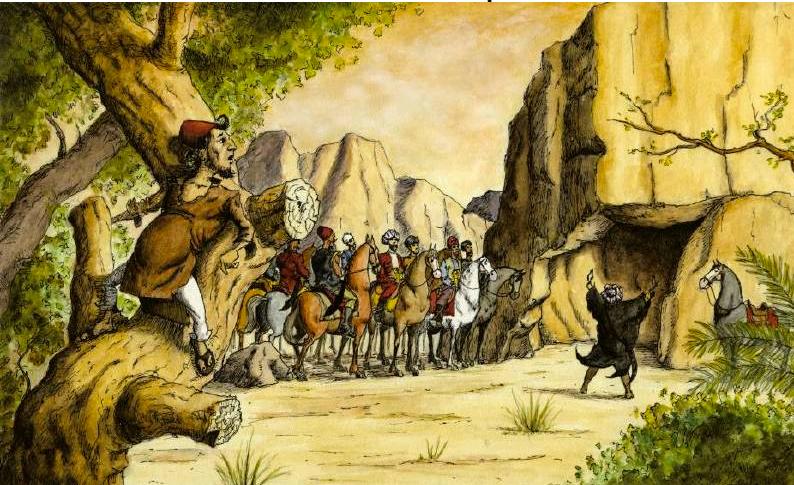
Prof Bill Buchanan OBE  
<http://asecuritysite.com/zero>



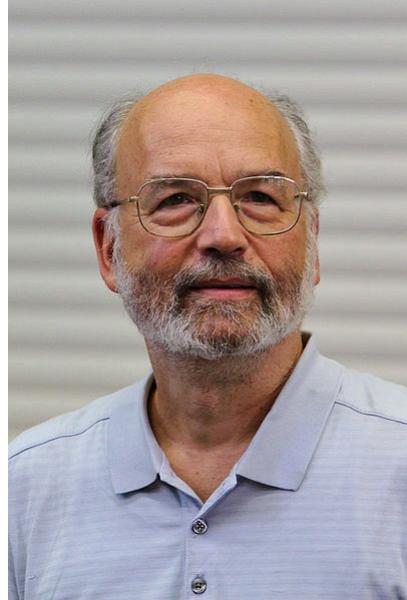
## Zero-knowledge Proof

- Peggy is the prover.
- Victor is the verifier.

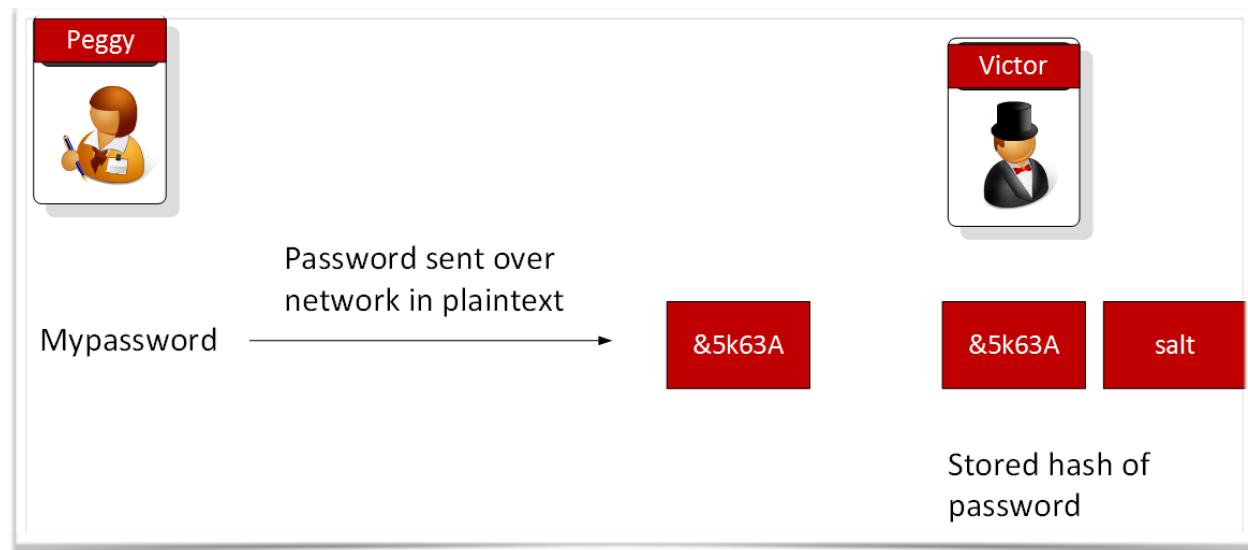
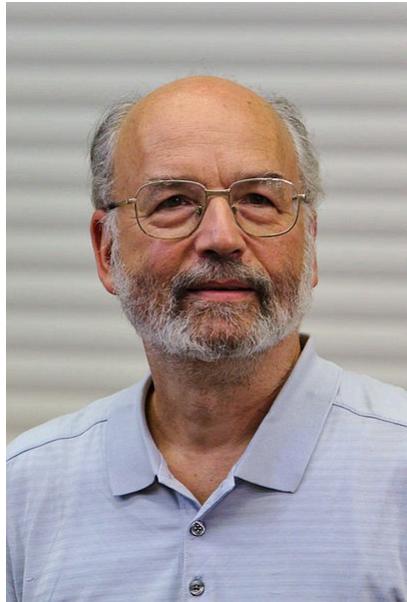
Ali Baba - poor woodcutter - discovers the secret of a thieves as "open sesame"



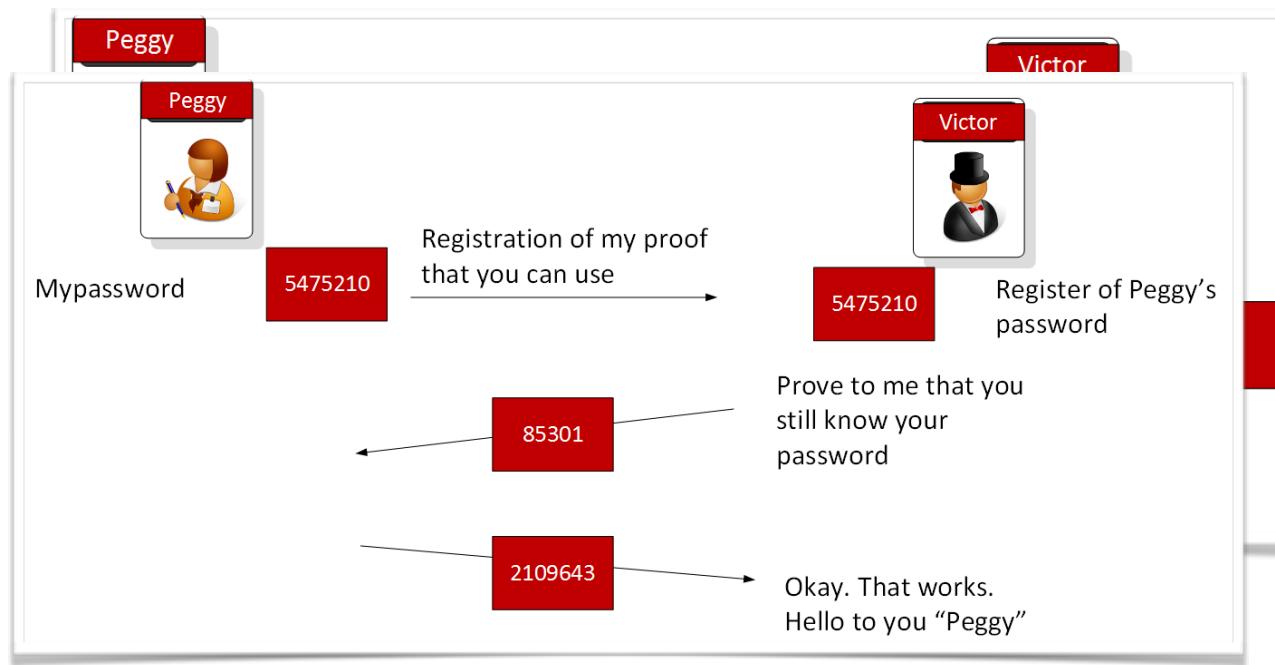
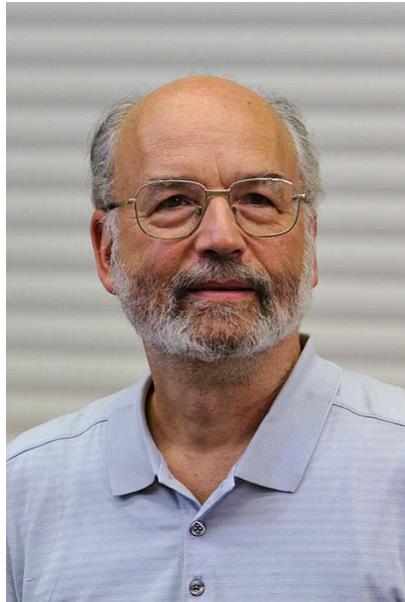
# Zero Knowledge Proof: Fiat-Shamir



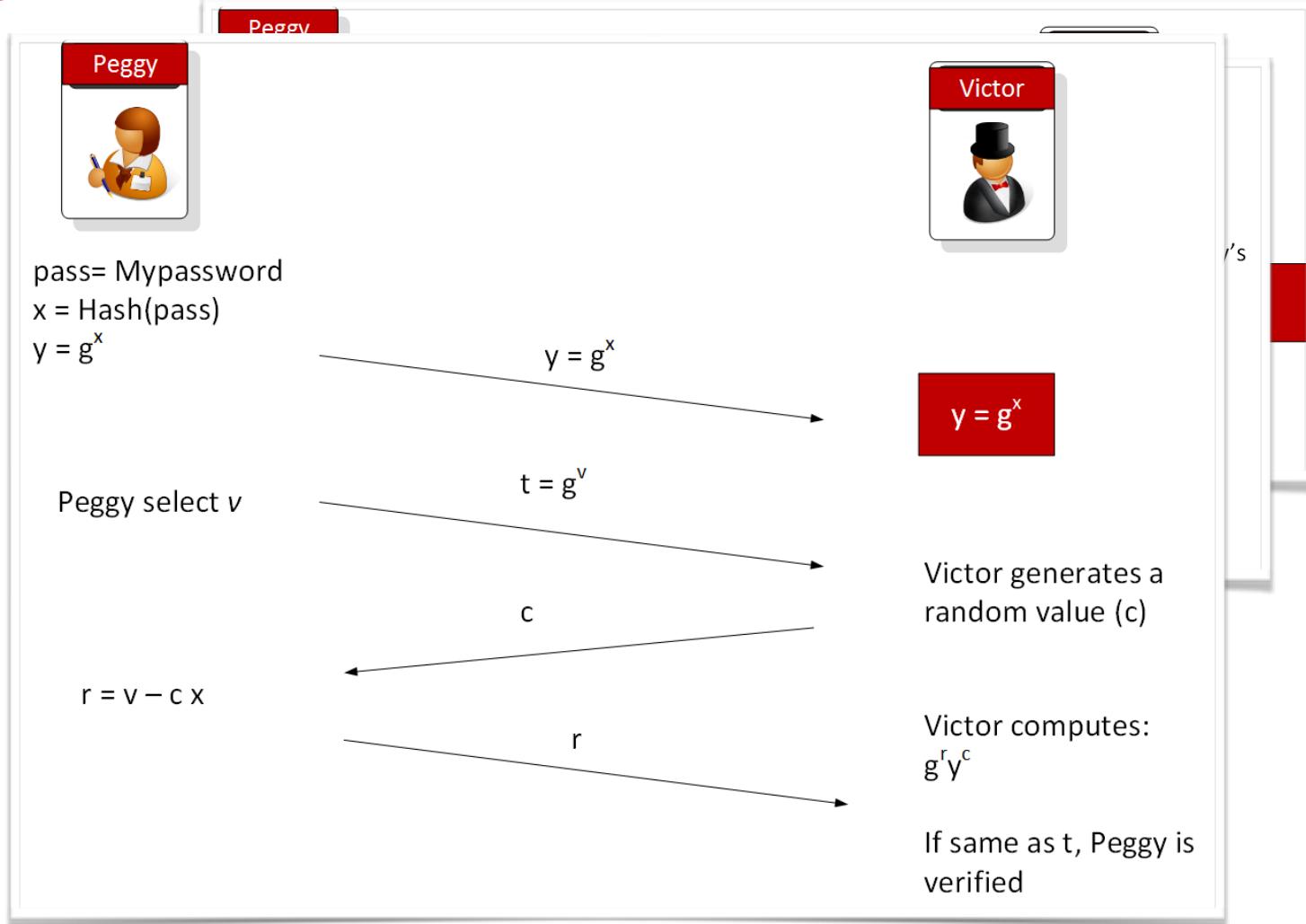
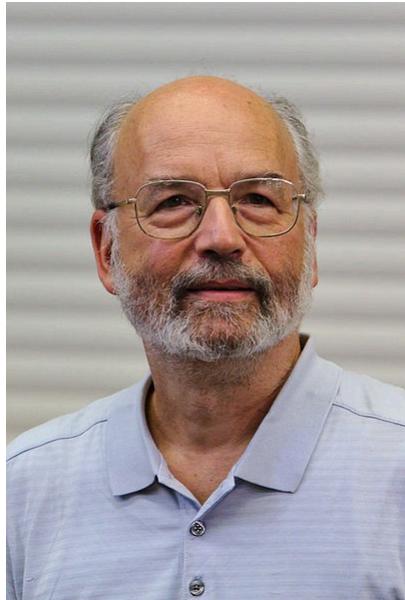
# Zero Knowledge Proof: Fiat-Shamir



# Zero Knowledge Proof: Fiat-Shamir



# Zero Knowledge Proof: Fiat-Shamir



## Bob proves and Alice verifies - Non-interactive random oracle access

Bob is the prover and knows the value of  $x$



Bob and Alice agree on  $G$  and  $p$

Alice is the verifier

Shared Secret:  $y = G^x$

Random value:  $v$

**Commitment:**  $t = g^v$

**Challenge:**  $c = \text{Hash}(g, y, t)$

**Response:**  $r = v - cx \pmod p$

Prove to me you still know  $x$ !

$(r, c)$

Check  $t' = g^r y^c$   
Recheck  $c = H(g, y, t')$

$$\begin{aligned} g^r y^c &= g^{v-cx} y^c \\ &= g^{v-cx} (g^x)^c \\ &= g^{v-cx+cx} \\ &= t \end{aligned}$$

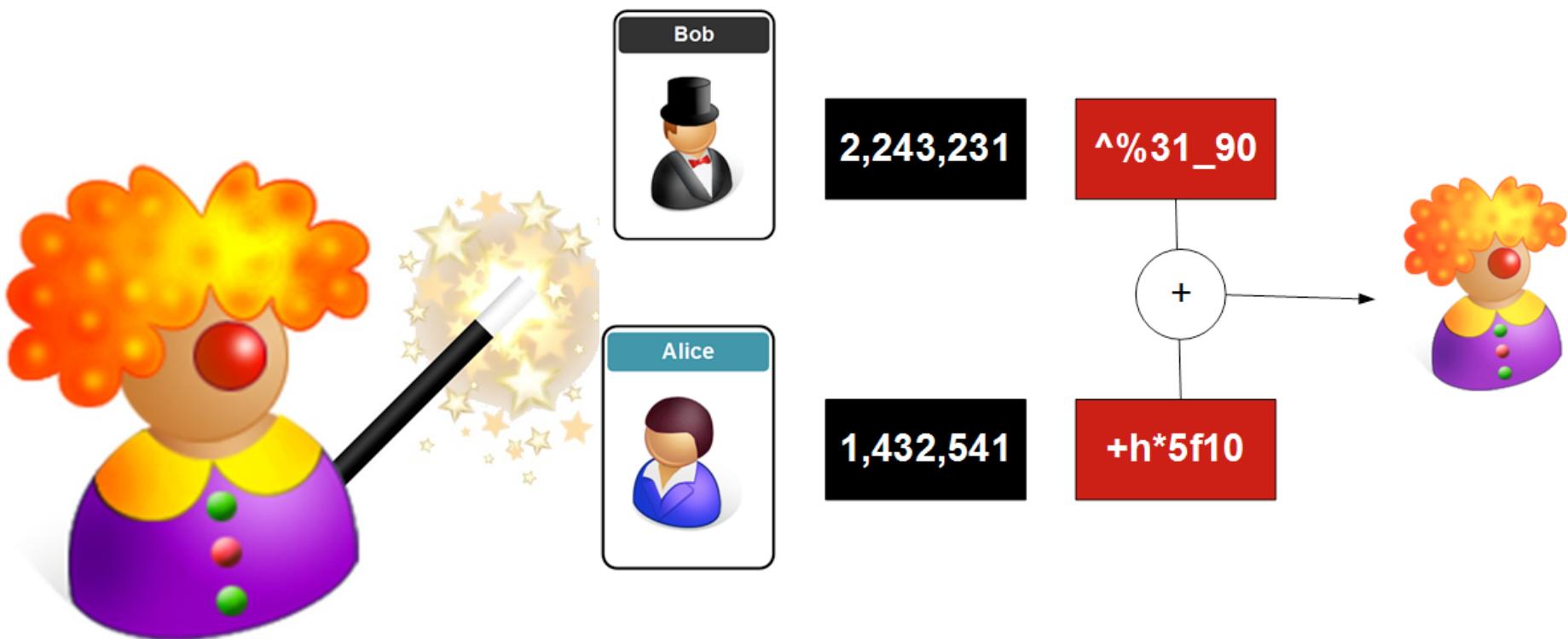
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Tokenization.  
Zero-knowledge.  
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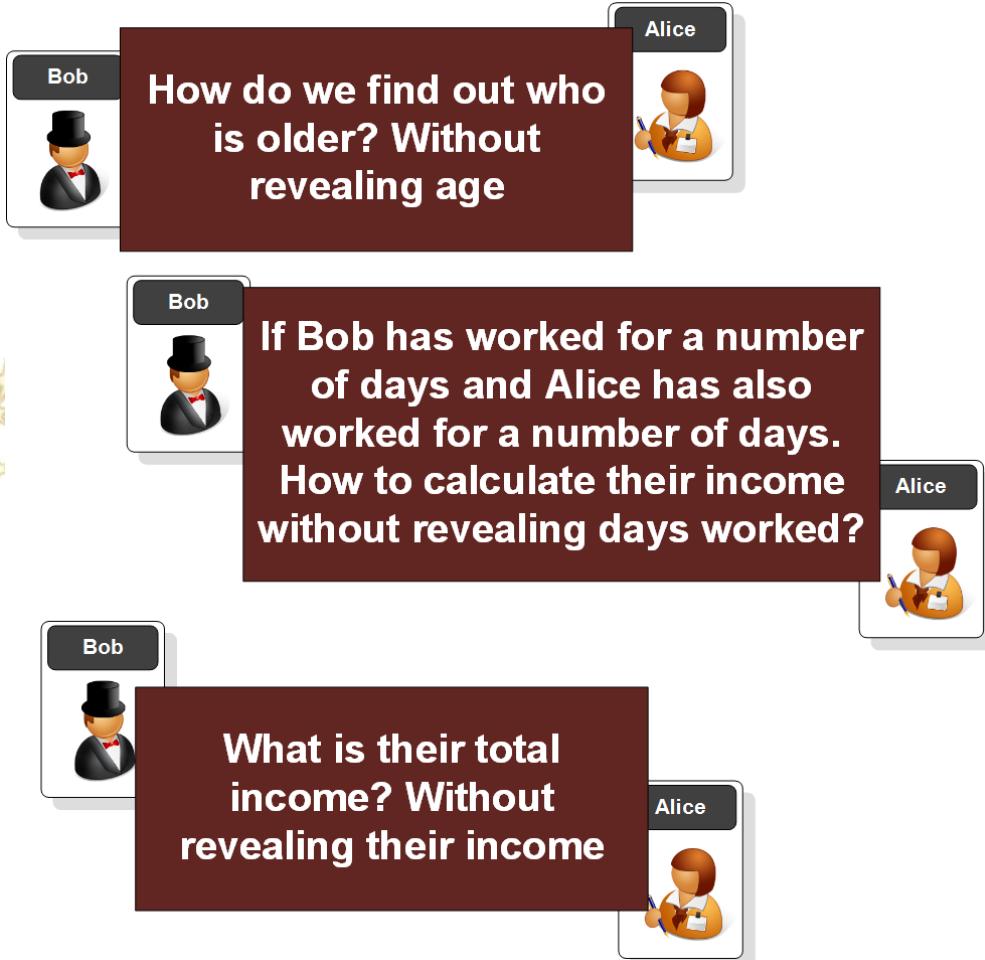
Prof Bill Buchanan OBE  
<http://asecuritysite.com/homomorphic>



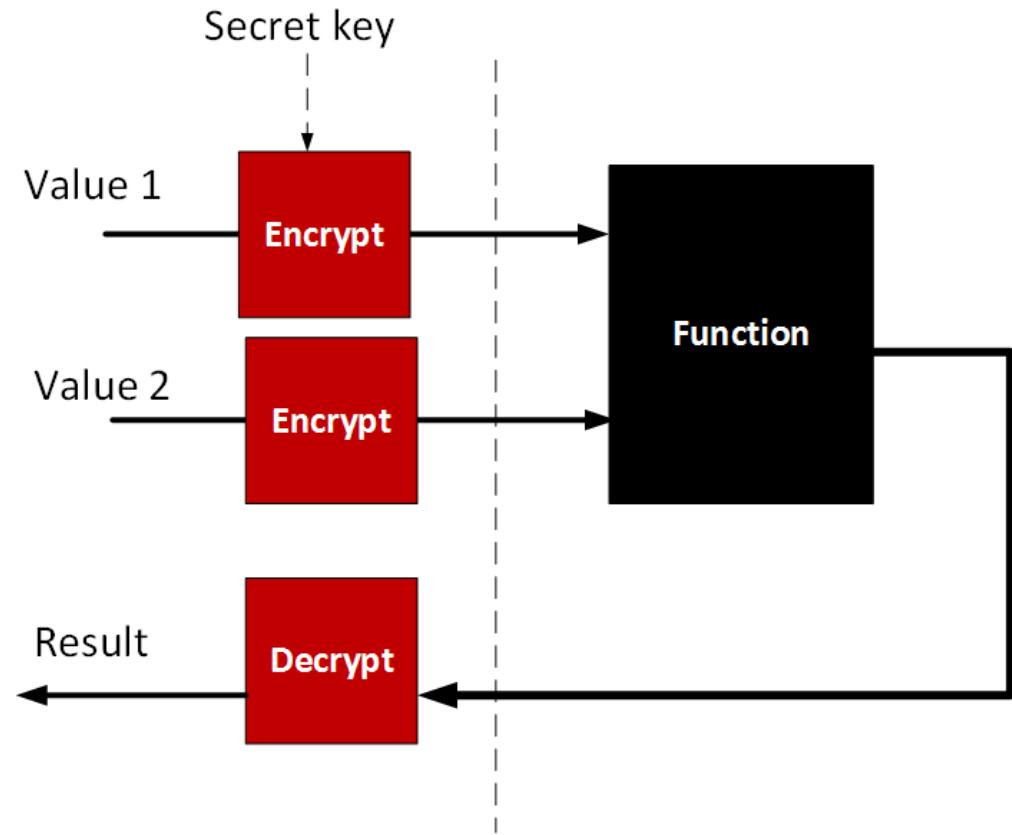
# Homomorphic Encryption



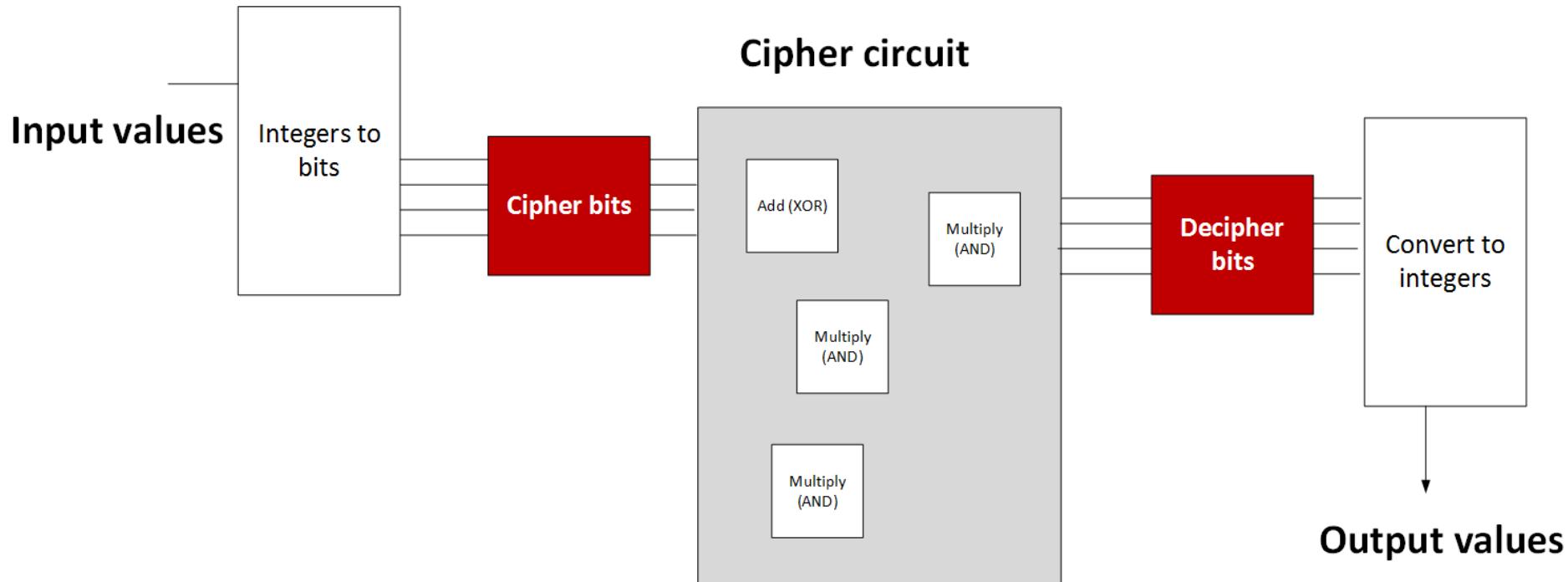
# Homomorphic Encryption



# Full Homomorphic Encryption - DGKV (Dijk, Gentry, Halevi and Vaikuntanathan)



# Full Homomorphic Encryption - DGKV (Dijk, Gentry, Halevi and Vaikuntanathan)



## Full Homomorphic Encryption - DGHV (Dijk, Gentry, Halevi and Vaikuntanathan



$$c = p \times q + 2 \times r + m$$

$$d = (c \mod p) \mod 2$$

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# zCash



Zcash uses ZKP

Humans that were at fault with a new Zcoin hack (Zcash) and which involved making transactions of £561,000 (\$699,000), and with an associated profit of £349,000 (\$435,000).

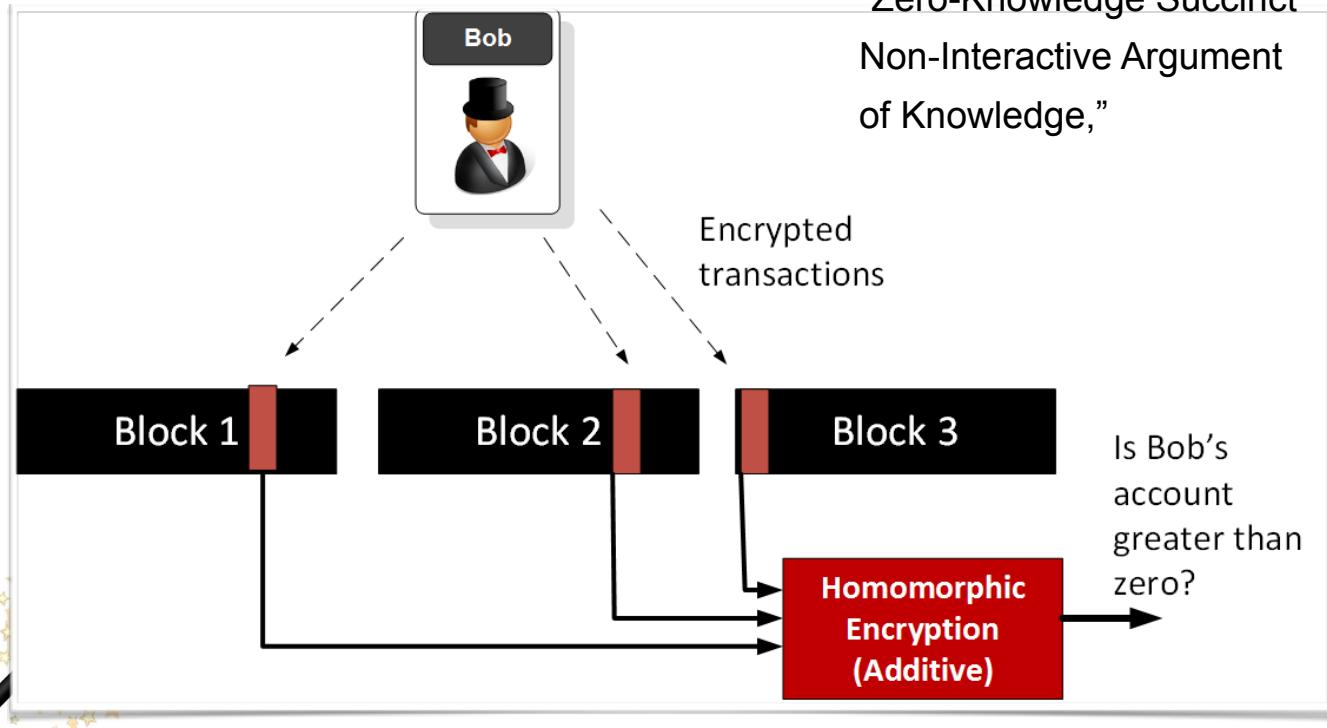
Benchmark	Time in seconds	Min	Max	Change	Trend
time createjoinsplit	44.64126	44.61028	44.98179	-0.65	-4.48%
time parameterloading	2.64027	2.63953	2.70091	-0.16	-2.60%
time solveequihash	30.78956	14.24525	107.95399	-32.47	-19.73%
time solveequihash 2 threads	49.32094	15.41534	115.41706	-0.46	-3.35%
time validatelargetx	0.60553	0.60509	0.60841	-0.06	0.10%
time verifyequihash	0.00155	0.00154	0.00371	-0.58	0.09%
time verifyjoinsplit	0.02776	0.02775	0.05627	-1.38	-4.41%
Average				-5.11	-4.91%

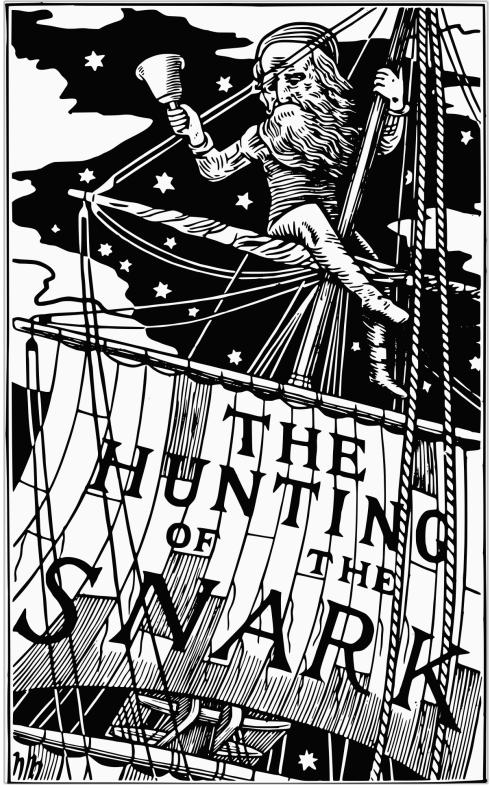
It happened with a single additional character in the source code, and allowed the creation of a Zerocoin spend transaction, and which was able to extract 370,000 Zcoins.

zk-SNARK stands for “Zero-Knowledge Succinct Non-Interactive Argument of Knowledge,”

# Zero-knowledge Proofs

zk-SNARK stands for  
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Non-Interactive Argument  
of Knowledge,”



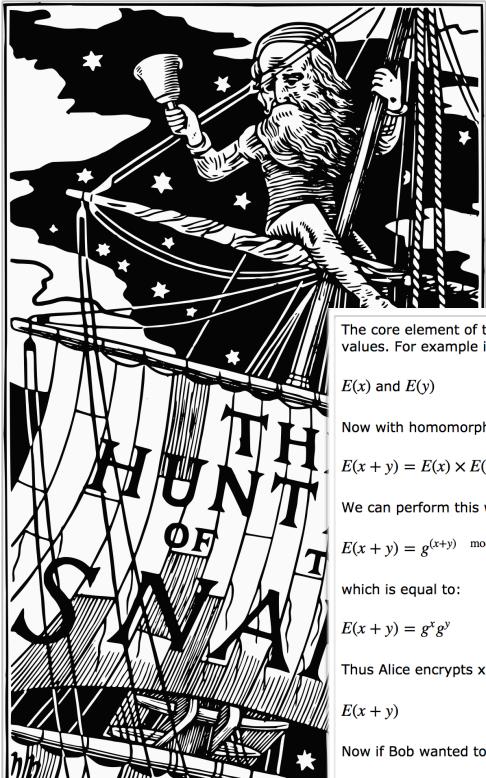


With HH we aim to prove that Alice knows two values ( $x, y$ ) to equal a given answer (ans)

Let's say you want to prove that Alice can produce two numbers which adds up to 8. Overcomes the major problem of Blockchain - which is the lack of privacy in computations and transacti

### Blind Evaluation

Bob doesn't want Alice to know the values that he is using and Alice doesn't want Bob to know the method she is using to compute a result



The core element of the method is the usage of HH (Homomorphic Hiding), and which allows us to perform a mathematical operation on encrypted values. For example if we have a value  $x$  and a value  $y$ , and we want to encrypt them we get:

$E(x)$  and  $E(y)$

Now with homomorphic encryption we can take the encrypted values and multiply them to get the addition:

$$E(x + y) = E(x) \times E(y)$$

We can perform this with discrete logs and where:

$$E(x + y) = g^{(x+y) \mod p-1}$$

which is equal to:

$$E(x + y) = g^x g^y$$

Thus Alice encrypts  $x$  at  $g^x$ , and  $y$  with  $g^y$ , and then just multiply the values together to get:

$$E(x + y)$$

Now if Bob wanted to know if  $x$  plus  $y$  equals 8, Bob will then encrypt:

$$E(8)$$

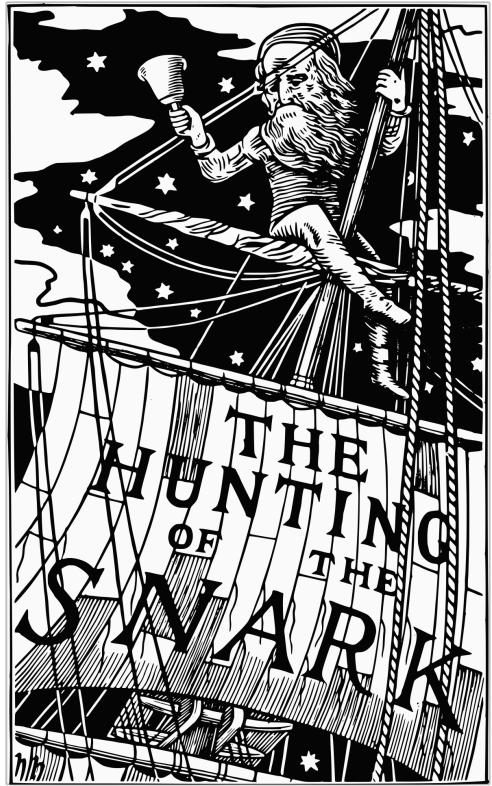
With HH we aim to prove that Alice knows two values ( $x, y$ ) to equal a given answer (ans)

Let's say you want to prove that Alice can produce two numbers which adds up to 8. Overcomes the major problem of Blockchain -

## Blind Evaluation

want Alice to know what he is using and want Bob to know what he is using to calculate the result.

# zkSNARK



## Hidden Homomorphic

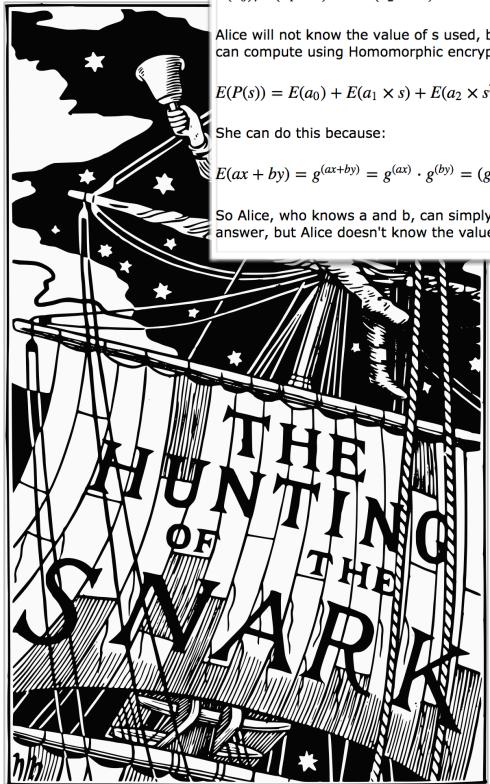
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# zkSNARK



For this we use polynomials, and where we have an equation such as:

$$P(x) = a_0 + a_1x + a_2x^2$$

Bob sends all the elements - known as hidings - of the computation for a value of s:

$$E(a_0), E(a_1 \times s) \text{ and } E(a_2 \times s^2)$$

Alice will not know the value of s used, but she knows the "wiring" of the function. In this case she knows that it is a simple adding operation, so she can compute using Homomorphic encryption:

$$E(P(s)) = E(a_0) + E(a_1 \times s) + E(a_2 \times s^2)$$

She can do this because:

$$E(ax + by) = g^{(ax+by)} = g^{(ax)} \cdot g^{(by)} = (g^x)^a \cdot (g^y)^b = E(x)^a \cdot E(y)^b$$

So Alice, who knows a and b, can simply raise the values received to the polynomial factors and multiply and return to Bob. Bob then knows the answer, but Alice doesn't know the value of s used.

## Hidden Homomorphic

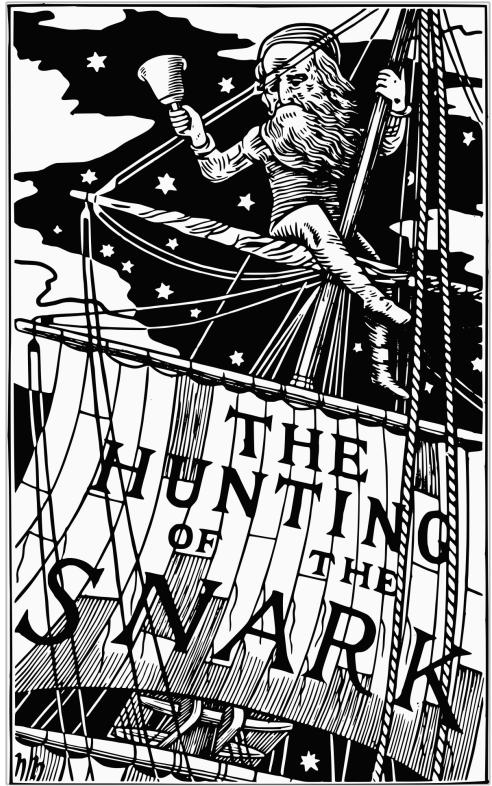
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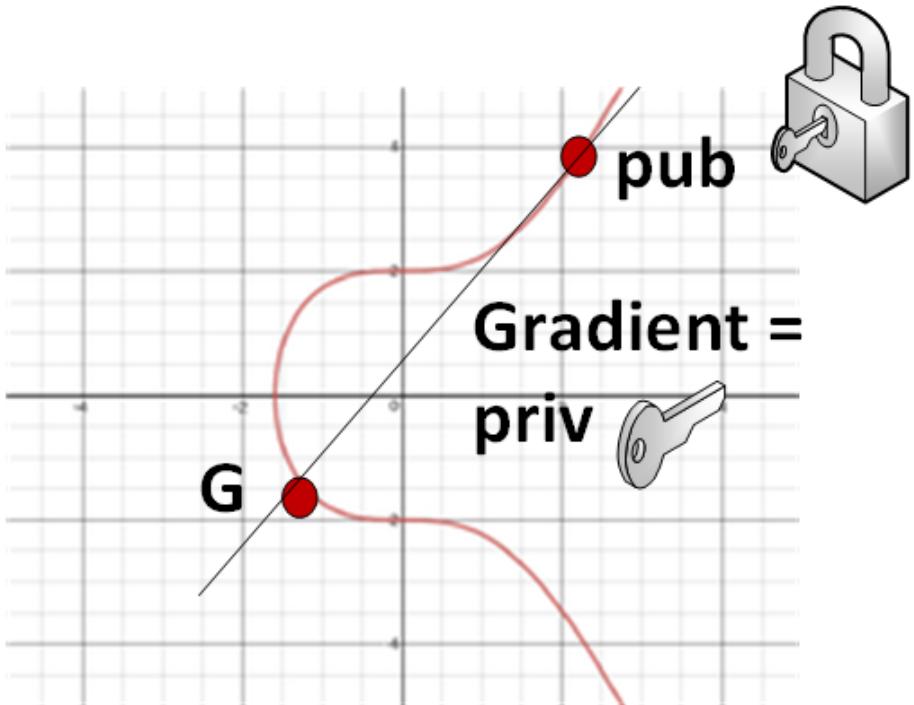
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Tokenization.  
Zero-knowledge.  
Homomorphic Encryption.  
zkSnarks, Range-proofs

Prof Bill Buchanan OBE  
<http://asecuritysite.com/zero>



# Public and private keys with ECC



**Private key:**

0xc9f4f55bdeb5ba0bd337f2dbc952a5439e20ef  
9af6203d25d014e7102d86aaeeL

**Public key:**

0xc44370819cb3b7b57b2aa7edf550a9a5410c23  
4d27aff497458bbbfc8b6a327,  
0x52a1a3e222cd89cbd2764b69bd9b0ea5c4fd6c  
a28861e1f2140eff9c2e76487

**G:**

(50662630222773436695787188951685343262  
50603453777594175500187360389116729240L

,

32670510020758816978083085130507043184  
47127338065924327593890433575733748242

4L)

# Pedersen Commitment and Mimblewimble



# Pedersen Commitment and Mimblewimble

## Adding a blinding value

For this, we can obscure the values in a transaction by adding a **blinding value**. Let's say that we have a transaction value of  $v$ , we can now define this as a point on the elliptic curve ( $H$ ) as:

$$v \times H$$

If we have three transactions ( $v_1$ ,  $v_2$  and  $v_3$ ), we can create a sum total of:

$$\text{Total} = v_1 \times H + v_2 \times H + v_3 \times H = (v_1 + v_2 + v_3) \times H$$

We can thus determine the sum of the transactions. But we could eventually find-out the values of  $v_1$ ,  $v_2$  and  $v_3$ , as they would always appear as the same value when multiplied by  $H$ . We can now add a blinding factor by adding a second point on another elliptic curve ( $G$ ) and a private key ( $r$ ). A transaction value is then (as defined as a Pedersen Commitment):

$$C = v \times H + r \times G$$



# Pedersen Commitment and Mimblewimble

## Addition a blinding value

MIMBLEWIMBLE

Tom Elvis Jedusor

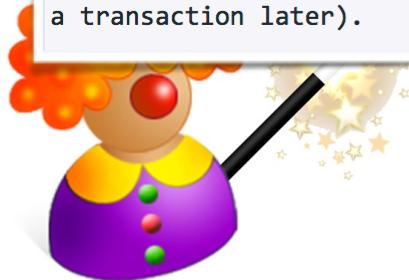
19 July, 2016

\\*\*\*\*/

Introduction

/\*\*\*\*\

Bitcoin is the first widely used financial system for which all the necessary data to validate the system status can be cryptographically verified by anyone. However, it accomplishes this feat by storing all transactions in a public database called "the blockchain" and someone who genuinely wishes to check this state must download the whole thing and basically replay each transaction, check each one as they go. Meanwhile, most of these transactions have not affected the actual final state (they create outputs that are destroyed a transaction later).



by adding a **blinding** value, we can now define this

create a sum total of:

But we could eventually always appear as the same blinding factor by adding a

second point on another elliptic curve ( $G$ ) and a private key ( $r$ ). A transaction value is then (as defined as a Pedersen Commitment):

$$C = v \times H + r \times G$$

# Pedersen Commitment and Mimblewimble

## Adding a blinding value

MIMBLEWIMBLE

Tom E.

19 Jul

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Intro

/\*\*\*\*

Bitco

data

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database

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**Ignotus Peverell**

ignopeverell

Block or report user

Sign in to view email

by adding a blinding

Overview

Repositories 5

Stars 2

Followers 135

Following 0

### Popular repositories

grin

Forked from [mimblewimble/grin](#)

Minimal implementation of the MimbleWimble protocol.

● Rust ★ 1

site-test

Test repository for a slightly more elaborate Grin Jekyll site

● HTML ★ 1 ⚡ 2

hacker

Forked from [pages-themes/hacker](#)

Hacker is a Jekyll theme for GitHub Pages

● CSS ⚡ 1

enumset

Forked from [Lymia/enumset](#)

A library for defining enums that can be used in compact bit sets.

● Rust

value is then (as defined as a Pedersen Commitment):

$$C = v \times H + r \times G$$

# Pedersen Commitment and Mimblewimble

## Adding a blinding value

MIMBLEWIMBLE

Tom E...  
19 Ju...

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Intro...

\*\*\*\*

Bitco...

data ...

Howev...

database

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check...

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a tra...

r=10  
(Blinding factor)



H – Point on Elliptic Curve  
G – Point on Elliptic Curve

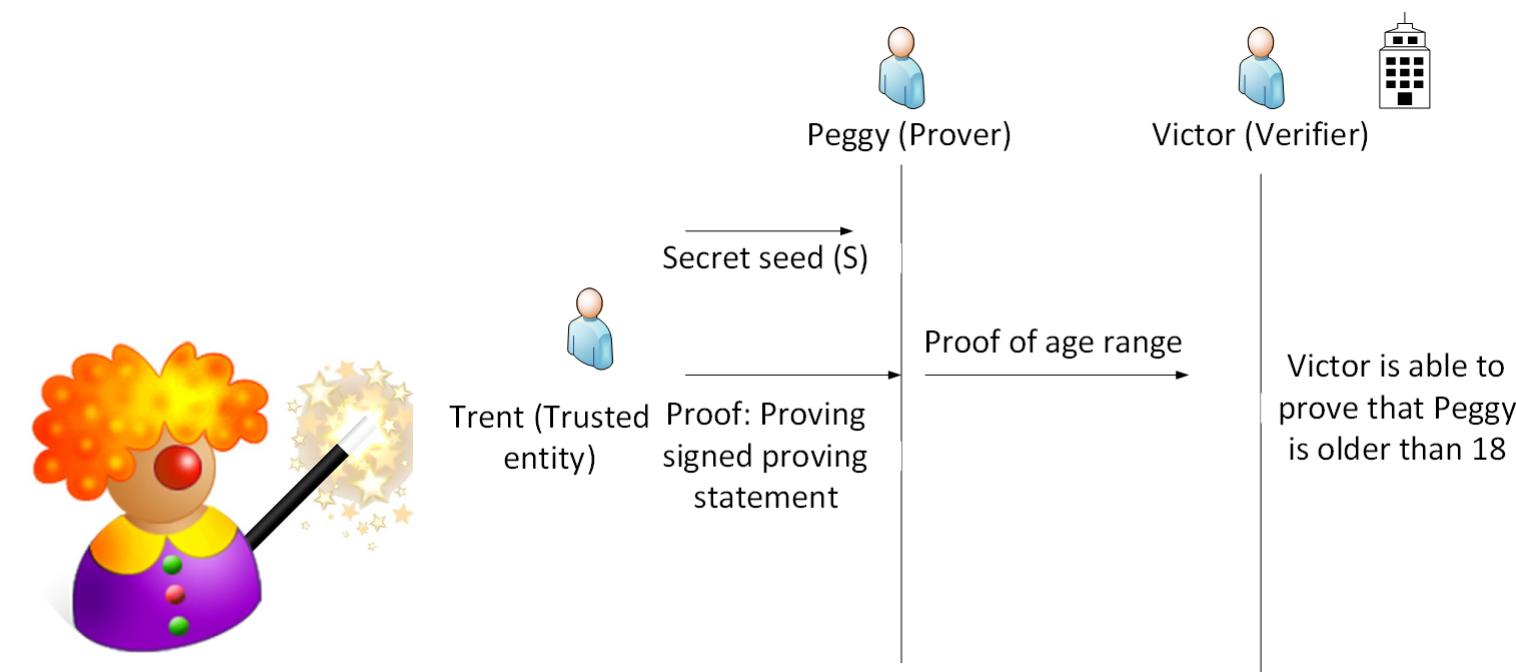
v=4 BTC



X = vH + rG

C = v×H+r×G

# Range Proof



# Range Proof

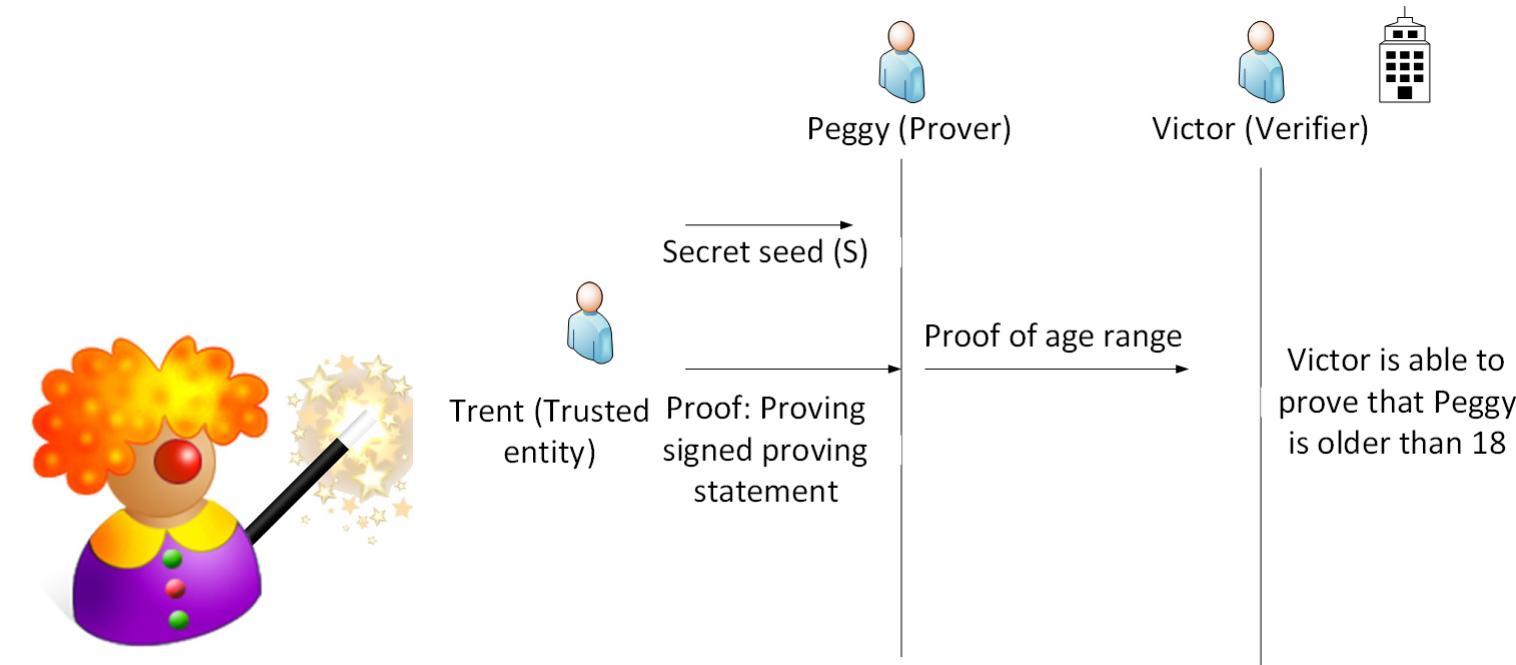
## Bulletproofs: Short Proofs for Confidential Transactions and More

Benedikt Bünz<sup>\*1</sup>, Jonathan Bootle<sup>†2</sup>, Dan Boneh<sup>‡1</sup>,  
Andrew Poelstra<sup>§3</sup>, Pieter Wuille<sup>¶3</sup>, and Greg Maxwell<sup>||</sup>

<sup>1</sup>Stanford University

<sup>2</sup>University College London

<sup>3</sup>Blockstream



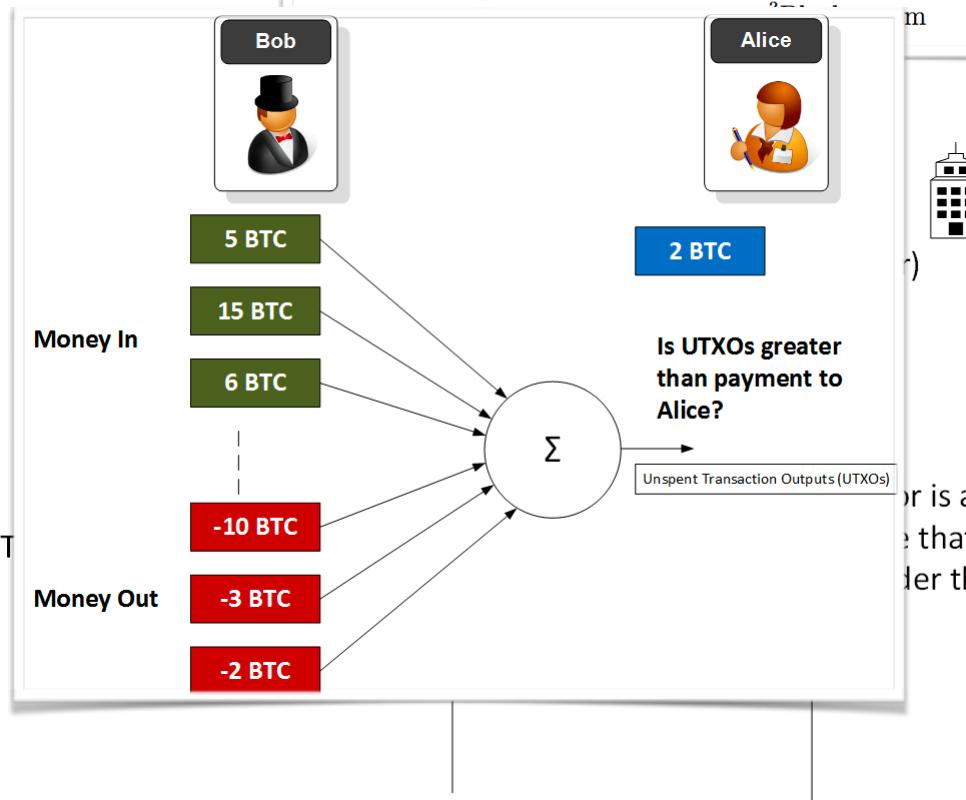
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# Range Proof

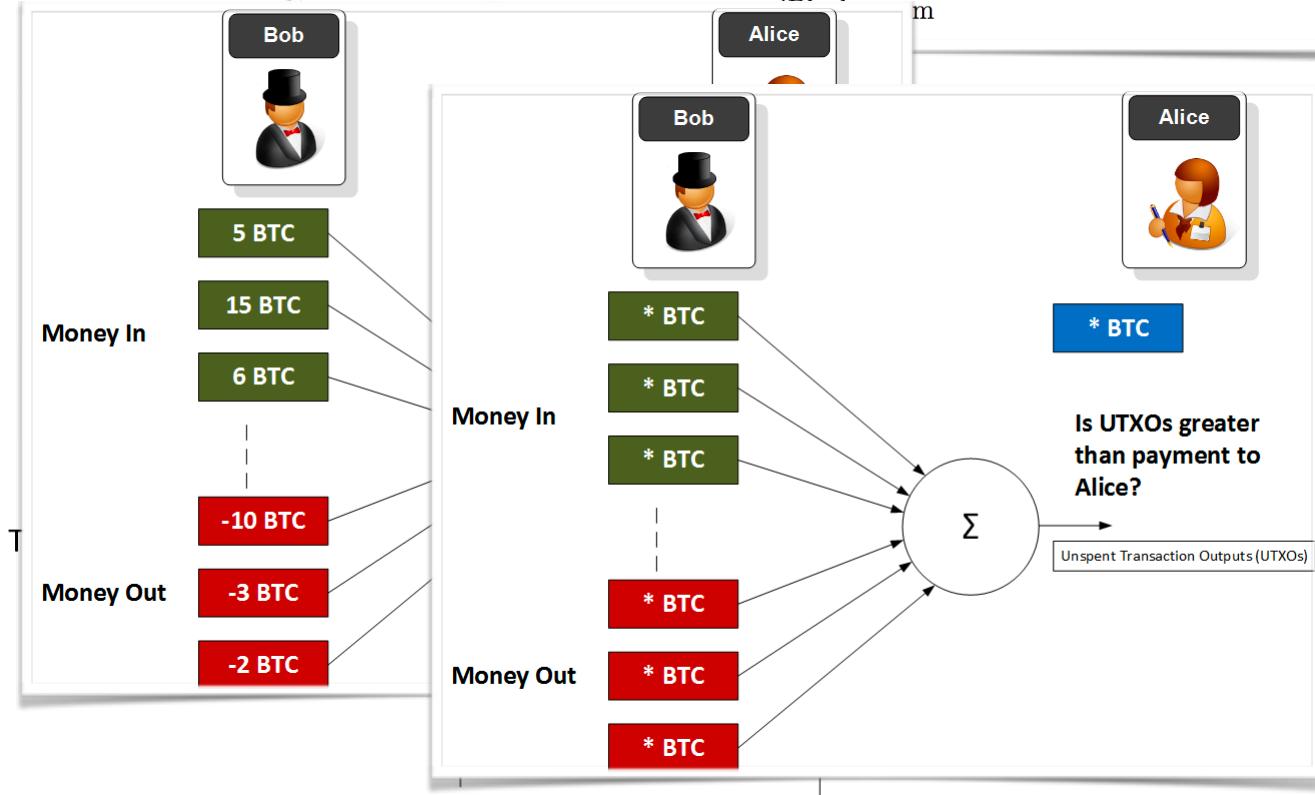
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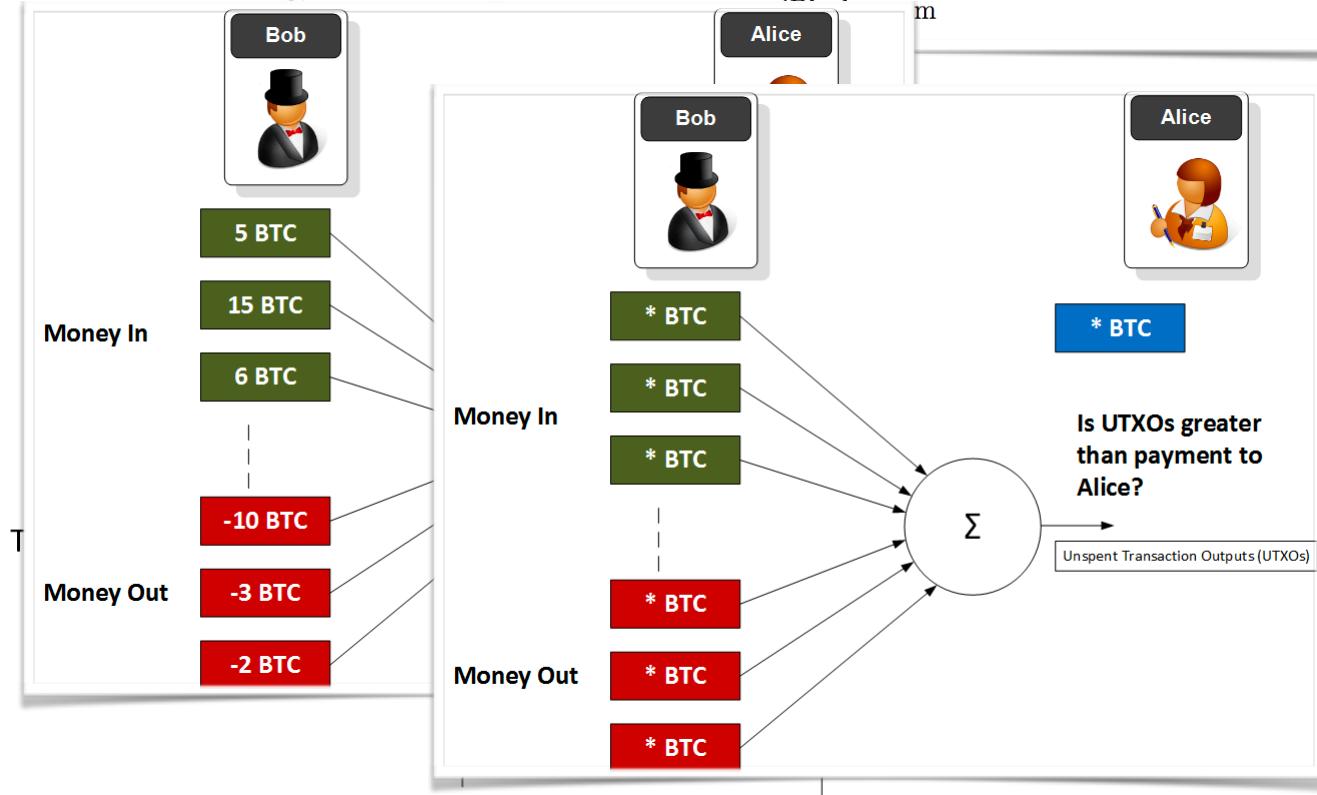
<sup>2</sup>University College London

m



Monero has seen an 80% reduction in transaction size, and which has also led to a significant reduction in the transaction fees.

Bob is applying for a loan from Alice, and now needs to prove that he has a salary of between \$60,000 and \$100,000, and that his employer – Trent – has at least \$1million in the bank



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## Range Proof

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<sup>2</sup>University College London

- Significant reduction in the size of the signature as opposed to other CT methods (such as zk-SNARKs and zk-STARKs).
- Significantly reduced transaction fees with shorter signatures.
- Supports MPC (Multiparty Computation) and where many parties can come together to create a single range proof, without revealing their secrets.
- Allow for the aggregation of range proofs and produces a single, and short, signature.
- Fast verification of proofs (and which are faster than most range proof methods, but still slower than zk-SNARKs).
- Design to be setup for blockchain integration.
- No need to setup a trust infrastructure. This often involves creating an initial set of encryption keys which are then used for trusted signatures. These keys should be used only once, and then deleted. If these keys are not deleted, there is a risk to future trustworthiness of the whole infrastructure.

Monero has seen an 80%

reduction in the size, and which led to a significant reduction in the transaction fees.

Range proofs have been used to prove that a financial institution has more than \$1 billion of liquidity ... “Prove that you have more than \$1 billion of liquidity”, and if they failed to prove this, we would quickly move to audit them. Fraud on a large-scale basis would thus be detected in seconds.

University College London

Bob is applying for a job from Alice, and she wants to prove that his salary is between \$60,000 and \$100,000, and his employer — TrustCo — has at least \$1 million in assets.

... merged into a single (short) bullet point.



- Significant reduction in the size of the signature as opposed to other CT methods (such as zk-SNARKs and zk-STARKs).
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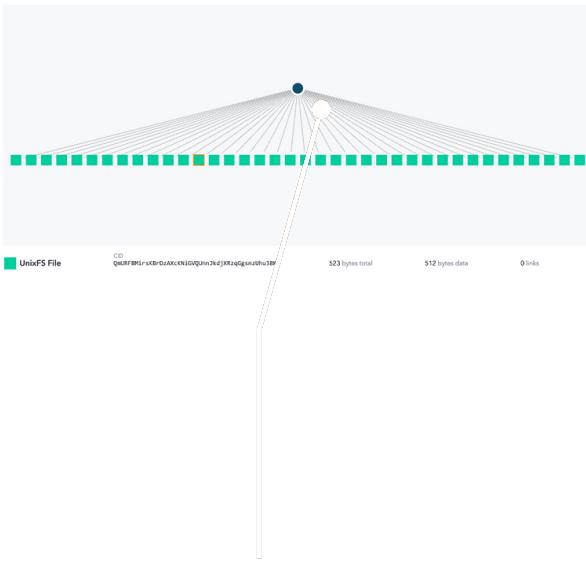
# IPFS

Light-weight crypto.  
Quantum-robust crypto  
Tokenization.  
Zero-knowledge.  
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zkSnarks, Range-proofs  
IPFS

Prof Bill Buchanan OBE  
<http://asecuritysite.com/zero>



# IPFS



Protobuf UnixFS [View on IPFS Gateway](#)

CID: QmZqkuqX1qTspb1GgmnyRFefiuMyA3CemvvgPZD39sPo

SIZE: 33 KB

LINKS: 3

DATA

▼ Object {type: "directory", data: undefined, blockSizes: Array[0]}

PATH	CID
0 1004 - Batman - alt.txt	QmY2JkRD74B1Sb8NRN8EpC1117h6VsZEX7oV16HH78aT11
1 1004 - Batman - transcript.txt	QmQM43UESfCSSQfFAheEq5jduc2fgx1HVX1M13zWc66uc
2 1004 - Batman.png	Qmb8nZBudfuGbzbDRTAhSVEYsoxCae5yBimuuVvYu3BMHG

CID INFO

QmZqkuqX1qTspb1GgmnyRFefiuMyA3CemvvgPZD39sPo

base58btc - cidv0 - dag-pb - sha2-256-256 - aae5699dbbf2a3...

BASE - VERSION - CODEC - MULTIHASH

MULTIHASH

0x12 = sha2-256

0x20 = 256 bits

HASH DIGEST

ebacd63c6468becc651522616878112

Protobuf UnixFS [View on IPFS Gateway](#)

CID: QmY2JkRD74B1Sb8NRN8EpC1117h6VsZEX7oV16HH78aT11

SIZE: 185 B

LINKS: 0

DATA

▼ Object {type: "file", data: Buffer[174], blockSizes: Array[0]}

type: "file"

▼ data: Buffer[174]

0:	73
1:	39
2:	109
3:	32
4:	114
5:	101
6:	97
7:	108
8:	108
9:	121
10:	32



# Next Generation Crypto

Light-weight crypto.  
Quantum-robust crypto  
Tokenization.  
Zero-knowledge.  
Homomorphic Encryption.  
zkSnarks, Range-proofs

Prof Bill Buchanan OBE  
<http://asecuritysite.com/encryption>

